



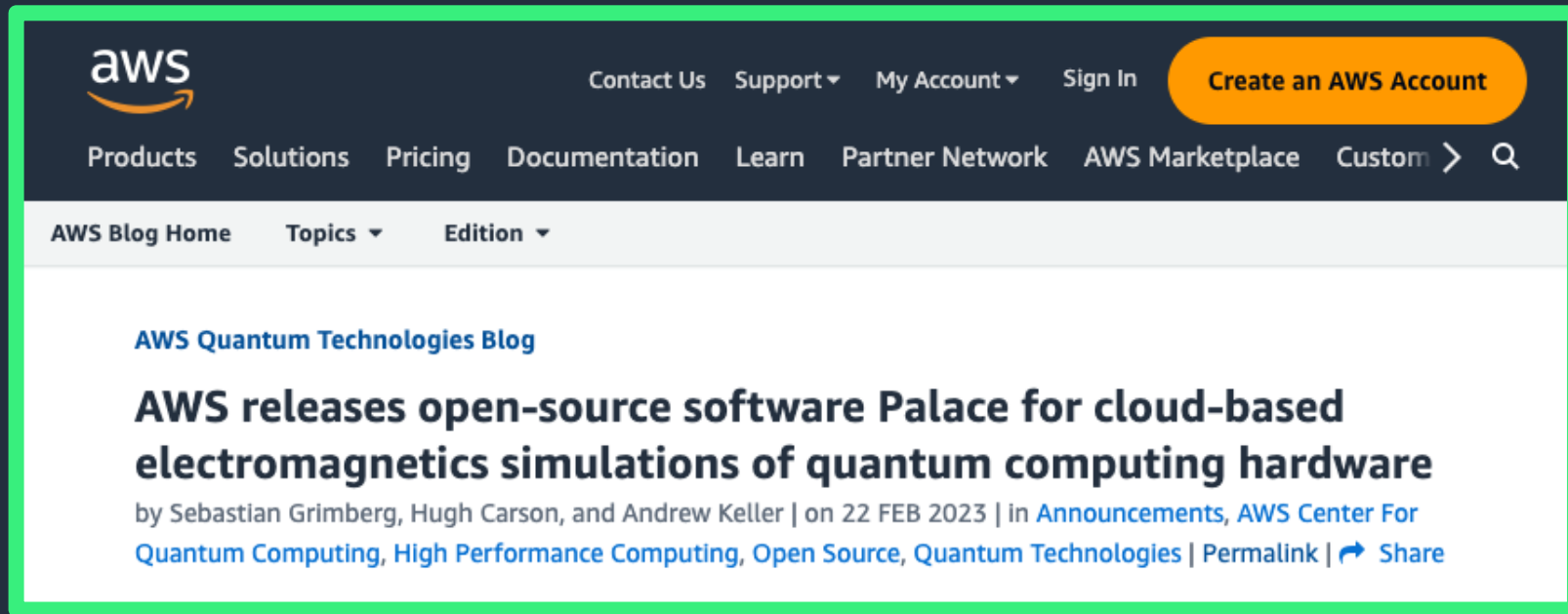
MFEM COMMUNITY WORKSHOP 2023

Palace: PArallel LArge-scale Computational Electromagnetics

Sebastian Grimberg

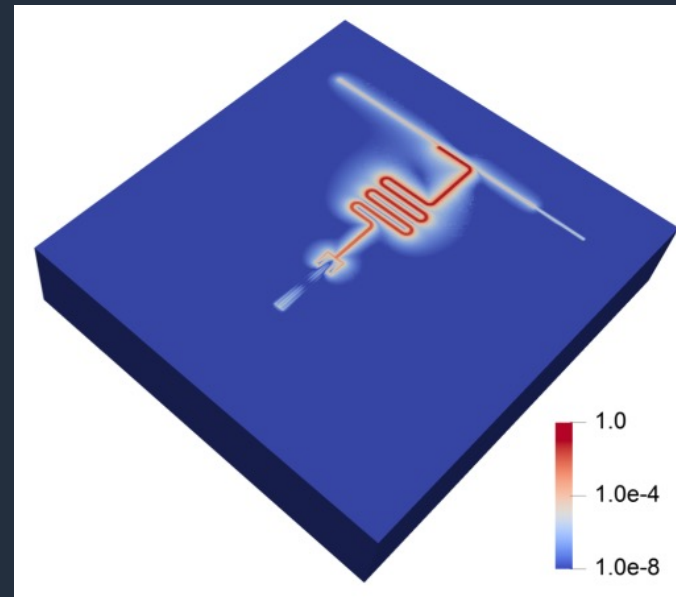
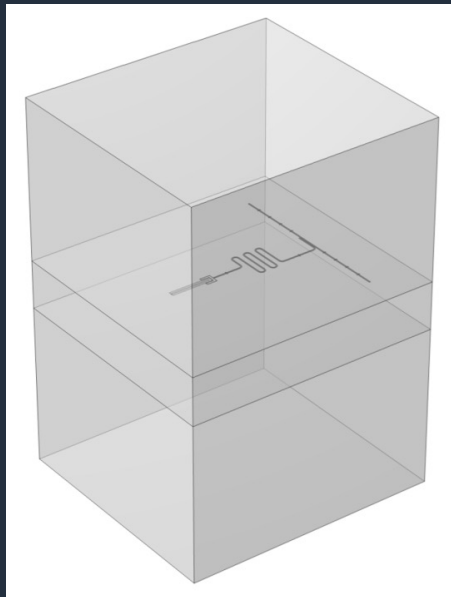
Sr. Applied Scientist
AWS

Palace: 3D finite element solver for computational electromagnetics



Palace is developed at the AWS Center for Quantum Computing to enable the design of quantum computing hardware

Palace: 3D finite element solver for computational electromagnetics



Uses MFEM and libCEED to perform full-wave 3D electromagnetic simulations in the frequency and time domain

Frequency and time domain electromagnetics models

Driven

$$\nabla \times (\mu^{-1} \nabla \times \mathbf{E}) + i\omega\sigma\mathbf{E} - \omega^2\varepsilon\mathbf{E} = 0$$

$$\mathbf{n} \times \mathbf{E} = 0, \mathbf{x} \in \partial\Omega_D$$

$$\mathbf{n} \times (\mu^{-1} \nabla \times \mathbf{E}) + i\omega Z_s^{-1} \mathbf{n} \times (\mathbf{n} \times \mathbf{E}) = \mathbf{U}_s, \mathbf{x} \in \partial\Omega_R$$

