Hazel Phi: 9-type-aliases

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SYNTAX

DECLARATIVES

 Δ ; $\Phi \vdash \kappa_1 \lesssim \kappa_2 \mid \kappa_1$ is a consistent subkind of κ_2

$$\begin{split} \overline{\Delta}; \Phi \vdash \mathsf{KHole} \lesssim \kappa & \overline{\Delta}; \Phi \vdash \kappa \lesssim \mathsf{KHole} \\ \\ \underline{\Delta}; \Phi \vdash \kappa_1 \equiv \kappa_2 \\ \overline{\Delta}; \Phi \vdash \kappa_1 \lesssim \kappa_2 & \underline{\Delta}; \Phi \vdash \mathsf{S}_\kappa(\tau) \lesssim \kappa & \underline{\Delta}; \Phi \vdash \Pi_{t::\kappa_1} \cdot \kappa_2 \lesssim \Pi_{t::\kappa_3} \cdot \kappa_4 \end{split}$$

 $\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2$ κ_1 is equivalent to κ_2

$$\frac{\Delta; \Phi \vdash \kappa_{2} \equiv \kappa_{1}}{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}} \qquad \frac{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{3}}{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}} \qquad \Delta; \Phi \vdash \kappa_{3} \equiv \kappa_{2}}{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}}$$

$$\frac{\Delta; \Phi \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{2}}{\Delta; \Phi \vdash S_{\kappa}(\tau_{1})} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} \cdot \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash T_{1}} \cdot \pi_{2}}{\Delta; \Phi \vdash T_{1}} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash T_{1}} \quad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi \vdash T_{1}} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} \cdot \kappa_{2}}{\Delta; \Phi$$

 $\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2$ τ_1 is equivalent to τ_2 at kind κ

$$\frac{\Delta; \Phi \vdash \tau :: \kappa}{\Delta; \Phi \vdash \tau \stackrel{\kappa}{=} \tau} \qquad \frac{\Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{=} \tau_1}{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_3 \qquad \Delta; \Phi \vdash \tau_3 \stackrel{\kappa}{=} \tau_1}{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2}$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\text{Type}}{=} \tau_3 \qquad \Delta; \Phi \vdash \tau_2 \stackrel{\text{Type}}{=} \tau_4}{\Delta; \Phi \vdash \tau_1 \oplus \tau_2 \stackrel{\text{Type}}{=} \tau_3 \oplus \tau_4} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2 \qquad \Delta; \Phi, t :: \kappa_1 \vdash \tau_1 \stackrel{\kappa}{=} \tau_2}{\Delta; \Phi \vdash \lambda t :: \kappa_1 \cdot \tau_1} \stackrel{\Pi_{t :: \kappa_1 \cdot \kappa_2}}{\equiv} \chi_2$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\Pi_{t :: \kappa_1 \cdot \kappa_2}}{\equiv} \tau_3 \qquad \Delta; \Phi \vdash \tau_2 \stackrel{\kappa_1}{\equiv} \tau_4}{\Delta; \Phi \vdash \tau_1 \stackrel{\pi_2}{\equiv} \tau_3} \chi_4$$

$$\frac{\Delta; \Phi \vdash \tau_1 :: \Pi_{t :: \kappa_1} \cdot \kappa_3 \qquad \Delta; \Phi \vdash \tau_2 :: \Pi_{t :: \kappa_1} \cdot \kappa_4 \qquad \Delta; \Phi, t :: \kappa_1 \vdash \tau_1 \quad t \stackrel{\kappa_2}{\equiv} \tau_2 \quad t}{\Delta; \Phi \vdash \tau_1 :: \Xi_{\kappa_1} \cdot \kappa_2} \chi_2$$

$$\frac{\Delta; \Phi \vdash \tau_1 :: \Pi_{t :: \kappa_1} \cdot \kappa_3 \qquad \Delta; \Phi \vdash \tau_2 :: \Pi_{t :: \kappa_1} \cdot \kappa_4}{\Delta; \Phi \vdash \tau_1 :: \Xi_{\kappa_2} \cdot \tau_2} \chi_3 \qquad \Delta; \Phi \vdash \tau_2 :: \kappa}{\Delta; \Phi \vdash \tau_1 :: \Xi_{\kappa_2} \cdot \tau_2}$$

$$\frac{\Delta; \Phi \vdash \tau_1 :: \Xi_{\kappa_2} \cdot \tau_2}{\Xi} \chi_2 \qquad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

$$\Delta; \Phi \vdash \tau_1 :: \Xi_{\tau_2} \qquad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

$$\Delta; \Phi \vdash \tau_1 :: \Xi_{\tau_2} \qquad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

$$\Delta; \Phi \vdash \tau_1 :: \Xi_{\tau_2} \qquad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

 $\Delta; \Phi \vdash \tau_1 \equiv \tau_2$ | τ_1 is equivalent to τ_2 at "top" kind

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_2}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_{::\kappa}}{\Delta; \Phi \vdash \tau \equiv \tau} \qquad \frac{\Delta; \Phi \vdash \tau_2 \equiv \tau_1}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_1 \equiv \tau_3}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_1 \equiv \tau_2}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2}$$

 $\Delta; \Phi \vdash \tau ::> \kappa$ τ has principal kind κ

$$\frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash \mathtt{bse} ::> \mathtt{S}_{\mathtt{Type}}(\mathtt{bse})} \qquad \frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash t ::> \mathtt{S}_{\kappa}(t)}$$

 $\Delta; \Phi \vdash \kappa \prod_{\Pi} \Pi_{t::\kappa_1}.\kappa_2$ κ has matched Π -kind $\Pi_{t::\kappa_1}.\kappa_2$

$$\frac{\Delta; \Phi \vdash \kappa \equiv \Pi_{t::\kappa_{1}}.\kappa_{2}}{\Delta; \Phi \vdash \text{KHole} \prod_{\Pi} \Pi_{t::\text{KHole}}.\text{KHole}}$$

 $\Delta; \Phi \vdash \tau :: \kappa$ τ is well formed at kind κ