Hazel PHI: 10-modules

July 1, 2021

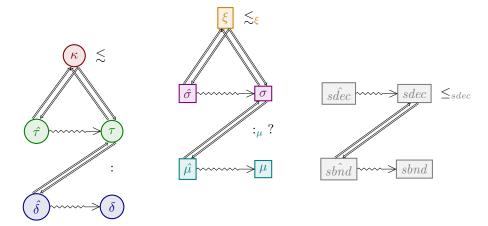
prerequisites

- Hazel PHI: 9-type-aliases-redux
 - github
 - $\ current \ commit: \ 4410cd565ce717707e580e44f64868d3175fe2a6$
- (optional) Hazel PHI: 1-labeled-tuples
 - github
 - $\ current \ commit: \ 0a7d0b53ee7286d03ea3be13a7ac91a86f1c90b1$

how to read

800000	kinds	D08000	signature kind
008000	types (constructors)	800080	signatures
000080	terms	008080	modules

notes



external typ/sig/mod syntax not written out yet (waiting for construction dust to settle); patterns not handled yet—will be left till end.

syntax



```
HTyp
                                                                                                                       type variable
                                              t
                                               bse
                                                                                                                           base type
                                                                                                                          type binop
                                              	au_1 \oplus 	au_2
                                                                                                                             list type
                                              [\tau]
                                                                                                                       type function
                                              \lambda t :: \kappa.\tau
                                                                                                                   type application
                                                                                                  labelled product type (record)
                                              \{lab_1 \hookrightarrow \tau_1, \dots \, lab_n \hookrightarrow \tau_n\}
                                                                                                          module type projection
                                                                                                                   empty type hole
                                              (|\tau|)
                                                                                                               nonempty type hole
               base type
                               bse
                                              Int
                                              Float
                                              Bool
          HTyp BinOp
                                \oplus
   external expression
                                              signature s = \hat{\sigma} in \hat{\delta}
                                              module m = \hat{\mu} in \hat{\delta}
                                              module m:_{\mu}s=\hat{\mu} in \hat{\delta}
                                              functor something = something in \hat{\delta}
                                              \hat{\mu}.lab
                                                                                                          module term projection
   internal expression
                                \delta
                                        ::=
                                              signature s=\sigma in \delta
                                              module m:_{\mu} s = \mu in \delta
                                              functor something = something in \delta
                                              \mu.lab
                                                                                                          module term projection
         signature kind
                                              SSigKind(\sigma)
                                              SigKHole
               signature
                                                                                                                 signature variable
                                              \{sdecs\}
                                                                                                                structure signature
                                              \Pi_{m:_{\mu}\sigma_{1}}.\sigma_{2}
                                                                                                                  functor signature
                                                                                                             empty signature hole
                                                                                                         nonempty signature hole
                                               (s)
                  module
                                                                                                                    module variable
                                              m
                                              \{sbnds\}
                                                                                                                            structure
                                                                                                                               functor
                                              \lambda m:_{\mu} \sigma.\mu
                                                                                                                functor application
                                              \mu_1 \mu_2
                                                                                                            submodule projection
                                              \mu.lab
                                                                                                                empty module hole
                                                                                                           nonempty module hole
                                               (\mu)
signature declarations
                              sdecs
                                              sdec, sdecs
 signature declaration
                               sdec
                                              type lab
                                              type lab::\kappa
                                              {\tt val}\ lab{:}	au
                                              module lab:_{\mu}\sigma
                                              functor lab:_{\mu}\sigma
    structure bindings
                             sbnds ::=
                                              sbnd, sbnds
     structure binding
                              sbnd ::= type t = \tau
                                              \mathtt{let}\ x{:}\tau = \delta
                                              {\tt module}\ m=\mu
                                              module m:_{\mu} s = \mu
```

