# Supplement to "Interaction structure constrains the emergence of conventions in group communication"

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# Feedback

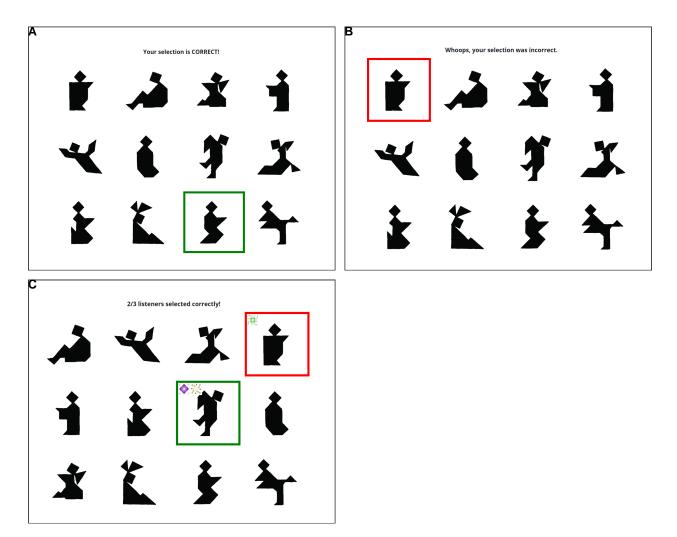


Figure 1: Feedback shown to participants. In low-coherence games, matchers saw feedback as shown in A and B. In all games, describers saw feedback like in C; icons were associated with players and indicated who selected which. In high feedback games, matchers saw grids like C, but with text as in A and B.

## Additional game transcripts

Table 1: Additional examples from 6-player thick games for the same image across repetitions. Describers are indicated with an asterisk.



## 6-person thick game

Rep 1: 5/5 correct

Q\* oh no. okay. this one is similar to the one i called minnesota, so like pretty simple, with just a distinct "head" diamond and then a body beneath

Q\* the body has sort of sloping shoulders

P BEAN SHAPED BODY?

O with a small triangle on the bottom right?

 $Q^*$  yeah i think so! bean is a good description lol

Q\* bean body

Rep 2: 5/5 correct

Q\* bean body!!

Rep 3: 5/5 correct

Q\* bean body!

Rep 4: 5/5 correct

Q\* bean body!

Rep 5: 5/5 correct

Q\* you guys are doin' great. :) bean body for this one

Rep 6: 5/5 correct

Q\* bean body for this one

#### 6-person thick game

Rep 1: 2/5 correct

V\* This shape hasn't got much sticking out. Small triangle pointing right, tilted square on top

Y Is the triangle on the right at the bottom?

V\* Long tall shape, not far off symmetrical.

V\* Yes triangle bottom right

W Are their two triangles on it?

X does it look like a rabbit?

V\* Not the rabbit

X does it look like someone on their back kicking a square soccer ball

V\* It's like one block like a gemstone

V\* but square on top

V\* Not on back

 $V^*$  It's the one with the least sharp corners I think

V\* One long gem shape with small triangle bottom right, tilted square on top

Rep 2: 4/5 correct

V\* Long tall shape. Little triangle sticking out bottom right. Diamond on top

Rep 3: 3/5 correct

V\* Long tall hexagon, triangle bottom right, diamond on top

Rep 4: 4/5 correct

V\* Long hexagon

V\* little triangle bottom right

V\* Diamond top

Rep 5: 4/5 correct

V\* Long hexagon.

V\* Diamond on top

V\* little triangle bottom right

Rep 6: 4/5 correct

V\* Long hexagon

V\* Triangle bottom right

Table 2: Additional examples from 6-player thin games for the same image across repetitions. Describers are indicated with an asterisk.

| 6-person thin game                                      |  |
|---|--|
| Rep 1: 2/5 correct                                      |  |
| J* Looks like a skinnier candle but with a              |  |
| shadow at the bottom                                    |  |
| K 🤔   |  |
| H 🗸   |  |
| J* The top square looks like the flame                  |  |
| J* It has a triangle leading to that flame              |  |
| I X   | 6-person thin game                             |
| Rep 2: 3/5 correct                                      | Rep 1: 2/5 correct                             |
| K 3   | A* Square on top                               |
| I* the simplest image in the whole, no much             | A* At the bottom of the base part of it sticks |
| issues  | out to the right                               |
| J 🤌   | A* The base has 8 faces (8 sides of the shape) |
| L 3   | C V  |
| I* 1 square as the head                                 | A* The square balances on a triangular point   |
| L 😕   | of the base                                    |
| J 🤔   | A* It is a thick base shape, the bottom curves |
| Н 🤔   | right  |
| K 3   | D V  |
| I* candle with more missing chunks                      | Rep 2: 5/5 correct                             |
| Rep 3: 1/5 correct                                      | B* tombstone and its shadow with a rotated     |
| L* looks like a candle with more chunks miss-           | square on top                                  |
|   | D V  |
| ing<br>J  | F 🗸  |
| I 3   | C 🤔  |
|   | Rep 3: 5/5 correct                             |
| L* The bottom part faces the right and forms a triangle | D* tombstone casting a shadow (sorry i've      |
| L* The top is a square                                  | pinched that from before)                      |
| I V   | C 🤔  |
| J X   | B 😂  |
| Rep 4: 3/5 correct                                      | E 🤔  |
| H* Candle one with shadow                               | C 🤔  |
| H* The straight one not the one with bits               | E 🤔<br>E 😕                                     |
| missing   |  |
| L 🤔   | D* square on top sitting on top of a triangle  |
| I 😂   | which is on top of a square, with 5 side       |
| L 💆   | shape at the bottom                            |
| H* Lower case j but the bottom swings to the            | Rep 4: 4/5 correct                             |
| right   | C* looks mummified                             |
| I V V V   | C* person with no limbs                        |
| Rep 5: 0/5 correct                                      | D 🗸  |
| K* Candle with chunks missing on the right              | B 🔅  |
|   | C* square atop, chunky with triangle bottom    |
| I   | right  |
|   | Rep 5: 5/5 correct                             |
| 1   | F* Gravestone casting shadow. Square on top    |
| left missing and added to the bottom right              | D V  |
| instead<br>K 🤔 🤔  | Rep 6: 5/5 correct                             |
| H 🗸   | E* tombstone                                   |
| I V   | D 🗸  |
| 1 V   |  |