Transient

$$\nabla \times (\mu^{-1} \nabla \times \mathbf{E}) + \sigma \frac{\partial \mathbf{E}}{\partial t} + \varepsilon \frac{\partial^2 \mathbf{E}}{\partial t^2} = 0$$

$$\mathbf{n} \times \mathbf{E} = 0, \mathbf{x} \in \partial\Omega_D$$

$$\mathbf{n} \times (\mu^{-1} \nabla \times \mathbf{E}) + Z_s^{-1} \mathbf{n} \times \left(\mathbf{n} \times \frac{\partial \mathbf{E}}{\partial t} \right) = \mathbf{U}_s, \mathbf{x} \in \partial\Omega_R$$

- Lumped ports, numeric wave ports, scattering parameter calculations
- Anisotropic and lossy material properties
- Absorbing boundary conditions

Frequency and time domain electromagnetics models

Eigenmode

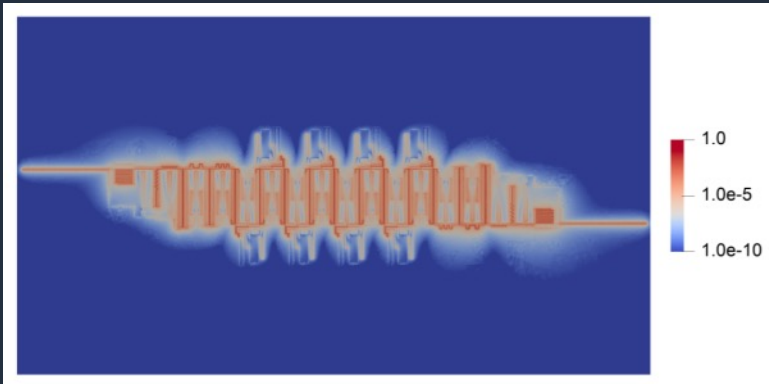
$$(K + i\omega C - \omega^2 M) u = 0$$

$$\begin{bmatrix} 0 & I \\ K & iC \end{bmatrix} \begin{bmatrix} u \\ \omega u \end{bmatrix} = \omega \begin{bmatrix} I & 0 \\ 0 & M \end{bmatrix} \begin{bmatrix} u \\ \omega u \end{bmatrix}$$

