## Assignment 42

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## 1

Say we have some search problem  $\Pi$  with input size n. Since every search problem in NP can be expressed as a series of decision problems, the worst case is that we have to examine both possible answers ("yes" and "no") for every single input  $\in [0, n]$ . So there are somewhere around  $2^n$  subproblems.

If it's nondeterministically solvable in polynomial time (that is, given a machine that can explore an arbitrary number of solutions simultaneously—the definition of NP), all these subproblems themselves must be also solvable in polynomial time, let's say specifically p(n).

So each problem costs at most p(n) for some polynomial function p. If there are  $2^n$  subproblems at worst, then the total cost for all problems in NP must be  $O(2^{p(n)})$ .