Hazel Phi: 9-type-aliases

July 13, 2021

SYNTAX

DECLARATIVES

 $\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2$ κ_1 is a consistent subkind of κ_2

$$\frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa \text{ KHole}} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2} \qquad \frac{\Delta; \Phi \vdash \tau :: \kappa}{\Delta; \Phi \vdash \mathsf{S}_\kappa(\tau) \lesssim \kappa_2}$$

 $\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2$ κ_1 is equivalent to κ_2

$$\frac{\Delta; \Phi \vdash \kappa_{2} \equiv \kappa_{1}}{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}} \qquad \frac{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{3}}{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}} \qquad \frac{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}}{\Delta; \Phi \vdash \kappa_{1} \equiv \kappa_{2}}$$

$$\frac{\Delta; \Phi \vdash \tau_{1} \stackrel{\kappa}{\equiv} \tau_{2}}{\Delta; \Phi \vdash S_{\kappa}(\tau_{1})} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad \frac{\Delta; \Phi \vdash \tau_{1} : \Pi_{t::\kappa_{1}} . \kappa_{2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_{1}} . \kappa_{2}}(\tau)} \qquad$$

 $\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2$ τ_1 is equivalent to τ_2 at kind κ

 $\Delta; \Phi \vdash \tau_1 \equiv \tau_2$ τ_1 is equivalent to τ_2 at "top" kind

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_2}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_{::\kappa}}{\Delta; \Phi \vdash \tau \equiv \tau} \qquad \frac{\Delta; \Phi \vdash \tau_2 \equiv \tau_1}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_1 \equiv \tau_3}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2} \qquad \frac{\Delta; \Phi \vdash \tau_1 \equiv \tau_3}{\Delta; \Phi \vdash \tau_1 \equiv \tau_2}$$

 $\Delta; \Phi \vdash \tau ::> \kappa$ τ has principal kind κ

$$\frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash \mathtt{bse} ::> \mathtt{S}_{\mathtt{Type}}(\mathtt{bse})} \qquad \qquad \frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash t ::> \mathtt{S}_{\kappa}(t)}$$

 $\Delta; \Phi \vdash \kappa \prod_{\Pi : \Pi_{t::\kappa_{1}}.\kappa_{2}} \mid \kappa \text{ has matched } \Pi\text{-kind } \Pi_{t::\kappa_{1}}.\kappa_{2}$

$$\frac{\Delta; \Phi \vdash \kappa \vdash \Pi_{t::\kappa_{1}}.\kappa_{2}}{\Delta; \Phi \vdash \kappa \vdash \Pi_{t::\kappa_{1}}.\kappa_{2} \vdash \Pi_{t::\kappa_{1}}.\kappa_{2}} \qquad \frac{\Delta; \Phi \vdash \kappa \equiv \Pi_{t::\kappa_{1}}.\kappa_{2}}{\Delta; \Phi \vdash S_{\kappa}(\tau) \prod_{\Pi} \Pi_{t::\kappa_{1}}.S_{\kappa_{2}}(\tau \ t)}$$

 $\Delta; \Phi \vdash \tau :: \kappa$ τ is well formed at kind κ