

Package ‘RDHonest’

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Title Honest inference in regression discontinuity designs

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Description Honest and nearly-optimal confidence intervals in fuzzy and sharp regression discontinuity designs and for inference at a point based on local polynomial regression.

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License GPL-3

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Formula

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cghs

*Oreopoulos (2006) UK general household survey dataset***Description**

Oreopoulos (2006) UK general household survey dataset

Usage

cghs

Format

A data frame with 73,954 rows and 2 variables:

earnings Annual earnings in 1998 (UK pounds)**yearat14** Year individual turned 14**Source**American Economic Review data archive, <https://doi.org/10.1257/000282806776157641>

References

Oreopoulos, P. (2006): "Estimating Average and Local Average Treatment Effects When Compulsory Education Schooling Laws Really Matter", *American Economic Review*, 96 (1), 152-175

 CVb

Critical values for CIs based on a biased Gaussian estimator.

Description

Computes the critical value $cv_{1-\alpha}(B)$ such that the confidence interval $X \pm cv_{1-\alpha}(B)$ will have coverage $1 - \alpha$, where X is normally distributed with variance equal to 1 and maximum bias at most B .

Usage

```
CVb(B, alpha = 0.05)
```

Arguments

B	Maximum bias, vector of non-negative numbers.
alpha	Determines CI level, $1 - \alpha$. Vector of values between 0 and 1.

Value

Data frame with the following columns:

bias Value of bias as specified by B

alpha Value of α as specified by alpha

cv Critical value

TeXDescription LaTeX-friendly description of the current row

Examples

```
## 90% critical value:
CVb(B = 1, alpha = 0.1)
## Returns data frame with 4 rows
CVb(B = c(0, 0.5, 1), alpha = c(0.05, 0.1))
```

EqKern	<i>Equivalent kernel for local linear regression.</i>
--------	-------------------------------------------------------

Description

Calculates equivalent kernel for local polynomial regression.

Usage

```
EqKern(kernel = "uniform", boundary = TRUE, order = 0)
```

Arguments

kernel	kernel type. Can be a function supported on $[0, 1]$ (boundary kernel) or $[-1, 1]$ (interior kernel), or else one of "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$).
boundary	Logical scalar, specifying whether we are at a boundary.
order	Order of local polynomial: 0 means local constant, 1 local linear, 2 local quadratic etc.

Value

Equivalent kernel function.

Examples

```
EqKern(kernel = "uniform", order = 2)
```

FRDDData	<i>Class Constructor for "FRDDData"</i>
----------	-----------------------------------------

Description

Convert data to a standardized format for use with low-level functions. If the cutoff for treatment is non-zero, shift the running variable so that the cutoff is at zero.

Usage

```
FRDDData(d, cutoff)
```

Arguments

- d** list with first element corresponding to the outcome vector, second element to the treatment vector, third element to running variable vector, and optionally an element called "sigma2" that is a matrix with four columns corresponding to the [1, 1], [1, 2], [2, 1], and [2, 2] elements of the conditional variance matrix of the outcome and the treatment (or an estimate of the conditional variance matrix)
- cutoff** specifies the cutoff for the running variable

Value

An object of class "FRDData", which is a list containing the following components:

- Ym** Matrix of outcomes and treatments for observations below cutoff
- Yp** Matrix of outcomes and treatments for observations above cutoff
- Xm** Running variable for observations below cutoff
- Xp** Running variable for observations above cutoff
- sigma2m** Matrix of conditional covariances for the outcome and the treatment for observations below cutoff
- sigma2p** Matrix of conditional covariances for the outcome and the treatment for observations above cutoff
- orig.cutoff** Original cutoff
- var.names** Names of the outcome, the treatment, and the running variable in supplied data frame

See Also

[RDDData](#) for sharp RD, and [LPPData](#) for inference at a point

Examples

```
## Transform retirement data
d <- FRDData(rcp[, c(6, 3, 2)], cutoff=0)
## Outcome in logs
d <- FRDData(cbind(logcn=log(rcp[, 6]), rcp[, c(3, 2)]), cutoff=0)
```

headst

Head Start data from Ludwig and Miller (2007)

Description

Subset of Ludwig-Miller data. Counties with missing poverty rate, or with both outcomes missing (hs and mortality) were removed. In the original dataset, Yellowstone County, MT (oldcode = 27056) was entered twice, here the duplicate is removed. Yellowstone National Park, MT (oldcode = 27057) is also removed due to it being an outlier for both outcomes. Counties with oldcode equal to (3014, 32032, 47010, 47040, 47074, 47074, 47078, 47079, 47096) matched more than one FIPS entry, so the county labels may not be correct. Mortality data is missing for Alaska.

Usage

```
headst
```

Format

A data frame with 3,127 rows and 9 variables:

statefp State FIPS code

countyfp County FIPS code

oldcode ID in Ludwig-Miller dataset

povrate60 Poverty rate in 1960 relative to 300th poorest county (which had poverty rate 59.1984)

mortHS Average Mortality rate per 100,000 for children aged 5-9 over 1973–83 due to causes addressed as part of Head Start’s health services.

mortInj Average Mortality rate per 100,000 for children aged 5-9 over 1973–83 due to injury.

highSchool High school completion rate in 1990 census, ages 18-24

statepc State postal code

county County name

Source

Douglas Miller’s website, <http://faculty.econ.ucdavis.edu/faculty/dlmiller/statafiles/>

References

Ludwig , J., and D. L. Miller (2007): "Does Head Start improve children’s life chances? Evidence from a regression discontinuity design," *Quarterly Journal of Economics*, 122 (1), 159-208.

IKBW.fit

Imbens and Kalyanaraman bandwidth

Description

Calculate bandwidth for sharp RD based on local linear regression using method by Imbens and Kalyanaraman (2012)

Usage

```
IKBW.fit(d, kern = "triangular", order = 1, verbose = FALSE)
```

Arguments

d	object of class "RDDData"
kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
order	Order of local regression 1 for linear, 2 for quadratic.
verbose	Print details of calculation?

