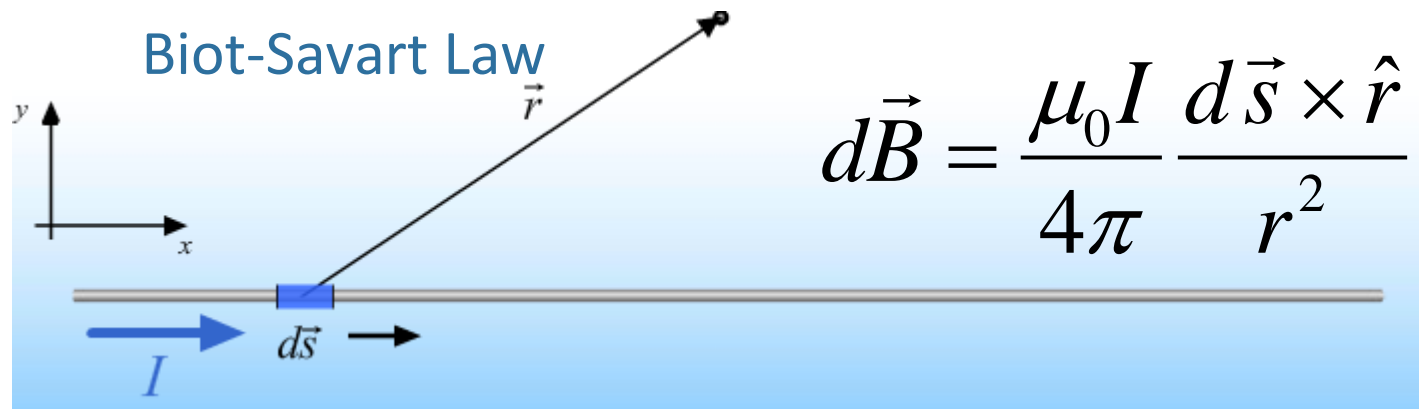


Physics 212

Lecture 14

Today's Concept:



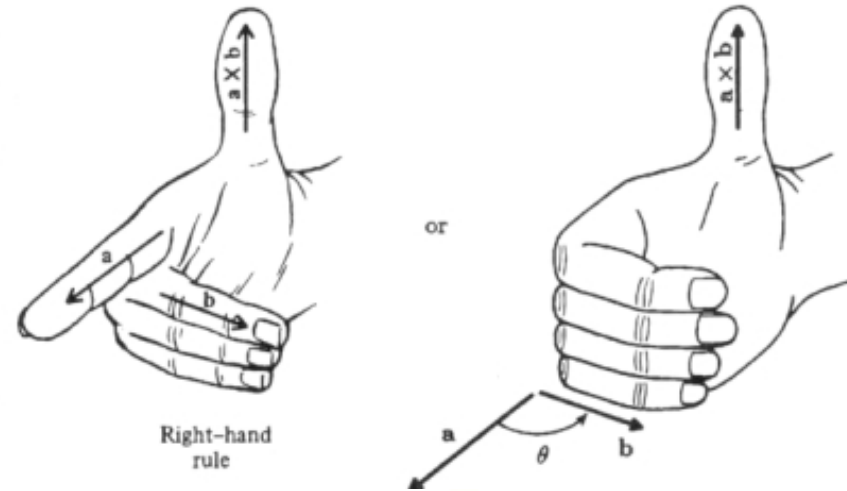
Right Hand Rule Review

1. ANY CROSS PRODUCT

$$\vec{F} = q\vec{v} \times \vec{B} \quad \vec{F} = I\vec{L} \times \vec{B}$$

$$\tau = \vec{r} \times \vec{F} \quad \tau = \vec{\mu} \times \vec{B}$$

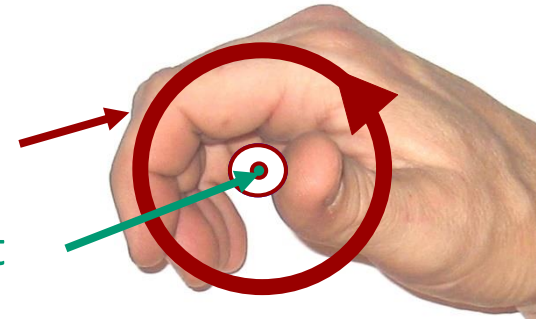
$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \hat{r}}{r^2}$$



2. Direction of Magnetic Moment

Fingers: Current in Loop

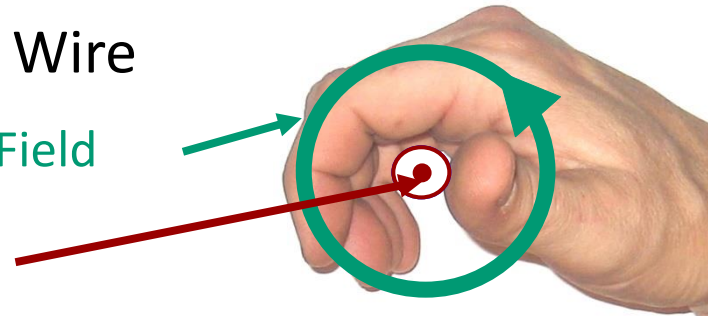
Thumb: Magnetic Moment



3. Direction of Magnetic Field from Wire

Fingers: Magnetic Field

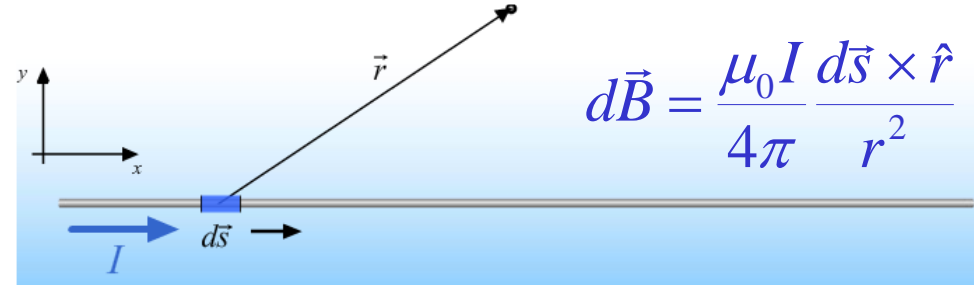
Thumb: Current



Biot-Savart Law:

What is it?