## Number of games

In experiment 3, the 6\* player games did not all have 6 players, both because games continued as participants dropped out and because if there weren't enough players after 5 minutes of waiting, the game would start with whoever was there. All analyses use "intent to treat" and call these 6 player games.

The number of games goes up in some cases because only complete blocks (where the describer said something every trial) are analysed. If there was initial confusion and a desciber missed a trial, that block was excluded.

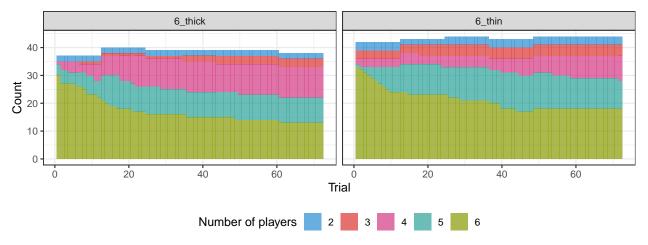


Figure 2: Number of players during 6 thin and 6 thick games in experiment 3. Blocks that were incomplete were excluded, so if a describer said nothing during a trial, that block was excluded.

Table 3: The number of games in each experiment and condition. Complete games finished all 6 blocks; partial games ended early due to disconnections, but contributed at least one complete block of data. 6\* indicates that some games started with fewer than 6 players or continued with fewer than 6 players after participants disconnected.

| Experiment        | Players | Complete | Partial | Total Participants |
|-------------------|---------|----------|---------|--------------------|
| 1: baseline       | 2       | 15       | 4       | 38                 |
| 1: baseline       | 3       | 18       | 2       | 60                 |
| 1: baseline       | 4       | 19       | 2       | 84                 |
| 1: baseline       | 5       | 17       | 3       | 100                |
| 1: baseline       | 6       | 12       | 6       | 108                |
| 2: same describer | 6       | 15       | 3       | 108                |
| 2: full feedback  | 6       | 13       | 4       | 102                |
| 2: thin           | 6       | 10       | 6       | 96                 |
| 3: thin           | 2       | 35       | 3       | 76                 |
| 3: thin           | 6*      | 44       | 0       | 235                |
| 3: thick          | 2       | 39       | 3       | 84                 |
| 3: thick          | 6*      | 38       | 2       | 222                |

## More on matcher utterances

Matchers' use of backchannel declined over the course of the game. The use of emoji in the thin games is not directly comparable to matcher language use in thick games, since some emoji usage (such as the green checkmark) are most likely equivalent to non-referential matcher language ("got it" etc.) that was excluded. The higher rate of emoji use versus referential language thus could be due to its non-equivalence, a lower level of accuracy in thin games, or matchers having a lower threshold for sending emojis compared to writing out clarifications.

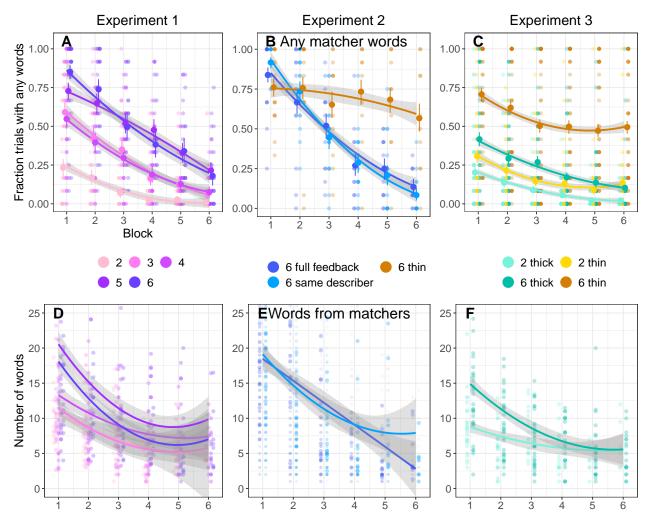


Figure 3: Matcher contributions. A-C: Fraction of trials where any matcher said anything that was referential. Dots are per game averages. Smooths are binomial fit lines. D-F: On trials where at least one matcher contributed, the number of words of referential language produced by matchers. Dots are per game averages. Smooths are quadratic fit lines. Y-axis is truncated, and a few outliers points are not visible.