Value

Imbens and Kalyanaraman bandwidth

References

Imbens, Guido, and Kalyanaraman, Karthik, "Optimal bandwidth choice for the regression discontinuity estimator." *The Review of Economic Studies* 79 (3): 933-959.

Examples

```
## Reproduce bandwidth from Section 6.2 in Imbens and Kalyanaraman (2012)
IKBW.fit(RDDData(lee08, cutoff=0))
```

kernC

Constants for common kernels.

Description

First four moments of uniform, triangular, and Epanechnikov equivalent kernels. Up to numerical integration precision, these moments are matched by `KernMoment()`. See vignette `lpkernels`

Usage

```
kernC
```

Format

A data frame with 18 rows and 19 variables:

kernel Kernel type.

order Order of local polynomial.

boundary Boundary regression?

mu0, mu1, mu2, mu3, mu4 $\int_X u^j k(u) du$, raw moments

nu0, nu1, nu2, nu3, nu4 $\int_X u^j k^2(u) du$, raw moments of kernel squared

pi0, pi1, pi2, pi3, pi4 $\int_X |u^j k(u)| du$, absolute moments

pMSE constant for pointwise MSE optimal bandwidth, $((p+1)!^2 \nu_0 / (2(p+1) \mu_{p+1}^2))^{1/(2p+3)}$, see page 67 in Fan and Gijbels (1996)

Source

Computed analytically using symbolic math software

References

Fan, J., and I. Gijbels (1996): *Local Polynomial Modelling and Its Applications*, *Monographs on Statistics and Applied Probability*. Chapman & Hall/CRC, New York, NY.

KernMoment	<i>Moments of a kernel.</i>
------------	-----------------------------

Description

Computes moments of a kernel over $X = [0, 1]$ (boundary case), or $X = [-1, 1]$ (interior case),

Usage

KernMoment(K, moment = 0, boundary = TRUE, type = "raw")

Arguments

- K kernel function.
- moment order j of moment to compute.
- boundary Logical scalar, specifying whether we are at a boundary.
- type Type of moment. "raw" computes $\int_X u^j k(u)$, "absolute" computes $\int_X |u^j k(u)|$, and "raw2" computes $\int_X u^j k(u)^2$.

Value

Integral value (a scalar).

Examples

```
KernMoment(function(u) abs(u) < 1, moment = 3, boundary = FALSE)
KernMoment(EqKern(kernel = "triangular", order = 2), moment = 3)
```

lee08	<i>Lee (2008) US House elections dataset</i>
-------	----------------------------------------------

Description

Lee (2008) US House elections dataset

Usage

lee08

Format

A data frame with 6,558 rows and 2 variables:

- voteshare** Vote share in next election
- margin** Democratic margin of victory

Source

Mostly Harmless Econometrics data archive, <https://economics.mit.edu/faculty/angrist/data1/mhe>

References

Lee, D. S. (2008): "Randomized experiments from non-random selection in U.S. House elections," *Journal of Econometrics*, 142 (2), 675-697.

LPPData

Class Constructor for "LPPData"

Description

Convert data to standardized format for use with low-level functions. If the point of interest x_0 is non-zero, shift the independent variable so that it is at zero.

Usage

```
LPPData(d, point)
```

Arguments

d	a data frame or a list with first column corresponding to the outcome variable, second column corresponding to the independent variable and optionally a column called "sigma2" that corresponds to the conditional variance of the outcome (or an estimate of the conditional variance)
point	specifies the point x_0 at which to calculate the conditional mean

Value

An object of class "LPPData", which is a list containing the following components:

Y Outcome vector

X Independent variable

sigma2 Conditional variance of the outcome

orig.point Original value of x_0

var.names Names of outcome and independent variable in supplied data frame

See Also

[FRDDData](#) for fuzzy RD, and [RDDData](#) for sharp RD

Examples

```
## Transform Lee data
d1 <- LPPData(lee08[lee08$margin>=0, ], point=0)
d2 <- LPPData(lee08, point=50)
```

LPPHonest

*Honest inference at a point***Description**

Calculate estimators and one- and two-sided honest CIs for value of conditional mean at a point based on a local polynomial estimator under second-order Taylor or Hölder smoothness class.

Usage

```
LPPHonest(formula, data, subset, point = 0, M, kern = "triangular",
  na.action, opt.criterion, h, se.method = "nn", alpha = 0.05,
  beta = 0.8, J = 3, sclass = "H", order = 1, se.initial = "EHW")
```

Arguments

formula	object of class "formula" (or one that can be coerced to that class) of the form <code>outcome ~ independent_variable</code>
data	optional data frame, list or environment (or object coercible by <code>as.data.frame</code> to a data frame) containing the outcome and independent variables in the model. If not found in data, the variables are taken from <code>environment(formula)</code> , typically the environment from which the function is called.
subset	optional vector specifying a subset of observations to be used in the fitting process.
point	specifies the point x_0 at which to calculate the conditional mean
M	Bound on second derivative of the conditional mean function.
kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
na.action	function which indicates what should happen when the data contain NAs. The default is set by the <code>na.action</code> setting of options (usually <code>na.omit</code>).
opt.criterion	<p>Optimality criterion that bandwidth is designed to optimize. The options are:</p> <p>"MSE" Finite-sample maximum MSE</p> <p>"FLCI" Length of (fixed-length) two-sided confidence intervals.</p> <p>"OCI" Given quantile of excess length of one-sided confidence intervals</p> <p>The methods use conditional variance given by <code>sigma2</code>, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by <code>se.initial</code>.</p>
h	bandwidth, a scalar parameter. For fuzzy or sharp RD, it can be a named vector of length two with names "p" and "m", in which case the bandwidth <code>h["m"]</code> is used for observations below the cutoff, and the bandwidth <code>h["p"]</code> is used for observations above the cutoff. If not supplied, optimal bandwidth is computed according to criterion given by <code>opt.criterion</code> .

<code>se.method</code>	<p>Vector with methods for estimating standard error of estimate. If NULL, standard errors are not computed. The elements of the vector can consist of the following methods:</p> <p>"nn" Nearest neighbor method</p> <p>"EHW" Eicker-Huber-White, with residuals from local regression (local polynomial estimators only).</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). Local polynomial estimators only.</p> <p>"plugin" Plug-in estimate based on asymptotic variance. Local polynomial estimators in sharp RD only.</p> <p>"supplied.var" Use conditional variance supplied by <code>sigma2</code> or <code>d</code> instead of computing residuals</p>
<code>alpha</code>	determines confidence level, $1-\alpha$ for constructing/optimizing confidence intervals.
<code>beta</code>	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
<code>J</code>	Number of nearest neighbors, if "nn" is specified in <code>se.method</code> .
<code>sclass</code>	Smoothness class, either "T" for Taylor or "H" for Hölder class.
<code>order</code>	Order of local regression 1 for linear, 2 for quadratic.
<code>se.initial</code>	<p>Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).</p> <p>"EHW" Based on residuals from a local linear regression using a triangular kernel, and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).</p> <p>"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)</p> <p>"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.</p> <p>"nn" Use nearest neighbor estimates, without assuming homoscedasticity</p>

Details

The bandwidth is calculated to be optimal for a given performance criterion, as specified by `opt.criterion`. It is calculated using the function [LPPOptBW](#). Alternatively, the bandwidth can be specified by `h`.

Value

Returns an object of class "NResults". The function `print` can be used to obtain and print a summary of the results. An object of class "NPRResults" is a list containing the following components

`estimate` Point estimate. This estimate is MSE-optimal if `opt.criterion="MSE"`

`lff` Not relevant for inference at a point

`maxbias` Maximum bias of estimate

`sd` Standard deviation of estimate

`lower, upper` Lower (upper) end-point of a one-sided CI based on estimate. This CI is optimal if `opt.criterion="OCI"`

`hl` Half-length of a two-sided CI based on estimate, so the CI is `c(estimate-hl, estimate+hl)`. The CI is optimal if `opt.criterion="FLCI"`

`eff.obs` Effective number of observations used by estimate

`hp, hm` Bandwidth used, both numbers are equal (i.e. `hp=hm`)

`naive` Coverage of CI that ignores bias and uses `qnorm(1-alpha/2)` as critical value

`call` The matched call

`fs` Not relevant for inference at a point

Note

`subset` is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.

References

Armstrong, Timothy B., and Michal Kolesár. 2019. "Simple and Honest Confidence Intervals in Nonparametric Regression", *arXiv: 1606.01200*.

See Also

[LPP0ptBW](#)

Examples

```
# Lee dataset
LPPHonest(votesshare ~ margin, data = lee08, subset = margin>0,
          kern = "uniform", M = 0.1, h = 10, sclass = "T")
```

LPPOptBW

*Optimal Bandwidth Selection for inference at a point***Description**

Estimate bandwidth based on local polynomial regression that optimizes either maximum mean squared error, or length or quantiles of excess length of a honest CI under second order Hölder or Taylor class.

Usage

```
LPPOptBW(formula, data, subset, point = 0, M, kern = "triangular",
  na.action, opt.criterion, alpha = 0.05, beta = 0.8, sclass = "H",
  order = 1, se.initial = "EHW")
```

Arguments

formula	object of class "formula" (or one that can be coerced to that class) of the form <code>outcome ~ independent_variable</code>
data	optional data frame, list or environment (or object coercible by <code>as.data.frame</code> to a data frame) containing the outcome and independent variables in the model. If not found in data, the variables are taken from <code>environment(formula)</code> , typically the environment from which the function is called.
subset	optional vector specifying a subset of observations to be used in the fitting process.
point	specifies the point x_0 at which to calculate the conditional mean
M	Bound on second derivative of the conditional mean function.
kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
na.action	function which indicates what should happen when the data contain NAs. The default is set by the <code>na.action</code> setting of options (usually <code>na.omit</code>).
opt.criterion	<p>Optimality criterion that bandwidth is designed to optimize. The options are:</p> <p>"MSE" Finite-sample maximum MSE</p> <p>"FLCI" Length of (fixed-length) two-sided confidence intervals.</p> <p>"OCI" Given quantile of excess length of one-sided confidence intervals</p> <p>The methods use conditional variance given by <code>sigma2</code>, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by <code>se.initial</code>.</p>
alpha	determines confidence level, $1 - \alpha$ for constructing/optimizing confidence intervals.
beta	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.

sclass	Smoothness class, either "T" for Taylor or "H" for Hölder class.
order	Order of local regression 1 for linear, 2 for quadratic.
se.initial	Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point). "EHW" Based on residuals from a local linear regression using a triangular kernel, and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression. "demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). "Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012) "SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals. "nn" Use nearest neighbor estimates, without assuming homoscedasticity

Value

Returns an object of class "NPRBW". The function `print` can be used to obtain and print a summary of the results. An object of class "NPRBW" is a list containing the following components:

h Bandwidth
sigma2 estimate of conditional variance at a point
call the matched call
na.action (where relevant) information on handling of missing data.

Note

subset is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.

References

Armstrong, Timothy B., and Michal Kolesár. 2019. "Simple and Honest Confidence Intervals in Nonparametric Regression", *arXiv: 1606.01200*.

See Also

[LPPHonest](#)

Examples

```
# Lee dataset
LPP0ptBW(voteshare ~ margin, data = lee08, subset=margin>0,
         kern = "uniform", M = 0.1, opt.criterion = "MSE", sclass = "H")
```

NPR_MROT.fit

Rule of thumb for choosing M

Description

Use global quartic regression to estimate a bound on the second derivative for inference under second order Hölder class. For RD, use a separate regression on either side of the cutoff

Usage

```
NPR_MROT.fit(d)
```

Arguments

d object of class "RDDData", "FRDDData", or "LPPData".

Examples

```
NPR_MROT.fit(RDDData(lee08, cutoff=0))
NPR_MROT.fit(LPPData(lee08[lee08$margin>0, ], point=0))
d <- FRDDData(cbind(logcn=log(rcp[, 6 ]), rcp[, c(3, 2)]), cutoff=0)
NPR_MROT.fit(d)
```

NPRHonest.fit

Honest inference in nonparametric regression

Description

Basic computing engine called by [RDHonest](#), [LPPHonest](#), and [FRDHonest](#) to compute honest confidence intervals for local polynomial estimators.

Usage

```
NPRHonest.fit(d, M, kern = "triangular", h, opt.criterion,
             bw.equal = TRUE, alpha = 0.05, beta = 0.8, se.method = "nn",
             J = 3, sclass = "H", order = 1, se.initial = "EHW", T0 = 0,
             T0bias = FALSE)
```

Arguments

<code>d</code>	object of class "RDDData", "FRDDData", or "LPPData"
<code>M</code>	Bound on second derivative of the conditional mean function.
<code>kern</code>	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
<code>h</code>	bandwidth, a scalar parameter. For fuzzy or sharp RD, it can be a named vector of length two with names "p" and "m", in which case the bandwidth $h["m"]$ is used for observations below the cutoff, and the bandwidth $h["p"]$ is used for observations above the cutoff. If not supplied, optimal bandwidth is computed according to criterion given by <code>opt.criterion</code> .
<code>opt.criterion</code>	Optimality criterion that bandwidth is designed to optimize. The options are: "mse" Finite-sample maximum MSE "flci" Length of (fixed-length) two-sided confidence intervals. "oci" Given quantile of excess length of one-sided confidence intervals The methods use conditional variance given by <code>sigma2</code> , if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by <code>se.initial</code> .
<code>bw.equal</code>	logical specifying whether bandwidths on either side of cutoff should be constrained to equal to each other.
<code>alpha</code>	determines confidence level, $1 - \alpha$ for constructing/optimizing confidence intervals.
<code>beta</code>	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
<code>se.method</code>	Vector with methods for estimating standard error of estimate. If NULL, standard errors are not computed. The elements of the vector can consist of the following methods: "nn" Nearest neighbor method "EHW" Eicker-Huber-White, with residuals from local regression (local polynomial estimators only). "demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). Local polynomial estimators only. "plugin" Plug-in estimate based on asymptotic variance. Local polynomial estimators in sharp RD only. "supplied.var" Use conditional variance supplied by <code>sigma2</code> or <code>d</code> instead of computing residuals
<code>J</code>	Number of nearest neighbors, if "nn" is specified in <code>se.method</code> .
<code>sclass</code>	Smoothness class, either "T" for Taylor or "H" for Hölder class.
<code>order</code>	Order of local regression 1 for linear, 2 for quadratic.
<code>se.initial</code>	Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).

	<p>"EHW" Based on residuals from a local linear regression using a triangular kernel, and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).</p> <p>"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)</p> <p>"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.</p> <p>"nn" Use nearest neighbor estimates, without assuming homoscedasticity</p>
T0	Initial estimate of the treatment effect for calculating the optimal bandwidth. Only relevant for Fuzzy RD.
T0bias	When evaluating the maximum bias of the estimate, use the estimate itself (if T0bias==FALSE), or use the preliminary estimate T0 (if T0bias==TRUE). Only relevant for Fuzzy RD.

Value

Returns an object of class "NPRResults", see descriptions in [RDHonest](#), [LPPHonest](#), and [FRDHonest](#).

Examples

```
d <- RDData(lee08, cutoff=0)
NPRHonest.fit(d, opt.criterion="MSE", M=NPR_MROT.fit(d))
```

NPROptBW.fit

Optimal bandwidth selection in nonparametric regression

Description

Basic computing engine called by [RDOptBW](#), [FRDOptBW](#), and [LPPOptBW](#) to compute the optimal bandwidth

Usage

```
NPROptBW.fit(d, M, kern = "triangular", opt.criterion, bw.equal = TRUE,
  alpha = 0.05, beta = 0.8, sclass = "H", order = 1,
  se.initial = "EHW", T0 = 0)
```

Arguments

<code>d</code>	object of class "RDData", "FRDDData", or "LPPData"
<code>M</code>	Bound on second derivative of the conditional mean function.
<code>kern</code>	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
<code>opt.criterion</code>	<p>Optimality criterion that bandwidth is designed to optimize. The options are:</p> <p>"MSE" Finite-sample maximum MSE</p> <p>"FLCI" Length of (fixed-length) two-sided confidence intervals.</p> <p>"OCI" Given quantile of excess length of one-sided confidence intervals</p> <p>The methods use conditional variance given by <code>sigma2</code>, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by <code>se.initial</code>.</p>
<code>bw.equal</code>	logical specifying whether bandwidths on either side of cutoff should be constrained to equal to each other.
<code>alpha</code>	determines confidence level, $1 - \alpha$ for constructing/optimizing confidence intervals.
<code>beta</code>	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
<code>sclass</code>	Smoothness class, either "T" for Taylor or "H" for Hölder class.
<code>order</code>	Order of local regression 1 for linear, 2 for quadratic.
<code>se.initial</code>	<p>Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).</p> <p>"EHW" Based on residuals from a local linear regression using a triangular kernel, and and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).</p> <p>"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)</p> <p>"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.</p> <p>"nn" Use nearest neighbor estimates, without assuming homoscedasticity</p>
<code>T0</code>	Initial estimate of the treatment effect for calculating the optimal bandwidth. Only relevant for Fuzzy RD.

Value

Returns an object of class "NPRBW", see descriptions in [RDOptBW](#), [FRDOptBW](#), and [LPPOptBW](#).

References

Imbens, Guido, and Kalyanaraman, Karthik, "Optimal bandwidth choice for the regression discontinuity estimator." *The Review of Economic Studies* 79 (3): 933-959.

Examples

```
## Lee data
d <- RDDData(lee08, cutoff=0)
NPROptBW.fit(d, M=0.1, opt.criterion="MSE")[c("hp", "hm")]
```

NPRPrelimVar.fit	<i>Compute preliminary estimate of variance</i>
------------------	-------------------------------------------------

Description

Compute estimate of variance, which can then be used in optimal bandwidth calculations.

Usage

```
NPRPrelimVar.fit(d, se.initial = "EHW")
```

Arguments

- | | |
|------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| d | object of class "RDDData", "FRDDData", or "LPPData" |
| se.initial | Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).

"EHW" Based on residuals from a local linear regression using a triangular kernel, and and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.
"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).
"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)
"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.
"nn" Use nearest neighbor estimates, without assuming homoscedasticity |

Value

object of the same class as d containing estimated variances.

NPRreg.fit

*Nonparametric Regression***Description**

Calculate fuzzy or sharp RD estimate, or estimate of a conditional mean at a point (depending on the class of d), and its variance using local polynomial regression of order order.

Usage

```
NPRreg.fit(d, h, kern = "triangular", order = 1, se.method = "nn",
  no.warning = FALSE, J = 3)
```

Arguments

d	object of class "LPPData", "RDDData", or "FRDDData"
h	bandwidth, a scalar parameter. For fuzzy or sharp RD, it can be a named vector of length two with names "p" and "m", in which case the bandwidth $h["m"]$ is used for observations below the cutoff, and the bandwidth $h["p"]$ is used for observations above the cutoff. If not supplied, optimal bandwidth is computed according to criterion given by <code>opt.criterion</code> .
kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
order	Order of local regression 1 for linear, 2 for quadratic.
se.method	Vector with methods for estimating standard error of estimate. If NULL, standard errors are not computed. The elements of the vector can consist of the following methods: "nn" Nearest neighbor method "EHW" Eicker-Huber-White, with residuals from local regression (local polynomial estimators only). "demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). Local polynomial estimators only. "plugin" Plug-in estimate based on asymptotic variance. Local polynomial estimators in sharp RD only. "supplied.var" Use conditional variance supplied by <code>sigma2</code> or <code>d</code> instead of computing residuals
no.warning	Don't warn about too few observations
J	Number of nearest neighbors, if "nn" is specified in <code>se.method</code> .

Value

list with elements:

estimate point estimate

se Named vector of standard error estimates, as specified by `se.method`.

w Implicit weight function used

sigma2 Estimate of $\sigma^2(X)$ for values of X receiving positive kernel weight. By default, estimates are based on squared regression residuals, as used in "EHW". If `se.method="demeaned"` or `se.method="nn"` is specified, estimates are based on that method, with "nn" method used if both are specified.

eff.obs Number of effective observations

Examples

```
NPRreg.fit(RDData(lee08, cutoff=0), h=5, order=2, se.method=c("nn", "plugin", "EHW"))
NPRreg.fit(LPPData(lee08[lee08$margin>=0, ], point=0), h=5, order=1)
d <- FRDData(cbind(logcn=log(rcp[, 6]), rcp[, c(3, 2)]), cutoff=0)
NPRreg.fit(d, h=10, order=1)
```

plot_RDscatter

Scatterplot of binned raw observations

Description

Scatterplot of raw observations in which each point corresponds to an binned average.

Usage

```
plot_RDscatter(d, avg = 10, xlab = NULL, ylab = NULL,
  window = NULL, vert = TRUE, propdotsize = FALSE)
```

Arguments

<code>d</code>	Object of class "RDdata"
<code>avg</code>	Number of observations to average over. If set to <code>Inf</code> , then take averages for each possible value of the running variable (convenient when the running variable is discrete).
<code>xlab, ylab</code>	x- and y-axis labels
<code>window</code>	Width of a window around cutoff to which the graph should be restricted. If not specified, full data range will be plotted
<code>vert</code>	Draw a vertical line at cutoff?
<code>propdotsize</code>	If <code>TRUE</code> , then size of points is proportional to number of observations that the point averages over (useful when <code>avg=Inf</code>). Otherwise the size of points is constant.

Examples

```
plot_RDscatter(RDData(lee08, cutoff=0), avg=20)
plot_RDscatter(RDData(data.frame(y=log(cghs$earnings), x=cghs$yearat14),
                               cutoff=1947), avg=Inf, proddotsize=TRUE)
```

rcp

*Battistin et al. (2009) retirement consumption puzzle dataset***Description**

Battistin et al. (2009) retirement consumption puzzle dataset

Usage

```
rcp
```

Format

A data frame with 30,006 rows and 6 variables:

survey_year Survey year

elig_year Years to/from eligibility (males)

retired Retirement status (males)

food Total household food expenditure

c Total household consumption

cn Total household nondurables expenditure

Source

American Economic Review data archive, <https://doi.org/10.1257/aer.99.5.2209>

References

Battistin, Erich, Agar Brugiavini, Enrico Rettore, and Guglielmo Weber. 2009. "The Retirement Consumption Puzzle: Evidence from a Regression Discontinuity Approach." *American Economic Review* 99 (5): 2209–26.

RDData

Class Constructor for "RDData"

Description

Convert data to a standardized format for use with low-level functions. If the cutoff for treatment is non-zero, shift the running variable so that the cutoff is at zero.

Usage

```
RDData(d, cutoff)
```

Arguments

d	a data frame or a list with first column corresponding to the outcome variable, second column corresponding to the running variable and optionally a column called "sigma2" that corresponds to the conditional variance of the outcome (or an estimate of the conditional variance)
cutoff	specifies the cutoff for the running variable

Value

An object of class "RDData", which is a list containing the following components:

Ym Outcome vector for observations below cutoff

Yp Outcome vector for observations above cutoff

Xm Running variable for observations below cutoff

Xp Running variable for observations above cutoff

sigma2m Conditional variance of the outcome for observations below cutoff

sigma2p Conditional variance of the outcome for observations above cutoff

orig.cutoff Original cutoff

var.names Names of the outcome and the running variable in supplied data frame

See Also

[FRDData](#) for fuzzy RD, and [LPPData](#) for inference at a point

Examples

```
## Transform Lee data
d <- RDData(lee08, cutoff=0)
```

RDHonest

*Honest inference in RD***Description**

Calculate estimators and one- and two-sided CIs based on local polynomial estimator in RD under second-order Taylor or Hölder smoothness class. If kern="optimal", calculate optimal estimators under second-order Taylor smoothness class.