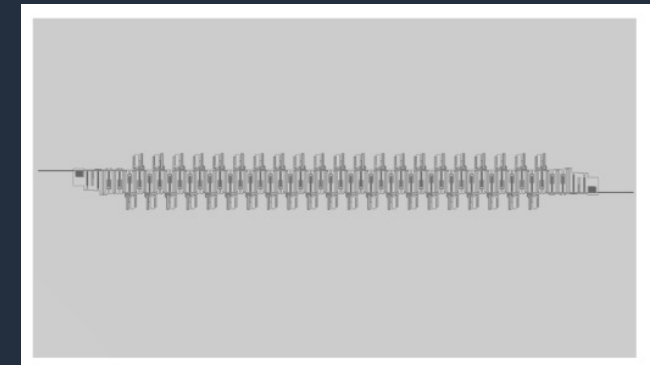
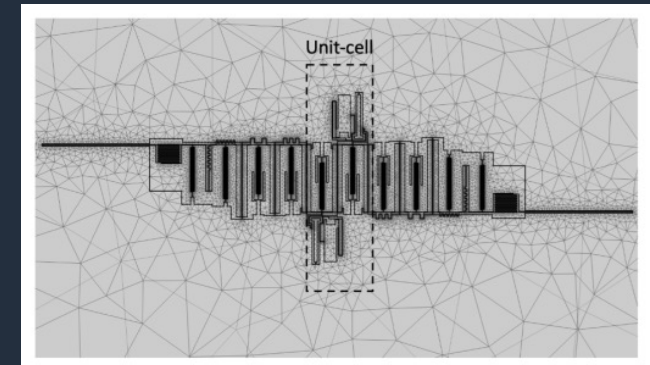
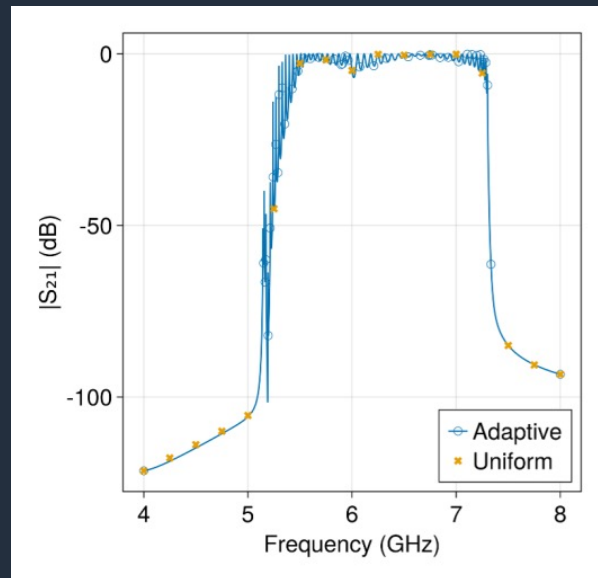
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Large-scale cloud-based electromagnetics simulation

- 3D models ranging from 242.2 million to 1.4 billion degrees of freedom
- Adaptive fast frequency sweep simulations: Smallest in 45 min. (10 samples), largest in 4 hours (40 samples)
- Up to 12,800 AWS Graviton3E cores (hpc7g.16xlarge), EFA network

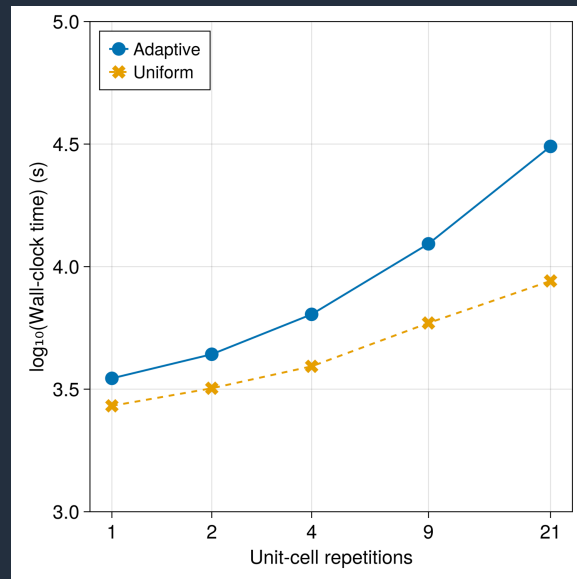


[AWS Quantum Technologies Blog](#)

