

# A Self-Adapting Genetic Algorithm for Project Scheduling under Resource Constraints

Sönke Hartmann

*Institut für Betriebswirtschaftslehre, Lehrstuhl für Production und Logistik,  
Christian-Albrechts-Universität zu Kiel, Olshausenstr. 40,  
D-24118 Kiel, Germany*

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**Abstract:** This paper deals with the classical resource-constrained project scheduling problem (RCPSP). There, the activities of a project have to be scheduled subject to precedence and resource constraints. The objective is to minimize the makespan of the project. We propose a new heuristic called self-adapting genetic algorithm to solve the RCPSP. The heuristic employs the well-known activity list representation and considers two different decoding procedures. An additional gene in the representation determines which of the two decoding procedures is actually used to compute a schedule for an individual. This allows the genetic algorithm to adapt itself to the problem instance actually solved. That is, the genetic algorithm learns which of the alternative decoding procedures is the more successful one for this instance. In other words, not only the solution for the problem, but also the algorithm itself is subject to genetic optimization. Computational experiments show that the mechanism of self-adaptation is capable to exploit the benefits of both decoding procedures. Moreover, the tests show that the proposed heuristic is among the best ones currently available for the RCPSP. © 2002 Wiley Periodicals, Inc. *Naval Research Logistics* 49: 433–448, 2002; Published online in Wiley InterScience (www.interscience.wiley.com). DOI 10.1002/nav.10029

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## 1. INTRODUCTION

In this paper, we consider the resource-constrained project scheduling problem (RCPSP). In the RCPSP, the activities of a project have to be scheduled such that the makespan of the project is minimized. Thereby, technological precedence constraints have to be observed as well as limited capacities of the renewable resources that are required to accomplish the activities. The RCPSP is a classical and challenging optimization problem that has attracted many researchers; for overviews see Brucker et al. [6], Kolisch and Hartmann [20], and Özdamar and Ulusoy [26]. Moreover, it is important for practitioners as well with various applications ranging from project management software to control systems for flexible manufacturing systems. An important task in project management is to schedule the project, i.e., to assign start times to the activities. The objective and constraints make this an NP-hard optimization problem (see Blazewicz, Lenstra,

and Rinnooy Kan [3]). Hence, for large projects, it is advisable to make use of heuristic scheduling algorithms.

In a recent paper, we proposed a genetic algorithm (GA) for the RCPSP (see Hartmann [11]). That GA makes use of the so-called activity list representation. In several computational experiments, it was shown that this GA outperformed GAs based on other representations. Thus, it was pointed out that the choice of the problem representation is crucial for the success of a GA. According a more recent study (cf. Hartmann and Kolisch [13]), the activity list based GA ranges among best heuristics currently available for the RCPSP. In fact, for medium and large sized project instances, it is the most promising one. This paper is a follow-up study that proposes a new RCPSP heuristic which builds upon the activity list based GA of [11]. We now examine the impact of the so-called decoding procedure which transforms the problem representation into a solution (in our case, schedule). As we will see, there are two algorithms that can be employed as decoding procedures. The idea is to leave the choice between them to the GA. Generally speaking, we obtain a GA in which an algorithmic component (the decoding procedure) is selected by means of evolution. The result is an extended GA paradigm which allows the GA to adapt itself. Hence, we call it *self-adapting* GA.

The basic framework for the self-adapting GA was developed in Hartmann [12]. Another general approach called *adaptive* GA was introduced by Derigs, Kabath, and Zils [9] (but not yet applied to the RCPSP). The latter considers different crossover, mutation, and selection operators. A mechanism based on a so-called scoreboard evaluates the success of the alternative operators dynamically. The main differences between this adaptive GA and our self-adapting GA are as follows: First, our self-adapting GA applies the same genetic operators and survival-of-the-fittest strategy to both the problem solution and the information related to self-adaptation (i.e., we do not have to employ a separate mechanism like the scoreboard). Second, in our application to the RCPSP, we use self-adaptation for selecting the decoding procedure rather than for the genetic operators (although, as we will point out later on, our approach can deal with different genetic operators as well).

The remainder is organized as follows: We begin with a description of the RCPSP in Section 2. Subsequently, the self-adapting GA approach is presented in Section 3. Section 4 then summarizes the results of our computational investigation. We analyze the behavior of the self-adapting GA and compare it to the plain activity list based GA without self-adaptation. Moreover, we compare it to several project scheduling heuristics from the literature. The paper closes with a general discussion of the proposed approach as well as a few remarks on research perspectives in Section 5.

