

$$w_0 + w_1 x$$

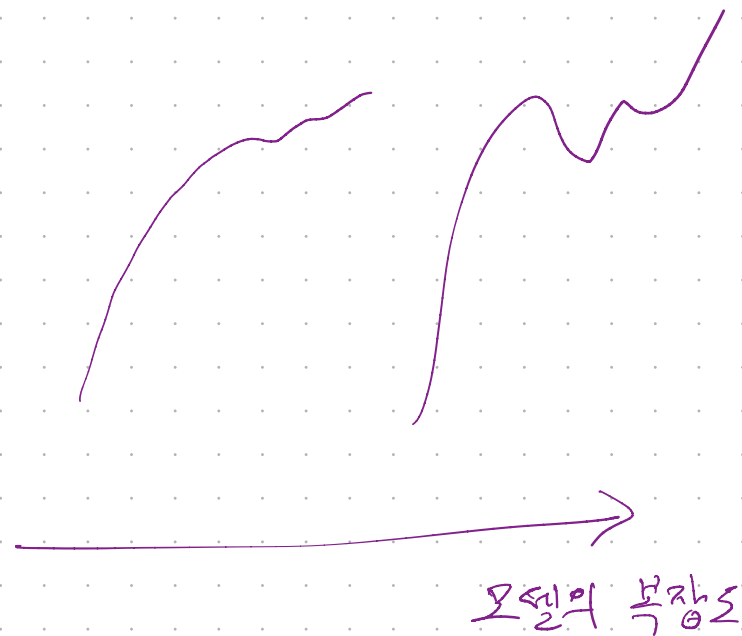
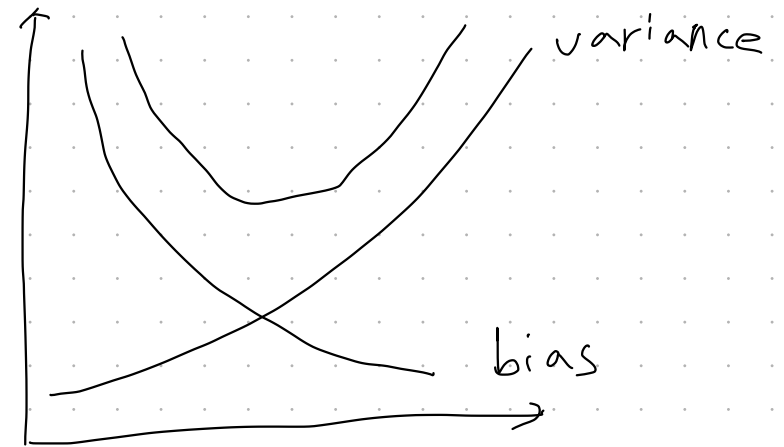
$$\checkmark w_0 + w_1 x + w_2 x^2$$

$$w_0 + w_1 x + w_2 x^2 + w_3 x^3 + w_4 x^4$$

모델의 복잡도

under-fitting = high bias

over-fitting = high variance



모델의 복잡도

$$|y' - y|^2 = \text{편차를 줄이는 방향} = \text{loss} \rightarrow \frac{\min(\text{loss})}{\text{훈련}}$$

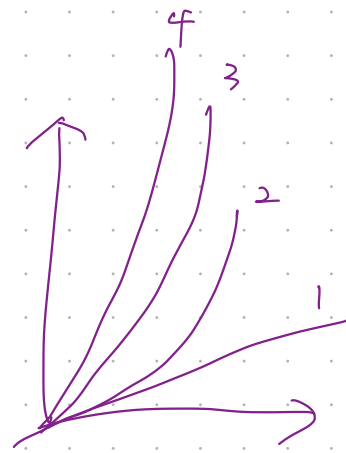
$$w_0 + w_1x + w_2x^2 + w_3x^3 + w_4x^4$$

$$\rightarrow w_0 + w_1x + w_2x^2 + \boxed{w_3x^3 + w_4x^4} \Rightarrow 0 \text{ 으로 가까이}$$

$$\begin{pmatrix} \text{loss} + L_1 \\ \text{loss} + L_2 \end{pmatrix} \quad \text{형태로 변환}$$

$$\frac{\min(\text{new loss})}{\text{훈련}}$$

$$\min_{\mathbf{w}} \left( w_0 + w_1 x + w_2 x^2 + w_3 x^3 + w_4 x^4 + \ell_1 \right)$$



$$\min_{\mathbf{w}} \left( \sum (w x) + \lambda \sum w \right) \quad \lambda \text{ 값을 조정}$$

