Tugasan 4

1. Janakan data mtcars dalam R

```
data = mtcars
head(mtcars,10)
```

```
##
                      mpg cyl disp hp drat
                                                 wt qsec vs am gear carb
## Mazda RX4
                     21.0
                            6 160.0 110 3.90 2.620 16.46
## Mazda RX4 Wag
                     21.0
                            6 160.0 110 3.90 2.875 17.02
                                                                         4
## Datsun 710
                     22.8
                            4 108.0 93 3.85 2.320 18.61
                     21.4
## Hornet 4 Drive
                            6 258.0 110 3.08 3.215 19.44
                                                                         1
## Hornet Sportabout 18.7
                            8 360.0 175 3.15 3.440 17.02
## Valiant
                     18.1
                            6 225.0 105 2.76 3.460 20.22
                                                                         1
## Duster 360
                     14.3
                            8 360.0 245 3.21 3.570 15.84
## Merc 240D
                     24.4
                                      62 3.69 3.190 20.00
                                                                         2
                            4 146.7
                                                              0
                                                           1
## Merc 230
                     22.8
                            4 140.8 95 3.92 3.150 22.90
                                                                         2
                                                           1
                            6 167.6 123 3.92 3.440 18.30
                                                                         4
## Merc 280
                     19.2
```

2. Skalakan data tersebut.

```
mtcars_scaled = scale(mtcars)
head(mtcars_scaled,10)
```

```
##
                           mpg
                                      cyl
                                                 disp
                                                              hp
                                                                       drat
                                                                  0.5675137
## Mazda RX4
                     0.1508848 -0.1049878 -0.57061982 -0.5350928
## Mazda RX4 Wag
                     0.1508848 - 0.1049878 - 0.57061982 - 0.5350928
                     0.4495434 -1.2248578 -0.99018209 -0.7830405
## Datsun 710
                                                                  0.4739996
## Hornet 4 Drive
                     0.2172534 -0.1049878 0.22009369 -0.5350928 -0.9661175
## Hornet Sportabout -0.2307345 1.0148821
                                          1.04308123 0.4129422 -0.8351978
## Valiant
                    -0.3302874 -0.1049878 -0.04616698 -0.6080186 -1.5646078
## Duster 360
                    -0.9607889 1.0148821 1.04308123
                                                      1.4339030 -0.7229809
## Merc 240D
                     0.7150178 -1.2248578 -0.67793094 -1.2351802
                                                                  0.1747545
## Merc 230
                     0.4495434 -1.2248578 -0.72553512 -0.7538702
                                                                  0.6049193
## Merc 280
                    -0.1477738 -0.1049878 -0.50929918 -0.3454858
                                                                  0.6049193
##
                              wt
                                       qsec
                                                    ٧s
                                                               am
## Mazda RX4
                    -0.610399567 -0.7771651 -0.8680278
                                                       1.1899014
                                                                  0.4235542
## Mazda RX4 Wag
                    -0.349785269 -0.4637808 -0.8680278 1.1899014
                                                                  0.4235542
## Datsun 710
                    -0.917004624
                                 0.4260068
                                             1.1160357
                                                       1.1899014
                                                                  0.4235542
## Hornet 4 Drive
                    -0.002299538
                                  0.8904872
                                             1.1160357 -0.8141431 -0.9318192
## Hornet Sportabout 0.227654255 -0.4637808 -0.8680278 -0.8141431 -0.9318192
## Valiant
                     0.248094592
                                 1.3269868
                                             1.1160357 -0.8141431 -0.9318192
## Duster 360
                     0.360516446 -1.1241264 -0.8680278 -0.8141431 -0.9318192
## Merc 240D
                    -0.027849959
                                  1.2038715
                                             1.1160357 -0.8141431
                                                                   0.4235542
## Merc 230
                    -0.068730634 2.8267546
                                            1.1160357 -0.8141431
                                                                  0.4235542
## Merc 280
```

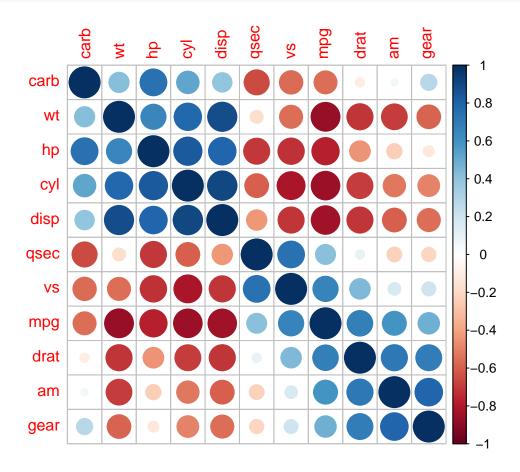
```
##
                            carb
                      0.7352031
## Mazda RX4
## Mazda RX4 Wag
                      0.7352031
## Datsun 710
                     -1.1221521
## Hornet 4 Drive
                     -1.1221521
## Hornet Sportabout -0.5030337
## Valiant
                     -1.1221521
## Duster 360
                      0.7352031
## Merc 240D
                     -0.5030337
## Merc 230
                     -0.5030337
## Merc 280
                      0.7352031
```

3. Jalankan analisis faktor untuk menurunkan dimensi data mtcars.

library(corrplot)

```
## Warning: package 'corrplot' was built under R version 4.4.2
## corrplot 0.95 loaded
```

corrplot(cor(mtcars_scaled), order='hclust')