## 2. THE RESOURCE-CONSTRAINED PROJECT SCHEDULING PROBLEM

The classical resource-constrained project scheduling problem (RCPSP) can be summarized as follows. We consider a project which consists of  $J$  activities (jobs) labeled  $j = 1, \dots, J$ . The set of activities is referred to as  $\mathcal{J} = \{1, \dots, J\}$ . Due to technological requirements, there are precedence relations between some of the jobs. These precedence relations are given by sets of immediate predecessors  $\mathcal{P}_j$  indicating that an activity  $j$  may not be started before all of its predecessors are completed. Analogously,  $\mathcal{S}_j$  is the set of the immediate successors of activity  $j$ . The precedence relations can be represented by an activity-on-node network which is assumed to be acyclic. We consider additional activities  $j = 0$  representing the single source and  $j = J + 1$  representing the single sink activity of the network.

With the exception of the (dummy) source and (dummy) sink activity, each activity requires certain amounts of (renewable) resources to be performed. The set of resources is referred to as  $K$ . For each resource  $k \in K$  the per-period-availability is constant and given by  $R_k$ . The processing time (duration) of an activity  $j$  is denoted as  $p_j$ , its request for resource  $k$  is given by  $r_{jk}$ . Once started, an activity may not be interrupted. Without loss of generality, we assume that the dummy source and the dummy sink activity have a duration of zero periods and no request for any resource.

The parameters are assumed to be nonnegative and integer valued. The objective is to determine a schedule with minimal makespan such that both the precedence and resource constraints are fulfilled. A mathematical programming formulation for the RCPSp was given by Pritsker, Watters, and Wolfe [30].

### 3. SELF-ADAPTING GENETIC ALGORITHM

#### 3.1. Basic Scheme

Genetic algorithms (cf. Holland [15] and Goldberg [10]) apply the principles of biological evolution to solve optimization problems. They combine existing solutions in order to form new ones. Together with a survival-of-the-fittest strategy, this leads to successively better solutions for the problem to be solved.

Our GA framework starts with the computation of an initial population, i.e., the first generation, which is described in subsection 3.3. The number of individuals in the population is referred to as  $POP$  which is assumed to be an even integer. The GA then determines the fitness values of the individuals of the initial population. After that, the population is randomly partitioned into pairs of individuals. To each resulting pair of (parent) individuals, we apply the crossover operator (see subsection 3.4) to produce two new (child) individuals. Subsequently, we apply the mutation operator (see subsection 3.5) to the genotypes of the newly produced children. After computing the fitness of each child individual, we add the children to the current population, leading to a population size of  $2 \cdot POP$ . Then we apply the selection operator (see subsection 3.6) to reduce the population to its former size  $POP$ . Doing so, we obtain the next generation to which we again apply the crossover operator and so on. This process is repeated for a prespecified number of generations which is denoted as  $GEN$  or, alternatively, until a given CPU time limit is reached.

