

**End-Semester Exam: Question 3**

**Time: 10.10 am - 10.45 am**

**Q3.** (a) A farmer wants to build a rectangular box without a top, with a volume of 500 cubic meters. Find the dimension of the box such that the amount of material required is minimum.

[10]

(b) Consider the function

$$f(x, y) = (y - 4x^2)(y - x^2).$$

Show that  $(0, 0)$  is a critical point of  $f$  and find out whether it is a local maximum or local minimum or a saddle point for the function. [6]