Usage

```
RDHonest(formula, data, subset, cutoff = 0, M, kern = "triangular",
  na.action, opt.criterion, bw.equal = TRUE, h, se.method = "nn",
  alpha = 0.05, beta = 0.8, J = 3, sclass = "H", order = 1,
  se.initial = "EHW")
```

Arguments

formula	object of class "formula" (or one that can be coerced to that class) of the form outcome ~ running_variable
data	optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the outcome and running variables in the model. If not found in data, the variables are taken from environment(formula), typically the environment from which the function is called.
subset	optional vector specifying a subset of observations to be used in the fitting process.
cutoff	specifies the RD cutoff in the running variable.
M	Bound on second derivative of the conditional mean function.
kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
na.action	function which indicates what should happen when the data contain NAs. The default is set by the na.action setting of options (usually na.omit).
opt.criterion	Optimality criterion that bandwidth is designed to optimize. The options are: "mse" Finite-sample maximum MSE "flci" Length of (fixed-length) two-sided confidence intervals. "oci" Given quantile of excess length of one-sided confidence intervals The methods use conditional variance given by sigma2, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by se.initial.
bw.equal	logical specifying whether bandwidths on either side of cutoff should be constrained to equal to each other.

h	bandwidth, a scalar parameter. For fuzzy or sharp RD, it can be a named vector of length two with names "p" and "m", in which case the bandwidth $h["m"]$ is used for observations below the cutoff, and the bandwidth $h["p"]$ is used for observations above the cutoff. If not supplied, optimal bandwidth is computed according to criterion given by <code>opt.criterion</code> .
se.method	<p>Vector with methods for estimating standard error of estimate. If NULL, standard errors are not computed. The elements of the vector can consist of the following methods:</p> <p>"nn" Nearest neighbor method</p> <p>"EHW" Eicker-Huber-White, with residuals from local regression (local polynomial estimators only).</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). Local polynomial estimators only.</p> <p>"plugin" Plug-in estimate based on asymptotic variance. Local polynomial estimators in sharp RD only.</p> <p>"supplied.var" Use conditional variance supplied by <code>sigma2</code> or <code>d</code> instead of computing residuals</p>
alpha	determines confidence level, 1-alpha for constructing/optimizing confidence intervals.
beta	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
J	Number of nearest neighbors, if "nn" is specified in <code>se.method</code> .
sclass	Smoothness class, either "T" for Taylor or "H" for Hölder class.
order	Order of local regression 1 for linear, 2 for quadratic.
se.initial	<p>Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).</p> <p>"EHW" Based on residuals from a local linear regression using a triangular kernel, and and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).</p> <p>"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)</p> <p>"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.</p> <p>"nn" Use nearest neighbor estimates, without assuming homoscedasticity</p>

Details

The bandwidth is calculated to be optimal for a given performance criterion, as specified by `opt.criterion`. For local polynomial estimators, this optimal bandwidth is calculated using the function [RDOptBW](#). Alternatively, for local polynomial estimators, the bandwidths above and below the cutoff can be specified by `h`.

Value

Returns an object of class "RDResults". The function `print` can be used to obtain and print a summary of the results. An object of class "RDResults" is a list containing the following components

`estimate` Point estimate. This estimate is MSE-optimal if `opt.criterion="MSE"`
`lff` Least favorable function, only relevant for optimal estimator under Taylor class.
`maxbias` Maximum bias of estimate
`sd` Standard deviation of estimate
`lower, upper` Lower (upper) end-point of a one-sided CI based on estimate. This CI is optimal if `opt.criterion=="OCI"`
`hl` Half-length of a two-sided CI based on estimate, so that the CI is given by `c(estimate-hl, estimate+hl)`. The CI is optimal if `opt.criterion="FLCI"`
`eff.obs` Effective number of observations used by estimate
`hp, hm` Bandwidths used above and below the cutoff
`naive` Coverage of CI that ignores bias and uses `qnorm(1-alpha/2)` as critical value
`call` the matched call
`fs` Not relevant for sharp RD

Note

`subset` is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.

References

Armstrong, Tim, and Michal Kolesár. 2018. "Optimal Inference in a Class of Regression Models." *Econometrica* 86 (2): 655–83.

Armstrong, Timothy B., and Michal Kolesár. 2019. "Simple and Honest Confidence Intervals in Nonparametric Regression", *arXiv: 1606.01200*.

Imbens, Guido, and Kalyanaraman, Karthik, "Optimal bandwidth choice for the regression discontinuity estimator." *The Review of Economic Studies* 79 (3): 933-959.

Kolesár, Michal, and Christoph Rothe. 2018. "Inference in Regression Discontinuity Designs with a Discrete Running Variable." *American Economic Review* 108 (8): 2277–2304.

