

Figure 1: Fraction of trials on which at least one listener produced the labelled emoji (or any emoji).

## Supplement

2023-05-05

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This supplement will get moved to a separate file, but for now is tacked on.

TODO graphs of how many players the 6\* games in expt 3 actually had

## Figures of listener performance

Emoji use is common in the 6 player thin games where most trials at least one listener used at least one emoji, but emoji use declines over blocks. SEE FIGURE WHATEVER IN SUPPLEMENT The use of emoji in the thin games is not directly comparable to listener contributes, since some emoji usage (such as the green checkmark) are most likely equivalent to non-referential listener language (“got it” etc.) that was excluded. The higher rate of emoji use versus referential language could be due to it’s non-equivalence, a lower level of accuracy in thin games, or emojis being a lower threshold for sending than written out questions.

## Distinctiveness of tangrams

Another way of looking at how language changes over the course of the game is looking at how games start to refer to different tangrams more differently. This could reflect initial overlap in describing many figures as sitting or standing or by leg and arm and head position.

Over the course of the game, descriptions for each tangram become more distinctive (-0.043 [-0.046, -0.039]). In all three subexperiments, the descriptions of tangrams become more distinctive within games across time. (2a -0.046 [-0.048, -0.044], 2b -0.025 [-0.028, -0.022], 2c -0.025 [-0.028, -0.022]).

Table 1: The number of games in each experiment and condition. Complete games finished all 6 blocks; partial games ended early due to disconnections, but contributed at least one complete block of data. 6\* indicates that some games started with fewer than 6 players or continued with fewer than 6 players after participants disconnected.

Experiment	Players	Complete	Partial	Total Participants
1: baseline	2	15	4	38
1: baseline	3	18	2	60
1: baseline	4	19	2	84
1: baseline	5	17	3	100
1: baseline	6	12	6	108
2: single speaker	6	15	3	108
2: full feedback	6	13	4	102
2: thin	6	10	6	96
3: thin	2	35	3	76
3: thin	6*	44	0	235
3: thick	2	39	3	84
3: thick	6*	38	2	222

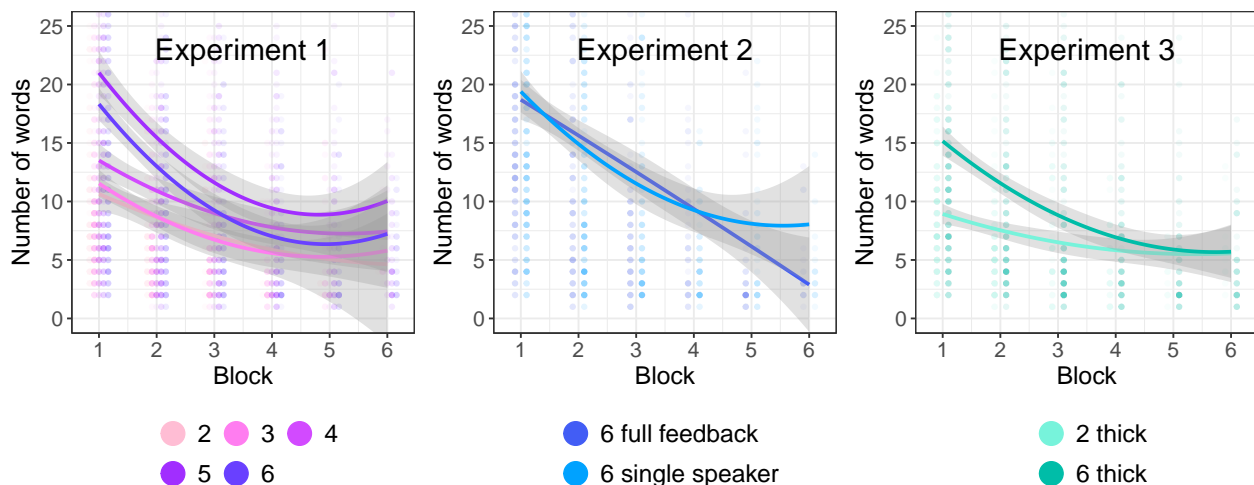


Figure 2: Number of words of referential language produced by listeners over time. Excludes trials where no listeners contributed descriptive language.

