Hazel Phi: 9-type-aliases

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SYNTAX

DECLARATIVES

 Δ ; $\Phi \vdash \kappa_1 \lesssim \kappa_2 \mid \kappa_1$ is a consistent subkind of κ_2

$$\begin{split} \overline{\Delta}; \Phi \vdash \mathsf{KHole} \lesssim \kappa & \overline{\Delta}; \Phi \vdash \kappa \lesssim \mathsf{KHole} \\ \underline{\Delta}; \Phi \vdash \kappa_1 \equiv \kappa_2 \\ \overline{\Delta}; \Phi \vdash \kappa_1 \lesssim \kappa_2 & \underline{\Delta}; \Phi \vdash \mathsf{S}_\kappa(\tau) \lesssim \kappa & \underline{\Delta}; \Phi \vdash \Pi_{t::\kappa_1}.\kappa_2 \lesssim \Pi_{t::\kappa_3}.\kappa_4 \end{split}$$

 $\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2$ κ_1 is equivalent to κ_2

$$\frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \kappa \equiv \kappa} \qquad \frac{\Delta; \Phi \vdash \kappa_2 \equiv \kappa_1}{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_3 \qquad \Delta; \Phi \vdash \kappa_3 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_2}{\Delta; \Phi \vdash S_{\kappa}(\tau_1)} \qquad \frac{\Delta; \Phi \vdash \tau_1 : S_{\kappa}(\tau_1)}{\Delta; \Phi \vdash S_{\kappa}(\tau_1)} \qquad \frac{\Delta; \Phi \vdash \tau_1 : \Pi_{t::\kappa_1} . \kappa_2}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_1} . \kappa_2}(\tau) \equiv \Pi_{t::\kappa_1} . S_{\kappa_2}(\tau t)}$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2 \qquad \Delta; \Phi, t::\kappa_1 \vdash \kappa_3 \equiv \kappa_4}{\Delta; \Phi \vdash \Pi_{t::\kappa_1} . \kappa_2} \qquad \frac{\Delta; \Phi \vdash \Pi_{t::\kappa_1} . \kappa_2 \equiv \Pi_{t::\kappa_3} . \kappa_4}{\Delta; \Phi \vdash \Pi_{t::\kappa_3} . \kappa_4}$$

 $\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2 \mid \tau_1 \text{ is equivalent to } \tau_2 \text{ at kind } \kappa$

$$\frac{\Delta; \Phi \vdash \tau_{1} :: S_{\kappa}(\tau_{2}) \qquad \Delta; \Phi \vdash \tau_{2} :: \kappa}{\Delta; \Phi \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{2}}$$

$$\frac{\Delta; \Phi \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{2}}{\Delta; \Phi \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{3}} \qquad \Delta; \Phi \vdash \tau_{3} \stackrel{\kappa}{\equiv} \tau_{1}}{\Delta; \Phi \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{3}} \qquad \Delta; \Phi \vdash \tau_{3} \stackrel{\kappa}{\equiv} \tau_{1}}$$

$$\Delta; \Phi \vdash \tau_{1} \stackrel{\text{Type}}{\equiv} \tau_{3} \qquad \Delta; \Phi \vdash \tau_{2} \stackrel{\text{Type}}{\equiv} \tau_{4}} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2} \qquad \Delta; \Phi, t :: \kappa_{1} \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{2}}$$

$$\Delta; \Phi \vdash \tau_{1} \oplus \tau_{2} \stackrel{\text{Type}}{\equiv} \tau_{3} \oplus \tau_{4} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2} \qquad \Delta; \Phi, t :: \kappa_{1} \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{2}}$$

$$\Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{3} \qquad \Delta; \Phi \vdash \tau_{2} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{3} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{3} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{3} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \kappa_{1} \equiv \kappa \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv} \tau_{2} \qquad \Delta; \Phi \vdash \tau_{1} \stackrel{\text{Tures}_{1} \cdot \kappa_{2}}{\equiv$$

