

## Lecture 2

Marginal Benefit: the value from the last unit consumed/produced

Marginal Cost: the cost of the last unit consumed/produced

Optimization:  $MB = MC$

### Preference Maps

Indifference Curves: map the set of bundles of goods that a consumer views as being equally desirable  
(Indifference map shows the complete set of a consumer's indifference curves)

Marginal Rate of Substitution: (MRS) the maximum amount of one good a consumer is willing to give up to obtain one more of another good.

$MRS = \text{slope of indifference curve}$

$$MRS_{x_1, x_2} = \frac{\Delta x_2}{\Delta x_1} \text{ is MRS of } x_2 \text{ for } x_1, \text{ number of } x_2 \text{ for } x_1$$

Convexity: IC are convex to the origin, because when consumers have more of a good, they will trade more of it for one unit of another good.

Utility: unit of measurement that expresses relative order of preference of bundles to consumers. Quantifies satisfaction? Ordinal measure!

Indifference Curves consist of bundles of goods that all have equal utility to a consumer. Further out  $\rightarrow$  more utility

Marginal Utility: the extra utility that a consumer gets from consuming the last unit of a good. Exhibits diminishing marginal utility: as consumers consume more of a good, their marginal utility decreases.

$$MU_a = \frac{\Delta U}{\Delta G}$$

\* Marginal Rate of Substitution (MRS) is equal to the negative ratio of the marginal utility of  $x_1$  to the marginal utility of  $x_2$ .

$$MRS_{x_1, x_2} = \frac{\Delta x_2}{\Delta x_1} = - \frac{MU_{x_1}}{MU_{x_2}}$$

Preferences:  $>, \leq \rightarrow$  Utility

$\gamma, \prec \rightarrow$  Preference

① Completeness: consumers will always have an opinion, infinite num. of ICs

② Transitivity: If  $A > B$  and  $B > C$ ,  $A > C$

③ Non-satiation: more is always better

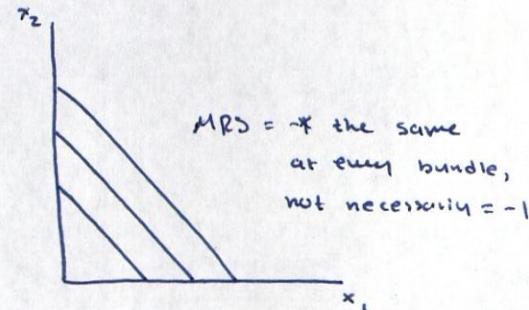
### Properties:

- Indifference curves further from the origin are preferred to those closer to the origin
- An indifference curve goes through every possible bundle
- Indifference curves do not cross
- Indifference curves slope downwards

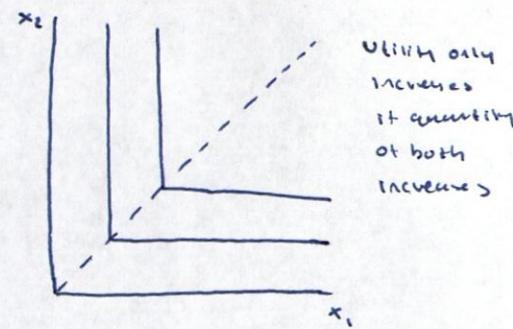
### Diminishing Rate of Substitution:

MRS approaches 0 as you move along an IC to the right

### Perfect Substitutes



### Perfect Complements



## Lecture 3

### Budget Constraint

Assume that the consumer's budget is given and that the only purchase two goods.

$$I = P_{x_1} X_1 + P_{x_2} X_2$$

where:  $I$  = Income

$P_{x_1}$  = Price of good  $x_1$ ,

$X_1$  = Quantity of  $x_1$ ,

$P_{x_2}$  = Price of good  $x_2$

$X_2$  = Quantity of  $x_2$

Budget line: the bundles of goods that can be bought if the entire budget is spent on those goods at given prices

Affordable set: all the bundles a consumer can buy, including all bundles inside the budget line and on the budget line/constraint

Slope of the Budget Constraint is determined by the relative prices of the two goods.

Marginal Rate of Transformation: (MRT) the trade-off the market imposes on the consumer in terms of the amount of one good the consumer must give up to obtain more of the other good. (= slope of the budget constraint)

$$MRT = \frac{X_2}{X_1} = -\frac{P_{x_1}}{P_{x_2}}$$

### Changes in Income

#### ① Increase

Increase in income increases the quantity of goods a consumer can purchase for both goods, shifting budget constraint outwards.

#### ② Decrease

Decrease in income decreases the quantity of goods a consumer can purchase for both goods, shifting budget constraint in.

