

## SEMESTER EXAM REVIEW

1. Sketch a possible graph over the interval  $[-4, 4]$  for a function  $g$  that has the stated properties.

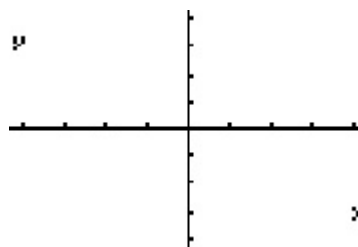
is defined

exists

is not continuous at  $x = 1$

does not exist

is not differentiable at  $x = 3$ , but is continuous



2. Determine the value of  $k$  such that the function  $h$  is continuous everywhere.

3- 4. Find the limit as a number,  $\infty$ , or does not exist. Show supportive work. Place answer on the line provided.

3.

4.

5 - 6. If  $\lim_{x \rightarrow 2} f(x) = 5$  and  $\lim_{x \rightarrow 2} g(x) = 3$ , find:

5.

6.

7 - 9. Given:

7. State the  $x$  - value, if any, at which  $h$  is not continuous.

8. State where the removable discontinuity occurs, if any.

9. State the equation of the vertical asymptote(s), if any, of the graph.

10. Multiple Choice: If  $\lim_{x \rightarrow 2} f(x) = 5$  and  $\lim_{x \rightarrow 2} g(x) = 3$ , which of the following will calculate the derivative of  $f(g(x))$  at  $x = 2$ ?

A.

B.

C.  
these

D.

E. None of

11 - 12. The tangent line to the graph of  $y = h(x)$  at the point  $(1, 2)$  passes through the point  $(2, 4)$ . Find:

11.  $h(4)$

12.

13. Find an equation for the tangent line to the graph of \_\_\_\_\_ at the point where  $x = 1$ .

14. Find \_\_\_\_\_ implicitly:

15. A point moves along the curve \_\_\_\_\_ in such a way that the  $y$ -value is decreasing at the rate of 2 units per second.

At what rate is  $x$  changing when \_\_\_\_\_? Work must be shown.

Given Rate: \_\_\_\_\_

Find: \_\_\_\_\_

\_\_\_\_\_ is changing at a rate of \_\_\_\_\_

16. In words, what is a derivative?

17 - 18. Find all critical numbers, if any, of the function.

2.

19. The derivative of  $y = f(x)$  is given as \_\_\_\_\_. At what value(s) of  $x$  does the graph of  $f$  have a relative minima \_\_\_\_\_ and a relative maxima \_\_\_\_\_.

20. Sand being emptied from a hopper at the rate of 10 \_\_\_\_\_ forms a conical pile whose height is always twice its radius. At what rate is the radius of the pile increasing when its height is 5 feet?

Given Rate :

Equation:

Find: