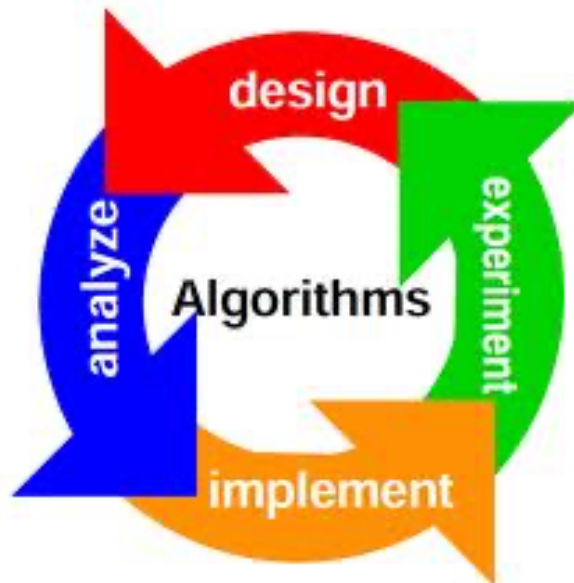


Data Structures and Algorithms II

CMPSC 130B



Course plan

- We are in the midst of a pandemic. Try your best.
- Instructor
 - Ambuj K Singh, ambuj@ucsb.edu
- Teaching Assistants
 - Kha-Dinh Luong, vluong@ucsb.edu
 - Chinmay Sonar, vaishali@ucsb.edu
- Undergraduate Learning Assistants
 - Gabriele Soule
 - Andrew Kraft
- “Welcome to UC Santa Barbara – where the land meets the sea, where brilliant minds meet each other, and where academic excellence and social engagement unite to spark creativity and discovery.”

Remote live lectures using zoom

- Resource for remote learning:
<https://keeplearning.id.ucsb.edu/>
- If you have logistical or technical issues with remote engagement, please email help@collaborate.ucsb.edu.
- Lectures and discussion sections will be recorded and made available on Gauchospace for students who may not be able to attend at this time.
- By default, your microphone and camera will be muted when you join the session. If you do not want to be included in the recording, simply keep your camera and microphone off.
- You may ask questions by unmuting or in the chat window.

Catalog description

Prerequisite: Computer Science 130A

Design and analysis of computer algorithms. Correctness proofs and solution of recurrence relations. Design techniques; divide and conquer, greedy strategies, dynamic programming, branch and bound, backtracking, and local search. Applications of techniques to problems from several disciplines. NP-completeness.

Prerequisite concepts

- Data structures:
 - Sets with insert/delete/member: Hashing
 - Sets with priority: Heaps, priority queues
 - Balanced search trees
 - Union/find
 - Graphs
 - Sorting
- Discrete mathematics
 - Functions, relations, recurrence equations, induction, logic, proofs, ...
- Programming
 - C++
- Program/algorithm complexity analysis

Objectives

- The goal of this course is to introduce you to a systematic study of algorithmic design techniques and intractability using examples across many areas of computer science and related fields. We will cover the following topics:
 - Greedy algorithms
 - Divide and conquer
 - Dynamic programming
 - NP-completeness
 - Approximation algorithms

Textbook

- Required:
 - *Algorithm Design*, Jon Kleinberg and Éva Tardos, 2006, Pearson.
- References:
 - *Algorithms*, Sanjoy Dasgupta, Christos Papadimitriou, Umesh Vazirani, McGraw-Hill
 - *Introduction to Algorithms*, Thomas H. Cormen, Charles Leiserson, Ronald Rivest, McGraw-Hill
 - *Data Structures and Algorithm Analysis in C++*, by Mark Allen Weiss (4th edition)
- For fun:
 - *Algorithms to Live By: The Computer Science of Human Decisions*, Brian Christian and Tom Griffiths, Holt & Co.

Assignments and grading

- Grades will be based on class participation, homework assignments, programming assignments, midterm exam, and final exam:
 - 7% class participation
 - 27% Homework assignments
 - 26% Programming assignments
 - 20% Midterm exam (Feb 3, during lecture)
 - 20% Final exam (March 17, 8-11 AM), optional
- Late assignments are not allowed.
- **All graded work turned in must be completely your own, including programming assignments.**
- There will be no makeup exams.

Topics covered

- Greedy Algorithms 4 Lectures
- Divide & Conquer 4L
- Dynamic Programming 3L
- NP-Hardness 4L
- Approximation Algorithms 2L

Syllabus discussion

A decorative L-shaped line in a dark blue color, starting from the top left and extending horizontally and vertically.

This week's goals

- Assigned reading
 - Chapter 4
- Discussion section plan
 - Algorithm complexity analysis
 - Proof by induction
 - Graph algorithms

The Idea of an Algorithm

- 9th-century Persian mathematician Muḥammad ibn Mūsā al-Khwārizmī (latinized *Algoritmi*).
- A sequence of unambiguous instructions for solving a problem.
- Finite – must eventually terminate.
- Complete – always gives a solution when there is one.
- Correct (sound) – always gives a “correct” solution.
- Efficient



Famous algorithms

- Constructions of Euclid
- Newton's root finding
- Fast Fourier Transform
- Compression (Huffman, Lempel-Ziv, GIF, MPEG)
- DES, RSA encryption
- Simplex for linear programming
- Shortest Path Algorithms (Dijkstra, Bellman-Ford)
- Error correcting codes (CDs, DVDs)
- TCP congestion control, IP routing
- Pattern matching (Genomics)
- Search Engines

Algorithms in modern world

- Enormous amount of data
 - E-commerce (Amazon, eBay)
 - Advertisement (Google)
 - Network traffic (telecom billing, monitoring)
 - Database transactions (Sales, inventory)
 - Scientific measurements (astrophysics, geology)
 - Sensor networks. RFID tags
 - Bioinformatics (genome, protein bank)
 - Drug discovery (high throughput screens)
 - Machine learning & AI
- Need for scalability

Why efficient algorithms matter?

- Suppose $N = 10^6$
- A PC can read/process N records in 1 sec.
- But if some algorithm does $N*N$ computations, then it takes 1M seconds \approx 11 days!!!
- 100 City **Traveling Salesman Problem**.
 - A supercomputer solved an instance with 85,900 points in 136 CPU-years.
- Fast factoring algorithms can break encryption schemes. Research determines what is safe code length (> 100 digits).
- Advent of quantum computing

$$O(n^2 2^n)$$

How to measure algorithm performance?

- What metric should be used to judge algorithms?
 - Length of the program (lines of code)
 - Ease of programming (bugs, maintenance)
 - Memory required
- ❑ **Running time**
- Running time is the dominant standard.
 - Quantifiable and easy to compare
 - Often the critical bottleneck

Average, Best, and Worst-Case

- On which input instances should the algorithm's performance be judged?
- Average case:
 - Real world distributions difficult to predict
 - Typically used in statistical machine learning
- Best case:
 - Seems unrealistic
- **Worst case:**
 - Gives an absolute guarantee
 - **Typical**

Caveats

- Follow the spirit, not the letter
 - A $100n$ algorithm is more expensive than an n^2 algorithm provided $n < 100$
- Other considerations:
 - a program used only a few times
 - a program run on small data sets
 - ease of coding, porting, maintenance
 - memory requirements

Worst case, Best case, and Average case

```
template<class T>
void SelectionSort(T a[], int n)
{ // Early-terminating version of selection sort
    bool sorted = false;
    for (int size=n; !sorted && (size>1); size--) {
        int pos = 0;
        sorted = true;
        // find largest in a[0,...,size-1]
        for (int i = 1; i < size; i++)
            if (a[pos] <= a[i]) pos = i;
        else sorted = false; // out of order
        Swap(a[pos], a[size - 1]);
    }
}
```

Worst case?

Best case?

Average case?

Breakout

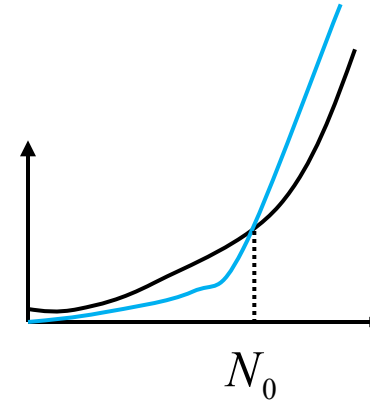
Asymptotic Notations

- **Big-O**, “bounded above by”: $T(n) = O(f(n))$
 - For some c and N , $T(n) \leq c \cdot f(n)$ whenever $n > N$.
- **Big-Omega**, “bounded below by”: $T(n) = \Omega(f(n))$
 - For some $c > 0$ and N , $T(n) \geq c \cdot f(n)$ whenever $n > N$.
 - Same as $f(n)$ is $O(T(n))$.
- **Big-Theta**, “bounded above and below by”: $T(n) = \Theta(f(n))$
 - $T(n)$ is $O(f(n))$ and also $T(n)$ is $\Omega(f(n))$
- **Little-o**, “strictly bounded above by”: $T(n) = o(f(n))$
 - $T(n)/f(n) \rightarrow 0$ as $n \rightarrow \infty$

In pictures

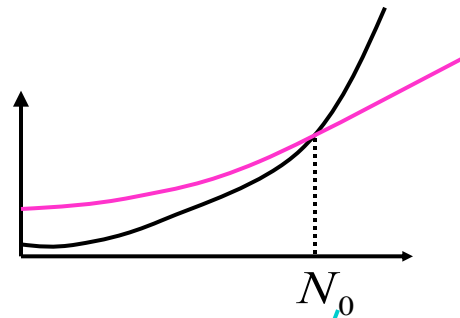
- **Big-Oh** (most commonly used)

- bounded above



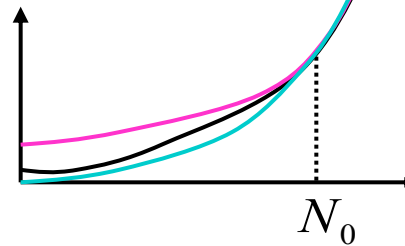
- **Big-Omega**

- bounded below



- **Big-Theta**

- exactly



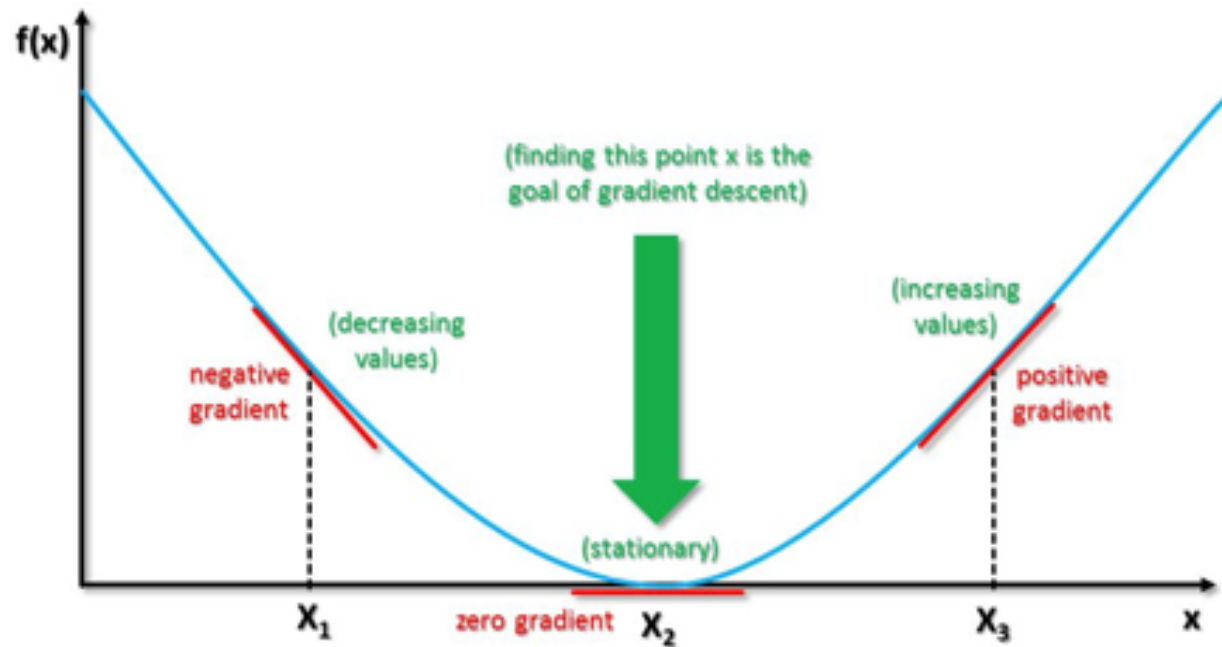
- **Small-o**

- not as expensive as ...

Design of algorithms

- Understand the problem, assess its difficulty
- Choose an approach (e.g., exact/approximate, deterministic/probabilistic)
- Choose strategy and appropriate data structures
- Prove
 - termination
 - correctness and completeness
- Evaluate complexity
 - We wish to not only find a solution, but to find the best or optimal solution.
 - Or, show that no efficient solution exists.
- Compare to other known approaches

Gradient descent in Deep Learning



How to tell man from mouse?

- Dynamic programming of DNA/protein sequences
- Global alignment algorithm of Needleman and Wunsch (1970)
- Local alignment algorithm of Smith and Waterman (1981)

```
1 MVHLTPEEKSAVTALWGKV--NVDEVGGEALGRLLVVYPWTQRFFESFGD      48
  || |:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|
1 MV-LSPADKTNVKAAWGKVGAHAGEYGAEALERMFLSFPTTKTYFPHF-D      48

49 LSTPDVAVMGNPKVKKAHGKKVLGAFSDGLAHL DNLKGT FATLSELHCDKLH    98
  ||      |:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|
49 LS-----HGSAQVKGHGKKVADAL TNAVAHVDDMPNALSALSDLHAHKLR    93

99 VDPENFRLLGNVLVCVLAHHFGKEFTPPVQAAYQKVVAGVANALAHKYH      147
  |||:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|:|
94 VDPVNFKLLSHCLLVTLAAHLPAEFTPAVHASLDKFLASVSTVLTSKYR      142
```

Matching of medical residents

- Residents rank colleges
- Colleges rank residents
- Find a stable matching:
 - There is no pair such that flipping the assignments leads to a “better” outcome.
- Solution runs in $O(n^2)$ time.
- Nobel prize in Economics 2012 to Shapley and Roth
- Many stable matchings are possible
 - Choosing the one that is best or that cannot be manipulated has been researched extensively.

Which webpages to display in a search

- Ranking based on keywords/topics
- Ranking based on importance of pages
- Examine the link structure of pages by random walk
- Display the central pages first
- **Good** authorities should be pointed by **good** authorities
 - The value of a node is determined by the value of the nodes that point to it.
- Google's PageRank