### Changes in Price

#### ① Increase

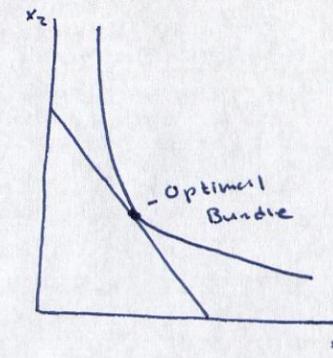
Increase in price decreases the quantity that a consumer can buy. The budget constraint will pivot in to reflect this. Reduces overall utility.

#### ② Decrease

Decrease in price increases the quantity of a good that a consumer can buy. The budget constraint will pivot out to reflect this. Increases overall utility.

### Optimal Bundle

The optimal bundle is that which gives the consumer the most pleasure (utility) out of their affordable set. This bundle will lie on an indifference curve that is tangent to their budget constraint. This way, they will be using all of their budget, and be on the furthest out indifference curve.



The optimal bundle lies at the point where Marginal Rate of Substitution = Marginal Rate of Transformation

$$MRS = MRT$$

$$MRS = -\frac{MU_{x_1}}{MU_{x_2}} = -\frac{P_{x_1}}{P_{x_2}} = MRT$$

where the slope of the budget constraint is equal to the slope of the indifference curve.

$$MRS = \text{Price Ratio}$$

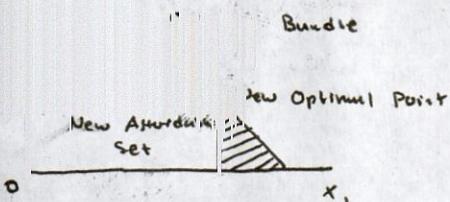
### Necessary Condition:

- ① The indifference curve is tangent to the budget constraint
- ② The consumer buys the bundle that is on the highest possible indifference curve
- ③  $MRS = MRT$
- ④ The last dollar spent on Good  $x_1$  gives the consumer as much utility as the last dollar spent on  $x_2$

## Exceptions

### Rationing

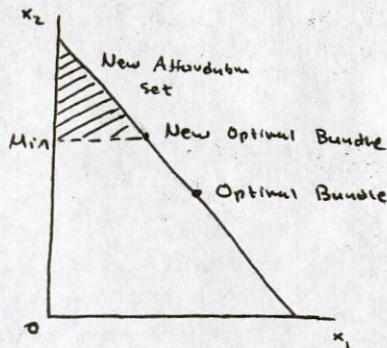
Rationing is a situation in which there is a maximum quantity of a good that you can buy.



- Utility has decreased for those whose optimal point was outside the new affordable set. For those whose original optimal bundle was in the new affordable set, nothing has changed.

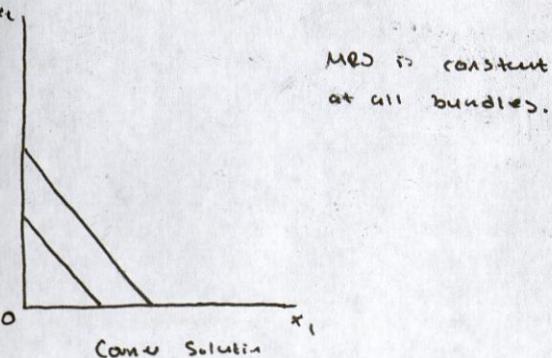
### Minimum Required Purchase

A situation in which there is a minimum quantity required to purchase a good.



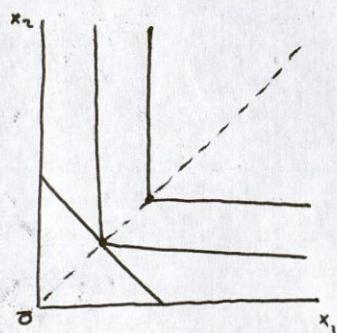
- Utility has decreased for those whose optimal bundle was outside the new affordable set. For those whose original optimal bundle was in the new affordable set, nothing has changed.

### Perfect Substitutes

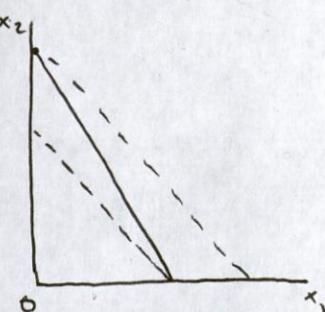


MRS is constant at all bundles.

### Perfect Complements



Utility only increases if the quantity of both goods increases. Extra units of one good don't increase utility without increasing the quantity of the other good. There will be an ideal ratio. Bundle must be on that line.