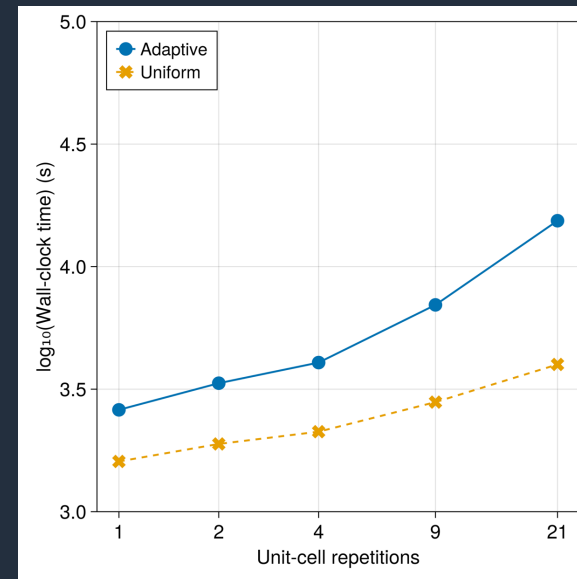


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Feb. 2023
c6gn.16xlarge



Oct. 2023
1.69x – 2.19x improvement

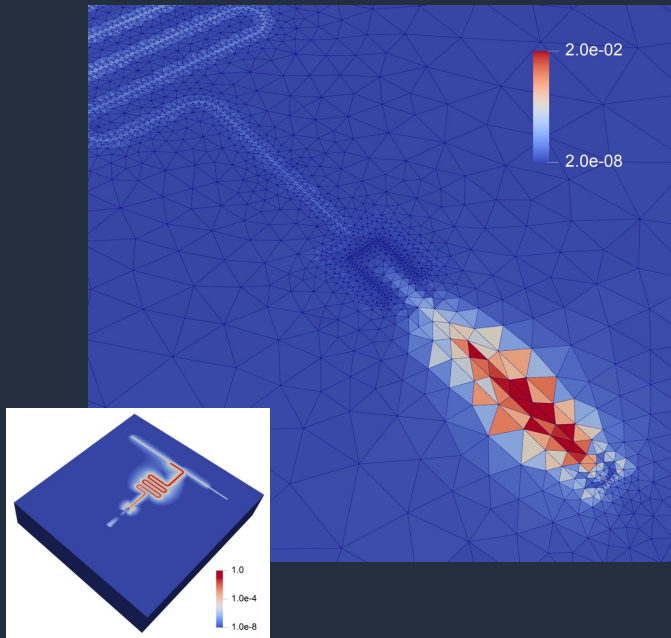
Adaptive mesh refinement

- Conforming refinement + rebalancing on tetrahedral meshes, general non-conforming refinement + coarsening + rebalancing for mixed meshes
- Non-conforming AMR for high-order Nédélec elements with triangular faces