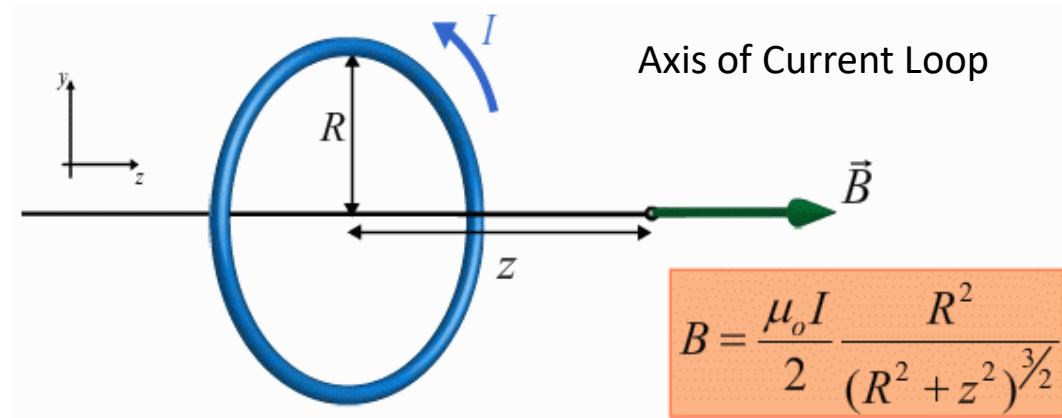
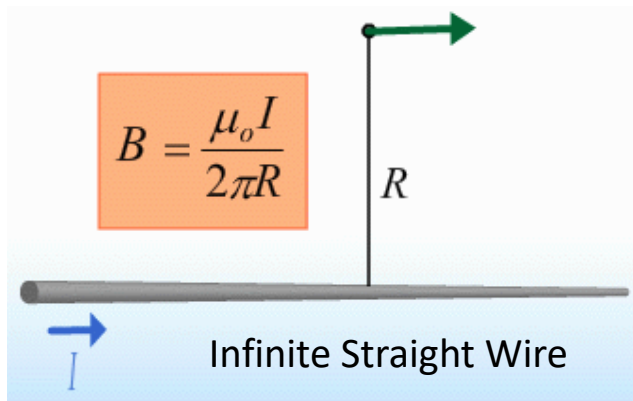
Fundamental law for determining the direction and magnitude of the magnetic field due to an element of current



We can use this law to calculate the magnetic field produced by ANY current distribution

BUT

Easy analytic calculations are possible only for a few distributions:



Plan for Today: Mainly use the results of these calculations!

GOOD NEWS: Remember Gauss' Law?
Allowed us to calculate E for symmetrical
charge distributions



NEXT TIME: Introduce Ampere's Law Allows
us to calculate B for symmetrical current
distributions

B from Infinite Line of Current

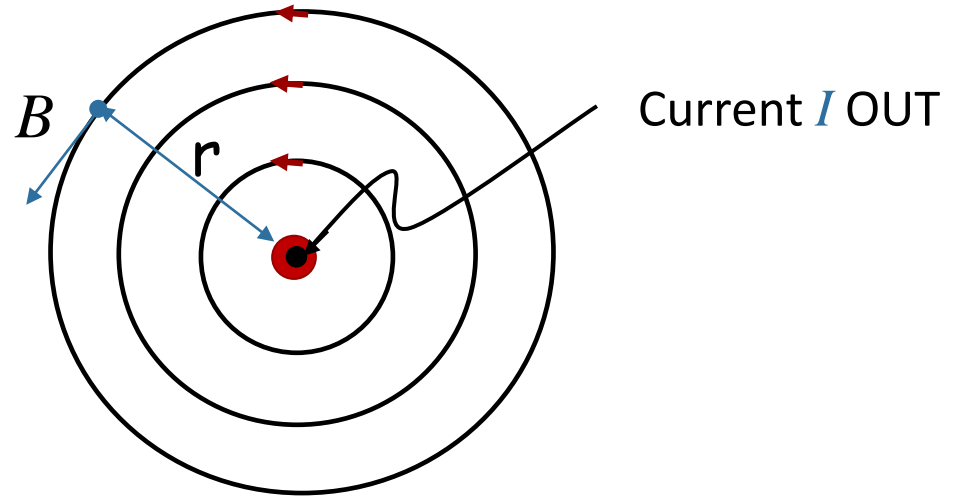
Integrating $d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \hat{r}}{r^2}$ gives result

Magnitude:

$$B = \frac{\mu_0 I}{2\pi r}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ Tm / A}$$

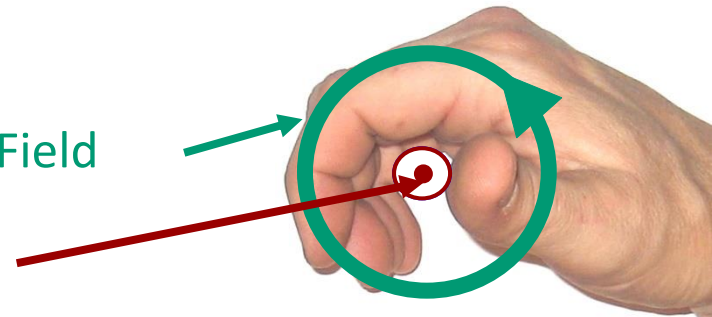
r = distance from wire



Direction:

Fingers: Magnetic Field

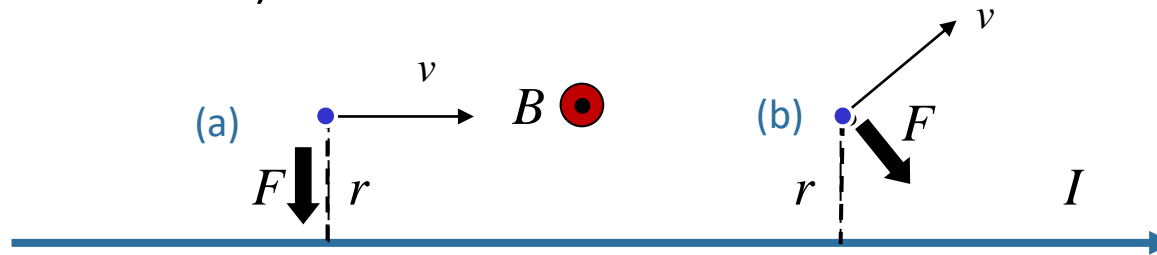
Thumb: Current



Currents + Charges



A long straight wire is carrying current from left to right. Two identical charges are moving with equal speed. Compare the magnitude of the force on charge *a* moving directly to the right, to the magnitude of the force on charge *b* moving up and to the right at the instant shown (i.e. same distance from the wire).



