MTH-101AA, Quiz II, 29-01-2021 Question 1, 5:10-5:20 PM

(1) Discuss the convergence or divergence of the improper integral

$$\int_{0}^{2} \frac{x(1+\sin^2 x)}{2-x} \ dx.$$

[4]

MTH-101AA, Quiz II, 29-01-2021 Question 2, 5:20-5:32 PM

(2) Let $f:[0,1] \to \mathbb{R}$ be a differentiable function such that $\int_0^1 f(t)dt = 1$ and f(0) = 0. Show that there exists $c \in (0,1)$ such that f'(c) = 2.

MTH-101AA, Quiz II, 29-01-2021 Question 3, 5:32-5:45PM

(3) Let R be the region bounded by the y-axis, the line y = 2x and the curve $y = 3-x^2$. Let S_1 be the solid obtained by revolving R about the x-axis and S_2 be the solid obtained by revolving R about the line y = -1. Find the volume of S_1 by the Washer Method and the volume of S_2 by the Shell Method.