Tangram distinctiveness within games increased over time ( $-0.027$   $[-0.029, -0.025]$ ). There might be more to say about other effects, but it's mostly a starting places being different in larger games and then the slopes also differ a bit?

### play with more diagrams

Comparing utterances between adjacent rounds reveals similar patterns. Thin games have lower similarity between adjacent blocks ( $-0.124$   $[-0.159, -0.088]$ ) as do larger games ( $-0.034$   $[-0.069, 0.003]$ ). Later in the game adjacent blocks are more similar than earlier adjacent blocks ( $0.046$   $[0.041, 0.052]$ ), painting an overall nonlinear convergent pattern (as seen in Figure @ref(fig:other)).

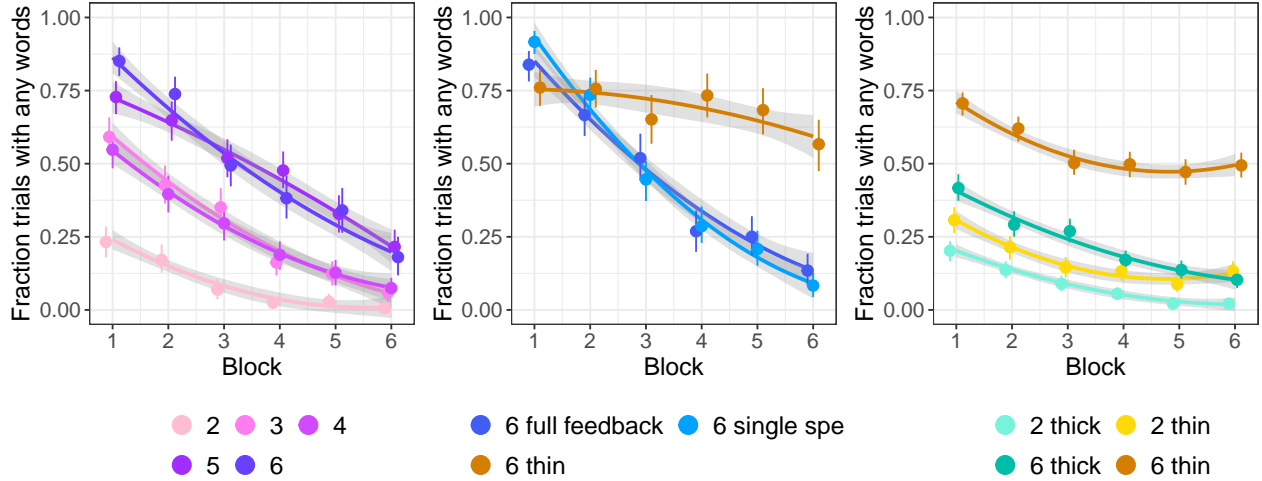


Figure 3: Fraction of trials when any reference language (or emoji) was produced by any listener.

## Models

Note that for all models, block was 0 indexed, so intercepts are what happened during the first block.

## Accuracy models

Accuracy models were all run as logistic models with  $\text{normal}(0,1)$  priors for both betas and sd. This model was not explicitly included in the experiment 1 and 2 pre-registrations; it was included with more ambitious mixed effects (which did not run in a timely manner) in the experiment 3 pre-reg.