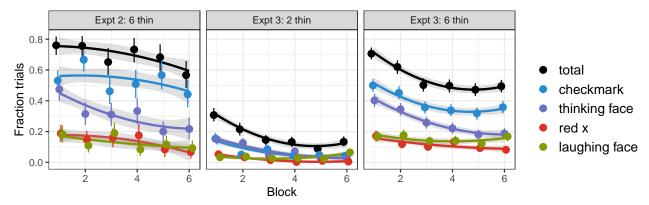


Figure 4: Fraction of trials on which at least one matcher produced the labelled emoji. Fraction of trials when any emoji was produced are shown in black. Dots are per condition, per block estimates with 95% bootstrapped CIs. Smooths are binomial fit lines.

We note a deviation from the pre-registration here in the analysis of the emojis. In the pre-registration we said we would "analyse the distribution of emoji's produced as a function of block and its relation to accuracy and speaker utterance length." We did not do this beyond the visualization shown here.

## Additional measure of convergence

The main text included the graph for convergence comparing utterances from blocks 1-5 to the utterance from block 6. Here we show two other measures of semantic shifts for descriptions for the same tangram in the same game: similarity to the first utterance and similarity to the next utterance.

Similarity to the first utterance is not very informative (but we pre-registered it). Similarity to the next utterance is what actually drives the convergence phenomena: pairs of utterances from adjacent blocks become closer together over time.

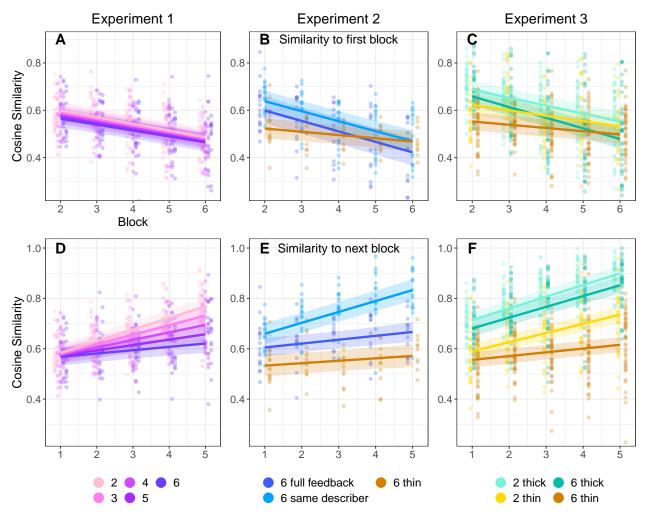


Figure 5: Additional measures of convergence and divergence. A-C is the similarity between utterances on a given block to the first block utterance for the same image, in the same game. Dots are per-game averages, smooths are quadratic. D-F is the similarity between utterances on a given block to the corresponding utterances in the next block. Dots are per-game averages, smooths are quadratic.

## Distinctiveness of tangrams

An additional measure of convergence/divergence patterns is how different tangrams get described in the same game – as nicknames evolve, different tangrams get more different descriptions.

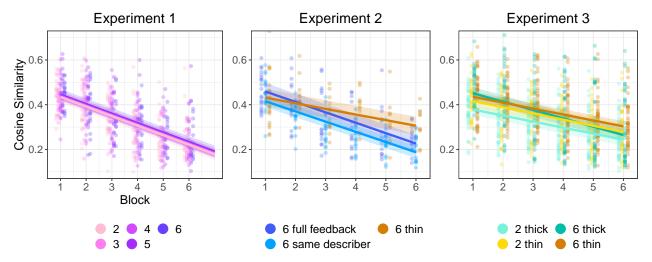


Figure 6: Divergence in descriptions of different tangrams. Cosine similarity between the descriptions of two different tangrams in the same block and group are shown. Dots are per-game averages, smooths are quadratic.

## Summaries of model outputs

The following sections contain model outputs. All models were run using BRMS. We report the priors and pre-registration status for each group of models. Tables provide the individual model formulae and the point estimates and 95% credible intervals for the fixed effects.

Note that for all models, block was 0 indexed, so intercepts are what happened during the first block.

## Accuracy models

Accuracy models were all run as logistic models with normal(0,1) priors for both betas and sd. This model was not explicitly included in the experiment 1 and 2 pre-registrations; it was included with more ambitious mixed effects (which did not run in a timely manner) in the experiment 3 pre-registration.

Table 4: Experiment 1 logistic model of matcher accuracy: correct.num  $\sim$  block  $\times$  numPlayers + (1|gameId)

| Est.  | 95% CrI               |
|-------|-----------------------|
| 2.10  | [1.57, 2.65]          |
| 0.44  | [0.31, 0.58]          |
| -0.02 | [-0.05, 0.01]         |
| -0.07 | [-0.2,  0.05]         |
|       | 2.10<br>0.44<br>-0.02 |

Table 5: Experiment 2: 6 same describer logistic model of matcher accuracy: correct.num  $\sim$  block + (1|gameId)

| Term               | Est.           | 95% CrI                     |
|--------------------|----------------|-----------------------------|
| Intercept<br>block | $1.78 \\ 0.45$ | [1.4, 2.19]<br>[0.39, 0.52] |

Table 6: Experiment 2: 6 full feedback logistic model of matcher accuracy: correct.num  $\sim$  block + (1|gameId)

| Term               | Est.           | 95% CrI                      |
|--------------------|----------------|------------------------------|
| Intercept<br>block | $1.35 \\ 0.47$ | [0.59, 2.06]<br>[0.39, 0.54] |

Table 7: Experiment 2: 6 thin logistic model of matcher accuracy: correct.num  $\sim$  block + (1|gameId)

| Term      | Est. | 95% CrI      |
|-----------|------|--------------|
| Intercept | 0.88 | [0.64, 1.12] |
| block     | 0.23 | [0.19, 0.28] |

Table 8: Experiment 3 logistic model of matcher accuracy: correct.num  $\sim$  block  $\times$  gameSize  $\times$  channel + (1|gameId)

| Term                              | Est.  | 95% CrI        |
|-----------------------------------|-------|----------------|
| Intercept                         | 1.69  | [1.39, 1.99]   |
| block                             | 0.41  | [0.32, 0.5]    |
| block:channelthin                 | -0.07 | [-0.18, 0.04]  |
| block:gameSize6                   | -0.34 | [-0.43, -0.25] |
| block: game Size 6: channel thin  | 0.07  | [-0.05, 0.19]  |
| channelthin                       | -0.36 | [-0.78, 0.05]  |
| gameSize6                         | -0.64 | [-1.05, -0.25] |
| ${\tt game Size 6: channel thin}$ | 0.31  | [-0.22, 0.87]  |

## Reduction models

## Primary reduction model

Reduction models were run as linear models with an intercept prior of normal(12,20), a beta prior of normal(0,10), an sd prior of normal(0,5) and a correlation prior of lkj(1). This model was pre-registered for each experiment and run with the mixed effects structure as pre-specified.

Table 9: Experiment 1: words  $\sim$  block  $\times$  numPlayers + (block|tangram) + (1|playerId) + (1|tangram:gameId) + (block|gameId)

| Term                      | Est.           | 95% CrI                         |
|---------------------------|----------------|---------------------------------|
| Intercept                 | 16.87          | [11.63, 21.89]                  |
| block<br>block:numPlayers | -3.36<br>-0.09 | [-4.56, -2.18]<br>[-0.37, 0.18] |
| numPlayers                | 1.60           | [0.62, 2.6]                     |

Table 10: Experiment 2: 6 same describer: words  $\sim$  block + (block|tangram) + (1|tangram:gameId) + (block|gameId)

| Term      | Est.  | 95% CrI        |
|-----------|-------|----------------|
| Intercept | 29.65 | [24.82, 34.49] |
| block     | -5.31 | [-6.35, -4.3]  |

Table 11: Experiment 2: 6 full feedback: words  $\sim$  block + (block|tangram) + (1|tangram:gameId) + (block|gameId)

| Term      | Est.  | 95% CrI        |
|-----------|-------|----------------|
| Intercept | 25.79 | [20.97, 30.29] |
| block     | -4.64 | [-5.81, -3.53] |

Table 12: Experiment 2: 6 thin: words  $\sim$  block + (block|tangram) + (1|tangram:gameId) + (block|gameId)

| Term      | Est. | 95% CrI        |
|-----------|------|----------------|
| Intercept | 20.3 | [17.37, 23.53] |
| block     | -2.1 | [-3.37, -1.12] |

Table 13: Experiment 3: words  $\sim$  block  $\times$  channel  $\times$  gameSize + (block  $\times$  channel  $\times$  gameSize|tangram) + (1|tangram:gameId) + (block|gameId)

| Term  | Est.  | 95% CrI   |
|---|---|---|
| Intercept block block:channelthin block:channelthin:gameSize6 block:gameSize6 channelthin | 14.74<br>-2.24<br>0.29<br>0.64<br>-1.22<br>0.80 | [11.68, 17.72]<br>[-2.92, -1.57]<br>[-0.56, 1.23]<br>[-0.59, 1.81]<br>[-2.06, -0.29]<br>[-2.85, 4.26] |
| channelthin:gameSize6<br>gameSize6  | -2.21<br>7.51                                   | [-7.16, 3.08]<br>[3.63, 11.3]   |

#### Extra reduction model

For experiment 1, we also pre-specified a model about whether the describer's correctness on the prior block (when they were a matcher) had an effect on how many words of description they produced. Priors were the same as for primary reduction model.

Table 14: Experiment 1: words  $\sim$  block  $\times$  numPlayers + block  $\times$  wasINcorrect + (block|tangram) + (1|playerId) + (1|tangram:gameId) + (block|gameId)

| Term               | Est.  | 95% CrI       |
|--------------------|-------|---------------|
| Intercept          | 12.16 | [6.48, 18.07] |
| block              | -2.17 | [-3.39, -1]   |
| block:numPlayers   | -0.22 | [-0.5, 0.06]  |
| block:wasINcorrect | 0.24  | [-0.24, 0.72] |
| numPlayers         | 2.09  | [0.88, 3.3]   |
| wasINcorrect       | 3.07  | [1.67, 4.45]  |

### Log reduction model

As an exploratory check, we reran some of the primary reduction models using the log number of words as the DV; otherwise model specifications and priors were the same.