context definitions

 Δ , ?; Γ , x: τ ; Φ , t:: κ ; Ξ , m: $_{\mu}\sigma$; Ψ , s:: $_{\sigma}\xi$

declarative statics

```
scratch
      \Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2 | \kappa_1 is a consistent subkind of \kappa_2
                                                                                                     KCSubsumption
                                                                                                     test
                                                                                                     test
\Delta; \Phi; \Xi; \Psi \vdash \xi_1 \lesssim_{\xi} \xi_2 \mid \xi_1 \text{ is a consistent sub signature kind of } \xi_2
                               nameMe
                                            \begin{array}{l} \exists sdec_x \in sdecs_1 \ st \ \Delta; \Phi; \Xi; \Psi \vdash \texttt{SSigKind}(\{sdec_x\}) \lesssim_{\pmb{\xi}} \texttt{SSigKind}(\{sdec_2\}) \\ \Delta; \Phi, \mathsf{type}(\Delta; \Phi; \Xi; \Psi, sdec_2); \Xi, \mathsf{submodule}(sdec_2); \Psi \vdash \{sdecs_1\} \lesssim_{\pmb{\xi}} \{sdecs_2\} \end{array} 
                               \Delta; \Phi; \Xi; \Psi \vdash \underline{\mathsf{SSigKind}}(\{sdec_{11}, s\overline{dec_{12}}, sdecs_{13} \text{ as } sdecs_1\}) \lesssim_{\xi} \underline{\mathsf{SSigKind}}(\{sdec_2, sdecs_2\})
          single
          \frac{\Delta; \Phi; \Xi; \Psi \vdash sdec_1 \leq_{sdec} sdec_2}{\Delta; \Phi; \Xi; \Psi \vdash \mathtt{SSigKind}(\{sdec_1\}) \lesssim_{\xi} \mathtt{SSigKind}(\{sdec_2\})} \qquad \frac{\mathtt{nll}}{\Delta; \Phi; \Xi; \Psi \vdash \mathtt{SSigKind}(\{sdec_3\}) \lesssim_{\xi} \mathtt{SSigKind}(\{\cdot\})}
                              varprop
                             nameMe?delete?
                funct
                \frac{\Delta; \Phi; \Xi; \Psi \vdash \mathsf{SSigKind}(\sigma_{21}) \lesssim_{\xi} \mathsf{SSigKind}(\sigma_{11})}{\Delta; \Phi; \Xi; \Psi \vdash \mathsf{SSigKind}(\Pi_{m:_{\mu}\sigma_{11}}, \sigma_{12})} \lesssim_{\xi} \mathsf{SSigKind}(\Pi_{m:_{\mu}\sigma_{21}}, \sigma_{22})}
            holes
             CSubSigKindHoleR
                                                                                    \Delta; \Phi; \Xi; \Psi \vdash \xi \lesssim_{\xi} SigKHole
\Delta; \Phi; \Xi; \Psi \vdash \sigma \Rightarrow \xi \mid \sigma \text{ synthesizes signature kind } \xi
            SynSigKndVar
                                                                                SynSigKndVarFail
            \frac{s ::_{\sigma} \xi \in \Psi}{\Delta; \Phi; \Xi; \Psi \vdash s \Rightarrow \texttt{SSigKind}(s)} \qquad \frac{s \notin \mathsf{dom}(\Psi)}{\Delta; \Phi; \Xi; \Psi \vdash s \Rightarrow \texttt{SigKHole}} \qquad \frac{\{sdecs\}wellformed?}{\vdash \{sdecs\}} \Rightarrow \frac{\mathsf{SSigKind}(\{sdecs\})}{\vdash \{sdecs\}}
     \Delta; \Phi; \Xi; \Psi \vdash \sigma \Leftarrow \xi  \sigma analyzes against signature kind \xi
```

$$\frac{\Delta; \Phi; \Xi; \Psi \vdash \sigma \Rightarrow \xi_1}{\Delta; \Phi; \Xi; \Psi \vdash \delta \Leftarrow \xi} \xrightarrow{\Delta; \Phi; \Xi; \Psi \vdash \delta \Leftarrow \xi}$$

