BinOp ⊕ ::= Product | Sum | Arrow

Kind κ ::= Ty | KHole

ConstantTypes c ::= Int | Float | Bool

UserHTyp $\hat{\tau}$::= $c \mid \hat{\tau}_1 \oplus \hat{\tau}_2 \mid \mathtt{list}(\hat{\tau}) \mid ()^u \mid (\hat{\tau})^u$ $\mathsf{InternalHTyp} \ \ \tau \ \ ::= \ c \mid \tau_1 \oplus \tau_2 \mid \mathsf{list}(\tau) \mid (\!)^u \mid (\!(\tau)^u)^u$

 $\lceil \kappa_1 \sim \kappa_2 \rceil$ κ_1 is consistent with κ_2

KCHole KCSymm KCRef
$$\frac{\kappa_1 \sim \kappa_2}{\kappa_2 \sim \kappa_1}$$
 KCRef $\kappa \sim \kappa$

 $\Phi \vdash \hat{\tau} \Rightarrow \kappa \leadsto \tau \dashv \Delta$ $\hat{\tau}$ synthesizes kind κ and elaborates to τ

TElabSConst

$$\overline{\Phi \vdash c \Rightarrow \mathsf{Ty} \leadsto c \dashv \cdot}$$

TElabSBinOp

$$\frac{\Phi \vdash \hat{\tau}_1 \Leftarrow \mathsf{Ty} \leadsto \tau_1 : \mathsf{Ty} \dashv \Delta_1 \qquad \Phi \vdash \hat{\tau}_2 \Leftarrow \mathsf{Ty} \leadsto \tau_2 : \mathsf{Ty} \dashv \Delta_2}{\Phi \vdash \hat{\tau}_1 \oplus \hat{\tau}_2 \Rightarrow \mathsf{Ty} \leadsto \tau_1 \oplus \tau_2 \dashv \Delta_1 \cup \Delta_2}$$

$$\frac{\Phi \vdash \hat{\tau} \Leftarrow \mathsf{Ty} \leadsto \tau : \mathsf{Ty} \dashv \Delta}{\mathsf{list}(\hat{\tau}) \vdash \mathsf{Ty} \Rightarrow \mathsf{list}(\tau) \leadsto \Delta \dashv} \qquad \frac{t : \kappa \in \Phi}{\Phi \vdash t \Rightarrow \kappa \leadsto t \dashv}$$

$$t:\kappa\in\Phi$$

$$\frac{t \not\in \Phi}{\Phi \vdash t \Rightarrow \mathtt{KHole} \leadsto (\!\!|t|\!\!)^u_{\mathsf{id}(\Phi)} \dashv u :: (\!\!|)[\Phi]}$$

TElabSHole

$$\overline{\Phi \vdash (\![)^u \Rightarrow \mathtt{KHole} \leadsto (\![)^u_{\mathsf{id}(\Phi)} \dashv u :: (\![)[\Phi]$$

TElabSNEHole

$$\frac{\Phi \vdash \hat{\tau} \Rightarrow \kappa \leadsto \tau \dashv \Delta}{\Phi \vdash (|\hat{\tau}|)^u \Rightarrow \mathsf{KHole} \leadsto (|\tau|)^u_{\mathsf{id}(\Phi)} \dashv \Delta, u :: (\![\![b]\!])}$$

 $\Phi \vdash \hat{\tau} \Leftarrow \kappa_1 \leadsto \tau : \kappa_2 \dashv \Delta$ $\hat{\tau}$ analyzes against type κ_1 and elaborates to τ of consistent type κ_2

$$\frac{\text{TElabASubsume}}{\hat{\tau} \neq \|)^u \qquad \hat{\tau} \neq \|\hat{\tau}'\|^u \qquad \Phi \vdash \hat{\tau} \Rightarrow \kappa' \leadsto \tau \dashv \Delta \qquad \kappa \sim \kappa'}{\Phi \vdash \hat{\tau} \Leftarrow \kappa \leadsto \tau : \kappa' \dashv \Delta}$$

TElabAEHole

$$\overline{\Phi \vdash (\!(\!)^u \Leftarrow \kappa \leadsto (\!(\!)^u_{\mathsf{id}(\Phi)} : \kappa \dashv u :: \kappa[\Phi])}$$

$$\begin{split} & \frac{\text{TElabANEHole}}{\Phi \vdash \hat{\tau} \Rightarrow \kappa' \leadsto \tau \dashv \Delta} \\ & \frac{\Phi \vdash (|\hat{\tau}|)^u \Leftarrow \kappa \leadsto (|\tau|)^u_{\text{id}(\Phi)} : \kappa \dashv \Delta, u :: \kappa[\Phi]} \end{split}$$