Table 15: Experiment 1 log reduction: logwords  $\sim$  block  $\times$  numPlayers + (block|tangram) + (1|playerId) + (1|tangram:gameId) + (block|gameId)

| Term             | Est.  | 95% CrI        |
|------------------|-------|----------------|
| Intercept        | 2.75  | [2.48, 3.01]   |
| block            | -0.38 | [-0.47, -0.29] |
| block:numPlayers | 0.01  | [-0.01, 0.03]  |
| numPlayers       | 0.07  | [0.02,  0.12]  |

Table 16: Experiment 3 log reduction: logwords  $\sim$  block  $\times$  channel  $\times$  gameSize + (block  $\times$  channel  $\times$  gameSize|tangram) + (1|tangram:gameId) + (block|gameId)

| Term                        | Est.  | 95% CrI        |
|-----------------------------|-------|----------------|
| Intercept                   | 2.50  | [2.32, 2.69]   |
| block                       | -0.27 | [-0.32, -0.22] |
| block:channelthin           | 0.06  | [0, 0.14]      |
| block:channelthin:gameSize6 | 0.03  | [-0.06, 0.13]  |
| block:gameSize6             | -0.02 | [-0.09, 0.04]  |
| channelthin                 | 0.06  | [-0.17, 0.29]  |
| channelthin:gameSize6       | -0.13 | [-0.44, 0.18]  |
| gameSize6                   | 0.45  | [0.23, 0.67]   |

#### Matcher reduction models

These models were not pre-registered.

For the model of how often any matchers used the backchannel, the priors were normal(0,1) for both beta and sd.

For the model of how much was said on trials when matchers talked, the priors were the same as for the primary (describer) reduction model.

Table 17: Experiment 1: words  $\sim$  block  $\times$  numPlayers + (block|gameId)

| Term             | Est.  | 95% CrI        |
|------------------|-------|----------------|
| Intercept        | 4.72  | [0.09, 9.44]   |
| block            | -0.17 | [-1.53, 1.3]   |
| block:numPlayers | -0.41 | [-0.72, -0.11] |
| numPlayers       | 2.07  | [1, 3.12]      |

Table 18: Experiment 1: is.words  $\sim$  block  $\times$  numPlayers + (1|gameId)

| Term             | Est.  | 95% CrI        |
|------------------|-------|----------------|
| Intercept        | -2.67 | [-3.54, -1.79] |
| block            | -0.80 | [-0.97, -0.62] |
| block:numPlayers | 0.03  | [-0.01, 0.07]  |
| numPlayers       | 0.79  | [0.58, 0.98]   |

#### Initial utterance reduction model

These models were not pre-registered. They looked at describer reduction only on words that were produced prior to the first matcher message each trial. These models were only run on experimental conditions where matchers could contribute textual responses.

Reduction models were run as linear models with the same priors as the primary reduction model.

Table 19: Experiment 1: words  $\sim$  block  $\times$  numPlayers + (block|tangram) + (1|tangram:gameId) + (block|gameId)

| Term             | Est.  | 95% CrI        |
|------------------|-------|----------------|
| Intercept        | 18.66 | [14.58, 22.71] |
| block            | -3.56 | [-4.54, -2.55] |
| block:numPlayers | 0.27  | [0.03, 0.5]    |
| numPlayers       | -0.33 | [-1.14, 0.53]  |

Table 20: Experiment 2: 6 same describer: words  $\sim$  block + (block|tangram) + (1|tangram:gameId) + (block|gameId)

| Term      | Est.  | 95% CrI        |
|-----------|-------|----------------|
| Intercept | 18.06 | [14.76, 21.44] |
| block     | -2.49 | [-3.19, -1.79] |

Table 21: Experiment 2: 6 full feedback: words  $\sim$  block + (block|tangram) + (1|tangram:gameId) + (block|gameId)

| Term      | Est.  | 95% CrI        |
|-----------|-------|----------------|
| Intercept | 16.69 | [13.41, 20.02] |
| block     | -2.49 | [-3.34, -1.62] |

Table 22: Experiment 3: words  $\sim$  block  $\times$  gameSize + (block  $\times$  gameSize|tangram) + (1|tangram:gameId) + (block|gameId)

| Term            | Est.  | 95% CrI        |
|-----------------|-------|----------------|
| Intercept       | 13.88 | [11.62, 16.2]  |
| block           | -2.08 | [-2.66, -1.47] |
| block:gameSize6 | -0.65 | [-1.43, 0.14]  |
| gameSize6       | 5.13  | [2, 7.95]      |

# Linguistic content models

We ran a number of models predicting the cosine similarity between pairs of S-BERT embeddings of utterances. For all of these models, we used linear models with the priors normal(.5,.2) for intercept, normal(0,.1) for beta, and normal(0,.05) for sd.