 $\Delta; \Phi; \Xi; \Psi \vdash sdec_1 \leq_{sdec} sdec_2$

 $sdec_1$ is a subsdec of $sdec_2$

singleType

$$\overline{\Delta; \Phi; \Xi; \Psi \vdash \text{type } lab :: \tau \leq_{sdec} \text{type } lab}$$

$$\begin{array}{c} \Delta; \Phi; \Xi; \Psi \vdash \tau_1 \equiv \tau_2 \\ \Delta; \Phi; \Xi; \Psi \vdash \mathsf{type} \; lab :: \tau_1 \leq_{sdec} \; \mathsf{type} \; lab :: \tau_2 \end{array} \qquad \begin{array}{c} \mathsf{singleType3} \\ \Delta; \Phi; \Xi; \Psi \vdash \mathsf{type} \; lab \leq_{sdec} \; \mathsf{type} \; lab \\ \end{array}$$

$$\Delta; \Phi; \Xi; \Psi \vdash \mathsf{type} \ lab :: \tau \leq_{sdec} \mathsf{type} \ lab$$

$$\Delta; \Phi; \Xi; \Psi \vdash \mathsf{type} \ lab:: \tau_1 \leq_{sdec} \mathsf{type} \ lab:: \tau_2$$

$$\Delta; \Phi; \Xi; \Psi \vdash \mathsf{type} \ lab \leq_{sdec} \mathsf{type} \ lab$$

singleVa

$$\Delta; \Phi; \Xi; \Psi \vdash \tau_1 \equiv \tau_2$$

$$\frac{\Delta; \Phi; \Xi; \Psi \vdash \tau_1 \equiv \tau_2}{\Delta; \Phi; \Xi; \Psi \vdash \mathsf{val} \; lab{:}\tau_1 \leq_{sdec} \mathsf{val} \; lab{:}\tau_2}$$

$$\Delta; \Phi; \Xi; \Psi \vdash \sigma_1 \Leftarrow SSigKind(\sigma_2)$$

$$\Delta; \Phi; \Xi; \Psi \vdash \text{module } lab:_{\mu}\sigma_{1} \leq_{sdec} \text{module } lab:_{\mu}\sigma_{2}$$

elaboration

 $\hat{\delta}$ synthesizes type τ and elaborates to δ with hole context Δ

SynElabLetMod

SynElabLetModAnn

$$\Phi;\Xi\vdash\hat{\sigma} \Rightarrow \xi\leadsto\sigma\dashv\Delta_1$$

$$\Gamma; \Phi; \Xi \vdash \hat{\mu} \Leftarrow \sigma \leadsto \mu \dashv \Delta_2$$

$$\Gamma; \Phi; \Xi, m:_{\mu} \sigma \vdash \hat{\delta} \Rightarrow \tau \leadsto \delta \dashv \Delta_3$$

$$\frac{\Phi;\Xi\vdash\hat{\sigma}\ \Rightarrow\ \xi\leadsto\sigma\dashv\Delta_1\qquad \Gamma;\Phi;\Xi\vdash\hat{\mu}\ \Leftarrow\ \sigma\leadsto\mu\dashv\Delta_2\qquad \Gamma;\Phi;\Xi,m:_{\mu}\sigma\vdash\hat{\delta}\ \Rightarrow\ \tau\leadsto\delta\dashv\Delta_3}{\Gamma;\Phi;\Xi\vdash\operatorname{module}\ m:_{\mu}\hat{\sigma}=\hat{\mu}\ \operatorname{in}\ \hat{\delta}\ \Rightarrow\ \tau\leadsto\operatorname{module}\ m:_{\mu}\sigma=\mu\ \operatorname{in}\ \delta\dashv\Delta_1\cup\Delta_2\cup\Delta_3}$$

SynElabModTermPrj

$$\frac{\Gamma; \Phi; \Xi \vdash \hat{\mu} \Rightarrow \sigma \leadsto \mu \dashv \Delta \qquad \Phi; \Xi \vdash \sigma \Rightarrow \xi}{\Gamma; \Phi; \Xi \vdash \hat{\mu}.lab \Rightarrow \tau \leadsto \mu.lab \dashv \Delta}$$

$$\Gamma; \Phi; \Xi \vdash \hat{\mu}.lab \Rightarrow \tau \leadsto \mu.lab \dashv \Delta$$

 $\Phi;\Xi\vdash\hat{\tau}\Rightarrow\kappa\leadsto\tau\dashv\Delta$ | $\hat{\tau}$ synthesizes kind κ and elaborates to τ with hole context Δ

SynElabModTypPrj

$$\Phi;\Xi\vdash m \Rightarrow \sigma\leadsto m\dashv\Delta \qquad something\sigma\kappa$$

$$\Phi;\Xi \vdash m.lab \Rightarrow \kappa \leadsto m.lab \dashv \Delta$$

 $\Phi;\Xi \vdash \hat{\tau} \Leftarrow \kappa \leadsto \tau \dashv \Delta \mid \hat{\tau}$ analyzes against kind κ and elaborates to τ with hole context Δ