Table 2: Experiment 1 logistic model of listener accuracy:  
 $\text{correct.num} \sim \text{block} \times \text{numPlayers} + (1|\text{gameId})$

Term	Est.	CrI
block	0.44	[0.31, 0.58]
block:numPlayers	-0.02	[-0.05, 0.01]
Intercept	2.10	[1.57, 2.65]
numPlayers	-0.07	[-0.2, 0.05]

Table 3: Experiment 2: 6 single speaker logistic model of listener accuracy:  
 $\text{correct.num} \sim \text{block} + (1|\text{gameId})$

Term	Est.	CrI
block	0.45	[0.39, 0.52]
Intercept	1.78	[1.4, 2.19]

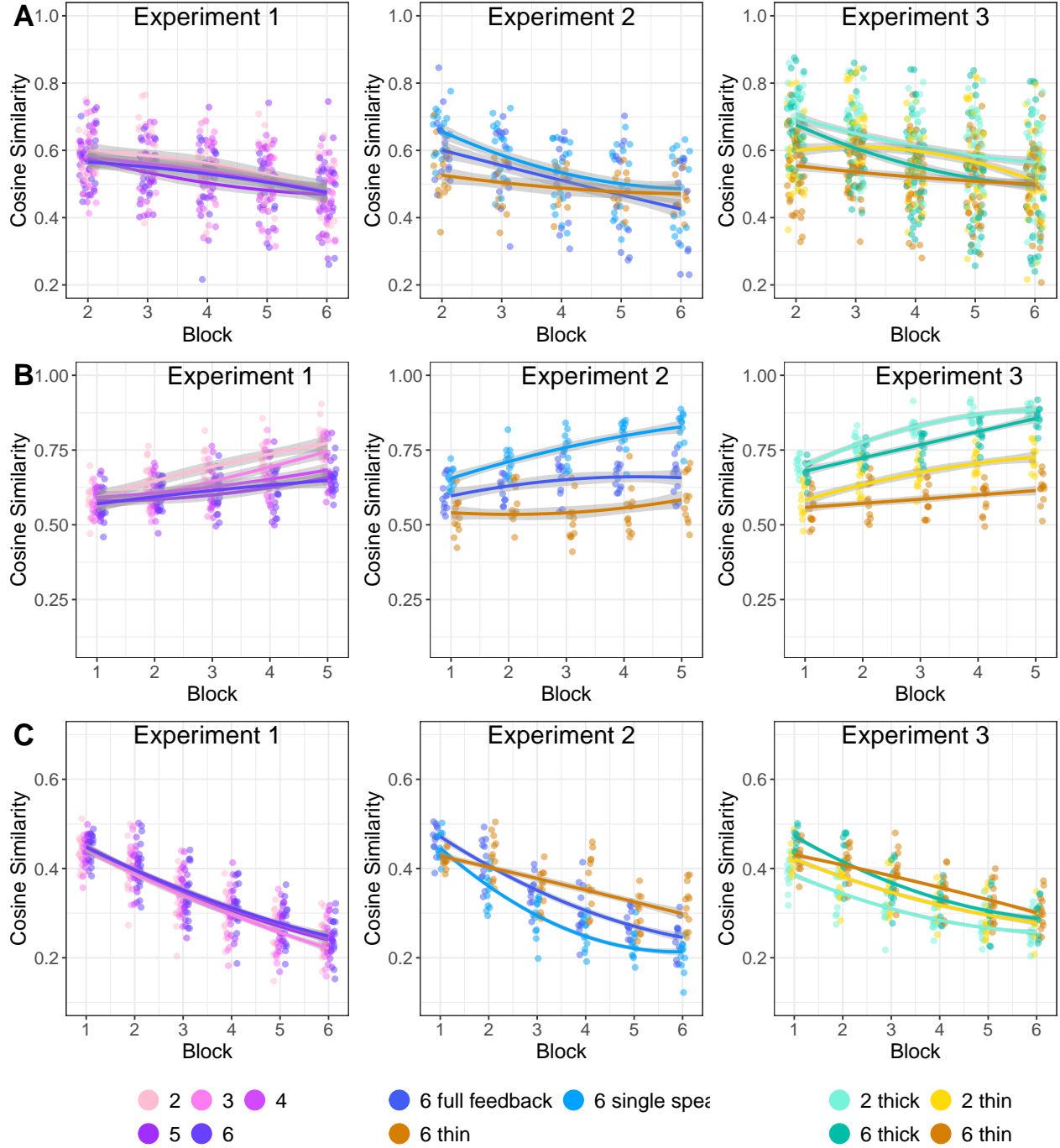


Figure 4: Additional measures of convergence and divergence. A is similarity to first utterance. B is similarity between utterances from adjacent blocks. C is divergence in descriptions of different tangrams within a group

