

Lecture 3 Problem Set

Problem 2.71

1. What is wrong with this code?

This function guarantees in a lot of cases that the sign extension is not kept when we mask with 0xFF.

2. Give a correct implementation using only left and right shifts along with 1 subtraction.

```
int xbyte(packed_t word, int bytenum)
{
    /* Shift all the way to the right */
    int t = (3 - bytenum) << 3;

    /* Shift back all the way to the left */
    int32_t res = (word << t) >> 24;
}
```

Problem 2.76

NOTE: I'll assume that the variable we're multiplying is called x.

1. K = 17

```
x = (x << 4) + x
```

2. K = -7

```
x = x - (x << 3)
```

3. K = 60

```
x = (x << 6) - (x << 2)
```

4. K = -112

```
x = (x << 4) - (x << 7)
```

Problem 2.81

1. $(x < y) == (-x > -y)$

Signed range is asymmetric, so supplying $x = \text{INT_MIN}$ (or equivalent minimum value) and almost anything for y will probably break this system, as negating INT_MIN gives us INT_MIN , and nothing is strictly smaller than INT_MIN , which is required for the righthand expression to be true.

2. $((x+y) << 4) + y - x == 17*y + 15*x$

True. $16*(x+y) + y - x == 16x - x + 16y + y == 17y + 15x$. There are no corner cases like there were in the last one.

3. $\sim x + \sim y + 1 == \sim(x+y)$

True. First, $\sim x + \sim y + 1 == -x - 1 + (\sim y) == -x - 1 - y$. Then, $\sim(x+y) == -(x+y) - 1 == -x - y - 1$. So they are equivalent.

4. $(ux - uy) == -(\text{unsigned})(y - x)$

False. If $x = -10$ and $y = -1$, then $10 - 1 == 9$ and $-(\text{unsigned})(-10 - (-1)) ==$

5. $((x \gg 2) \ll 2) \leq x$

True. The binary representation of a number increases monotonically as the number itself increases even in the case of negative numbers (*i.e.*, for any number n , the binary representation of $n + 1$ is larger than n was) and therefore when you divide by two and multiply by a power of 2 (*e.g.*, $x = x/n * 2^n$), you will at best end up with the same number, and at worst, a smaller number.