 $\hat{\mu}$ synthesizes signature σ and elaborates to μ with hole context Δ $\Gamma; \Phi; \Xi \vdash \hat{\mu} \Rightarrow \sigma \leadsto \mu \dashv \Delta$

SynElabModVar

$$m:_{\mu}\sigma\in\Xi$$

$$\frac{m:_{\mu}\sigma\in\Xi}{\Gamma;\Phi;\Xi\vdash m\ \Rightarrow\ \sigma\leadsto m\dashv\cdot}$$

SynElabModVarFail

$$m \notin \mathsf{dom}(\Xi)$$

$$\frac{m \not\in \mathsf{dom}(\Xi)}{\Gamma; \Phi; \Xi \vdash m \ \Rightarrow \ (\!\!\!\! \| \, \leadsto \, (\!\!\! \| m)\!\!\!\!)^{\mathtt{u}} \dashv u {:}_{\mu} (\!\!\!\! \|)}$$

SynElabConsStruct

$$\Gamma; \Phi; \Xi \vdash \hat{sbnd} \Rightarrow sdec \leadsto sbnd \dashv \Delta_1$$

$$\frac{\Gamma, \mathsf{val}(sdec); \Phi, \mathsf{type}(\Delta_1; \Phi; \Xi; \Psi, sdec); \Xi, \mathsf{submodule}(sdec) \vdash \{sb\hat{n}ds\} \ \Rightarrow \ \{sdecs\} \leadsto \{sbnds\} \dashv \Delta_2}{\Gamma; \Phi; \Xi \vdash \{s\hat{n}d, s\hat{n}ds\} \ \Rightarrow \ \{sdec, sdecs\} \leadsto \{sbnd, sbnds\} \dashv \Delta_1 \cup \Delta_2}$$

SynElabNilStruct

SynElabEmptyModHole

SynElabNonemptyModHole

functor stuff

$$\overline{\Gamma; \Phi; \Xi \vdash \{\cdot\} \Rightarrow \{\cdot\} \leadsto \{\cdot\} \dashv \cdot}$$

$$\overline{\Gamma;\Phi;\Xi\vdash (\!(\!)^{\mathbf{u}} \Rightarrow (\!(\!)\!) \rightsquigarrow (\!(\!)^{\mathbf{u}}\dashv u:_{\mu}(\!(\!)\!)}$$

$$\overline{\Gamma;\Phi;\Xi\vdash\{\cdot\}\ \Rightarrow\ \{\cdot\}\rightsquigarrow\{\cdot\}\dashv\cdot}\qquad \overline{\Gamma;\Phi;\Xi\vdash())^{\mathrm{u}}\ \Rightarrow\ ()\!\!\!/} \ \to\ ()\!\!\!\!/} \ \to\ ()\!\!\!\!/} \ \to\ ()\!\!\!\!/} \ \overline{\Gamma;\Phi;\Xi\vdash(m)^{\mathrm{u}}\ \Rightarrow\ ()\!\!\!\!/} \ \to\ (m)^{\mathrm{u}}\dashv u:_{\mu}()\!\!\!\!/}$$

$$\Gamma; \Phi; \Xi \vdash \hat{\mu} \leftarrow \sigma \leadsto \mu \dashv \Delta$$
 $\hat{\mu}$ analyzes against signature σ and elaborates to μ with hole context Δ

AnaElabModSubsumption

$$\Gamma; \Phi; \Xi \vdash \hat{\mu} \Rightarrow \sigma \leadsto \mu \dashv \Delta$$

$$\Gamma; \Phi; \Xi \vdash \hat{\mu} \Leftarrow \sigma \leadsto \mu \dashv \Delta$$

 $\Gamma; \Phi; \Xi \vdash s\hat{bnd} \Rightarrow sdec \leadsto sbnd \dashv \Delta$ | $s\hat{bnd}$ synthesizes declaration sdec and elaborates to sbnd with hole context Δ