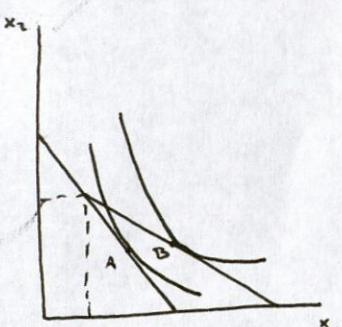


With perfect substitutes, MRS is fixed at 1, so you should buy whichever you can buy more of.

This is called a corner solution.

### Volume Discounts

Volume discount means that after a certain quantity, price falls.



FIRM  
Point  
(at x  
quantity)

This changes the MRS. Will result in an increase of consumption of that good, leads to higher utility. Optimal Bundle is still when  $MRS = \text{Price Ratio}$

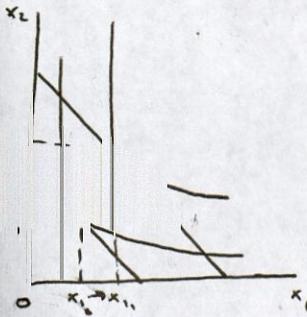
## Lecture 4

Ceteris Paribus: "with other things the same"

Comparative Statistics: an exercise in which you alter a variable within a model to see what happens

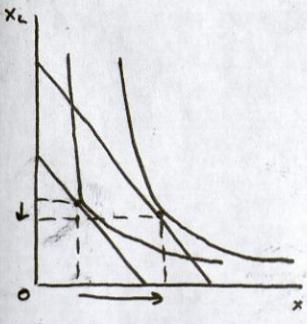
Normal Goods: goods for which quantity demanded increases as income increases

Income Increases

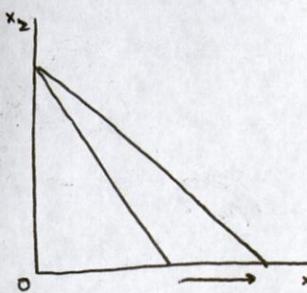


Income increases will shift the budget constraint outwards in a fashion such that the two BC's are parallel. Quantity of both goods at optimal bundle increases.

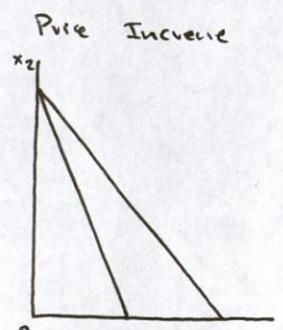
Income Increase with an Inferior Good



Price Decrease



Increases quantity of good for which price decreased.  
Expands affordable set.



Decreases quantity for which price increased.  
Contracts affordable set.

Exception: whenever exactly double both income and all prices, the budget constraint remains the same. The optimal bundle will remain the same.

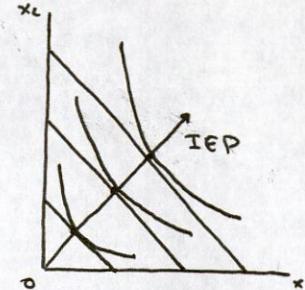
Inferior Goods: goods for which quantity demanded falls as income increases

Giffen Goods: goods for which quantity demanded increases as price increases

Income Expansion Path

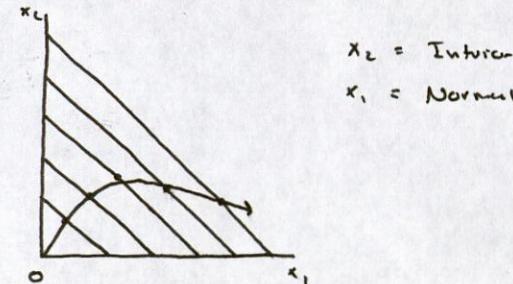
The income expansion path is the curve that connects all of the optimal bundles as income increases from zero.

For two Normal Goods:



For two normal goods, the IEP will be increasing on both axes

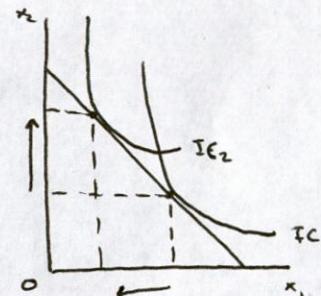
For one Normal and one Inferior



$x_2 = \text{Inferior}$   
 $x_1 = \text{Normal}$

Preference Changes

Indifference curves change when a consumer's preferences change.