## Reduction models

Reduction models were run as linear models with an intercept prior of  $\text{normal}(12,20)$ , a beta prior of  $\text{normal}(0,10)$ , an sd prior of  $\text{normal}(0,5)$  and a correlation prior of  $\text{lkj}(1)$ . This model was pre-registered for each experiment and run with the mixed effects structure as prespecified.

Table 4: Experiment 2: 6 full feedback logistic model of listener accuracy:  
 $\text{correct.num} \sim \text{block} + (1|\text{gameId})$

Term	Est.	CrI
block	0.47	[0.39, 0.54]
Intercept	1.35	[0.59, 2.06]

Table 5: Experiment 2: 6 thin logistic model of listener accuracy:  
 $\text{correct.num} \sim \text{block} + (1|\text{gameId})$

Term	Est.	CrI
block	0.23	[0.19, 0.28]
Intercept	0.88	[0.64, 1.12]

Table 6: Experiment 3 logistic model of listener accuracy:  
 $\text{correct.num} \sim \text{block} \times \text{gameSize} \times \text{channel} + (1|\text{gameId})$

Term	Est.	CrI
block	0.41	[0.32, 0.5]
block:channelthin	-0.07	[-0.18, 0.04]
block:gameSize6	-0.34	[-0.43, -0.25]
block:gameSize6:channelthin	0.07	[-0.05, 0.19]
channelthin	-0.36	[-0.78, 0.05]
gameSize6	-0.64	[-1.05, -0.25]
gameSize6:channelthin	0.31	[-0.22, 0.87]
Intercept	1.69	[1.39, 1.99]

Table 7: Experiment 1:  
 $\text{words} \sim \text{block} \times \text{numPlayers} + (\text{block}|\text{tangram}) + (1|\text{playerId}) + (1|\text{tangram:gameId}) + (\text{block}|\text{gameId})$

Term	Est.	CrI
block	-3.37	[-4.54, -2.24]
block:numPlayers	-0.10	[-0.36, 0.17]
Intercept	16.79	[11.96, 21.93]
numPlayers	1.66	[0.66, 2.61]

Table 8: Experiment 2: 6 single speaker:  
 $\text{words} \sim \text{block} + (\text{block}|\text{tangram}) + (1|\text{tangram:gameId}) + (\text{block}|\text{gameId})$

Term	Est.	CrI
block	-5.39	[-6.46, -4.31]
Intercept	29.93	[24.92, 34.84]

### Extra reduction model

For experiment 1, we also pre-specified models about whether the speaker’s correctness (as a listener) on the prior block had an effect

Table 9: Experiment 2: 6 full feedback:

$\text{words} \sim \text{block} + (\text{block}|\text{tangram}) + (1|\text{tangram:gameId}) + (\text{block}|\text{gameId})$

Term	Est.	CrI
block	-4.68	[-5.88, -3.52]
Intercept	26.03	[21.12, 30.58]

Table 10: Experiment 2: 6 thin:  $\text{words} \sim \text{block} + (\text{block}|\text{tangram}) + (1|\text{tangram:gameId}) + (\text{block}|\text{gameId})$

Term	Est.	CrI
block	-2.15	[-3.44, -1.12]
Intercept	20.50	[17.26, 23.76]

Table 11: Experiment 3:

$\text{words} \sim \text{block} \times \text{channel} \times \text{gameSize} + (\text{block} \times \text{channel} \times \text{gameSize}|\text{tangram}) + (1|\text{tangram:gameId}) + (\text{block}|\text{gameId})$