$d = \text{learning rate}$

$$\left( w_{\text{다음}} = w - d | \hat{y} - y |^2 \right) = \text{loss function}$$

$$\min_{\mathbf{w}} \left( w - d \left( w_0 + w_1 x_i + w_2 x_i^2 + w_3 x_i^3 + w_4 x_i^4 \right) + \lambda w \right)$$

$$x^3 \Rightarrow 0 \quad x^4 \Rightarrow 0$$

$$\lambda \Rightarrow 100, 1000$$

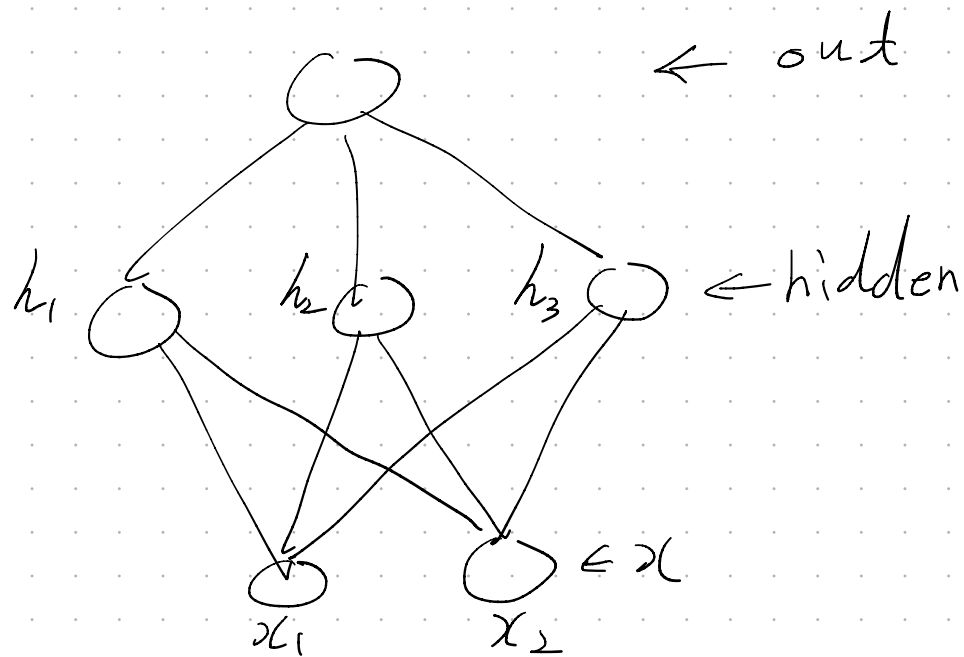
$\lambda$  커지면

점점 라기  $\lambda$  값을 조정 라면?

$$w_0 + w_1 x + w_2 x^2 + (w_3 \times 0.0000.1) + (w_4 \times 0.000.1)$$

$$\left( \sum_{i=1}^n \text{loss}_i + \lambda w \right) \Rightarrow \ell_1$$

$$\left( \sum_{i=1}^n \text{loss}_i + \lambda w^2 \right) \Rightarrow \ell_2$$



$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \quad h = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \end{bmatrix}$$

$$x^T W = h$$

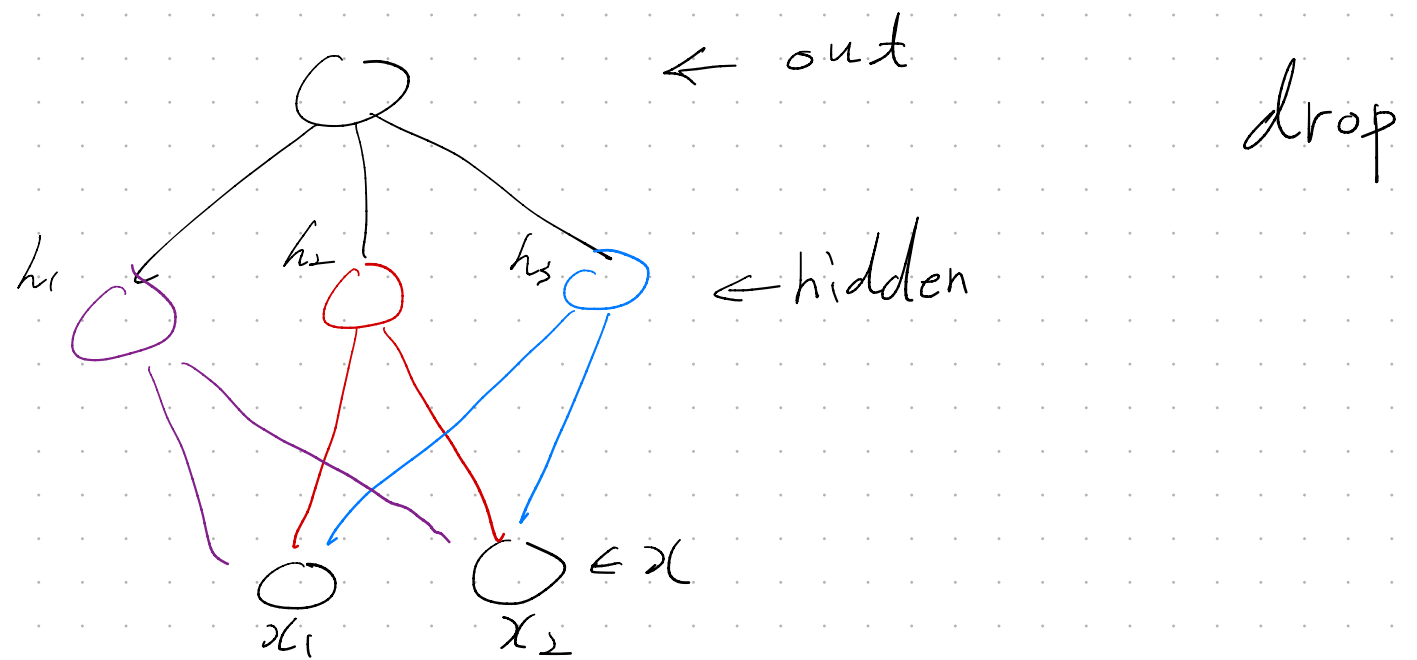
$$W = \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \end{bmatrix}$$