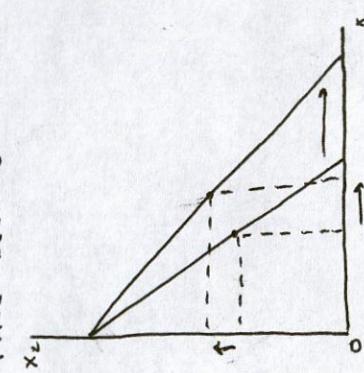


Picture for  $x_1$  decreases,  
not willing to trade  $x_1$  w/  $x_2$   
 $MRS_{x_1, x_2} \uparrow$

### Complements

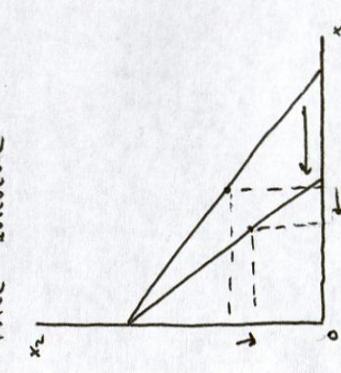
Two goods are considered complements if an increase in the price of one good leads to a decrease in the demand for the other. Conversely, if a price decrease in one will lead to an increase in the demand for the other.

Price Decrease



- Price of  $x_1$  decreases
- Demand for  $x_1$  increases
- Demand for  $x_2$  increases

Price Increase

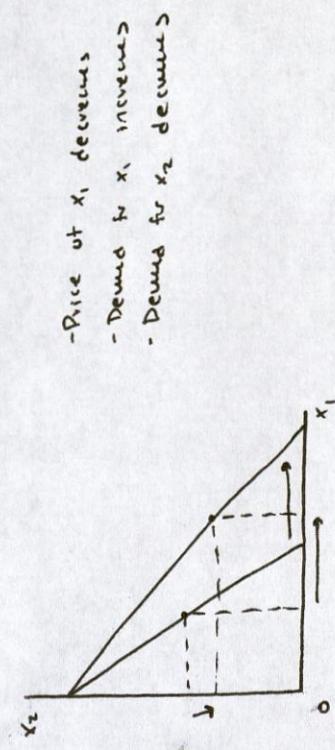


- Price of  $x_1$  increases
- Demand for  $x_1$  decreases
- Demand for  $x_2$  decreases

### Substitutes

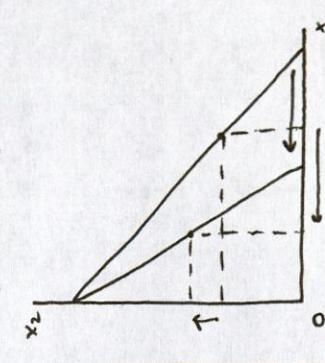
Two goods are considered substitutes if an increase in the price of one good leads to an increase in the demand for the other. Conversely, a decrease in the price of one will lead to an increase in demand for the other.

Price Decrease



- Price of  $x_1$  decreases
- Demand for  $x_1$  increases
- Demand for  $x_2$  increases

Price Increase



- Price of  $x_1$  increases
- Demand for  $x_1$  decreases
- Demand for  $x_2$  decreases

Substitution Effect, Income Effect, and  
Total Effect

Changes in the price of a good  
has two effects on an individual's  
demand:

Substitution Effect: the change in  
quantity demanded that results  
from substitution due to one  
good becoming relatively more  
expensive and the other becoming  
relatively less expensive.  
Consumers substitute towards  
the good that is less  
expensive.

Income Effect: the change in  
quantity demanded that results  
from the change in the  
consumer's income power.  
Price increase  $\rightarrow$  lower goes  $\uparrow$   
 $\downarrow$  demand

Total Effect: the overall change  
in quantity demanded that  
results from a change in  
price.  $TE = SE + IE$

	TE	SE	IE
Good 1			
Good 2			

\* Assuming price change in Good 1

TE of G1: If normal....

TE  $\uparrow$  if PL

TE  $\downarrow$  if PT

IS inferior

TE

TE

TE of G2: If normal

Substitutes:

TE  $\uparrow$  if PT

TE  $\downarrow$  if PL

Complements

TE  $\uparrow$  if PL

TE  $\downarrow$  if PT

SE of G1: SE  $\uparrow$  if PL

SE  $\downarrow$  if PT

SE of G2: SE  $\uparrow$  if PT

SE  $\downarrow$  if PL } Substitutes

SE  $\uparrow$  if PL } Complements

SE  $\downarrow$  if PT }

IE of Good 1: if normal

IE  $\uparrow$  if PL

IE  $\downarrow$  if PT

if inferior

IE  $\uparrow$  if PT

IE  $\downarrow$  if PL

IE of Good 2: if normal

IE  $\uparrow$  if PL

IE  $\downarrow$  if PT

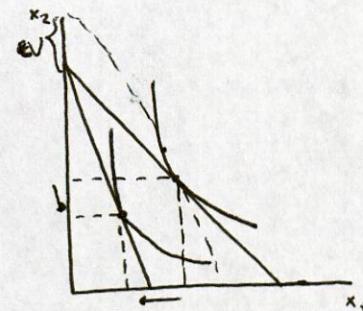
if inferior

IE  $\uparrow$  if PT

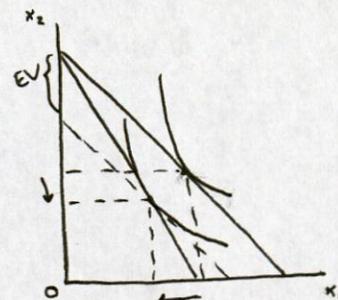
IE  $\downarrow$  if PL

## Lecture 5

**Compensating Variation:** (CV) the amount of money one would have to give a consumer to offset the harm done by a price increase (or take from a consumer to offset the benefit of a price decrease).



