Hazel Phi: 9-type-aliases

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SYNTAX

DECLARATIVES

 $\Delta; \Phi \vdash \tau ::> \kappa \mid \tau \text{ has principal kind } \kappa$

$$\frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash \mathsf{bse} ::> \mathsf{S}_{\mathsf{Type}}(\mathsf{bse})} \qquad \frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash t ::> \mathsf{S}_{\kappa}(t)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} :: \mathsf{Type} \qquad \Delta; \Phi \vdash \tau_{2} :: \mathsf{Type}}{\Delta; \Phi \vdash \tau_{1} \oplus \tau_{2} ::> \mathsf{S}_{\mathsf{Type}}(\tau_{1} \oplus \tau_{2})} \\ \frac{u :: \kappa \in \Delta}{\Delta; \Phi \vdash (||)^{\mathsf{u}} ::> \kappa} \qquad \frac{u :: \kappa \in \Delta \qquad \Delta; \Phi \vdash \tau :: \kappa_{1}}{\Delta; \Phi \vdash (|\tau|)^{\mathsf{u}} ::> \kappa} \qquad \frac{u :: \kappa \in \Delta \qquad t \not\in \mathsf{dom}(\Phi)}{\Delta; \Phi \vdash (|t|)^{\mathsf{u}} ::> \kappa} \\ \frac{\Delta; \Phi \vdash (|\tau|)^{\mathsf{u}} ::> \kappa}{\Delta; \Phi \vdash \lambda t :: \kappa_{1} . \tau ::> \mathsf{S}_{\Pi_{t :: \kappa_{1}} . \kappa_{2}}(\lambda t :: \kappa_{1} . \tau)} \\ \frac{\Delta; \Phi \vdash \tau_{1} ::> \kappa \qquad \Delta; \Phi \vdash \kappa \prod_{\Pi} \Pi_{t :: \kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash \tau_{1} \tau_{2} ::> [\tau_{2}/t] \kappa_{2}} \qquad \Delta; \Phi \vdash \tau_{2} :: \kappa_{1}}$$

 $\Delta; \Phi \vdash \tau :: \kappa$ τ is well formed at kind κ

$$\frac{\Delta; \Phi \vdash \tau ::> \kappa}{\Delta; \Phi \vdash \tau ::: \kappa} \qquad \frac{\Delta; \Phi \vdash \tau :: S_{\kappa}(\tau_{1})}{\Delta; \Phi \vdash \tau :: \kappa}$$

$$\frac{\Delta; \Phi \vdash \tau ::> \kappa_{1} \qquad \Delta; \Phi \vdash \kappa_{1} \lesssim \kappa}{\Delta; \Phi \vdash \tau :: \kappa}$$

$$\frac{\Delta; \Phi \vdash \tau ::S_{\kappa}(\tau_{1})}{\Delta; \Phi \vdash \tau_{1} ::S_{\kappa}(\tau_{2})} \qquad \frac{\Delta; \Phi \vdash \tau_{1} :: S_{\kappa}(\tau_{3}) \qquad \Delta; \Phi \vdash \tau_{3} :: S_{\kappa}(\tau_{2})}{\Delta; \Phi \vdash \tau_{1} :: S_{\kappa}(\tau_{2})}$$

 $\Delta; \Phi \vdash \kappa \prod_{\Pi} \Pi_{t::\kappa_1}.\kappa_2$ κ has matched Π -kind $\Pi_{t::\kappa_1}.\kappa_2$

$$\frac{\Delta; \Phi \vdash \kappa \equiv \Pi_{t::\kappa_1}.\kappa_2}{\Delta; \Phi \vdash \mathsf{KHole} \overset{\blacktriangleright}{\Pi} \Pi_{t::\mathsf{KHole}}.\mathsf{KHole}}$$

 $\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2$ κ_1 is equivalent to κ_2

$$\frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \kappa \equiv \kappa} \qquad \frac{\Delta; \Phi \vdash \kappa_2 \equiv \kappa_1}{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_3 \qquad \Delta; \Phi \vdash \kappa_3 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_2}{\Delta; \Phi \vdash S_{\kappa}(\tau_1) \equiv S_{\kappa}(\tau_2)} \qquad \frac{\Delta; \Phi \vdash \tau_1 : S_{\kappa}(\tau_1)}{\Delta; \Phi \vdash S_{\kappa}(\tau_1)(\tau) \equiv S_{\kappa}(\tau_1)} \qquad \frac{\Delta; \Phi \vdash \tau_1 : \Pi_{t::\kappa_1}.\kappa_2}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_1}.\kappa_2}(\tau) \equiv \Pi_{t::\kappa_1}.S_{\kappa_2}(\tau t)}$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2 \qquad \Delta; \Phi, t::\kappa_1 \vdash \kappa_3 \equiv \kappa_4}{\Delta; \Phi \vdash \Pi_{t::\kappa_2}.\kappa_4}$$

 $\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2$ κ_1 is a consistent subkind of κ_2

$$\frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \text{ KHole}} \leq \kappa \qquad \qquad \frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \kappa \lesssim \text{ KHole}}$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_3 \qquad \Delta; \Phi \vdash \kappa_3 \lesssim \kappa_4 \qquad \Delta; \Phi \vdash \kappa_4 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2}$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2} \qquad \frac{\Delta; \Phi \vdash \kappa_3 \lesssim \kappa_4 \qquad \Delta; \Phi \vdash \kappa_4 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2}$$

$$\frac{\Delta; \Phi \vdash \kappa_3 \lesssim \kappa_1 \qquad \Delta; \Phi, t :: \kappa_3 \vdash \kappa_2 \lesssim \kappa_4}{\Delta; \Phi \vdash \Pi_{t :: \kappa_1} . \kappa_2 \lesssim \Pi_{t :: \kappa_3} . \kappa_4}$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2 \qquad \Delta; \Phi \vdash \tau_1 \stackrel{\kappa_1}{\equiv} \tau_2}{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa_1}{\equiv} \tau_2}$$

 $\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2 \mid \tau_1 \text{ is equivalent to } \tau_2 \text{ at kind } \kappa$

$$\frac{\Delta; \Phi \vdash \tau_1 :: S_{\kappa}(\tau_2)}{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2}$$

 $\Delta; \Phi \vdash \kappa \text{ OK} \quad \kappa \text{ is well formed}$

$$\frac{\Delta; \Phi \vdash \tau :: \kappa}{\Delta; \Phi \vdash \mathsf{Type} \; \mathsf{OK}} \qquad \frac{\Delta; \Phi \vdash \kappa_{2} \; \mathsf{OK}}{\Delta; \Phi \vdash \mathsf{S}_{\kappa}(\tau) \; \mathsf{OK}} \qquad \frac{\Delta; \Phi \vdash \kappa_{1} \; \mathsf{OK} \quad \Delta; \Phi \vdash \kappa_{2} \; \mathsf{OK}}{\Delta; \Phi \vdash \Pi_{t :: \kappa_{1}}.\kappa_{2} \; \mathsf{OK}}$$