A) $|F_a| > |F_b|$

B) $|F_a| = |F_b|$

C) $|F_a| < |F_b|$

$$\vec{F} = q\vec{v} \times \vec{B}$$

$$|\vec{F}| = qvB \sin \theta$$

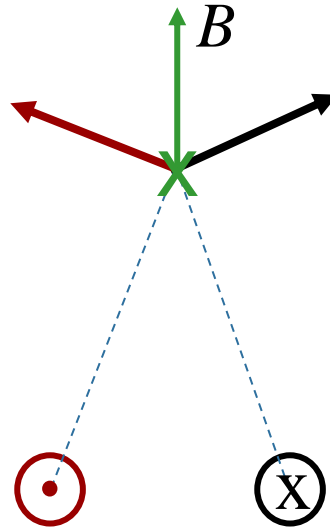
Same q , $|v|$, B and $\theta (=90)$

Forces are in different directions

Adding Magnetic Fields



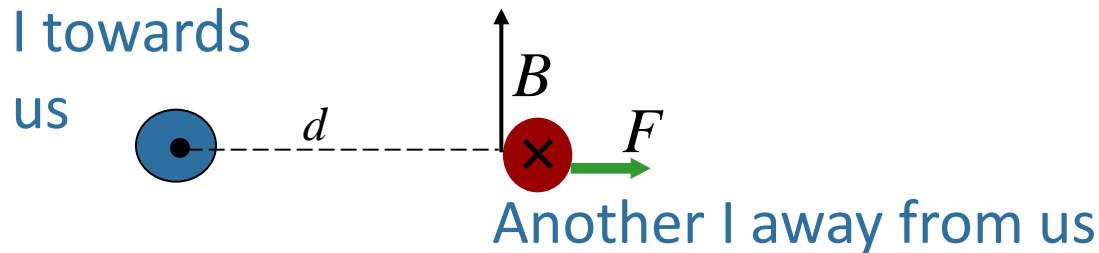
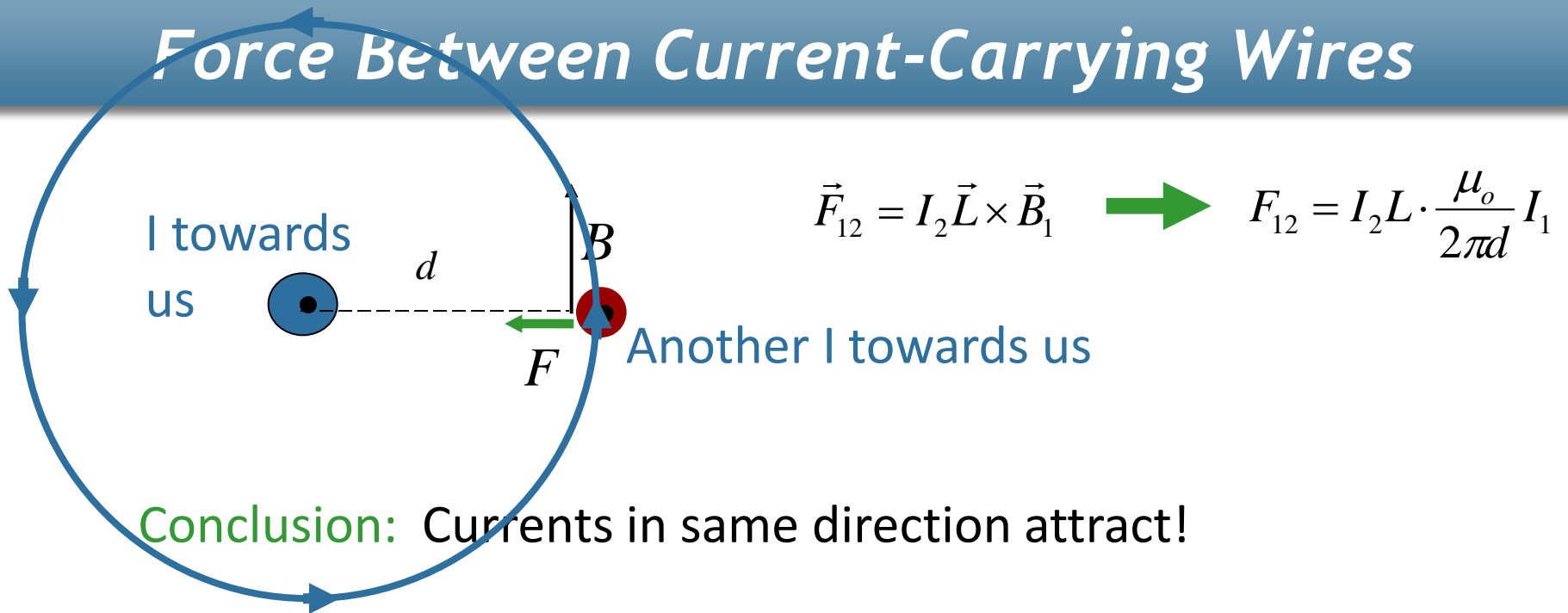
Two long wires carry opposite current

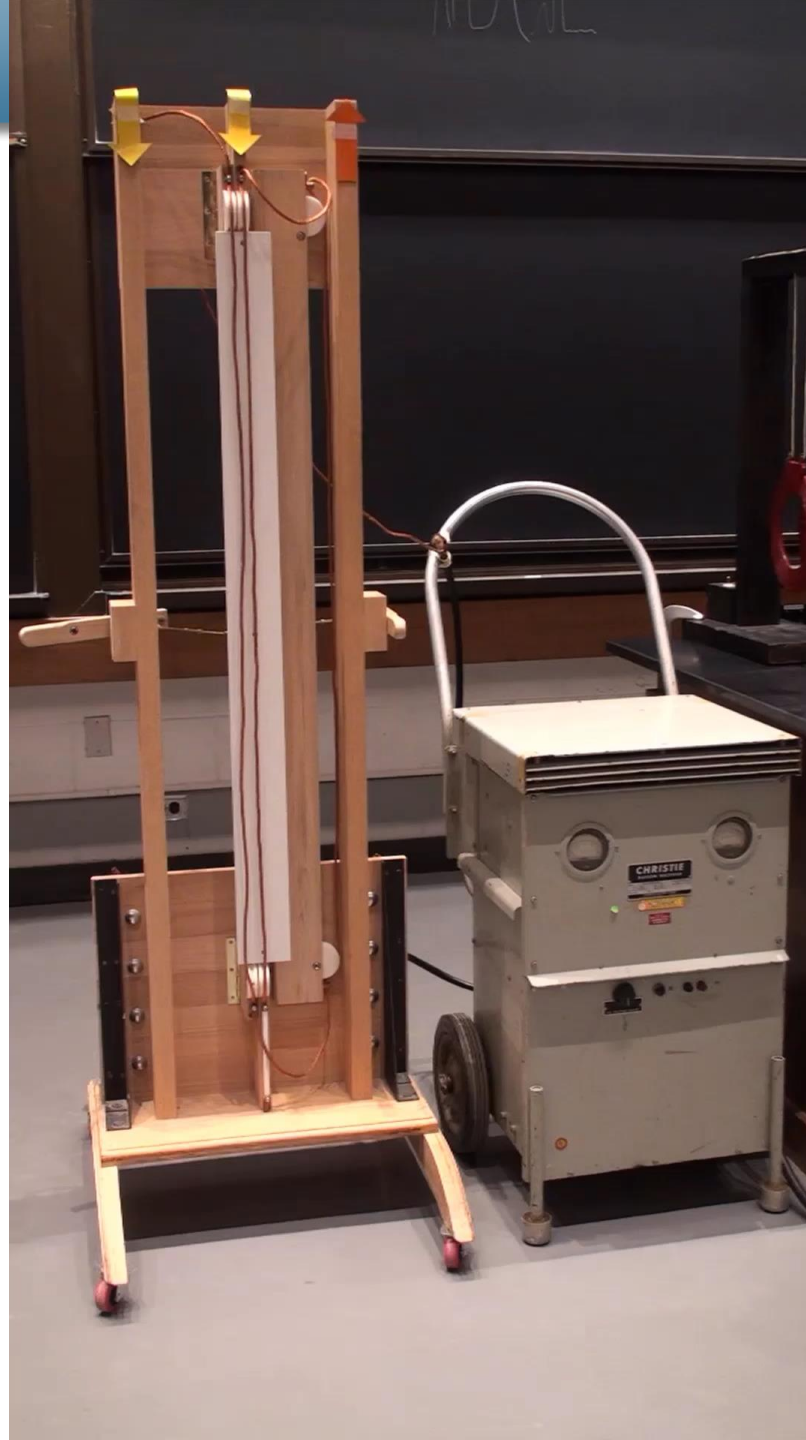


What is the direction of the magnetic field above, and midway between the two wires carrying current – at the point marked “X”?