These models were verbally described (but not formally specified) in the pre-registrations for experiment 2 in the full feedback and thin conditions and for experiment 3, for looking at divergence between games, convergence within games (compared to first block, next block, and last block utterances), and divergence between tangrams within games.

#### Convergence within games: comparison to last round

This is the primary convergence metric presented in the main paper.

Table 23: Experiment 1:  $sim \sim earlier \times condition + (1|tangram) + (1|gameId)$ 

| Term                              | Est.                     | 95% CrI   |
|-----------------------------------|--------------------------|---|
| Intercept<br>condition<br>earlier | 0.517<br>-0.008<br>0.089 | [0.458, 0.573]<br>[-0.021, 0.005]<br>[0.076, 0.102] |
| earlier:condition                 | -0.008                   | [-0.011, -0.005]                                    |

Table 24: Experiment 2: 6 same describer:  $sim \sim earlier + (1|tangram) + (1|gameId)$ 

| Term                 | Est.             | 95% CrI                          |
|----------------------|------------------|----------------------------------|
| Intercept<br>earlier | $0.499 \\ 0.086$ | [0.444, 0.556]<br>[0.078, 0.094] |

Table 25: Experiment 2: 6 full feedback:  $sim \sim earlier + (1|tangram) + (1|gameId)$ 

| Term                 | Est.             | 95% CrI                          |
|----------------------|------------------|----------------------------------|
| Intercept<br>earlier | $0.438 \\ 0.062$ | [0.389, 0.487]<br>[0.051, 0.072] |

Table 26: Experiment 2: 6 thin:  $sim \sim earlier + (1|tangram) + (1|gameId)$ 

| Term                 | Est.             | 95% CrI                         |
|----------------------|------------------|---------------------------------|
| Intercept<br>earlier | $0.498 \\ 0.023$ | [0.453, 0.54]<br>[0.013, 0.033] |

Table 27: Experiment 3:  $sim \sim earlier \times channel \times gameSize + (1|tangram) + (1|gameId)$ 

| Term                            | Est.   | 95% CrI          |
|---------------------------------|--------|------------------|
| Intercent                       | 0.581  | [0.542, 0.62]    |
| Intercept                       |        |                  |
| channelthin                     | -0.034 | [-0.08, 0.011]   |
| $channel thin: {\tt gameSize6}$ | 0.039  | [-0.021, 0.097]  |
| earlier                         | 0.080  | [0.074, 0.086]   |
| earlier:channelthin             | -0.025 | [-0.033, -0.017] |
| earlier:channelthin:gameSize6   | -0.035 | [-0.047, -0.025] |
| earlier:gameSize6               | 0.009  | [0.001,  0.017]  |
| gameSize6                       | -0.069 | [-0.113, -0.025] |

## Divergence across games

This is the divergence metric presented in the paper.

Table 28: Experiment 1:  $sim \sim block \times condition + (1|tangram)$ 

| Term            | Est.   | 95% CrI          |
|-----------------|--------|------------------|
| Intercept       | 0.468  | [0.429, 0.507]   |
| block           | -0.035 | [-0.038, -0.032] |
| block:condition | 0.001  | [0.001, 0.002]   |
| condition       | 0.002  | [0, 0.004]       |

Table 29: Experiment 2: 6 same describer:  $sim \sim block + (1|tangram)$ 

| Term      | Est.   | 95% CrI          |
|-----------|--------|------------------|
| Intercept | 0.484  | [0.442, 0.526]   |
| block     | -0.041 | [-0.043, -0.039] |

Table 30: Experiment 2: 6 full feedback:  $sim \sim block + (1|tangram)$ 

| Term      | Est.   | 95% CrI         |
|-----------|--------|-----------------|
| Intercept | 0.502  | [0.46, 0.546]   |
| block     | -0.038 | [-0.04, -0.035] |

Table 31: Experiment 2: 6 thin:  $sim \sim block + (1|tangram)$ 

| Term               | Est.         | 95% CrI                            |
|--------------------|--------------|------------------------------------|
| Intercept<br>block | 0.434 -0.004 | [0.406, 0.465]<br>[-0.006, -0.001] |

Table 32: Experiment 3:  $sim \sim block \times channel \times gameSize + (1|tangram)$ 

| Term                        | Est.   | 95% CrI          |
|-----------------------------|--------|------------------|
| Intercept                   | 0.411  | [0.368, 0.453]   |
| block                       | -0.024 | [-0.025, -0.023] |
| block:channelthin           | 0.004  | [0.002, 0.005]   |
| block:channelthin:gameSize6 | 0.017  | [0.015, 0.019]   |
| block:gameSize6             | -0.008 | [-0.01, -0.007]  |
| channelthin                 | 0.014  | [0.01, 0.018]    |
| channelthin:gameSize6       | -0.030 | [-0.035, -0.024] |
| gameSize6                   | 0.051  | [0.047,  0.055]  |

## Divergence across tangrams

This is an additional metric comparing the similiarities between descriptions for different tangrams within a game. It measures how distinct the descriptions for different tangram images are.