 $\Delta; \Phi \vdash \tau ::> \kappa \mid \tau \text{ has principal kind } \kappa$

$$\frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash \mathsf{bse} ::> \mathsf{S}_{\mathsf{Type}}(\mathsf{bse})} \qquad \frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash t ::> \mathsf{S}_{\kappa}(t)} \qquad \frac{\Delta; \Phi \vdash \tau_1 :: \mathsf{Type} \qquad \Delta; \Phi \vdash \tau_2 :: \mathsf{Type}}{\Delta; \Phi \vdash \tau_1 \oplus \tau_2 ::> \mathsf{S}_{\mathsf{Type}}(\tau_1 \oplus \tau_2)}$$

$$\frac{\mathsf{u} :: \kappa \in \Delta}{\Delta; \Phi \vdash (||\tau||^{\mathsf{u}} ::> \kappa} \qquad \frac{\mathsf{u} :: \kappa \in \Delta \qquad \Delta; \Phi \vdash \tau :: \kappa_1}{\Delta; \Phi \vdash (|\tau||^{\mathsf{u}} ::> \kappa} \qquad \frac{\mathsf{u} :: \kappa \in \Delta \qquad t \notin \mathsf{dom}(\Phi)}{\Delta; \Phi \vdash (|t|)^{\mathsf{u}} ::> \kappa}$$

$$\frac{\Delta; \Phi \vdash \tau_1 ::> \kappa}{\Delta; \Phi \vdash \lambda t :: \kappa_1 \cdot \tau} ::> \frac{\mathsf{S}_{\mathsf{II}_{t :: \kappa_1} \cdot \kappa_2}(\lambda t :: \kappa_1 \cdot \tau)}{\Delta; \Phi \vdash \tau_2 ::: \kappa_1}$$

$$\frac{\Delta; \Phi \vdash \tau_1 ::> \kappa \qquad \Delta; \Phi \vdash \kappa \prod_{\mathsf{II}} \mathsf{II}_{t :: \kappa_1} \cdot \kappa_2}{\Delta; \Phi \vdash \tau_2 ::: \kappa_1} \qquad \Delta; \Phi \vdash \tau_2 :: \kappa_1}$$

$$\frac{\Delta; \Phi \vdash \tau_1 ::> \kappa \qquad \Delta; \Phi \vdash \kappa \prod_{\mathsf{II}} \mathsf{II}_{t :: \kappa_1} \cdot \kappa_2}{\Delta; \Phi \vdash \tau_2 ::: \kappa_1} \qquad \Delta; \Phi \vdash \tau_2 :: \kappa_1}$$

 $\Delta; \Phi \vdash \kappa \prod_{\Pi} \Pi_{t::\kappa_1}.\kappa_2$ κ has matched Π -kind $\Pi_{t::\kappa_1}.\kappa_2$

$$\frac{\Delta;\Phi \vdash \kappa \equiv \Pi_{t::\kappa_1}.\kappa_2}{\Delta;\Phi \vdash \mathsf{KHole} \overset{\blacktriangleright}{\Pi} \Pi_{t::\mathsf{KHole}}.\mathsf{KHole}}$$

 $\Delta; \Phi \vdash \tau :: \kappa \mid \tau \text{ is well formed at kind } \kappa$

$$\frac{\Delta; \Phi \vdash \tau ::> \mathtt{S}_{\kappa}(\tau)}{\Delta; \Phi \vdash \tau ::\kappa} \qquad \frac{\Delta; \Phi \vdash \tau :: \mathtt{S}_{\kappa}(\tau_{1}) \qquad \Delta; \Phi \vdash \tau_{1} ::\kappa}{\Delta; \Phi \vdash \tau ::\kappa} \qquad \frac{\Delta; \Phi \vdash \tau ::> \kappa_{1} \qquad \Delta; \Phi \vdash \kappa_{1} \lesssim \kappa}{\Delta; \Phi \vdash \tau ::\kappa}$$