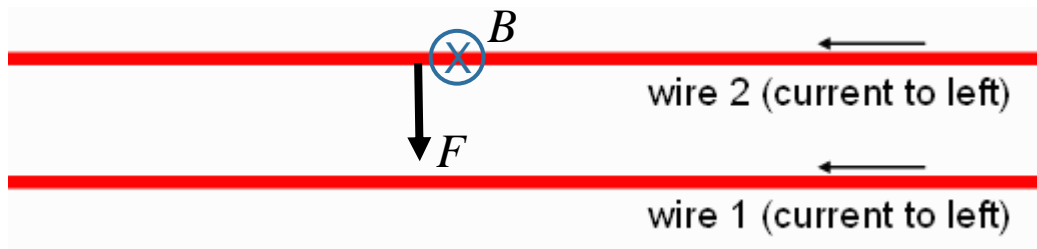
- A) Left B) Right C) Up D) Down E) Zero

Force Between Current-Carrying Wires





Check Point 1



$$\vec{F}_{12} = I_2 \vec{L} \times \vec{B}_1$$

What is the direction of the force on **wire 2** due to **wire 1**?

- A) Up B) Down C) Into Screen D) Out of screen E) Zero

2 wires with same-direction currents are attracted

What is the direction of the torque on **wire 2** due to **wire 1**?

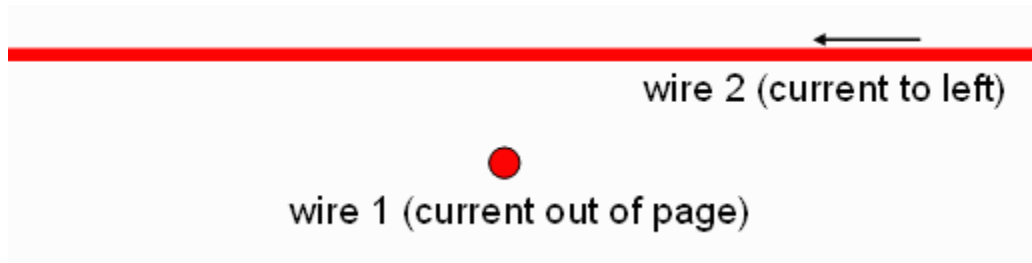
- A) Up B) Down C) Into Screen D) Out of screen E) Zero

Uniform force at every segment of wire



No torque about any axis

Check Point 2



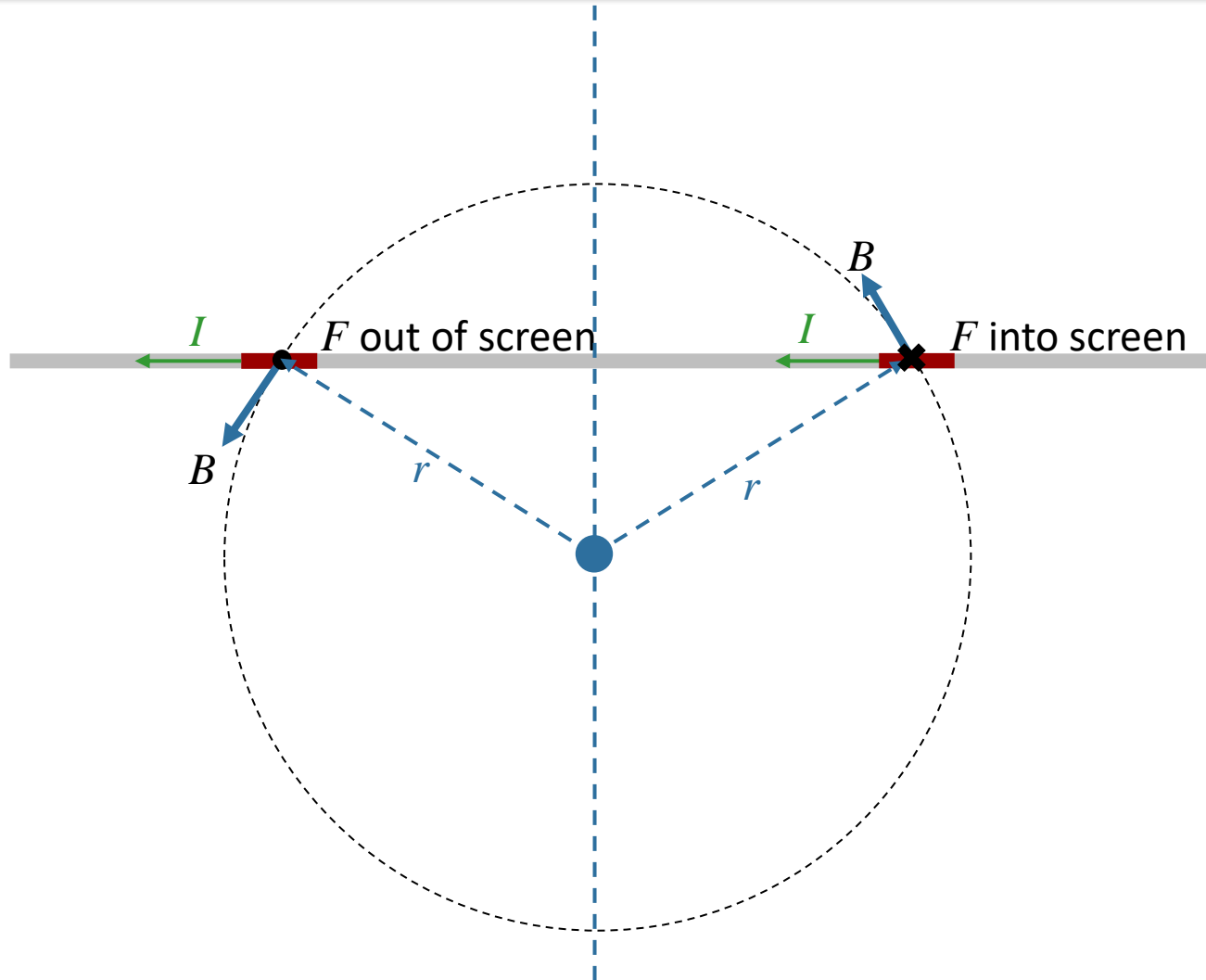
What is the direction of the force on **wire 2** due to **wire 1**?

- A) Up B) Down C) Into Screen D) Out of screen E) Zero

WHY?

DRAW PICTURE!

Consider Force on Symmetric Segments

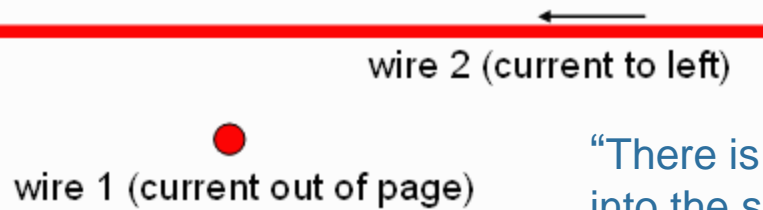


Net Force is Zero!