More formally, the GA scheme can be summarized as follows.  $\mathcal{POP}$  denotes the current population (i.e., a set of individuals), and  $\mathcal{CHI}$  is the set of children.  $G$  is the current generation number. Note that exactly  $POP \cdot GEN$  individuals (and thus schedules) are computed if a time limit is not given.

```

 $G := 1$ ;
generate initial population  $\mathcal{POP}$ ;
compute fitness for individuals  $I \in \mathcal{POP}$ ;
WHILE  $G < GEN$  AND time limit is not reached DO
BEGIN
   $G := G + 1$ ;
  produce children  $\mathcal{CHI}$  from  $\mathcal{POP}$  by crossover;
  apply mutation to children  $I \in \mathcal{CHI}$ ;
  compute fitness for children  $I \in \mathcal{CHI}$ ;
   $\mathcal{POP} := \mathcal{POP} \cup \mathcal{CHI}$ ;

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reduce population  $\mathcal{POP}$  by means of selection;

**END.**

### 3.2. Representation and Self-Adaptation

For many optimization problems, GAs do not operate directly on the solutions for the problems. Instead, they make use of problem-specific representations of the solutions. The genetic operators modify the representation which is then transformed into a solution by means of a so-called decoding procedure.

For the RCPSP, a solution is given by a schedule  $S = (s_1, \dots, s_J)$  which assigns a start time  $s_j$  to every activity  $j$ . As outlined in Hartmann [11], such a solution can be represented within a GA by an activity list  $\lambda = (j_1, \dots, j_J)$ . An activity list must be precedence feasible, that is, any activity must occur in the list after all its predecessors. Formally, that is  $\mathcal{P}_{j_i} \subseteq \{0, j_1, \dots, j_{i-1}\}$  for  $i = 1, \dots, J$ . The activity list is transformed into a schedule by a decoding procedure which is called serial schedule generation scheme (SGS). The serial SGS constructs schedules from activity lists as follows: First, the dummy source activity is started at time 0. Then the activities are scheduled in the order that is prescribed by the list  $(j_1, \dots, j_J)$ . Thereby, each activity is assigned the earliest precedence and resource feasible start time. In fact, in Hartmann [11] it is shown that the activity list representation (together with the serial SGS as decoding procedure) leads to better results than other representations for the RCPSP.

In the context of priority rule based heuristics, another scheduling algorithm for the RCPSP, the so-called parallel SGS, has been employed (cf. Kolisch [18]). It works as follows: Having scheduled the dummy sink activity at time 0, the parallel SGS computes a so-called decision point which is the time at which an activity to be scheduled is started. This decision point is determined by earliest finish time of the activities currently in process. For each decision point, the set of eligible activities is computed as the set of those activities that can be feasibly started at the decision point. The eligible activities are selected successively and started until none are left. Then the next decision point and a related set of eligible activities are computed. This is repeated until all activities are feasibly scheduled.

To the best of our knowledge, all metaheuristics in the RCPSP literature that employ the activity list representation also make use of the serial SGS as decoding procedure (see Baar, Brucker, and Knust [1], Boctor [4], Bouleimen and Lecocq [5], Hartmann [11], and Pinson, Prins, and Rullier [29]). Usually, no reason for the selection of the serial SGS is given—the serial SGS appears to be the “natural choice.”

We propose to use not only the serial but also the parallel SGS as decoding procedure for the activity list representation. In fact, the parallel SGS can easily be applied to activity lists: In each step, we simply choose that activity from the eligible set that has the lowest index in the activity list.

Now we have two possible decoding procedures for the activity list representation of the RCPSP. This leads us to the question which of them should be used. In fact, there is no general answer to this question. This is due to the differences between the serial and the parallel SGS: Whereas the serial SGS constructs so-called active schedules, the parallel one constructs so-called non-delay schedules (cf. Sprecher, Kolisch, and Drexel [34]). The set of the nondelay schedules is a (in most cases proper) subset of the set of the active schedules. While the set of the active schedules always contains an optimal schedule, this does not hold for the set of the nondelay schedules. Consequently, the parallel SGS may miss an optimal schedule. On the other

hand, it produces schedules of good average quality because it tends to utilize the resources as early as possible, leading to compact schedules.

This results in different behaviors of the SGS in computational experiments (cf., e.g., Kolisch [18] and Hartmann and Kolisch [13]): On instances with many activities and/or scarce resource capacities, the parallel SGS performs better than the serial one. Moreover, if long computation times are allowed (i.e., if many schedules can be computed), the serial SGS leads to better results than the parallel one. These observations can be explained as follows: Many activities and scarce resources imply larger search spaces, where the focus on compact, but often only suboptimal nondelay schedules is a promising heuristic strategy. Longer computation times may allow to find an optimal or a near optimal solution, which is typically only possible if the serial SGS is used.

However, it is usually impossible to predict which of the SGS will perform better for an arbitrary instance of the RCPSP. The idea is now to allow both SGS to be employed as decoding procedures within our GA. To do so, we define the genotype as follows: An individual  $I = (\lambda, SGS)$  consists of an activity list  $\lambda$  and an indicator

$$SGS = \begin{cases} 1, & \text{if activity list } \lambda \text{ is to be decoded by the serial SGS,} \\ 0, & \text{if activity list } \lambda \text{ is to be decoded by the parallel SGS.} \end{cases}$$

For a given individual, we compute a schedule using the SGS specified in the genotype. The fitness of the individual is defined as the makespan of the schedule. That is, a lower fitness implies a better individual (and thus a higher chance to survive).

The extended representation proposed here includes an additional gene that determines the SGS type to be used as decoding procedure for the related activity list. As with all genes in GAs, also this one is subject to the genetic operators crossover, mutation, and selection. Therefore, the SGS type leading to better results will survive while the other one will probably die over the generations. Thus the mechanism of evolution decides for the specific instance currently to be solved which decoding procedure is the more promising one. This enables the GA to adapt itself dynamically to each instance, leading to what we call a self-adapting GA.

### 3.3. Initial Population

Next, we have to define how to determine an initial population containing *POP* individuals of the genotype introduced above. We will proceed in two steps. First, we will consider the construction of an activity list. Second, we will describe the selection of the decoding procedure to be used, i.e., one of the two SGS.

An activity list is constructed by a modified priority rule based sampling heuristic (cf. Kolisch [18]). The next activity for the list is successively chosen from those unscheduled activities the predecessors of which have already been selected for the list. This way, we obtain a precedence feasible activity list. The decision which activity is chosen next is made on the basis of one of two well-known priority rules. We first select the priority rule; either the LFT (latest finish time) or the LST (latest start time) rule is chosen with a probability of 0.5 each. From the resulting priority values of the activities, we derive regret based biased selection probabilities that are used to select the next activity (for details on the priority rules and the regret based biased sampling approach, we refer to Kolisch [18]). Using two good priority rules and a randomized activity selection method leads to a diversified initial population of good activity lists.

Next, we have to choose an SGS in order to make the current activity list a complete genotype. Of course, both SGS must appear in the population because we want the genetic algorithm to decide which of them is more promising. We examined the following three alternative approaches:

- (a) The most straightforward method is to select each of the SGS types with a probability of  $p = 0.5$ .
- (b) The following idea was designed to lead to a good initial distribution of the SGS types with respect to the project actually to be scheduled. We have discussed above that, roughly speaking, the serial SGS is more favorable for smaller projects. This motivated the following approach where the probability to select the serial SGS is defined as  $p^{\text{serial}} = \frac{\alpha}{j}$ , where  $\alpha$  is a constant. Clearly, we set  $p^{\text{parallel}} = 1 - p^{\text{serial}}$ . This way, the more activities we have in a project, the higher the probability to select the parallel SGS in the initial population.
- (c) Similarly, we know that the parallel SGS is superior in case of scarce resource capacities. A formal measure for the scarceness is the resource strength  $RS$  (see Kolisch, Sprecher, and Drexel [22]). A low resource strength implies scarce capacities. Thus, we simply set  $p^{\text{serial}} = RS$ . Again, we set  $p^{\text{parallel}} = 1 - p^{\text{serial}}$ . Obviously, a low resource strength leads to a low probability for selecting the serial SGS (note that  $RS$  is between 0 and 1 by definition).

In computational experiments with a large number of test instances, these three approaches gave similar results on the average. This indicates that the initial distribution is not crucial for the evolution as long as both SGS obtain a sufficient fraction in the initial population. As none of the methods was clearly superior, we selected the simplest approach (a).

### 3.4. Crossover

Let us assume that two individuals of the current population have been selected for crossover. We have a mother individual  $M = (\lambda^M, SGS^M)$  and a father individual  $F = (\lambda^F, SGS^F)$ . Now two child individuals have to be constructed, a daughter  $D = (\lambda^D, SGS^D)$  and a son  $S = (\lambda^S, SGS^S)$ .

We start with a definition of the daughter  $D$ . In a first step, we determine the daughter's activity list  $\lambda^D$ . Combining the parent's activity lists, we have to make sure that each activity appears exactly once in the daughter's activity list. Therefore, we adapt a general crossover technique presented by Reeves [31] for permutation based genotypes. Our approach also secures that precedence feasibility is maintained. We perform a two-point crossover for which we draw two random integers  $q_1$  and  $q_2$  with  $1 \leq q_1 < q_2 \leq J$ . Now the daughter's activity list  $\lambda^D$  is determined by taking the activity list of the positions  $i = 1, \dots, q_1$  from the mother, that is,

$$j_i^D := j_i^M.$$

The positions  $i = q_1 + 1, \dots, q_2$  are derived from the father. However, the activities already selected may not be considered again. We obtain:

$$j_i^D := j_k^F, \quad \text{where } k \text{ is the lowest index such that } j_k^F \notin \{j_1^D, \dots, j_{i-1}^D\}.$$

The remaining positions  $i = q_2 + 1, \dots, J$  are again taken from the mother, that is,

$$j_i^D := j_k^M, \quad \text{where } k \text{ is the lowest index such that } j_k^M \notin \{j_1^D, \dots, j_{i-1}^D\}.$$

As proven by Hartmann [11], this crossover strategy constructs precedence feasible offspring, given that the parents' activity lists were precedence feasible as well.

The second step determines the daughter's decoding procedure. The daughter inherits the information which SGS should be used from the mother, that is, we set

$$SGS^D := SGS^M.$$

The son individual is computed analogously. For the son's activity list, the first and the third part are taken from the father and the second one is taken from the mother. He inherits the gene that determines his decoding procedure from the father.

### 3.5. Mutation

The following mutation operator is applied to each newly produced child individual. The mutation operator modifies the genes of the genotype with a probability of  $p_{\text{mutation}}$ .

First, we show how the mutation operator modifies the individual's activity list. We move through the activity list from left to right. Thereby, we apply a right shift to each activity with a probability of  $p_{\text{mutation}}$ . Consider a current position  $i \in \{1, \dots, J-1\}$  in the activity list

$$\lambda = (j_1, \dots, j_i, \dots, j_h, \dots, j_J).$$

Now activity  $j_i$  can be shifted after some position  $h \in \{i+1, \dots, J\}$ , which leads to activity list

$$\lambda' = (j_1, \dots, j_{i-1}, j_{i+1}, \dots, j_h, j_i, j_{h+1}, \dots, j_J).$$

That is, activity  $j_i$  is right shifted within the activity list and inserted immediately after some activity  $j_h$ . Clearly, such a shift is executed only if the resulting activity list is still precedence feasible.

Second, we consider the gene indicating the decoding procedure. Interpreting the gene as a boolean indicator for the SGS to be used, we set  $SGS := \neg SGS$  with a probability of  $p_{\text{mutation}}$ . That is, by applying mutation, the serial SGS is replaced by the parallel one in the current individual and vice versa.

On the basis of preliminary computational experiments, we selected a mutation probability of  $p_{\text{mutation}} = 0.05$ .

### 3.6. Construction of the Next Generation

As described in Section 3.1, we employ a generational management in the self-adapting GA. After the application of crossover and mutation, we add the newly produced children to the current population. The next step now is to select the individuals that survive and make up the next generation.



We have tested several variants of the selection operator which follow a survival-of-the-fittest strategy. We considered the ranking method, the proportional selection as well as the tournament selection (cf., e.g., Michalewicz [25]). In preliminary computational studies, we observed that the ranking method gave better results than the other alternatives. This is in line with the findings of our previous study (Hartmann [11]). Therefore, we fixed the selection component to the ranking approach. The ranking method sorts the individuals with respect to their fitness values and selects the *POP* best ones while the remaining ones are deleted from the population (ties are broken arbitrarily).

### 3.7. Dealing with Clones

Crossover (together with mutation) may produce children that are copies of individuals that already exist in the population. These identical individuals are called clones. Often, clones are considered to be worth avoiding because computational effort is wasted by computing solutions (in our case, schedules) that had been computed before. Moreover, clones reduce the genetic variety in the population. On the other hand, one might argue that the occurrence of clones means that more copies of fit information are available for reproduction.

In the self-adapting GA, we analyzed the number of clones occurring during the evolution. In case of small search spaces (i.e., test sets with small projects), we had at most 6% clones during the evolution. The average fraction of clones was less than 2%. For large search spaces, we hardly observed any clone. Hence, we decided not to include a specific mechanism to avoid clones. It should be noted, however, that for very long computation times, which allow to explore a huge number of individuals, avoiding clones can be promising.

### 3.8. Acceleration

We have implemented two methods to speed up the self-adapting GA. They are both based on the relaxation of the resource constraints.

The first approach has similarly been used by Kolisch [17]. It can be summarized as follows: We compute a lower bound on the makespan which is given by the earliest possible project end that would be obtained from relaxing the resource constraints. If we have found a schedule with a makespan equal to the lower bound, we have found an optimal solution and stop the GA.

The second method makes use of the worst upper bound  $Z$  on the makespan that occurs in the current population. Proceeding from this upper bound  $Z$ , we determine the so-called latest start time  $LS_j$  for each activity  $j \in \mathcal{J}$ .  $LS_j$  reflects the latest time at which activity  $j$  must start to allow the project to be completed in period  $Z$  when the resource constraints are relaxed. If, while computing the schedule for a new child individual, an activity  $j$  is assigned a start time  $s_j \geq LS_j$ , we can stop the scheduling process for this individual and remove it from the population immediately. Clearly, the latter situation would lead to a schedule with a makespan  $Z' \geq Z$ . That is, it would be removed from the population by means of the ranking selection anyway. By not completely computing a schedule for some individual, we save computation time.

## 4. COMPUTATIONAL RESULTS

### 4.1. Test Design

In this section we present the results of the computational studies. The experiments have been performed on a Pentium-based IBM-compatible personal computer with 133 MHz clock-pulse



**Table 1.** Average deviations (%) from optimal makespan—ProGen set  $J = 30$ .

Algorithm	Reference	Iterations	
		1000	5000
Self-adapting GA	(New)	0.38	0.22
Simulated annealing	Bouleimen and Lecocq [5]	0.38	0.23
Activity list GA	Hartmann [11]	0.54	0.25
Adaptive sampling	Schirmer [33]	0.65	0.44
Tabu search	Baar, Brucker, and Knust [1]	0.86	0.44
Adaptive sampling	Kolisch and Drex1 [19]	0.74	0.52
Serial sampling (LFT)	Kolisch [18]	0.83	0.53
Random key GA	Hartmann [11]	1.03	0.56
Priority rule GA	Hartmann [11]	1.38	1.12
Parallel sampling (LFT)	Kolisch [18]	1.40	1.29
Problem space GA	Leon and Ramamoorthy [24]	2.08	1.59

and 32 MB RAM. The self-adapting GA for the RCPSP has been coded in ANSI C, compiled with the GNU C compiler, and tested under Linux.

We have performed experiments with two different designs. First, we have taken three standard sets of RCPSP instances from the literature which were constructed by the project generator ProGen of Kolisch, Sprecher, and Drex1 [22]. These instance sets are available from the web-based project scheduling problem library PSPLIB (cf. Kolisch and Sprecher [21]). The first two sets contain 480 instances with 30 and 60 activities per project, respectively. The third one consists of 600 instances with 120 activities. The self-adapting GA computed 1000 schedules for each project (with parameter settings  $POP = 40$ ,  $GEN = 25$ ) and, in an additional run, not more than 5000 schedules (with  $POP = 90$ ,  $GEN = 55$ ). This test design allowed us to compare our results with those obtained for several RCPSP heuristics from the literature which were tested for the evaluation study of Hartmann and Kolisch [13]. In that study, also 1000 and 5000 schedules were computed by each heuristic for each instance. This allows to evaluate the heuristics both in a short-term and in a medium-term optimization. The authors of the heuristics tested their approaches themselves such that they were able to adjust the parameters in order to obtain the best possible results. As the computational effort for constructing one schedule can be assumed to be similar in all of the tested heuristics, this test design should allow for a fair comparison.

The second experimental design uses the well-known instance set assembled by Patterson [28]. It contains 110 RCPSP instances with up to 51 activities. This instance set enabled us to compare the self-adapting GA with some heuristics for which no results for the ProGen set were available. We report the results of the respective heuristics given in the literature by the authors of the approaches. Here, however, the number of schedules computed for each instance was not equal (and the results were obtained on different computers and with different computation times). As a basis for the comparison, we therefore selected a time limit of 5 s per instance for the self-adapting GA.

#### 4.2. Comparison with Other Heuristics for the RCPSP

The results of our experimental study on the ProGen instance sets are summarized in Tables 1–3. They compare the self-adapting GA with several RCPSP heuristics from the literature. The

**Table 2.** Average deviations (%) from critical path lower bound—ProGen set  $J = 60$ .

Algorithm	Reference	Iterations	
		1000	5000
Self-adapting GA	(New)	12.21	11.70
Activity list GA	Hartmann [11]	12.68	11.89
Simulated annealing	Bouleimen and Lecocq [5]	12.75	11.90
Adaptive sampling	Schirmer [33]	12.94	12.59
Priority rule GA	Hartmann [11]	13.30	12.74
Adaptive sampling	Kolisch and Drexler [19]	13.51	13.06
Parallel sampling (LFT)	Kolisch [18]	13.59	13.23
Random key GA	Hartmann [11]	14.68	13.32
Tabu search	Baar, Brucker, and Knust [1]	13.80	13.48
Problem space GA	Leon and Ramamoorthy [24]	14.33	13.49
Serial sampling (LFT)	Kolisch [18]	13.96	13.53

metaheuristics considered here are the schedule scheme based tabu search method of Baar, Brucker, and Knust [1], the activity list based simulated annealing approach of Bouleimen and Lecocq [5], the three GAs of Hartmann [11] based on different representations, and the problem space based GA of Leon and Ramamoorthy [24]. The tested priority rule based sampling methods include the adaptive procedure of Kolisch and Drexler [19], the latest finish time (LFT) rule based method of Kolisch [18], and the adaptive approach of Schirmer [33]. The LFT based sampling method was tested separately with the serial and the parallel SGS.

Table 1 gives the average percentage deviations from the optimal makespan for the ProGen instance set with 30 activities in a project obtained from the evaluation of 1000 and 5000 schedules, respectively. As for the ProGen instance sets with 60 and 120 activities per project some of the optimal solutions are not known, we measured for these sets the average percentage deviation from a lower bound. As lower bound, we chose the critical path based lower bound (cf. Stinson, Davis, and Khumawala [35]). As this bound can be easily computed, this allows other researchers to compare their results with those reported here. The lower bound based results for the instances with 60 and 120 activities can be found in Tables 2 and 3, respectively. In each table, the heuristics are sorted according to descending performance with respect to 5000 iterations.

**Table 3.** Average deviations (%) from critical path lower bound—ProGen set  $J = 120$ .

Algorithm	Reference	Iterations	
		1000	5000
Self-adapting GA	(New)	37.19	35.39
Activity list GA	Hartmann [11]	39.37	36.74
Simulated annealing	Bouleimen and Lecocq [5]	42.81	37.68
Priority rule GA	Hartmann [11]	39.93	38.49
Adaptive sampling	Schirmer [33]	39.85	38.70
Parallel sampling (LFT)	Kolisch [18]	39.60	38.75
Adaptive sampling	Kolisch and Drexler [19]	41.37	40.45