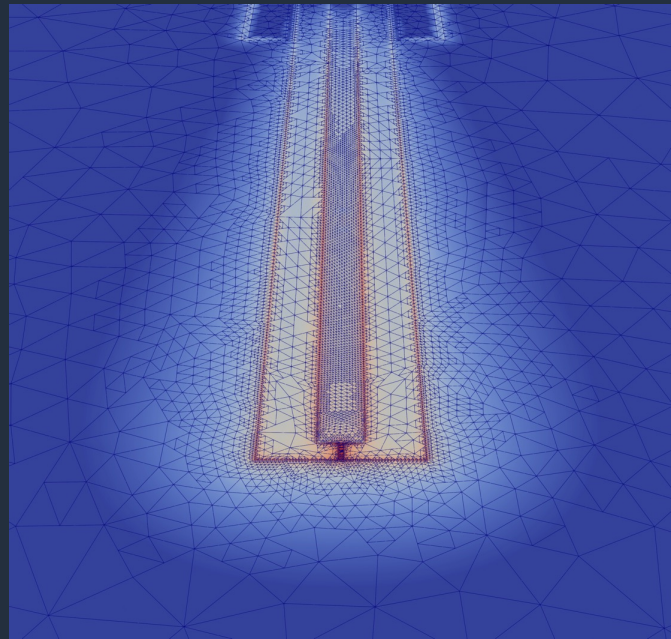
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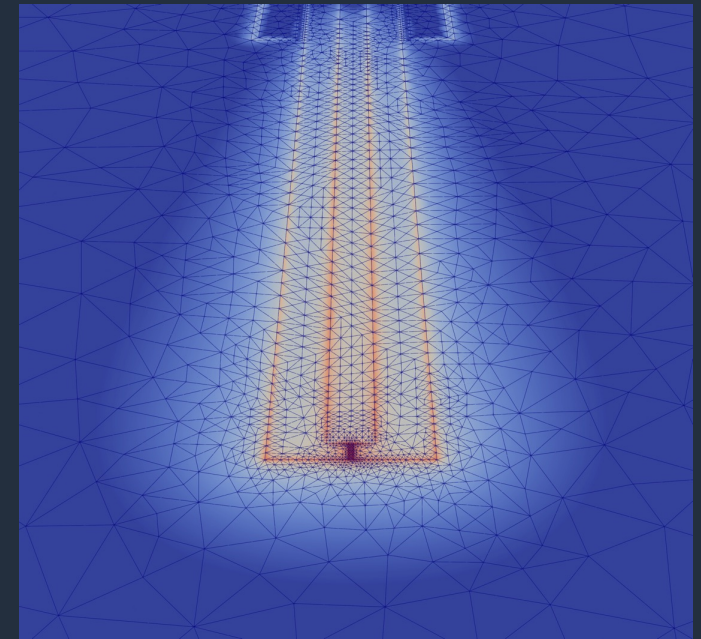
Indicator