Check Point 3



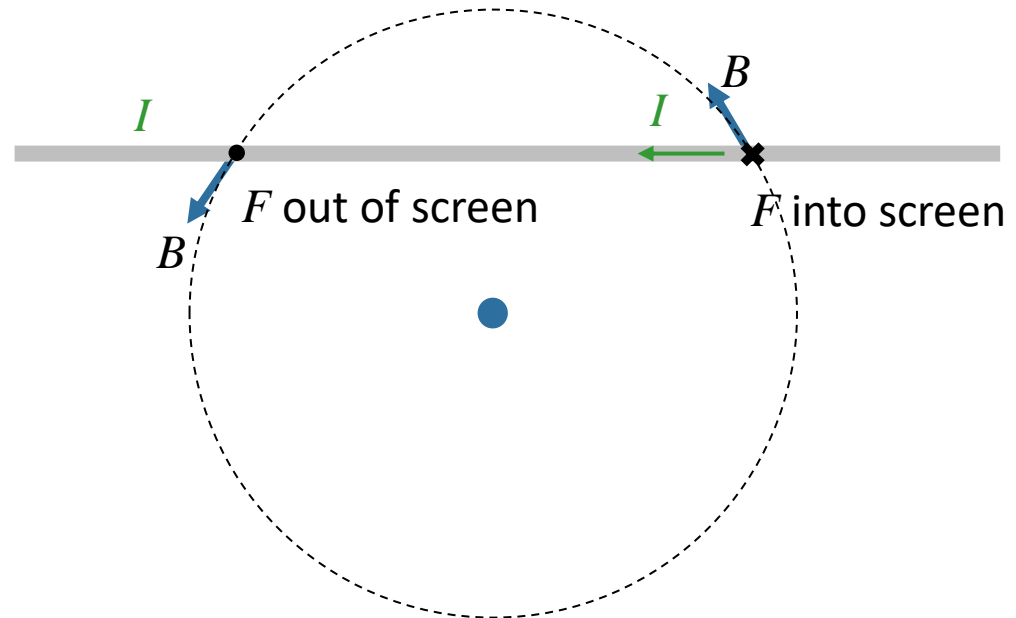
What is torque on wire 2, due to wire 1?



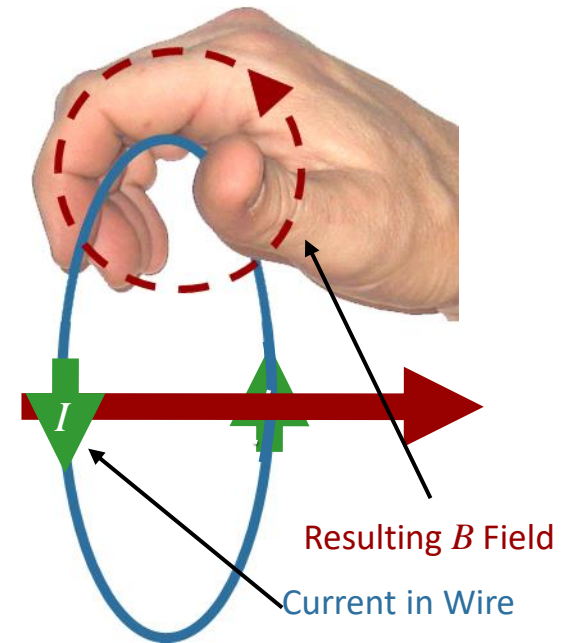
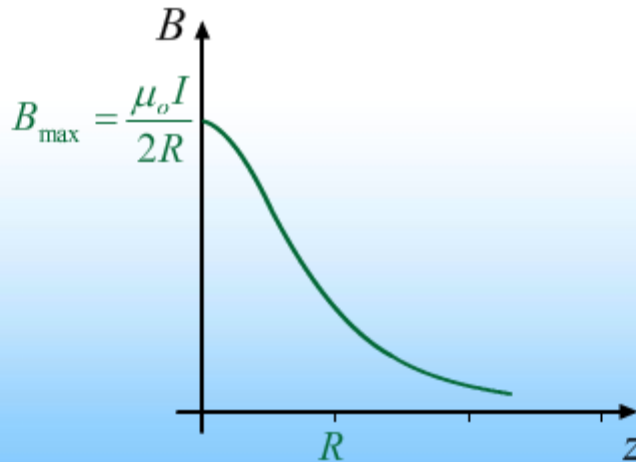
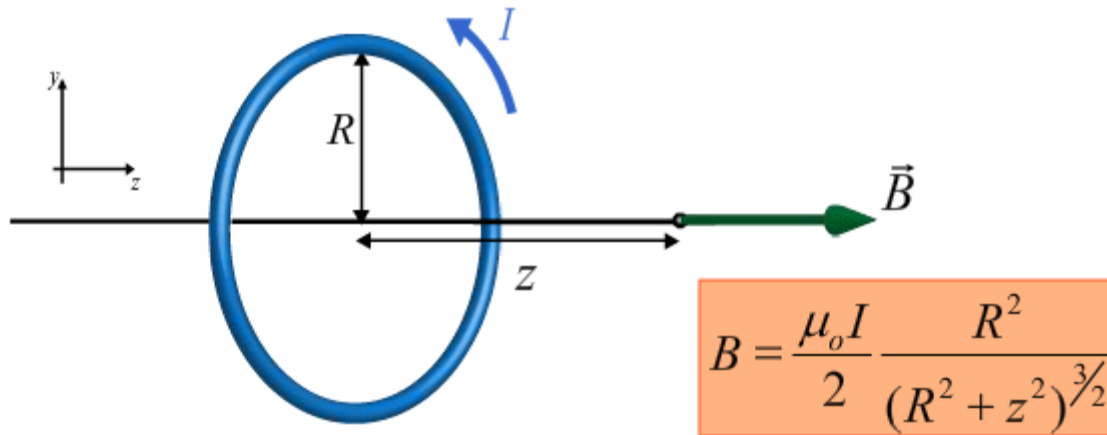
“There is a net force on the right side pointing into the screen and a net force on the left side pointing out of the screen. Using the right hand rule, this means that the torque is pointing up.”

The wire will try to align with wire 1.