Problem space GA	Leon and Ramamoorthy [24]	42.91	40.69
Serial sampling (LFT)	Kolisch [18]	42.84	41.84
Random key GA	Hartmann [11]	45.82	42.25

**Table 4.** Average deviations (%) from best lower bound currently known.

Algorithm	ProGen Set	Iterations	
		1000	5000
Self-adapting GA	$J = 60$	3.26	2.88
	$J = 120$	9.69	8.33

For the self-adapting GA, Table 4 additionally displays the average percentage deviation from the best lower bounds currently known. The results show that the solution gap is rather small. The underlying lower bounds have been computed by Brucker and Knust [7] and Heilmann and Schwindt [14] as well as Klein and Scholl [16]. The bounds are frequently updated in the library PSPLIB of Kolisch and Sprecher [21] (the results of Table 4 are based on the bounds reported there in October 2000).

Finally, the results for the classical Patterson instances are provided in Table 5. In addition to the self-adapting GA, it includes the two-phase heuristic of Bell and Han [2], the extended random key based simulating annealing method of Cho and Kim [8], the activity list based GA of Hartmann [11], the random key based simulating annealing method of Lee and Kim [23], the problem space based GA of Leon and Ramamoorthy [24], the local constraint based analysis (LCBA) approach of Özdamar and Ulusoy [27], the local search procedure of Sampson and Weiss [32], and the tabu search method of Thomas and Salhi [36]. We give the average percentage deviation from the optimal makespan, the percentage of instances for which an optimal schedule was found, and information about the computation time and the computer that was used for testing. The procedures are sorted according to increasing deviation from the optimum.

The results show that the new self-adapting algorithm leads to the best results on all instance sets, outperforming several heuristics from the literature. This makes it the most promising heuristic to solve the RCPSP. For all instances of the Patterson instance set, an optimal solution is found within at most 5 s of CPU time (this also holds for the activity list based GA of Hartmann [11]).

**Table 5.** Comparison of heuristics—Patterson instance set.

Algorithm	Reference	Av. Dev.	Optimal	CPU-s
Self-adapting GA	(New)	0.00%	100.0%	5.0 <sup>a</sup>
GA	Hartmann [11]	0.00%	100.0%	5.0 <sup>a</sup>
Simulated annealing	Cho and Kim [8]	0.14%	93.6%	18.4 <sup>b</sup>
Simulated annealing	Lee and Kim [23]	0.57%	82.7%	17.0 <sup>b</sup>
Problem space GA	Leon and Ramamoorthy [24]	0.74%	75.5%	7.5 <sup>c</sup>
LCBA	Özdamar and Ulusoy [27]	1.14%	63.6%	0–25 <sup>d</sup>
Local search	Sampson and Weiss [32]	1.98%	55.5%	10.2 <sup>b</sup>
Tabu search	Thomas and Salhi [36]	2.30%	46.4%	218.7 <sup>e</sup>
Two-phase method	Bell and Han [2]	2.60%	44.5%	28.4 <sup>f</sup>

<sup>a</sup> Maximal CPU-time on a Pentium 133 MHz.

<sup>b</sup> Average CPU-time on a Pentium 60 MHz.

<sup>c</sup> Average CPU-time on an IBM RS 6000.

<sup>d</sup> CPU-time range on an IBM PC 486.

<sup>e</sup> Average CPU-time on a Sun Sparc Station 10.

<sup>f</sup> Average CPU-time on a Macintosh plus.

**Table 6.** Average computation times of the self-adapting GA (s).

Test Set	Iterations	
	1000	5000
$J = 30$	0.30	1.40
$J = 60$	0.57	2.52
$J = 120$	3.13	14.05

Observe that metaheuristics typically give better results than priority rule based methods. This is due to the fact that metaheuristics usually exploit knowledge from one or more previously examined solutions whereas priority rule based procedures generate each solution independently. It should be emphasized, however, that using a metaheuristic strategy alone does not guarantee a good performance. This can be seen from the different results of the tested GA approaches.

Let us now return to the difference in the behavior of the two SGS that motivated the definition of the genotype of the self-adapting GA. Consider the sampling method based on the LFT priority rule. It was tested in two variants, that is, separately with the serial and the parallel SGS. As the only difference lies in the SGS, the computational results show the impact of the choice of the SGS. On the average, the serial SGS performs better on the ProGen set with 30 activities while the parallel SGS becomes superior on the set with 120 activities. This demonstrates that instance characteristics influence the performance. These results indicate that it is a promising approach to include both SGS into a GA and let the genetic operators select the more successful one—as done in our self-adapting GA.

#### 4.3. Computation Times

Let us now take a brief look at the computation times. Table 6 lists the average computation times for the three ProGen sets of test instances, both for constructing 1000 and 5000 schedules. Recall that the times were obtained on a Pentium-based computer with 133 MHz. (Note that the design of the set with  $J = 120$  is different from the set with  $J = 60$ . Therefore, the average computation times for the set with  $J = 120$  are not approximately twice as long as those for the set with  $J = 60$ .)

#### 4.4. Behavior of the Self-Adapting Genetic Algorithm

We will now examine the mechanism of self-adaptation in more detail. Our goal is to study what factors have an impact on the selection of the SGS in the artificial evolution.

We begin with a closer look at the distribution of the SGS in the population. Considering the ProGen test set with  $J = 60$ , Table 7 displays the average percentage of the serial SGS in the

**Table 7.** Average fraction (%) of the serial SGS over the generations ( $J = 60$ ).

Generation	1	2	5	10	15	20	25	30	35	40	45	50
$RS = 0.2$	50	30	18	18	19	20	20	20	21	21	21	21
$RS = 0.5$	50	39	35	36	36	34	34	35	36	37	38	39
$RS = 0.7$	50	44	56	64	67	67	67	67	67	67	67	67

**Table 8.** SGS in the best solution found w.r.t. resource strength ( $J = 60$ ).

SGS	$RS = 0.2$	$RS = 0.5$	$RS = 0.7$	Overall