Table 33: Experiment 1:  $sim \sim block \times condition + (1|gameId)$ 

| Term                         | Est.             | 95% CrI                            |
|------------------------------|------------------|------------------------------------|
| Intercept<br>block           | 0.429<br>-0.043  | [0.382, 0.473]<br>[-0.046, -0.039] |
| block:condition<br>condition | $0.000 \\ 0.003$ | [-0.001, 0.001]<br>[-0.008, 0.014] |

Table 34: Experiment 2: 6 same describer:  $sim \sim block + (1|gameId)$ 

| Term      | Est.   | 95% CrI          |
|-----------|--------|------------------|
| Intercept | 0.416  | [0.389, 0.443]   |
| block     | -0.046 | [-0.048, -0.044] |

Table 35: Experiment 2: 6 full feedback:  $sim \sim block + (1|gameId)$ 

| Term      | Est.   | 95% CrI          |
|-----------|--------|------------------|
| Intercept | 0.459  | [0.422, 0.496]   |
| block     | -0.047 | [-0.049, -0.044] |

Table 36: Experiment 2: 6 thin:  $sim \sim block + (1|gameId)$ 

| Term      | Est.   | 95% CrI          |
|-----------|--------|------------------|
| Intercept | 0.432  | [0.393, 0.471]   |
| block     | -0.025 | [-0.028, -0.022] |

Table 37: Experiment 3:  $sim \sim block \times channel \times gameSize + (1|gameId)$ 

| Term                               | Est.             | 95% CrI                             |
|------------------------------------|------------------|-------------------------------------|
| Intercept                          | 0.378            | [0.352, 0.404]                      |
| block<br>block:channelthin         | -0.027<br>-0.001 | [-0.029, -0.025]<br>[-0.003, 0.002] |
| block:channelthin:gameSize6        | 0.001            | [0.008, 0.002]                      |
| block:gameSize6                    | -0.010           | [-0.013, -0.008]                    |
| channelthin                        | 0.038            | [-0.001, 0.082]                     |
| channelthin:gameSize6<br>gameSize6 | -0.053 $0.073$   | [-0.115, 0]  [0.035, 0.113]         |

## Convergence to next

We also looked at how similar an utterance was to the next block utterance for the same image in the same group: this can be thought of as the derivative of the to-last comparison. (Although cosine similarities are not actually additive in the same way integrals are).

Table 38: Experiment 1:  $sim \sim earlier \times condition + (1|tangram) + (1|gameId)$ 

| Term              | Est.   | 95% CrI          |
|-------------------|--------|------------------|
| Intercept         | 0.591  | [0.541, 0.641]   |
| condition         | -0.004 | [-0.014, 0.006]  |
| earlier           | 0.063  | [0.051, 0.075]   |
| earlier:condition | -0.008 | [-0.011, -0.006] |

Table 39: Experiment 2: 6 same describer:  $sim \sim earlier + (1|tangram) + (1|gameId)$ 

| Term                 | Est.             | 95% CrI                         |
|----------------------|------------------|---------------------------------|
| Intercept<br>earlier | $0.660 \\ 0.043$ | [0.619, 0.702]<br>[0.037, 0.05] |

Table 40: Experiment 2: 6 full feedback:  $sim \sim earlier + (1|tangram) + (1|gameId)$ 

| Term                 | Est.             | 95% CrI                          |
|----------------------|------------------|----------------------------------|
| Intercept<br>earlier | $0.605 \\ 0.015$ | [0.569, 0.643]<br>[0.006, 0.024] |

Table 41: Experiment 2: 6 thin:  $sim \sim earlier + (1|tangram) + (1|gameId)$ 

| Term                 | Est.             | 95% CrI                     |
|----------------------|------------------|-----------------------------|
| Intercept<br>earlier | $0.533 \\ 0.010$ | [0.49, 0.578]<br>[0, 0.019] |

Table 42: Experiment 3:  $\sin \sim \text{earlier} \times \text{channel} \times \text{gameSize} + (1|\text{tangram}) + (1|\text{gameId})$ 

| Term                          | Est.   | 95% CrI          |
|-------------------------------|--------|------------------|
| Intercept                     | 0.714  | [0.682, 0.746]   |
| channelthin                   | -0.124 | [-0.159, -0.088] |
| channelthin:gameSize6         | 0.000  | [-0.051, 0.049]  |
| earlier                       | 0.046  | [0.041, 0.052]   |
| earlier:channelthin           | -0.010 | [-0.018, -0.002] |
| earlier:channelthin:gameSize6 | -0.018 | [-0.029, -0.007] |
| earlier:gameSize6             | -0.003 | [-0.011, 0.004]  |
| gameSize6                     | -0.034 | [-0.069, 0.003]  |

## Divergence from first

We also looked at how similar an utterance was to the first block utterance for the same image. This is not very informative because first round utterances tend to be pretty noisy with lots of hedges and filler words.