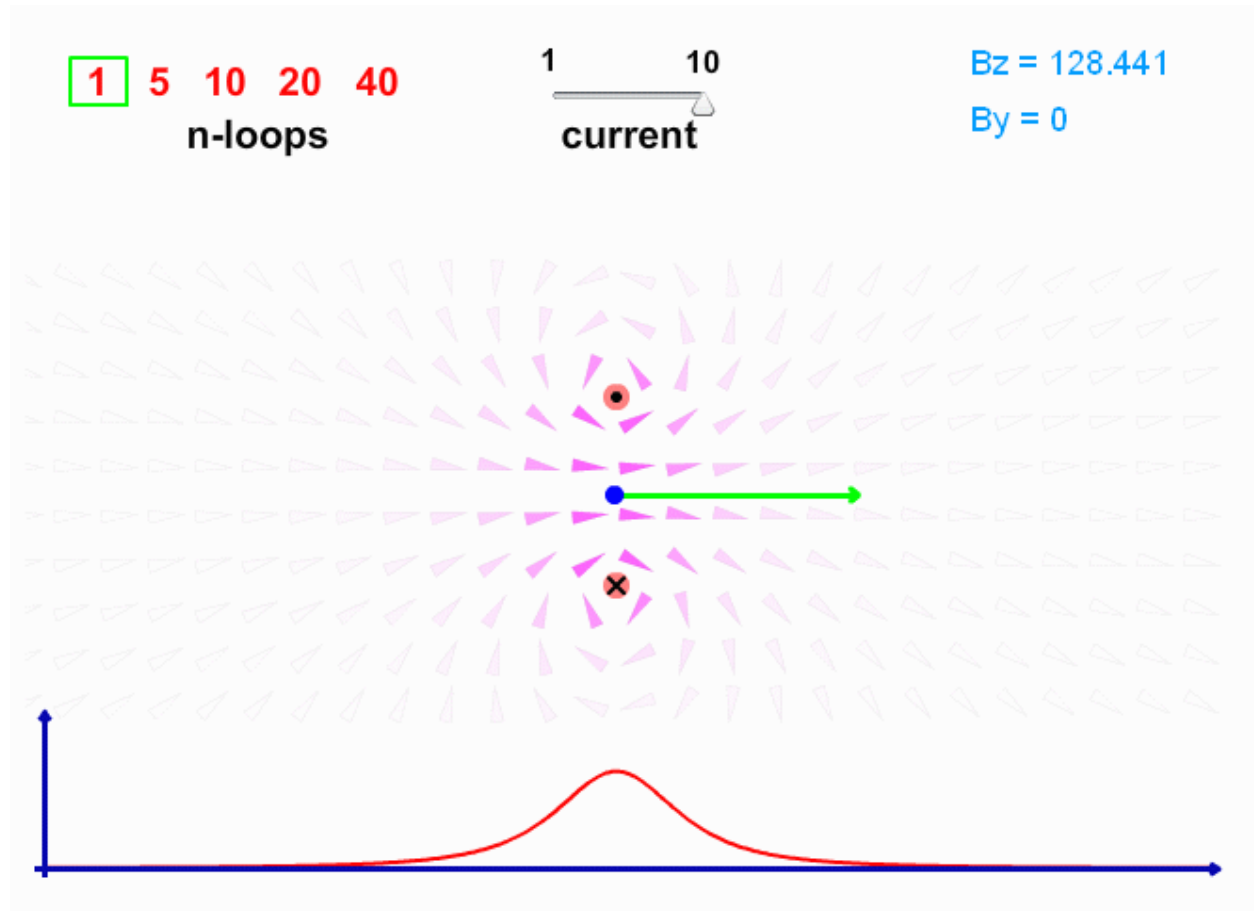
- A) Up B) Down C) Into Screen D) Out of screen E) Zero



B on axis from Current Loop



What about Off-Axis ?



Two Current Loops

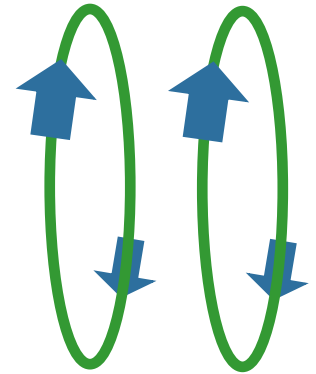


Two identical loops are hung next to each other. Current flows in the same direction in both.

The loops will:

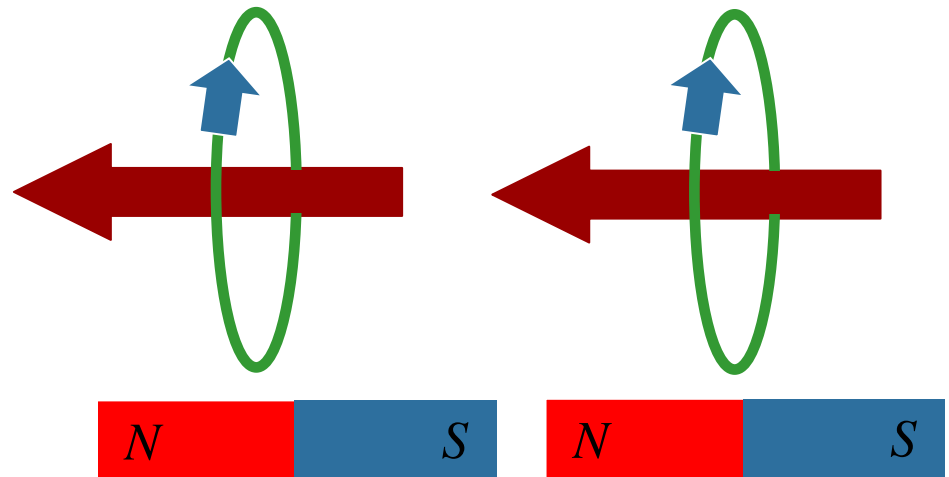
A) Attract each other

B) Repel each other



Two ways to see this:

- 1) Like currents attract
- 2) Look like bar magnets

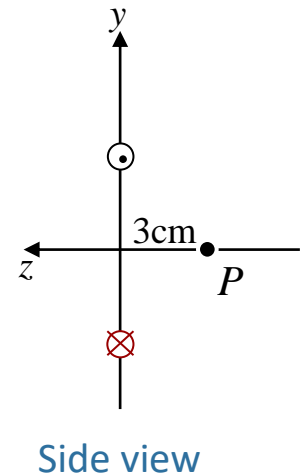
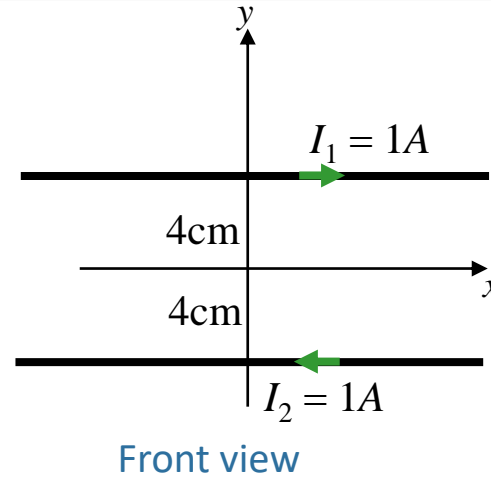




Calculation

Two parallel horizontal wires are located in the vertical (x,y) plane as shown. Each wire carries a current of $I = 1A$ flowing in the directions shown.

What is the B field at point P ?



Conceptual Analysis

Each wire creates a magnetic field at P

B from infinite wire: $B = \mu_0 I / 2\pi r$

Total magnetic field at P obtained from superposition

Strategic Analysis

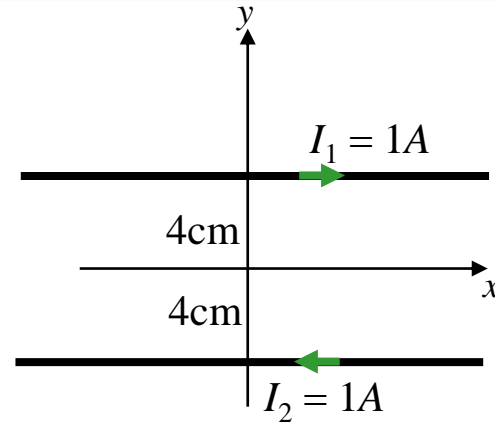
Calculate B at P from each wire separately

Total B = vector sum of individual B fields

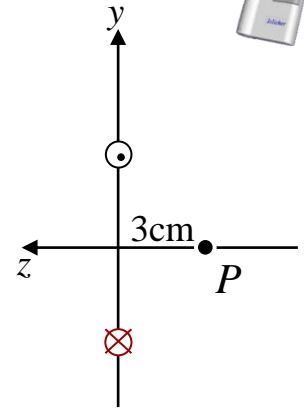
Calculation



Two parallel horizontal wires are located in the vertical (x,y) plane as shown. Each wire carries a current of $I = 1A$ flowing in the directions shown.