Non-conforming refinement

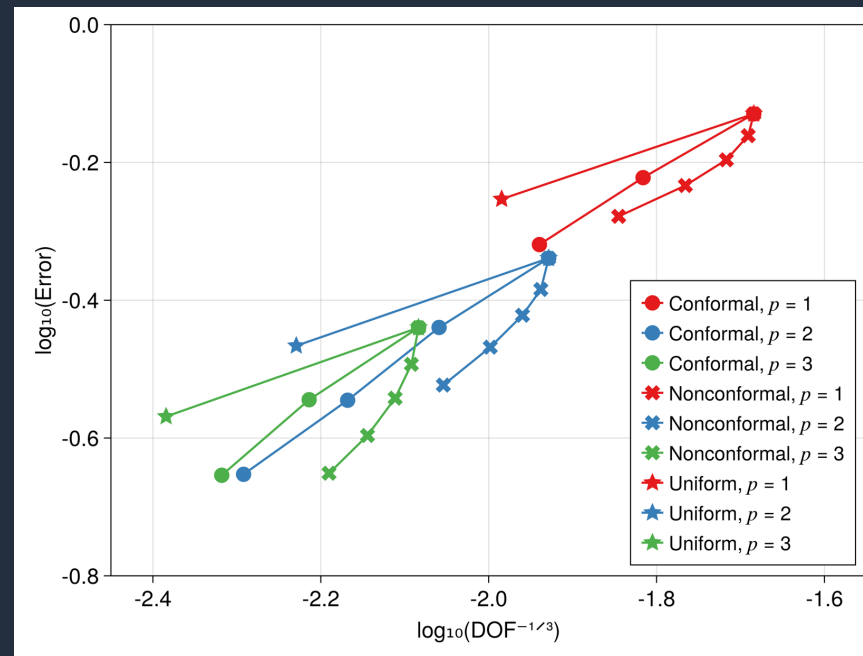


Conforming refinement



Adaptive mesh refinement

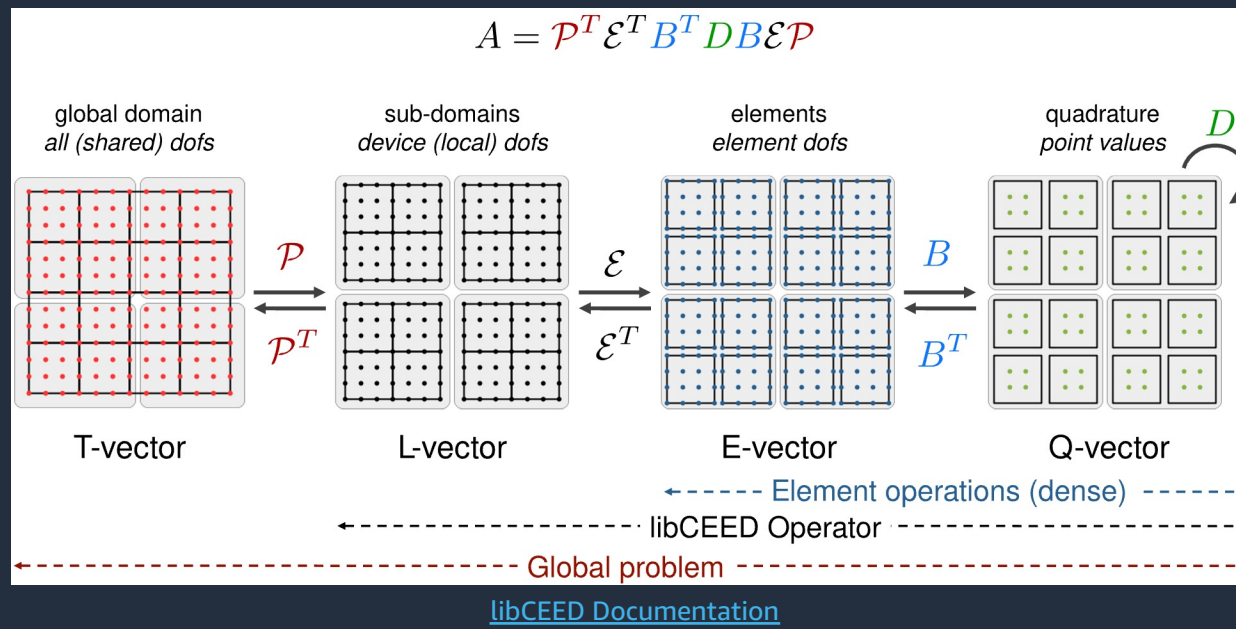
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Operator assembly and linear solvers

Operator assembly and linear solvers

- Matrix-free p -multigrid preconditioning with partial assembly of high-order operators
- Partial assembly support: Simplex elements and mixed meshes, (mixed) operators on H^1 -, $H(\text{curl})$ -, and $H(\text{div})$ -conforming spaces, boundary integrators, matrix-valued coefficients, all using libCEED

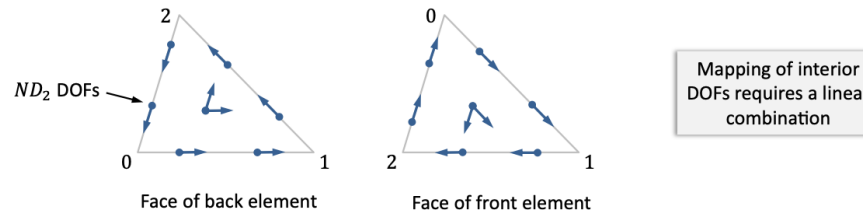


Operator assembly and linear solvers

- Special element restriction operator $\mathcal{E}_{ND} = \mathcal{T}\mathcal{E}_{H^1}$ for high-order Nédélec elements with triangular faces

Highlight: Higher-order H(curl) on tetrahedra

- Added support for *arbitrary global-to-element* DOF transformations
- For most FE types the DOF transformation is *permutation + optional sign flip*
- Allows for any tetrahedron orientation with HO ($p \geq 2$) H(curl) FEs
- Also needed for HO ($p \geq 2$) H(curl) FEs on prisms and pyramids



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- Auxiliary-space smoothing for non-static Maxwell problems (time and frequency domain):

$$B = B_{ND} + GB_{H^1}G^T$$

(construct the operator $A_{H^1} = G^T A_{ND} G$ for B_{H^1} directly without a sparse matrix triple product)

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- Coarse solve ($p = 1$, real-valued $A_0 = \text{Re}\{A_0\} + \text{Im}\{A_0\}$):