$$\begin{bmatrix} x_1 & x_2 \end{bmatrix} \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \end{bmatrix} = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \end{bmatrix}$$

$i = x$  index

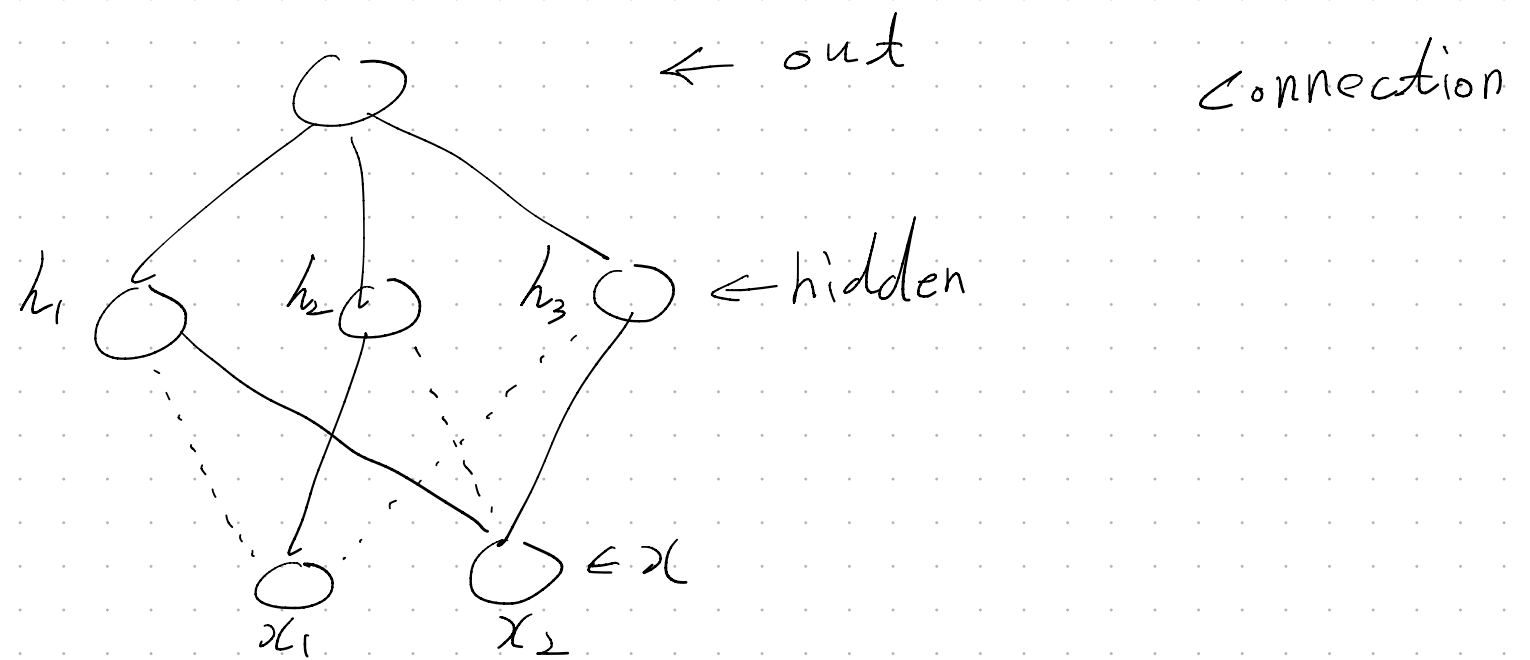
$j = h$  index





$$[x_1 \ x_2] \begin{bmatrix} \boxed{w_{11}} & \boxed{w_{12}} & \boxed{w_{13}} \\ \boxed{w_{21}} & \boxed{w_{22}} & \boxed{w_{23}} \end{bmatrix} = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \end{bmatrix}$$

$$w[:, -1, :] \rightarrow h_3 \text{ skip}$$



$$[x_1 \ x_2] \begin{bmatrix} 0 & w_{12} & 0 \\ w_{21} & 0 & w_{23} \end{bmatrix} = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \end{bmatrix}$$

↓  $\exists \Phi$

$$\begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \end{bmatrix}$$

$$\|w\|_2 \leq r$$

