

## Assignment 26

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### 1

First find  $\phi(N)$ :  $(p-1)(q-1) = 504$ . This is the Euler Totient Function; we'll call it  $n$  for short. Given that  $e = 5$ . The smallest  $x$  such that  $5x \equiv 1 \pmod{504}$  is  $x = 101$ . Thus  $\mathbf{d} = \mathbf{101}$ . Pretty simple.

### 2

Encrypting 55 is pretty straightforward. Given  $m^e \pmod{n}$ , we have  $55^5 \pmod{504} = 55$ . If that doesn't seem right, we can reverse it given  $m^d \pmod{504}$ :  $55^{101} \pmod{504} = 55$ .

### 3

Given the above, this is super simple.  $189^{101} \pmod{504} = 189$ . We can confirm this odd result by  $189^5 \pmod{504} = 189$ .