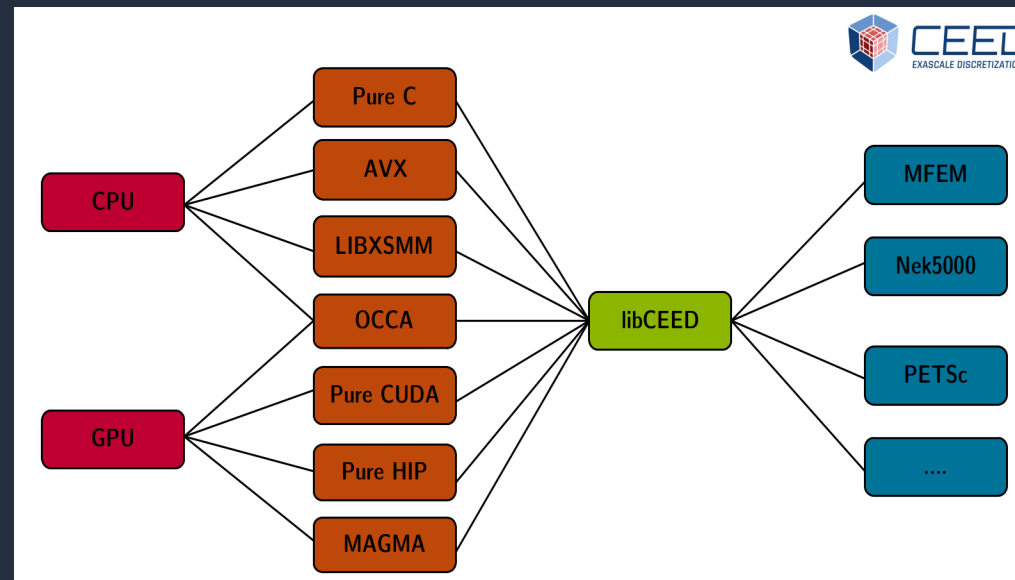
Electrostatics: Standard AMG (Hypre)

Magnetostatic and transient: Auxiliary-space Maxwell Solver (AMS)

Driven and eigenmode (complex symmetric, indefinite): AMS with SPD preconditioner matrix,
or parallel sparse-direct solve (SuperLU_DIST, STRUMPACK, MUMPS)

Backends and GPU support

- Runtime backend selection for performance portability
- Support for NVIDIA and AMD GPUs using MFEM and libCEED's CUDA and HIP backends
- *Work in progress, but expected to release in coming weeks*



[libCEED Documentation](#)

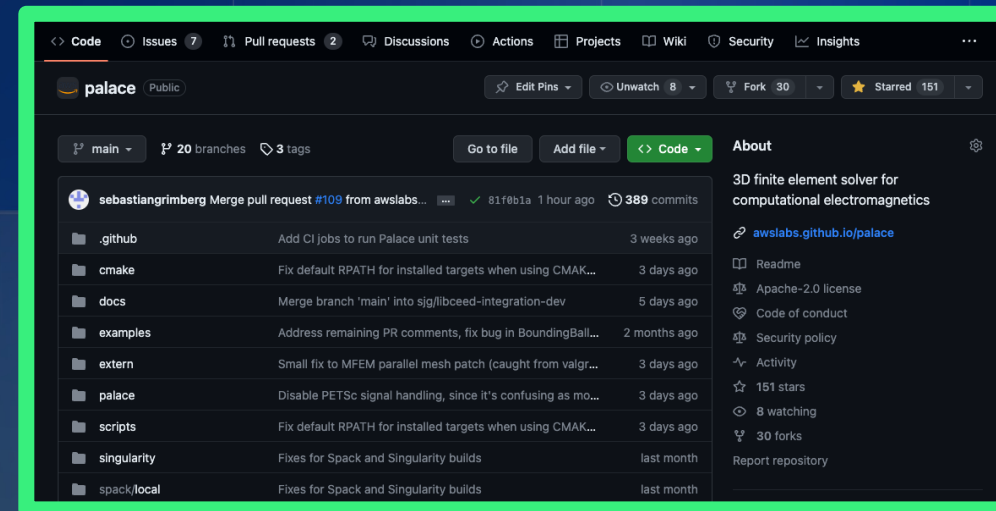


Thank you!

Sebastian Grimberg
sjg@amazon.com

Hugh Carson
hughcars@amazon.com

Andrew Keller
kllrak@amazon.com



<https://github.com/aws-labs/palace>