SynElabTypeSbnd

$$\Phi:\Xi\vdash\hat{\tau} \Rightarrow \kappa \leadsto \tau\dashv \Lambda$$

$$\frac{\Phi;\Xi\vdash\hat{\tau}\ \Rightarrow\ \kappa\leadsto\tau\dashv\Delta}{\Gamma;\Phi;\Xi\vdash\mathsf{type}\ t=\hat{\tau}\ \Rightarrow\ \mathsf{type}\ t::\tau\leadsto\mathsf{type}\ t=\tau\dashv\Delta} \qquad \frac{\Phi;\Xi\vdash\hat{\tau}\ \Rightarrow\ \kappa\leadsto\tau\dashv\Delta_1}{\Gamma;\Phi;\Xi\vdash\mathsf{let}\ x:\hat{\tau}=\hat{\delta}\ \Rightarrow\ \mathsf{val}\ x:\tau\leadsto\mathsf{let}\ x:\tau=\delta\dashv\Delta_1\cup\Delta_2}{\Gamma;\Phi;\Xi\vdash\mathsf{let}\ x:\hat{\tau}=\hat{\delta}\ \Rightarrow\ \mathsf{val}\ x:\tau\leadsto\mathsf{let}\ x:\tau=\delta\dashv\Delta_1\cup\Delta_2}$$

SynElabValSbnd

$$\Phi;\Xi \vdash \hat{\tau} \implies \kappa \leadsto \tau \dashv \Delta_1 \qquad \Gamma;\Phi;\Xi \vdash \hat{\delta} \iff \tau \leadsto \delta \dashv \Delta_2$$

$$\Gamma; \Phi; \Xi \vdash \mathsf{let} \ x : \hat{\tau} = \hat{\delta} \ \Rightarrow \ \mathsf{val} \ x : \tau \leadsto \mathsf{let} \ x : \tau = \delta \dashv \Delta_1 \cup \Delta_2$$

$$\Gamma; \Phi; \Xi \vdash \hat{\mu} \Rightarrow \sigma \leadsto \mu \dashv \Delta$$

$$\begin{array}{c} \Gamma;\Phi;\Xi\vdash\hat{\mu}\ \Rightarrow\ \sigma\leadsto\mu\dashv\Delta\\ \hline \Gamma;\Phi;\Xi\vdash \mathrm{module}\ m=\hat{\mu}\ \Rightarrow\ \mathrm{module}\ m{:}_{\mu}\sigma\leadsto\mathrm{module}\ m{:}_{\mu}\sigma=\mu\dashv\Delta \end{array}$$

SynElabModAnnSbnd

$$\Phi; \Xi \vdash \hat{\sigma} \Rightarrow \xi \leadsto \sigma_1 \dashv \Delta_1$$

$$\Gamma; \Phi; \Xi \vdash \hat{\mu} \Rightarrow \sigma_2 \rightsquigarrow \mu \dashv \Delta_2$$

$$\Phi; \Xi; \Psi \vdash \sigma_2 \Leftarrow \xi$$

$$\frac{\dot{\Phi};\Xi\vdash\hat{\sigma}\ \Rightarrow\ \xi\leadsto\sigma_1\dashv\Delta_1\qquad \Gamma;\Phi;\Xi\vdash\hat{\mu}\ \Rightarrow\ \sigma_2\leadsto\mu\dashv\Delta_2\qquad \Phi;\Xi;\Psi\vdash\sigma_2\ \Leftarrow\ \xi}{\Gamma;\Phi;\Xi\vdash\mathrm{module}\ m:_{\mu}\hat{\sigma}=\hat{\mu}\ \Rightarrow\ \mathrm{module}\ m:_{\mu}\sigma_1\leadsto\mathrm{module}\ m:_{\mu}\sigma_1=\mu\dashv\Delta_1\cup\Delta_2}$$

 $\Gamma; \Phi; \Xi \vdash s\hat{bnd} \Leftarrow sdec \leadsto sbnd \dashv \Delta$ sbnd analyzes against declaration sdec and elaborates to sbnd with hole context Δ

$$\frac{\Gamma; \Phi; \Xi; l\Psi \vdash s\hat{bnd} \Rightarrow sdec_1 \leadsto sbnd \dashv \Delta \qquad \Delta; \Phi; \Xi; \Psi \vdash sdec_1 \leq_{sdec} sdec}{\Gamma; \Phi; \Xi; \Psi \vdash s\hat{bnd} \Leftarrow sdec \leadsto sbnd \dashv \Delta}$$

$$\Gamma; \Phi; \Xi; \Psi \vdash s\hat{bnd} \Leftarrow sdec \leadsto sbnd \dashv \Delta$$