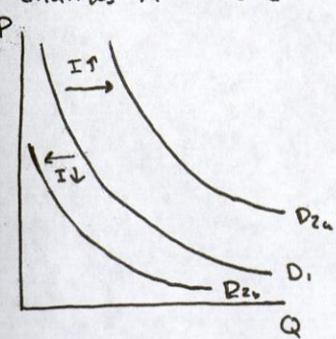
**Equivalent Variation:** (EV) the amount of money you would have to take from a consumer to harm them as much as a price increase (or give to a consumer to benefit them as much as a price decrease).



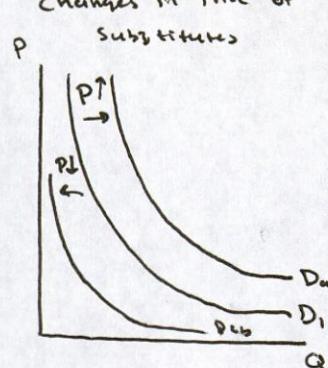
### Movement vs. Shift in the Demand Curve

Movements along the demand curve are caused by the good changing in price. Actual shifts of the demand curve are caused by: changes in income, changes in price of complements, changes in price of substitutes, changes in preferences.

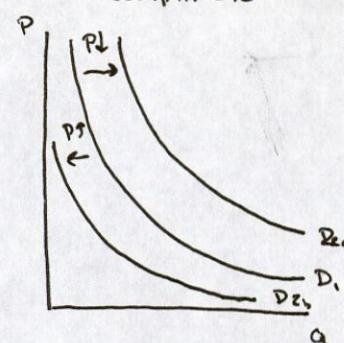
#### Changes in Income



#### Changes in Price of Substitutes



#### Changes in Price of Complements



Individuals  $\rightarrow$  Market Demand & Market Demand Curve

Market Demand: the sum of all individuals' quantity demanded for a given price

Market Demand Curve plots market demand at given prices.

Deriving Market Demand Equation

## Lecture 6

**Revealed Preference:** consumers reveal their preferences by their purchasing behavior

**Elasticity:** measures how responsive people are to a change in a given variable

General Form:  $\epsilon = \frac{\Delta Q/Q}{\Delta P/P}$

**Own-Price Elasticity:** the percent change in quantity demanded in response to a given percent change in the price of that good

Elasticity over Time:

- Goods tend to become more elastic over time due to:
  - high transportation costs
  - need to wait for producers to change
  - technological advances

$$\epsilon = \frac{\Delta Q/Q}{\Delta P/P} = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

**Cross-Price Elasticity:** the percent change in quantity demanded in response to a given percent change in the price of another good ( $\rightarrow C, + \rightarrow S$ )

$$\epsilon = \frac{\Delta Q/Q}{\Delta P/P} = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

**Income Elasticity:** the percent change in quantity demanded in response to a given percent change in a consumer's income

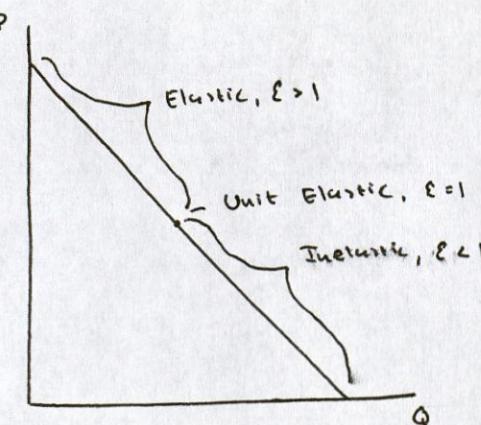
- Necessities have income elasticity between 0 & 1
- Luxuries have income elasticity  $> 1$

$$\epsilon = \frac{\Delta Q/Q}{\Delta Y/Y} = \frac{\Delta Q}{\Delta Y} \cdot \frac{Y}{Q}$$