See Also

[RDOptBW](#)

Examples

```
# Lee dataset
RDHonest(votesshare ~ margin, data = lee08, kern = "uniform", M = 0.1,
         h = 10, sclass = "T")
```

RDHonestBME	<i>CIs in sharp RD with discrete regressors under bounded misspecification error class</i>
-------------	--------------------------------------------------------------------------------------------

Description

Computes honest CIs for local linear regression with uniform kernel under the bounded misspecification error class of functions, as considered in Kolesár and Rothe (2018)

Usage

```
RDHonestBME(formula, data, subset, cutoff = 0, na.action, h = Inf,
            alpha = 0.05, order = 0, regformula)
```

Arguments

formula	object of class "formula" (or one that can be coerced to that class) of the form <code>outcome ~ running_variable</code>
data	optional data frame, list or environment (or object coercible by <code>as.data.frame</code> to a data frame) containing the outcome and running variables in the model. If not found in data, the variables are taken from <code>environment(formula)</code> , typically the environment from which the function is called.
subset	optional vector specifying a subset of observations to be used in the fitting process.
cutoff	specifies the RD cutoff in the running variable.
na.action	function which indicates what should happen when the data contain NAs. The default is set by the <code>na.action</code> setting of options (usually <code>na.omit</code>).
h	bandwidth, a scalar parameter. For fuzzy or sharp RD, it can be a named vector of length two with names "p" and "m", in which case the bandwidth <code>h["m"]</code> is used for observations below the cutoff, and the bandwidth <code>h["p"]</code> is used for observations above the cutoff. If not supplied, optimal bandwidth is computed according to criterion given by <code>opt.criterion</code> .
alpha	determines confidence level, $1 - \alpha$
order	Order of local regression 1 for linear, 2 for quadratic.
regformula	Explicitly specify regression formula as alternative to local linear regression, with y and x denoting the outcome and the running variable, and cutoff is normalized to 0. Local linear regression (<code>order = 1</code>) is equivalent to <code>regformula = "y~x*I(x>0)"</code> . Inference is done on the <code>order+2</code> th element of the design matrix

Note

subset is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.

References

Kolesár, Michal, and Christoph Rothe. 2018. "Inference in Regression Discontinuity Designs with a Discrete Running Variable." *American Economic Review* 108 (8): 2277–2304.

Examples

```
RDHonestBME(log(cghs$earnings)~yearat14, data=cghs, h=3,
              order=1, cutoff=1947)
## Equivalent to
RDHonestBME(log(cghs$earnings)~yearat14, data=cghs, h=3,
              cutoff=1947, order=1, regformula="y~x*I(x>=0)")
```

RDOptBW

Optimal Bandwidth Selection in Regression Discontinuity

Description

Estimate bandwidth for sharp RD based on local polynomial regression that optimizes either maximum mean squared error, or length or quantiles of excess length of a honest CI under second order Hölder or Taylor class.

Usage

```
RDOptBW(formula, data, subset, cutoff = 0, M, kern = "triangular",
         na.action, opt.criterion, bw.equal = TRUE, alpha = 0.05,
         beta = 0.8, sclass = "H", order = 1, se.initial = "EHW")
```

Arguments

formula	object of class "formula" (or one that can be coerced to that class) of the form outcome ~ running_variable
data	optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the outcome and running variables in the model. If not found in data, the variables are taken from environment(formula), typically the environment from which the function is called.
subset	optional vector specifying a subset of observations to be used in the fitting process.
cutoff	specifies the RD cutoff in the running variable.
M	Bound on second derivative of the conditional mean function.

kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
na.action	function which indicates what should happen when the data contain NAs. The default is set by the na.action setting of options (usually na.omit).
opt.criterion	<p>Optimality criterion that bandwidth is designed to optimize. The options are:</p> <p>"MSE" Finite-sample maximum MSE</p> <p>"FLCI" Length of (fixed-length) two-sided confidence intervals.</p> <p>"OCI" Given quantile of excess length of one-sided confidence intervals</p> <p>The methods use conditional variance given by sigma2, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by se.initial.</p>
bw.equal	logical specifying whether bandwidths on either side of cutoff should be constrained to equal to each other.
alpha	determines confidence level, 1-alpha for constructing/optimizing confidence intervals.
beta	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
sclass	Smoothness class, either "T" for Taylor or "H" for Hölder class.
order	Order of local regression 1 for linear, 2 for quadratic.
se.initial	<p>Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).</p> <p>"EHW" Based on residuals from a local linear regression using a triangular kernel, and and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).</p> <p>"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)</p> <p>"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.</p> <p>"nn" Use nearest neighbor estimates, without assuming homoscedasticity</p>

Value

Returns an object of class "RDBW". The function print can be used to obtain and print a summary of the results. An object of class "RDBW" is a list containing the following components:

hp bandwidth for observations above cutoff

`hm` bandwidth for observations below cutoff, equal to `hp` unless `bw.equal==FALSE`
`sigma2m, sigma2p` estimate of conditional variance just above and just below cutoff, $\sigma_+^2(0)$ and $\sigma_-^2(0)$
`f0` estimate of density of running variable at cutoff, if bandwidth computed using asymptotic method
`call` the matched call
`na.action` (where relevant) information on handling of missing data.

Note

subset is evaluated in the same way as variables in formula, that is first in data and then in the environment of formula.

References

Imbens, Guido, and Kalyanaraman, Karthik, "Optimal bandwidth choice for the regression discontinuity estimator." *The Review of Economic Studies* 79 (3): 933-959.

See Also

[RDHonest](#)

Examples

```
## Use Lee dataset
RDOptBW(voteshare ~ margin, data = lee08, kern = "uniform",
        M = 0.1, opt.criterion = "MSE", sclass = "H")
```

RDSmoothnessBound	<i>Lower bound on smoothness constant M in RD designs</i>
-------------------	-----------------------------------------------------------

Description

Estimate a lower bound on smoothness constant M and provide a lower confidence interval.

Usage

```
RDSmoothnessBound(d, s, separate = TRUE, multiple = TRUE,
  alpha = 0.05, sclass = "T")
```

Arguments

d	object of class "RDDData"
s	Number of support points that curvature estimates should average over
separate	If TRUE, report estimates separately for data above and below cutoff. If FALSE, report pooled estimates
multiple	If TRUE, use multiple curvature estimates. If FALSE, use a single estimate using only observations closest to the cutoff.
alpha	determines confidence level $1-\alpha$.
sclass	Smoothness class, either "T" for Taylor or "H" for Hölder class.