 $\Gamma; \Phi; \Xi; \Psi \vdash s \hat{dec} \leadsto s dec \dashv \Delta$ | $s \hat{dec}$ elaborates to s dec with hole context Δ

 $\frac{\mathsf{opq}}{\Gamma;\Phi;\Xi;\Psi\vdash\mathsf{type}\;\mathit{lab}\leadsto\mathsf{type}\;\mathit{lab}\dashv\cdot} \qquad \frac{\mathsf{trn}}{\Gamma;\Phi;\Xi;\Psi\vdash\hat{\tau}\;\Rightarrow\;\kappa\leadsto\tau\dashv\Delta} \qquad \frac{\mathsf{val}}{\Gamma;\Phi;\Xi;\Psi\vdash\hat{\tau}\;\Rightarrow\;\kappa\leadsto\tau\dashv\Delta} \qquad \frac{\Gamma;\Phi;\Xi;\Psi\vdash\hat{\tau}\;\Rightarrow\;\kappa\leadsto\tau\dashv\Delta}{\Gamma;\Phi;\Xi;\Psi\vdash\mathsf{val}\;\mathit{lab}:\hat{\tau}\leadsto\mathsf{val}\;\mathit{lab}:\tau\dashv\Delta}$

$$\Gamma; \Phi; \Xi; \Psi \vdash \hat{\sigma} \Rightarrow \xi \leadsto \sigma \dashv \Delta$$

$$\frac{\Gamma; \Phi; \Xi; \Psi \vdash \hat{\sigma} \implies {\color{red}\xi} \leadsto \sigma \dashv \Delta}{\Gamma; \Phi; \Xi; \Psi \vdash \mathtt{module} \ lab:_{\mu} \hat{\sigma} \leadsto \mathtt{module} \ lab:_{\mu} \sigma \dashv \Delta}$$

we're going to need HOFunctors so we don't need to preclude users from typing a functor into a module and vice versa

 $\Phi; \Xi; \Psi \vdash \hat{\sigma} \Rightarrow \xi \leadsto \sigma \dashv \Delta \mid \hat{\sigma}$ synthesizes signature kind ξ and elaborates to σ with hole context Δ

SynSigEmptyHole

SynSigNonEmptyHole

 $\overline{\Phi;\Xi;\Psi\vdash (\!(\!)^{\mathbf{u}}\ \Rightarrow\ \mathsf{SigKHole}\rightsquigarrow (\!(\!)^{\mathbf{u}}\dashv u::_{\sigma}\mathsf{SigKHole}}$

 $\Phi;\Xi\vdash\hat{\sigma} \leftarrow \xi \leadsto \sigma\dashv\Delta$ $\hat{\sigma}$ analyzes against signature kind ξ and elaborates to σ with hole context Δ

misc functions

$$\label{eq:val} \mathsf{val}(sdec) = \begin{cases} lab{:}\tau & sdec = \mathsf{val}\ lab{:}\tau \\ \cdot & \text{otherwise} \end{cases}$$

$$\mathsf{type}(cntxts,sdec) = \begin{cases} lab{:}:\mathsf{Type} & sdec = \mathsf{type}\ lab \\ lab{:}\kappa & sdec = \mathsf{type}\ lab{:}\kappa \\ \cdot & \text{otherwise} \end{cases}$$

$$\mathsf{submodule}(sdec) = \begin{cases} lab{:}_{\mu}\sigma & sdec = \mathsf{module}\ lab{:}_{\mu}\sigma \\ \cdot & \text{otherwise} \end{cases}$$

$$\mathtt{S}_{\mathtt{Type}}(\tau) := \mathtt{S}(\tau)$$

$$S_{S(\tau_t)}(\tau) := S(\tau)$$

$$S_{\texttt{KHole}}(au) := \texttt{KHole}$$

theorems

Kind Synthesis Precision

If cntxts $\vdash \tau \implies \kappa$ then $\forall \kappa_1.$ cntxts $\vdash \tau :: \kappa_1 \implies \text{cntxts} \vdash \kappa \lesssim \kappa_1$