Table 43: Experiment 1:  $sim \sim later \times condition + (1|tangram) + (1|gameId)$ 

| Term                            | Est.                      | 95% CrI   |
|---------------------------------|---------------------------|---|
| Intercept<br>condition<br>later | 0.647<br>-0.010<br>-0.030 | [0.591, 0.705]<br>[-0.022, 0.003]<br>[-0.041, -0.019] |
| later:condition                 | 0.001                     | [-0.041, -0.019]<br>[-0.002, 0.004]                   |

Table 44: Experiment 2: 6 same describer:  $sim \sim later + (1|tangram) + (1|gameId)$ 

| Term      | Est.   | 95% CrI          |
|-----------|--------|------------------|
| Intercept | 0.680  | [0.628, 0.728]   |
| later     | -0.042 | [-0.049, -0.035] |

Table 45: Experiment 2: 6 full feedback:  $sim \sim later + (1|tangram) + (1|gameId)$ 

| Term               | Est.         | 95% CrI                            |
|--------------------|--------------|------------------------------------|
| Intercept<br>later | 0.644 -0.044 | [0.584, 0.706]<br>[-0.052, -0.037] |

Table 46: Experiment 2: 6 thin:  $sim \sim later + (1|tangram) + (1|gameId)$ 

| Term      | Est.            | 95% CrI                           |
|-----------|-----------------|-----------------------------------|
| Intercept | 0.537<br>-0.014 | [0.49, 0.584]<br>[-0.023, -0.004] |

Table 47: Experiment 3:  $sim \sim later \times channel \times gameSize + (1|tangram) + (1|gameId)$ 

| Term                        | Est.   | 95% CrI          |
|-----------------------------|--------|------------------|
| Intercept                   | 0.721  | [0.681, 0.76]    |
| channelthin                 | -0.076 | [-0.123, -0.026] |
| channelthin:gameSize6       | -0.062 | [-0.127, 0.001]  |
| gameSize6                   | -0.017 | [-0.062, 0.03]   |
| later                       | -0.034 | [-0.039, -0.028] |
| later:channelthin           | 0.011  | [0.003, 0.019]   |
| later:channelthin:gameSize6 | 0.021  | [0.01, 0.032]    |
| later:gameSize6             | -0.011 | [-0.019, -0.004] |
|                             |        |                  |

# Exploratory Mega-analytic models

As an exploratory measure, we combined data across all experiments and re-run the core set of models (same structure and priors as for the individual models). We binarized game thickness: all games that were not thin were counted as thick. The intercept condition is a 2-player game, in the thick condition, for the first block. Thinner means the game was in the thin condition; larger is per additional player, and block is per later block. Group size was coded based on assigned condition, not based on actual number of players at the time.

Table 48: Mega-analytic on accuracy: correct.num  $\sim$  block  $\times$  thinner  $\times$  larger + (1|gameId)

| Term                 | Est.  | 95% CrI        |
|----------------------|-------|----------------|
| Intercept            | 1.83  | [1.6, 2.07]    |
| block                | 0.46  | [0.4, 0.52]    |
| block:larger         | -0.07 | [-0.09, -0.05] |
| block:thinner        | -0.12 | [-0.21, -0.02] |
| block:thinner:larger | 0.01  | [-0.02, 0.04]  |
| larger               | -0.07 | [-0.15, 0]     |
| thinner              | -0.50 | [-0.89, -0.08] |
| thinner:larger       | -0.02 | [-0.14, 0.11]  |

Table 49: Mega-analytic of reduction: words  $\sim$  block  $\times$  thinner  $\times$  larger + (block|gameId)

| Term                 | Est.  | 95% CrI        |
|----------------------|-------|----------------|
| Intercept            | 17.38 | [15.59, 19.21] |
| block                | -2.80 | [-3.24, -2.36] |
| block:larger         | -0.36 | [-0.51, -0.2]  |
| block:thinner        | 0.79  | [0.04, 1.52]   |
| block:thinner:larger | 0.26  | [0, 0.51]      |
| larger               | 2.12  | [1.5, 2.75]    |
| thinner              | -1.59 | [-4.61, 1.55]  |
| thinner:larger       | -0.90 | [-1.92, 0.11]  |

Table 50: Mega-analytic on divergence between groups:  $sim \sim block \times thinner \times larger$ 

| Term                 | Est.   | 95% CrI          |
|----------------------|--------|------------------|
| Intercept            | 0.428  | [0.426,  0.431]  |
| block                | -0.026 | [-0.026, -0.025] |
| block:larger         | -0.002 | [-0.002, -0.002] |
| block:thinner        | 0.005  | [0.004,  0.007]  |
| block:thinner:larger | 0.004  | [0.004, 0.005]   |
| larger               | 0.012  | [0.011,  0.013]  |
| thinner              | -0.003 | [-0.007, 0.001]  |
| thinner:larger       | -0.007 | [-0.008, -0.006] |

Table 51: Mega-analytic on convergence to last:  $sim \sim earlier \times larger \times thinner$ 

| Term                   | Est.   | 95% CrI          |
|------------------------|--------|------------------|
| Intercept              | 0.546  | [0.534, 0.558]   |
| earlier                | 0.072  | [0.067, 0.077]   |
| earlier:larger         | 0.000  | [-0.002, 0.002]  |
| earlier:larger:thinner | -0.007 | [-0.01, -0.004]  |
| earlier:thinner        | -0.016 | [-0.025, -0.008] |
| larger                 | -0.016 | [-0.021, -0.012] |
| larger:thinner         | 0.009  | [0.002, 0.016]   |
| thinner                | 0.001  | [-0.021, 0.021]  |