Serial	24%	58%	67%	49%
Parallel	76%	42%	33%	51%

first two and then in every fifth generation. Thereby, we distinguish three different levels of the resource strength  $RS$ . This parameter measures the availability of the resources. A low resource strength (i.e., a value close to 0) implies that the resource capacities in those project instances are scarce.

According to Table 7, scarce resources lead to a higher fraction of the parallel SGS in the population. As already pointed out above, scarce resources make the problem harder to solve. In such a situation, the parallel SGS which constructs nondelay schedules yields better results. Hence, the resource strength is a problem parameter that influences the performance of the two SGS. As the GA lets the best individuals survive, we can state that the mechanism of self-adaptation is capable of detecting the more promising decoding procedure for some project instance dynamically.

Moreover, Table 7 indicates that the distribution of the SGS in the population changes over the generations. For all considered levels of the resource strength  $RS$ , the percentage of the serial SGS in the initial generation is approximately 50% by construction. Afterwards, the fraction of the serial SGS decreases over the first generations and then increases again. Clearly, the GA always selects the more successful SGS. This shows that the parallel SGS is useful at an early stage of the search because it is well suited for quickly finding schedules of good average quality. In contrast, the serial SGS is the better choice for getting closer to the optimum. Thus, the advantage of the parallel SGS is exploited in the beginning of the evolution while using the serial SGS pays in a later phase.

So far, we have examined how often the two SGS types occur in the population. Next, we study how often the SGS types are contained in the best solution found for each project instance. Considering again the instance set with  $J = 60$ , Table 8 shows the distribution of the SGS among the best solutions found. On the average, approximately half of the best solutions contain the serial SGS while the other half contain the parallel SGS. Again, however, the resource strength  $RS$  of a project instance has an impact on the SGS selection. Table 8 shows that in case of scarce resources (i.e., a low resource strength), the parallel SGS leads to more best solutions than the serial one. In case of more resource capacities, the best solutions contain the serial SGS more often than the parallel one.

Summing up, the mechanism of self-adaptation is capable of exploiting the benefits of both SGS during the genetic search. In particular, it is able to adapt the selection of the decoding procedure to the resource scarceness of a project.

## 5. CONCLUSIONS

In this paper, we have presented a new genetic algorithm based heuristic for the classical resource-constrained project scheduling problem. The computational experiments on a large set of standard test instances have shown that the proposed heuristic leads to better results than several heuristics from the literature.

But we have not only obtained a promising heuristic for the RCPSP. The proposed self-adapting GA can be viewed as a powerful and general framework to tackle difficult optimization

problems. When designing a classical GA for some optimization problem, one would do a lot of experiments using test instances in order to find the best configuration of the GA. However, this might lead to a heuristic that is only suboptimal:

- The instances of an optimization problem are often heterogenous in the sense that for some problem characteristics one GA component performs best but for other problem characteristics another variant is better. This would make the choice of a fixed GA variant as the overall best questionable.
- It is not *a priori* clear which set of test problems can be viewed as representative for the real-world application of the GA after its design is completed. Clearly, different test sets may favor different GA variants. In particular, if one has optimized a GA for some test set, this GA is not necessarily a good heuristic for other (e.g., real-world) instances.
- Often, one has many degrees of freedom when designing a GA. There may be too many combinations of components and parameter settings to allow for a systematic test to determine the best GA variant.
- Some component might be better suited for longer computation times whereas an alternative one is superior for short-term optimization.
- Some component may perform well in the first generations of the GA (which is usually characterized by a rough search not yet close to the optimum) while an alternative one is favorable for the later generations.

These disadvantages associated with the design process of a classical GA are avoided in our self-adapting GA. We suggest to let the GA decide which component or parameter setting is promising. In this paper, we have demonstrated the benefit of self-adaptation for the choice among alternative decoding procedures. But it should be emphasized that self-adaptation can also deal with, e.g., alternative crossover strategies. One simply has to integrate all promising components that can be used within the GA. The evolution can make use of additional genes in order to decide which of them are the best. That is, the evolution leads to a good solution for the problem and to a good algorithm to solve the problem at the same time. In other words, the best algorithmic variant is determined dynamically for the problem instance actually solved. Future research in this direction appears to be promising, and it seems to be worthwhile to develop self-adapting GAs for other combinatorial optimization problems as well.

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