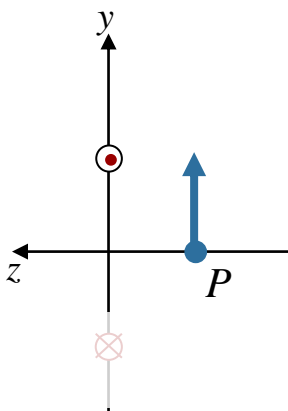
Front view



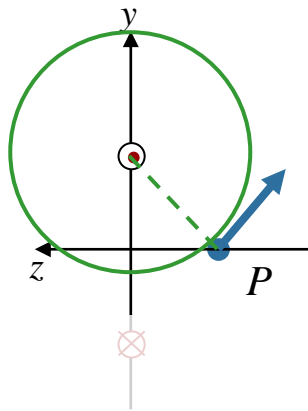
Side view

What is the B field at point P ?

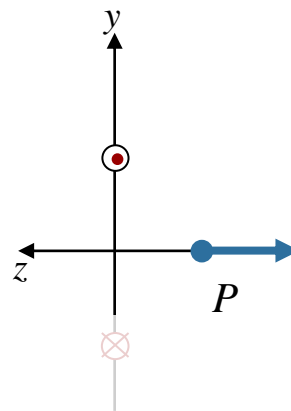
What is the direction of *Magnetic Field* at P produced by the top current I_1 ?



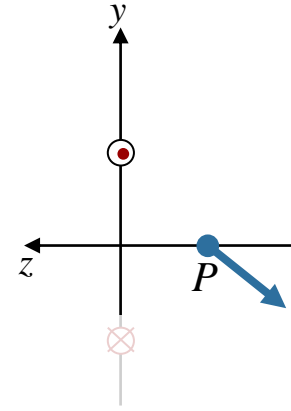
A



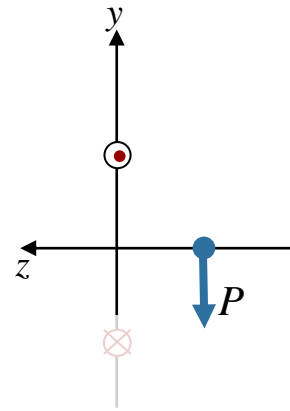
B



C



D

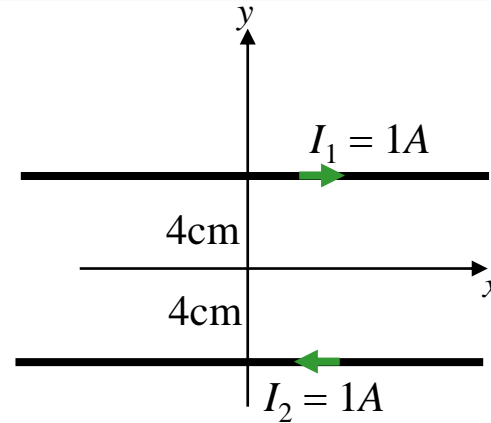


E

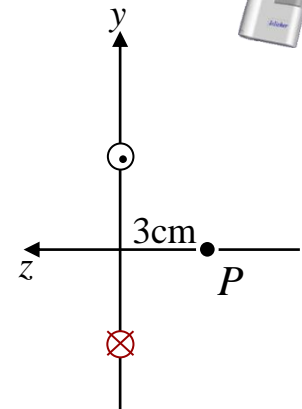
Calculation



Two parallel horizontal wires are located in the vertical (x,y) plane as shown. Each wire carries a current of $I = 1A$ flowing in the directions shown.



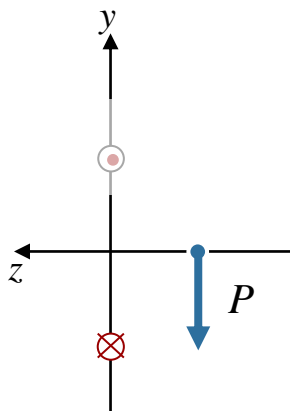
Front view



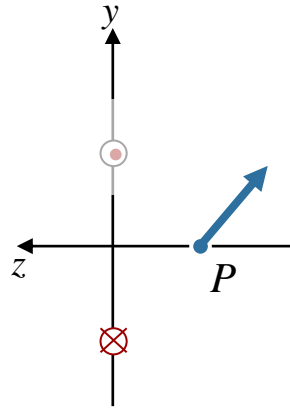
Side view

What is the B field at point P ?

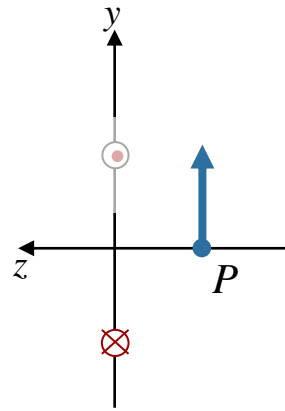
What is the direction of *Magnetic Field* at P produced by the bottom current I_2 ?



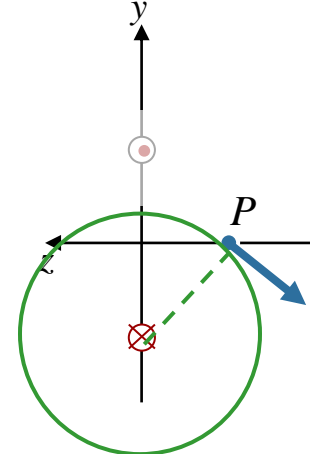
A



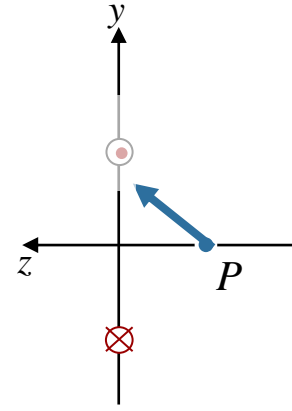
B



C



D

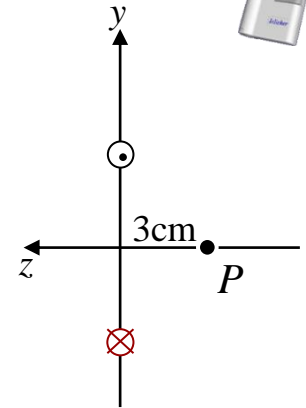
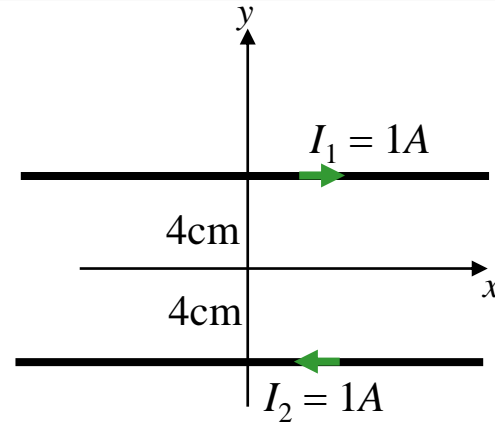


E

Calculation



Two parallel horizontal wires are located in the vertical (x,y) plane as shown. Each wire carries a current of $I = 1A$ flowing in the directions shown.