Value

Returns a list with the following elements

mu+, mu- Lower bound of CI for observations above and below cutoff
 Z+, Z- Point estimate used for lower bound
 sd+, sd- Standard deviations of point estimates

RDTEfficiencyBound *Finite-sample efficiency bounds for minimax CIs*

Description

Compute efficiency of minimax one-sided CIs at constant functions and half-length of Pratt CIs.

Usage

```
RDTEfficiencyBound(d, M, opt.criterion = "FLCI", alpha = 0.05,
  beta = 0.5, se.initial = "EHW")
```

Arguments

d	object of class "RDDData"
M	Bound on second derivative of the conditional mean function.
opt.criterion	Optimality criterion that bandwidth is designed to optimize. The options are: "MSE" Finite-sample maximum MSE "FLCI" Length of (fixed-length) two-sided confidence intervals. "OCI" Given quantile of excess length of one-sided confidence intervals The methods use conditional variance given by sigma2, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by se.initial.
alpha	determines confidence level, $1-\alpha$ for constructing/optimizing confidence intervals.

beta	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
se.initial	Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point). "EHW" Based on residuals from a local linear regression using a triangular kernel, and and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression. "demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). "Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012) "SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals. "nn" Use nearest neighbor estimates, without assuming homoscedasticity

RDTOpt.fit

Optimal inference in RD under Taylor class

Description

Basic computing engine called by [RDHonest](#) to compute honest confidence intervals for local optimal estimators in RD under second-order Taylor class.

Usage

```
RDTOpt.fit(d, M, opt.criterion, alpha = 0.05, beta = 0.5,
  se.method = "supplied.var", J = 3, se.initial = "IKEHW")
```

Arguments

d	object of class "RDDData"
M	Bound on second derivative of the conditional mean function.
opt.criterion	Optimality criterion that bandwidth is designed to optimize. The options are: "MSE" Finite-sample maximum MSE "FLCI" Length of (fixed-length) two-sided confidence intervals. "OCI" Given quantile of excess length of one-sided confidence intervals The methods use conditional variance given by sigma2, if supplied. Otherwise, for the purpose of estimating the optimal bandwidth, conditional variance is estimated using the method specified by se.initial.

alpha	determines confidence level, 1-alpha for constructing/optimizing confidence intervals.
beta	Determines quantile of excess length to optimize, if bandwidth optimizes given quantile of excess length of one-sided confidence intervals; otherwise ignored.
se.method	<p>Vector with methods for estimating standard error of estimate. If NULL, standard errors are not computed. The elements of the vector can consist of the following methods:</p> <p>"nn" Nearest neighbor method</p> <p>"EHW" Eicker-Huber-White, with residuals from local regression (local polynomial estimators only).</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope). Local polynomial estimators only.</p> <p>"plugin" Plug-in estimate based on asymptotic variance. Local polynomial estimators in sharp RD only.</p> <p>"supplied.var" Use conditional variance supplied by sigma2 or d instead of computing residuals</p>
J	Number of nearest neighbors, if "nn" is specified in se.method.
se.initial	<p>Method for estimating initial variance for computing optimal bandwidth. Except for "nn", all methods assume homoskedasticity on either side of cutoff (for RD), or for all data (for inference at a point).</p> <p>"EHW" Based on residuals from a local linear regression using a triangular kernel, and and bandwidth given by a rule-of-thumb bandwidth (for inference at a point, see ROTBW.fit), or IK bandwidth (for fuzzy and sharp RD, see IKBW.fit). For fuzzy RD, the IK bandwidth is based on the reduced-form regression.</p> <p>"demeaned" Like EHW, but instead of using the regression residuals, estimate σ_i^2 by subtracting the estimated intercept from the outcome (and not subtracting the estimated slope).</p> <p>"Silverman" Use residuals from local constant regression with uniform kernel and bandwidth selected using Silverman's rule of thumb, as in Equation (14) in Imbens and Kalyanaraman (2012)</p> <p>"SilvermanNN" Use Silverman's rule of thumb to pick the bandwidth, but use nearest neighbor estimates, rather than the residuals.</p> <p>"nn" Use nearest neighbor estimates, without assuming homoscedasticity</p>

Value

Returns an object of class "RDResults", see description in [RDHonest](#)

rebp	<i>Austrian unemployment duration data from Lalive (2008)</i>
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Description

Subset of Lalive data for individuals in the regions affected by the REBP program

Usage

rebp

Format

A data frame with 29,371 rows and 4 variables:

age Age in years, at monthly accuracy

period Indicator for whether REBP is in place

female Indicator for female

duration unemployment duration in weeks

Source

Rafael Lalive's website, <https://sites.google.com/site/rafaellalive/>

References

Lalive, R. (2008): "How Do Extended Benefits Affect Unemployment Duration? A Regression Discontinuity Approach." *Journal of Econometrics*, 142 (2): 785-806.

ROTBW.fit	<i>Rule of thumb bandwidth for inference at a point</i>
-----------	---------------------------------------------------------

Description

Calculate bandwidth for inference at a point on local linear regression using method in Fan and Gijbels (1996, Chapter 4.2).

Usage

```
ROTBW.fit(d, kern = "triangular", order = 1, boundary = NULL)
```

Arguments

d	object of class "LPPData"
kern	specifies kernel function used in the local regression. It can either be a string equal to "triangular" ($k(u) = (1 - u)_+$), "epanechnikov" ($k(u) = (3/4)(1 - u^2)_+$), or "uniform" ($k(u) = (u < 1)/2$), or else a kernel function.
order	Order of local regression 1 for linear, 2 for quadratic.
boundary	Is point at a boundary?

Value

ROT bandwidth

References

Fan, J., and I. Gijbels (1996): Local Polynomial Modelling and Its Applications, Monographs on Statistics and Applied Probability. Chapman & Hall/CRC, New York, NY.

Examples

```
dp <- LPPData(lee08[lee08$margin>0, ], point=0)
bp1 <- ROTBW.fit(dp, kern="uniform", order=1)
```

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