Term	Est.	CrI
block	-2.29	[-2.95, -1.6]
block:channelthin	0.32	[-0.65, 1.24]
block:channelthin:gameSize6	0.64	[-0.61, 1.89]
block:gameSize6	-1.21	[-2.06, -0.3]
channelthin	0.63	[-3.18, 4.73]
channelthin:gameSize6	-2.11	[-7.41, 2.98]
gameSize6	7.41	[3.57, 11.18]
Intercept	14.99	[11.86, 17.89]

Model of whether speaker's correct/incorrect answer in previous block has an effect

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## [1] "words~$\\sim$ block~$\\times$ numPlayers~+ block~$\\times$ wasINcorrect~+ (block|tangram)~+ (1|playerId)~+ (1|tangram:gameId)~+ (block|gameId)"
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Table 12: Experiment 1:

$\text{words} \sim \text{block} \times \text{numPlayers} + \text{block} \times \text{wasINcorrect} + (\text{block}|\text{tangram}) + (1|\text{playerId}) + (1|\text{tangram:gameId}) + (\text{block}|\text{gameId})$

Term	Est.	CrI
block	-2.15	[-3.35, -0.98]
block:numPlayers	-0.23	[-0.51, 0.06]
block:wasINcorrect	0.25	[-0.24, 0.74]
Intercept	11.98	[6.31, 17.7]
numPlayers	2.15	[0.93, 3.36]
wasINcorrect	3.08	[1.69, 4.42]

## Listener models

Table 13: Experiment 1: words  $\sim$  block  $\times$  numPlayers + (block|gameId)

Term	Est.	CrI
block	-0.17	[-1.63, 1.24]
block:numPlayers	-0.41	[-0.72, -0.09]
Intercept	4.67	[0.09, 9.32]
numPlayers	2.12	[1.03, 3.12]

Table 14: Experiment 1: is.words  $\sim$  block  $\times$  numPlayers + (1|gameId)

Term	Est.	CrI
block	-0.80	[-0.97, -0.63]
block:numPlayers	0.03	[0, 0.07]
Intercept	-2.65	[-3.5, -1.83]
numPlayers	0.78	[0.58, 0.98]

## SBERT models

For all of the models of sbert similarity, we used linear models with the priors normal(.5,.2) for intercept, normal(0,.1) for beta, and normal(0,.05) for sd.

These models were verbally described (but not formally specified) in the pre-registrations for experiment 2 in the full feedback and thin conditions and for experiment 3, for looking at divergence between games, convergence within games (compare to first, next, and last), and divergence between tangrams within games.

## Convergence within games: comparison to last round

This is the convergence metric presented in the paper.

Table 15: Experiment 1: sim  $\sim$  earlier  $\times$  condition + (1|tangram) + (1|gameId)

Term	Est.	CrI
condition	-0.008	[-0.021, 0.005]
earlier	0.089	[0.076, 0.102]
earlier:condition	-0.008	[-0.011, -0.005]
Intercept	0.517	[0.458, 0.573]

Table 16: Experiment 2: 6 single speaker: sim  $\sim$  earlier + (1|tangram) + (1|gameId)

Term	Est.	CrI
earlier	0.086	[0.078, 0.094]
Intercept	0.499	[0.444, 0.556]

Table 17: Experiment 2: 6 full feedback:sim  $\sim$  earlier + (1|tangram) + (1|gameId)

Term	Est.	CrI
earlier	0.062	[0.051, 0.072]
Intercept	0.438	[0.389, 0.487]

Table 18: Experiment 2: 6 thin:sim  $\sim$  earlier + (1|tangram) + (1|gameId)

Term	Est.	CrI
earlier	0.023	[0.013, 0.033]
Intercept	0.498	[0.453, 0.54]

Table 19: Experiment 3:sim  $\sim$  earlier  $\times$  channel  $\times$  gameSize + (1|tangram) + (1|gameId)