**Elastic:** change in quantity demanded was greater than price change.  $\epsilon > 1$

The higher is price, the more elastic

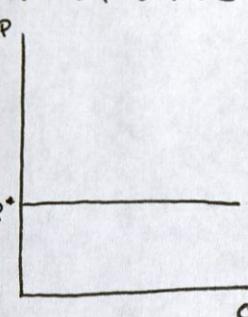
**Unit-Elastic:** change in quantity demanded was equal to change in price.  $\epsilon = 1$



**Inelastic:** change in quantity demanded was less than the change in price.  $\epsilon < 1$

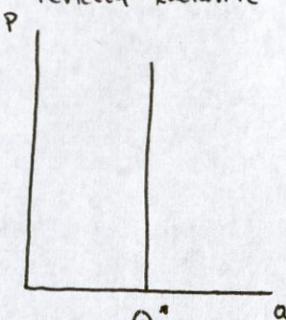
### Constant Elasticity

#### Perfectly Elastic



Consumers are willing to purchase any quantity at price  $P^*$ . Any price change  $\rightarrow$  no demand.

#### Perfectly Inelastic



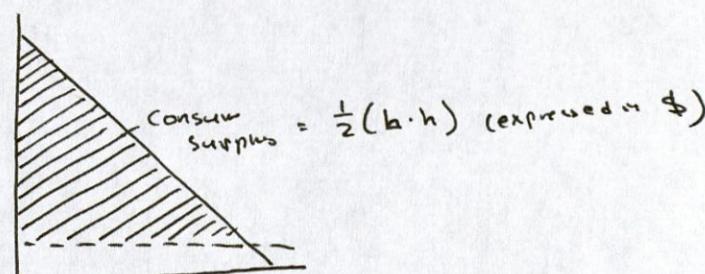
Consumers will purchase/demand  $Q^*$  regardless of the price. Happy with essential goods.

### Maximizing Profit

Expenditure = Revenue

- Move left towards point of unit elasticity increases revenue
- Revenue is maximized at point of unit-elasticity

### Consumer Surplus



## Lecture 7

**Expected Value:** the average outcome of an experiment if it were to be repeated many times

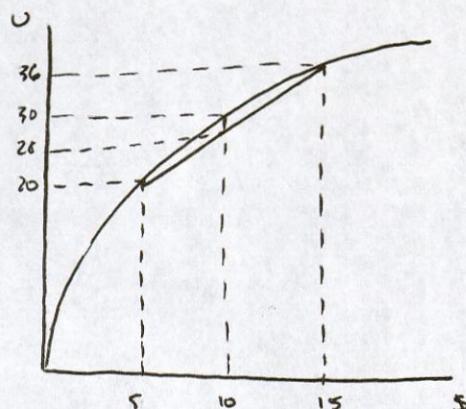
$$EV[x] = P(x_1)(x_1) + P(x_2)(x_2) + \dots P(x_n)(x_n)$$

**Fair Bet:** a wager for which the expected value = 0

**Expected Utility:** the probability-weighted average of the outcome of an experiment

$$EU(x) = P(x_1)U(x_1) + P(x_2)U(x_2) + \dots P(x_n)U(x_n)$$

**Risk Aversion:** those who are risk averse dislike risk and are less willing to take a fair bet. This is the case with most people, and happens due to the diminishing marginal utility of wealth.



\$10,000 income. 50/50 bet to withdraw \$5,000.

$$U(15) = 36, U(10) = 30, U(5) = 20$$

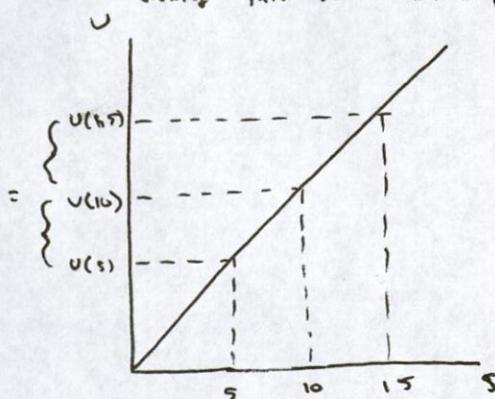
$$EV = (0.5)(15) + (0.5)(5) = 10$$

$$EU = (0.5)(36) + (0.5)(20) = 28$$

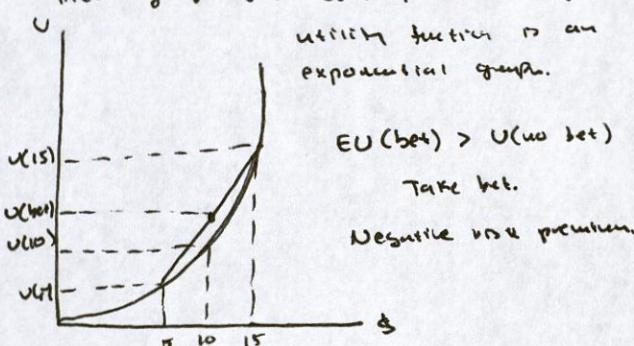
$$EU(\text{bet}) = 28 < 30 = U(30)$$

Don't take bet

**Risk Neutral:** Those who are risk neutral base decisions on expected value. They do not have diminishing marginal utility of wealth. Their utility function is a straight line. They are indifferent towards taking fair bets. Risk premium = 0