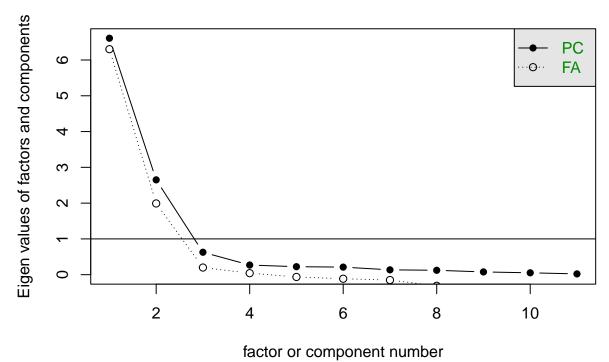
library(psych)

Warning: package 'psych' was built under R version 4.4.2

```
scree(mtcars_scaled)
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs = np.obs, : ## The estimated weights for the factor scores are probably incorrect. Try a ## different factor score estimation method.
```

Scree plot



4. Kenalpasti faktor pendam yang sesuai yang boleh menerangkan data asal.

```
F.A = factanal(mtcars_scaled, factors=3, scores = 'regression',rotation='varimax')
F.A

##
## Call:
## factanal(x = mtcars_scaled, factors = 3, scores = "regression", rotation = "varimax")
##
## Uniquenesses:
## mpg cyl disp hp drat wt qsec vs am gear carb
## 0.135 0.055 0.090 0.127 0.290 0.060 0.051 0.223 0.208 0.125 0.158
##
```

```
## Loadings:
##
        Factor1 Factor2 Factor3
## mpg
         0.643
                -0.478
                        -0.473
## cyl -0.618
                 0.703
                          0.261
## disp -0.719
                 0.537
                          0.323
## hp
        -0.291
                 0.725
                          0.513
## drat 0.804
                -0.241
## wt
        -0.778
                 0.248
                         0.524
## qsec -0.177
                -0.946
                        -0.151
## vs
         0.295
                -0.805
                        -0.204
## am
         0.880
## gear 0.908
                          0.224
  carb 0.114
                          0.719
##
                 0.559
##
##
                  Factor1 Factor2 Factor3
## SS loadings
                    4.380
                             3.520
                                     1.578
## Proportion Var
                    0.398
                             0.320
                                     0.143
## Cumulative Var
                    0.398
                             0.718
                                     0.862
##
## Test of the hypothesis that 3 factors are sufficient.
## The chi square statistic is 30.53 on 25 degrees of freedom.
## The p-value is 0.205
```

head(F.A\$scores,20)

```
##
                                    Factor2
                        Factor1
                                               Factor3
## Mazda RX4
                     0.84659011 0.672117481 -0.27829936
## Mazda RX4 Wag
                     0.72212550
                                0.383521909 0.02456662
## Datsun 710
                     0.68627400 -0.592149628 -0.56444514
## Hornet 4 Drive
                    -0.86578979 -0.673352726 -0.76659243
                    ## Hornet Sportabout
## Valiant
                    -1.06151049 -1.068850264 -0.38290802
## Duster 360
                    -0.55880772 1.244212537 -0.19899809
## Merc 240D
                     0.07740501 -1.500123830
                                           0.40929935
## Merc 230
                    -0.24200520 -2.610411470
                                            1.22842059
## Merc 280
                     0.18320755 -0.591355337
                                           0.91024316
## Merc 280C
                     0.09100657 -0.829974474 1.08883341
## Merc 450SE
                    ## Merc 450SL
                    -0.84060251
                                0.465272798 -0.32537080
## Merc 450SLC
                    ## Cadillac Fleetwood -1.43625243 -0.017745759
                                            1.38774949
## Lincoln Continental -1.41670671 -0.005943498
                                            1.51793494
## Chrysler Imperial
                    -1.23182157 0.177238534
                                           1.32548587
## Fiat 128
                     0.75376560 -0.908814970 -0.80869775
## Honda Civic
                     1.20771953 -0.470502250 -0.97181997
                     0.81876601 -0.981070416 -0.99396734
## Toyota Corolla
```

5. Berikan tafsiran yang bersesuaian bagi setiap faktor pendam terhadap data asal.

Factor 1: seems to be related to performance vehicle

• High positive loadings:

- Rear axle ratio (0.804)
- Transmission (0.880)
- Number of forward gears (0.908)
- Moderate negative loadings:
 - Miles/(US) gallon (-0.643)
 - Displacement (-0.719)
 - Weight (-0.778)

Factor 2: reflects engine characteristics and power

- High positive loadings:
 - Number of cylinders (0.703)
 - Gross horsepower (0.725)
 - -1/4 mile time (-0.946)
- Moderate negative loadings:
 - Engine Shape (-0.805)

Factor 3: seems to reflect heavier, less fuel-efficient vehicles

- High positive loadings:
 - Weight (0.524)
 - Number of carburetors (0.719)
- Moderate negative loadings:
 - Miles (-0.473)
 - Gross horsepower (0.513)

Summary of Factors:

- 1. **Factor 1** seems to be related to **performance** vehicles, with manual transmissions, higher gear ratios, and larger engine sizes that are less fuel-efficient.
- 2. Factor 2 reflects engine characteristics and power, including high horsepower and large engine displacement, likely representing powerful vehicles with a focus on engine strength rather than fuel efficiency or acceleration speed.
- 3. Factor 3 seems to reflect heavier, less fuel-efficient vehicles with potentially more complex carburetor systems and greater emphasis on weight and engine characteristics rather than speed or fuel economy.