Term	Est.	CrI
channelthin	-0.034	[-0.08, 0.011]
channelthin:gameSize6	0.039	[-0.021, 0.097]
earlier	0.080	[0.074, 0.086]
earlier:channelthin	-0.025	[-0.033, -0.017]
earlier:channelthin:gameSize6	-0.035	[-0.047, -0.025]
earlier:gameSize6	0.009	[0.001, 0.017]
gameSize6	-0.069	[-0.113, -0.025]
Intercept	0.581	[0.542, 0.62]

### Divergence across games

To look at how games diverged from each other ... TODO

Table 20: Experiment 1:sim  $\sim$  block  $\times$  condition + (1|tangram)

Term	Est.	CrI
block	-0.035	[-0.038, -0.032]
block:condition	0.001	[0.001, 0.002]
condition	0.002	[0, 0.004]
Intercept	0.468	[0.429, 0.507]

Table 21: Experiment 2: 6 single speaker:sim  $\sim$  block + (1|tangram)

Term	Est.	CrI
block	-0.041	[-0.043, -0.039]
Intercept	0.484	[0.442, 0.526]



Table 22: Experiment 2: 6 full feedback:sim  $\sim$  block + (1|tangram)

Term	Est.	CrI
block	-0.038	[-0.04, -0.035]
Intercept	0.502	[0.46, 0.546]

Table 23: Experiment 2: 6 thin:sim  $\sim$  block + (1|tangram)

Term	Est.	CrI
block	-0.004	[-0.006, -0.001]
Intercept	0.434	[0.406, 0.465]

Table 24: Experiment 3:sim  $\sim$  block  $\times$  channel  $\times$  gameSize + (1|tangram)

Term	Est.	CrI
block	-0.024	[-0.025, -0.023]
block:channelthin	0.004	[0.002, 0.005]
block:channelthin:gameSize6	0.017	[0.015, 0.019]
block:gameSize6	-0.008	[-0.01, -0.007]
channelthin	0.014	[0.01, 0.018]
channelthin:gameSize6	-0.030	[-0.035, -0.024]
gameSize6	0.051	[0.047, 0.055]
Intercept	0.411	[0.368, 0.453]

### Divergence across tangrams

Table 25: Experiment 1:sim  $\sim$  block  $\times$  condition + (1|gameId)

Term	Est.	CrI
block	-0.043	[-0.046, -0.039]
block:condition	0.000	[-0.001, 0.001]
condition	0.003	[-0.008, 0.014]
Intercept	0.429	[0.382, 0.473]

Table 26: Experiment 2: 6 single speaker:sim  $\sim$  block + (1|gameId)

Term	Est.	CrI
block	-0.046	[-0.048, -0.044]
Intercept	0.416	[0.389, 0.443]

Table 27: Experiment 2: 6 full feedback:sim  $\sim$  block + (1|gameId)

Term	Est.	CrI
block	-0.047	[-0.049, -0.044]
Intercept	0.459	[0.422, 0.496]

Table 28: Experiment 2: 6 thin:sim  $\sim$  block + (1|gameId)

Term	Est.	CrI
block	-0.025	[-0.028, -0.022]
Intercept	0.432	[0.393, 0.471]

Table 29: Experiment 3:sim  $\sim$  block  $\times$  channel  $\times$  gameSize + (1|gameId)

Term	Est.	CrI
block	-0.027	[-0.029, -0.025]
block:channelthin	-0.001	[-0.003, 0.002]
block:channelthin:gameSize6	0.011	[0.008, 0.015]
block:gameSize6	-0.010	[-0.013, -0.008]
channelthin	0.038	[-0.001, 0.082]
channelthin:gameSize6	-0.053	[-0.115, 0]
gameSize6	0.073	[0.035, 0.113]
Intercept	0.378	[0.352, 0.404]

### convergence to next

We also looked at how similar an utterance was to the next round utterance: this can be thought of as the derivative of the to-last comparison. (although cosine similarities are not actually additive in the same way integrals are)