**Risk Loving:** Those who are risk loving love risk and prefer to make a fair bet. They exhibit increasing marginal utility of wealth. Their utility function is an exponential graph.



$$EU(\text{bet}) > U(\text{no bet})$$

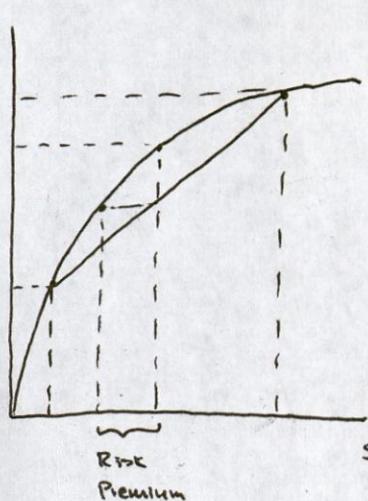
Take bet.

Negative risk premium.

## Insurance

People buy insurance in order to avoid the negative consequences of gambles that are unavoidable.

$$\text{Expected Loss} = P(L) \cdot V(L)$$



Risk Premium is the amount of money a consumer would be willing to pay to avoid the bet. This will be the level of income that provides the same level of expected utility as the bet.

\* AFP doesn't change with consumers having varying degrees of risk aversion. Solely based on the insure's expected loss.

Example: AFP with two risk types

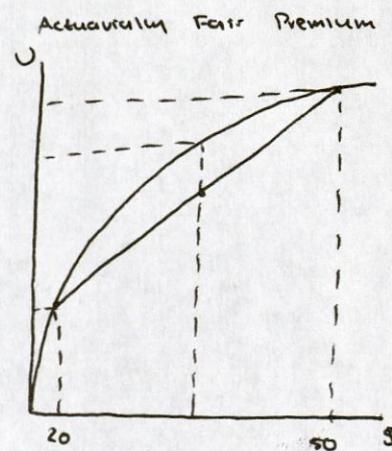
Ned and How both make \$50,000, and both would pay \$30,000 if sick. Ned has a 25% chance of getting sick.

How has a 75% chance of getting sick. Insurer can't tell who is who, what is the AFP?

$$EL(\text{Ned}) = (0.25)(30) = 7.5K$$

$$EL(\text{How}) = (0.75)(30) = 22.5K$$

$$AFP = \frac{(0.25)(30) + (0.75)(30)}{2} = 15K$$



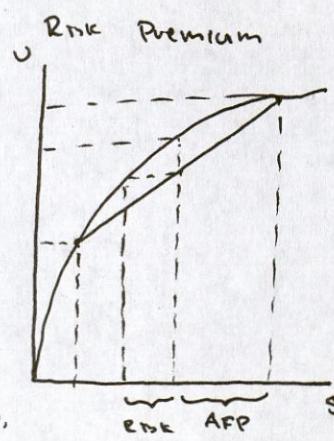
Ned has an income of \$50,000. He has a 25% of becoming sick when medical bills = \$30,000. What is the minimum he would have to pay for insurance?

$$EV = (0.75)(50) + (0.25)(20) = 42.5K$$

$$EL = (0.25)(30) = 7.5K$$

The Actuarially Fair Premium is the amount that the insurer would have to charge in order to break even.

$$AFP = EL$$



What is the maximum amount of money Ned would be willing to pay for insurance?

$$\text{where } U = EU(\text{bet})$$

Asymmetric Information

Hidden Characteristic

Hidden Action, Opportunistic Behavior

Adverse Selection: when one party in a transaction has knowledge of a hidden characteristic that the other doesn't about (AI) and takes economic advantage of it.

With How buying insurance and Ned opting out, the insurers'  $EL = (0.75)(30) = 22.5 > 7.5$ , which would make  $AFP = 22.5K$ . How wants to go into market with Ned, but Ned is unhappy.

- Insurance companies can't distinguish between risk profiles, charging the same AFP, only risky people end up

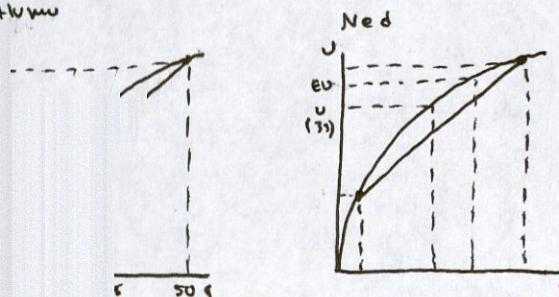
Avoiding AI: with insurance, insurers were off

Underwriting: process by which insurers screen for risk type

- Prevent good risks from dropping out (mandatory insurance, ACA)

- Make the bad risks better (certain pre-existing conditions)

Humor



How is happy, because his  $EU < U(\text{insurance})$ . He buys insurance.

