

**Insert (NAME, ID):**

- **Time Complexity:**  $O(\log n)$ 
  - In an AVL tree, the height is maintained as  $O(\log n)$  due to balancing operations. Therefore, inserting a new node takes  $O(\log n)$  time in the worst case.

### Remove (ID):

- **Time Complexity:**  $O(\log n)$ 
  - Removal in an AVL tree involves finding the node to remove and rebalancing the tree if necessary, which takes  $O(\log n)$  time in the worst case due to the tree's balanced height.

**Search (ID):**

- **Time Complexity:**  $O(\log n)$ 
  - Searching for an ID in an AVL tree follows the binary search pattern, taking  $O(\log n)$  time in the worst case.

**Search (NAME):**

- **Time Complexity:**  $O(n)$ 
  - Since names are not ordered lexicographically in the AVL tree, searching by name involves traversing the entire tree, which takes  $O(n)$  time in the worst case.

**Print Inorder:**

- **Time Complexity:**  $O(n)$ 
  - Inorder traversal visits each node exactly once, so the time complexity is  $O(n)$ .

**Print Preorder:**

- **Time Complexity:**  $O(n)$ 
  - Preorder traversal also visits each node once, leading to a time complexity of  $O(n)$ .

**Print Postorder:**

- **Time Complexity:**  $O(n)$ 
  - Postorder traversal similarly visits each node once, resulting in  $O(n)$  time complexity.

**Print Level Count:**

- **Time Complexity:**  $O(n)$ 
  - Level-order traversal visits each node in the tree once, making the time complexity  $O(n)$ .

### Remove Inorder (N):

- **Time Complexity:**  $O(n)$ 
  - Removing the  $n$ th node in inorder involves first collecting the nodes in an inorder traversal, which takes  $O(n)$  time. The actual removal process is  $O(\log n)$ , but the traversal dominates the time complexity.

What would you do differently ?

The search by name currently has a time complexity of  $O(n)$  due to the need to traverse both left and right subtrees. I would consider alternative ways to store names or implement an auxiliary data structure (like a hashmap) to enable faster lookups by name.

[illegible]