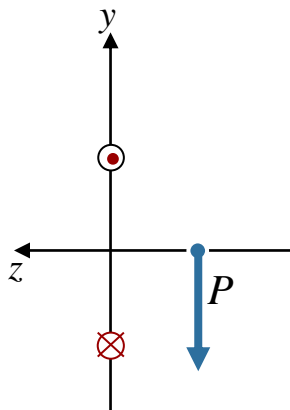


What is the B field at point P ?

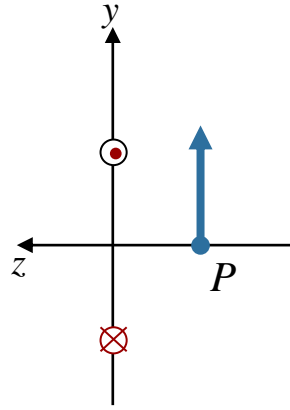
What is the direction of *Magnetic Field* at P ?

Front view

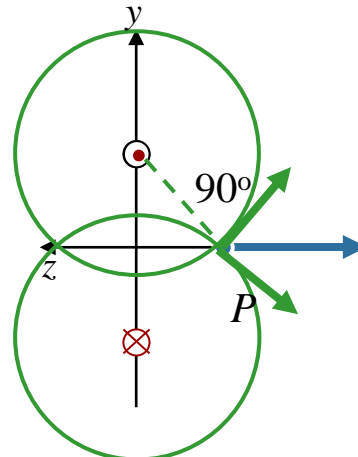
Side view



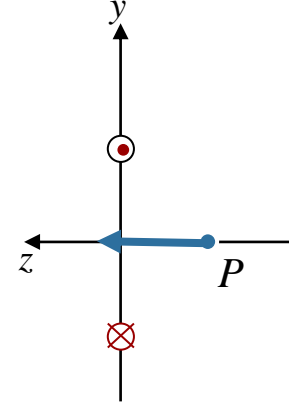
A



B



C

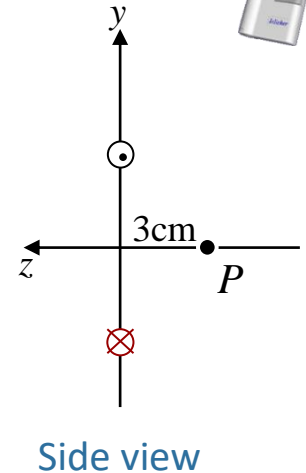
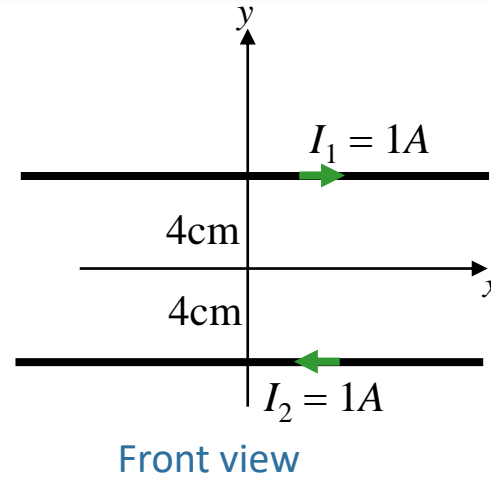


D

Calculation



Two parallel horizontal wires are located in the vertical (x,y) plane as shown. Each wire carries a current of $I = 1A$ flowing in the directions shown.



What is the B field at point P ?

$$B = \frac{\mu_0 I}{2\pi r}$$

What is the magnitude of B at P produced by the top current I_1 ?

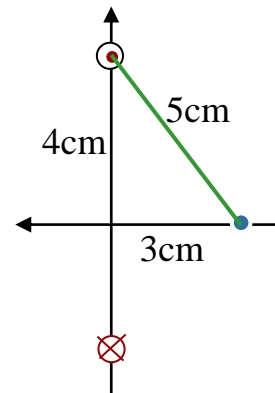
$$(\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A})$$

- A) $4.0 \times 10^{-6} \text{ T}$ B) $5.0 \times 10^{-6} \text{ T}$ C) $6.7 \times 10^{-6} \text{ T}$

What is r ?

r = distance from wire axis to P

$$B = \frac{\mu_0 I}{2\pi r} = \frac{(4\pi \times 10^{-7}) \times 1}{2\pi r} = 40 \times 10^{-7}$$

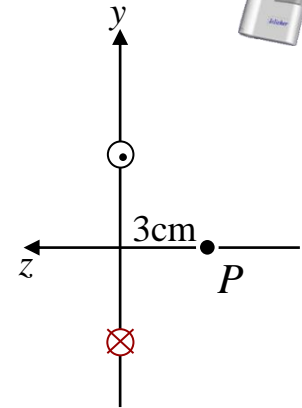
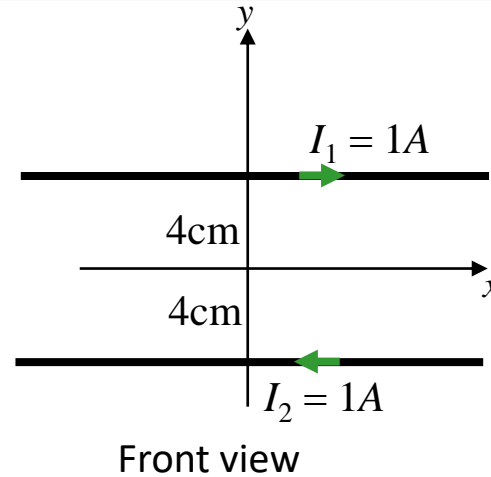


$$r = \sqrt{3^2 + 4^2} = 5\text{cm}$$

Calculation



Two parallel horizontal wires are located in the vertical (x,y) plane as shown. Each wire carries a current of $I = 1A$ flowing in the directions shown.

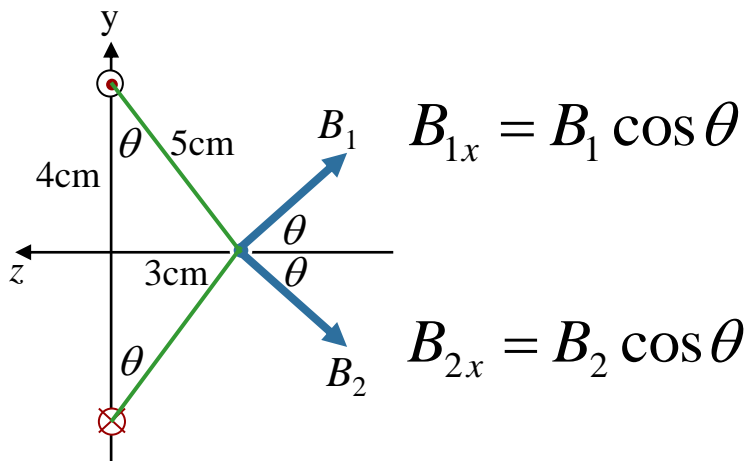


What is the B field at point P ?

$$B_{top} = 4 \times 10^{-6} T$$

What is the magnitude of B at P ? ($\mu_0 = 4\pi \times 10^{-7} T - m/A$)

- A) $3.2 \times 10^{-6} T$ B) $4.8 \times 10^{-6} T$ C) $6.4 \times 10^{-6} T$ D) $8.0 \times 10^{-6} T$



$$\Rightarrow B_x = 2B_1 \cos \theta = 2 \times 4 \times 10^{-6} \times \left(\frac{4}{5} \right) = 6.4 \times 10^{-6}$$



Have a great weekend!