Ned is not happy, because his  $EU > U(\text{insurance})$ . He does not buy insurance.

## Incentive Compatibility

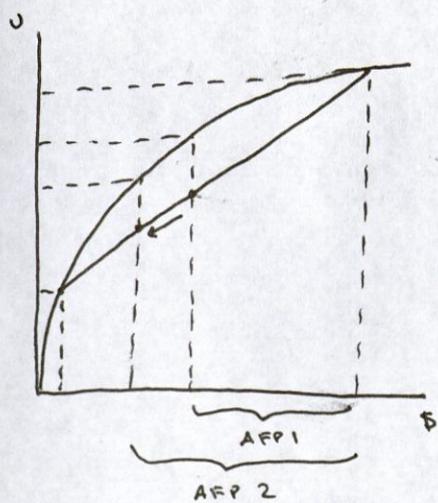
Pooling Equilibrium: where dissimilar people are treated or behave alike. Here, Ned and Homer are treated the same and pay the same premium.

Separating Equilibrium: where individuals can take actions to distinguish themselves from others. Here, Ned and Homer pay individual premiums based on risk profile.

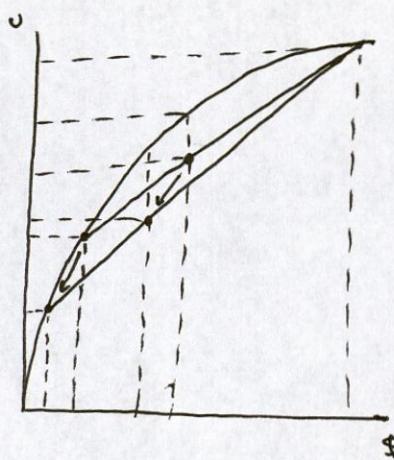
Incentive Compatible: situation in which each participant can achieve their own best interest. Here, Ned and Homer would behave in their best interests and reveal their risk types naturally.

## Moral Hazard

Ex-Ante Moral Hazard: the insured actor increases the likelihood of the insured-against event occurring, either by engaging in risky behavior, or failing to take preventative steps.



Ex-Post Moral Hazard: once the insured-against event occurs, the policy-holder makes the loss worse by incurring costs she would not have incurred if she had not been insured.



## Lecture 8

Rational Consumer: - Fully informed about all options

- Fully opionated about all options

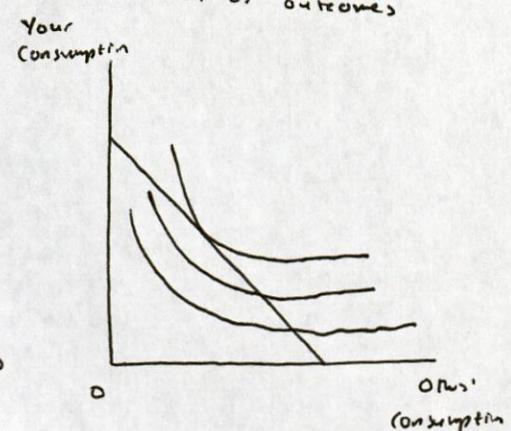
- Important factors: preferences/utility, prices, income, probability of outcomes

Altruism: Altruistic people consider the well-being

of others as part of their utility function

Pure Altruism: trading one's own utility to increase the utility of someone else with no expectation of compensation

Impure Altruism: the act of giving increases our own utility by increasing self-esteem and making us look better (warm glow) with warm glow, impure altruists have high utility when others' utilities are high and have the ability to raise their own utility by raising others'



Social Welfare Function

$$W = a_1 U_1 + a_2 U_2 + \dots + a_n U_n$$

where  $a_i$  = Social weight, i.e.

how much they matter in the decision process

Sunk Costs: costs that are beyond recovery at the time the decision is made.

(Rational consumers do not consider, irrational do)

Framing: the way questions are framed can change people's decisions

Asymmetric Value Function

Loss Aversion: Losing \$X decreases utility more than \$X increases it

Heuristics: simple rules (shortcuts) that humans use to make decisions

① Availability: mental shortcut that relies on the first examples that come to mind relating to something

② Representativeness: we pay more attention to extroavagant cues, even though they may not reflect the true prevalence of an event

③ Anchoring: we tend to not adjust away enough from our preliminary estimate