Table 30: Experiment 1:sim  $\sim$  earlier  $\times$  condition + (1|tangram) + (1|gameId)

Term	Est.	CrI
condition	-0.004	[-0.014, 0.006]
earlier	0.063	[0.051, 0.075]
earlier:condition	-0.008	[-0.011, -0.006]
Intercept	0.591	[0.541, 0.641]

Table 31: Experiment 2: 6 single speaker:sim  $\sim$  earlier + (1|tangram) + (1|gameId)

Term	Est.	CrI
earlier	0.043	[0.037, 0.05]
Intercept	0.660	[0.619, 0.702]

Table 32: Experiment 2: 6 full feedback:sim  $\sim$  earlier + (1|tangram) + (1|gameId)

Term	Est.	CrI
earlier	0.015	[0.006, 0.024]
Intercept	0.605	[0.569, 0.643]

Table 33: Experiment 2: 6 thin:sim  $\sim$  earlier + (1|tangram) + (1|gameId)

Term	Est.	CrI
earlier	0.010	[0, 0.019]
Intercept	0.533	[0.49, 0.578]

Table 34: Experiment 3:sim  $\sim$  earlier  $\times$  channel  $\times$  gameSize + (1|tangram) + (1|gameId)

Term	Est.	CrI
channelthin	-0.124	[-0.159, -0.088]
channelthin:gameSize6	0.000	[-0.051, 0.049]
earlier	0.046	[0.041, 0.052]
earlier:channelthin	-0.010	[-0.018, -0.002]
earlier:channelthin:gameSize6	-0.018	[-0.029, -0.007]
earlier:gameSize6	-0.003	[-0.011, 0.004]
gameSize6	-0.034	[-0.069, 0.003]
Intercept	0.714	[0.682, 0.746]

### divergence from first

We also looked at how similar an utterance was to the first round utterance. This is not very informative because first round utterances tend to be pretty unwieldy. TODO explain more or don't include

Table 35: Experiment 1:sim  $\sim$  later  $\times$  condition + (1|tangram) + (1|gameId)

Term	Est.	CrI
condition	-0.010	[-0.022, 0.003]
Intercept	0.647	[0.591, 0.705]
later	-0.030	[-0.041, -0.019]
later:condition	0.001	[-0.002, 0.004]

Table 36: Experiment 2: 6 single speaker:sim  $\sim$  later + (1|tangram) + (1|gameId)

Term	Est.	CrI
Intercept	0.680	[0.628, 0.728]
later	-0.042	[-0.049, -0.035]

Table 37: Experiment 2: 6 full feedback:sim  $\sim$  later + (1|tangram) + (1|gameId)

Term	Est.	CrI
Intercept	0.644	[0.584, 0.706]
later	-0.044	[-0.052, -0.037]

Table 38: Experiment 2: 6 thin:sim  $\sim$  later + (1|tangram) + (1|gameId)

Term	Est.	CrI
Intercept	0.537	[0.49, 0.584]
later	-0.014	[-0.023, -0.004]

Table 39: Experiment 3:sim  $\sim$  later  $\times$  channel  $\times$  gameSize + (1|tangram) + (1|gameId)

Term	Est.	CrI
channelthin	-0.076	[-0.123, -0.026]
channelthin:gameSize6	-0.062	[-0.127, 0.001]
gameSize6	-0.017	[-0.062, 0.03]
Intercept	0.721	[0.681, 0.76]
later	-0.034	[-0.039, -0.028]
later:channelthin	0.011	[0.003, 0.019]
later:channelthin:gameSize6	0.021	[0.01, 0.032]
later:gameSize6	-0.011	[-0.019, -0.004]

### Extra emoji analysis

Written about 6thin in experiment 2 and for 2 and 6 thin in 3 Additionally, exclusive to this condition, we will analyse the distribution of emoji’s produced as a function of block and its relation to accuracy and speaker utterance length.