Hazel Phi: 9-type-aliases

July 16, 2021

SYNTAX

DECLARATIVES

 $\Delta; \Phi \vdash \tau ::> \kappa \mid \tau \text{ has principal (well formed) kind } \kappa$

$$\frac{\Delta; \Phi \vdash \mathsf{bse} ::> \mathsf{S}_{\mathsf{Type}}(\mathsf{bse})}{\Delta; \Phi \vdash \mathsf{bse} ::> \mathsf{S}_{\mathsf{Type}}(\mathsf{bse})} \ 1 \qquad \frac{t :: \kappa \in \Phi}{\Delta; \Phi \vdash t ::> \mathsf{S}_{\kappa}(t)} \ 2 \qquad \frac{\Delta; \Phi \vdash \tau_1 :: \mathsf{Type}}{\Delta; \Phi \vdash \tau_1 \oplus \tau_2 ::> \mathsf{S}_{\mathsf{Type}}(\tau_1 \oplus \tau_2)} \ 3 \\ \frac{u :: \kappa \in \Delta}{\Delta; \Phi \vdash (||)^{\mathsf{u}} ::> \kappa} \ 4 \qquad \frac{u :: \kappa \in \Delta \quad \Delta; \Phi \vdash \tau :: \kappa_1}{\Delta; \Phi \vdash (|\tau|)^{\mathsf{u}} ::> \kappa} \ 5 \qquad \frac{u :: \kappa \in \Delta \quad t \notin \mathsf{dom}(\Phi)}{\Delta; \Phi \vdash (|t|)^{\mathsf{u}} ::> \kappa} \ 6 \\ \frac{\Delta; \Phi \vdash (|\tau|)^{\mathsf{u}} ::> \kappa}{\Delta; \Phi \vdash \lambda t :: \kappa_1 \cdot \tau ::> \mathsf{S}_{\mathsf{\Pi}_{t :: \kappa_1} \cdot \kappa_2}(\lambda t :: \kappa_1 \cdot \tau)} \ 7 \\ \frac{\Delta; \Phi \vdash \tau_1 ::> \kappa \quad \Delta; \Phi \vdash \kappa \prod_{\mathsf{II}} \mathsf{\Pi}_{t :: \kappa_1} \cdot \kappa_2}{\Delta; \Phi \vdash \tau_1 \tau_2 ::> [\tau_2/t] \kappa_2} \ 8 \\ \frac{\Delta; \Phi \vdash \tau_1 ::> \kappa}{\Delta; \Phi \vdash \tau_1 \tau_2 ::> [\tau_2/t] \kappa_2} \ 8$$

 $\Delta; \Phi \vdash \tau :: \kappa$ τ is well formed at kind κ

$$\frac{\Delta; \Phi \vdash \tau ::> \kappa}{\Delta; \Phi \vdash \tau ::\kappa} \quad 9 \qquad \frac{\Delta; \Phi \vdash \tau :: S_{\kappa}(\tau_{1})}{\Delta; \Phi \vdash \tau ::\kappa} \quad 10$$

$$\frac{\Delta; \Phi \vdash \tau ::> \kappa_{1}}{\Delta; \Phi \vdash \tau ::\kappa} \quad \Delta; \Phi \vdash \kappa_{1} \lesssim \kappa$$

$$\frac{\Delta; \Phi \vdash \tau ::> \kappa_{1}}{\Delta; \Phi \vdash \tau ::\kappa} \quad 11$$

$$\frac{\Delta; \Phi \vdash \tau_{2} :: S_{\kappa}(\tau_{1})}{\Delta; \Phi \vdash \tau_{1} :: S_{\kappa}(\tau_{2})} \quad 12$$

$$\frac{\Delta; \Phi \vdash \tau_{1} :: S_{\kappa}(\tau_{3})}{\Delta; \Phi \vdash \tau_{1} :: S_{\kappa}(\tau_{2})} \quad 13$$

 $\Delta; \Phi \vdash \kappa \stackrel{\blacktriangleright}{\Pi} \Pi_{t::\kappa_1}.\kappa_2$ κ has matched Π -kind $\Pi_{t::\kappa_1}.\kappa_2$

$$\frac{\Delta; \Phi \vdash \kappa \equiv \Pi_{t::\kappa_{1}}.\kappa_{2}}{\Delta; \Phi \vdash \kappa \text{ Hole } \prod_{\Pi_{t::KHole}.KHole}} 14 \qquad \qquad \frac{\Delta; \Phi \vdash \kappa \equiv \Pi_{t::\kappa_{1}}.\kappa_{2}}{\Delta; \Phi \vdash \kappa \prod_{\Pi_{t::\kappa_{1}}.\kappa_{2}}} 15$$

 $\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2$ κ_1 is equivalent to κ_2

$$\frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \kappa \equiv \kappa} \text{ 16} \qquad \frac{\Delta; \Phi \vdash \kappa_2 \equiv \kappa_1}{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2} \text{ 17} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_3}{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2} \text{ 18}$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_2}{\Delta; \Phi \vdash S_{\kappa}(\tau_1) \equiv S_{\kappa}(\tau_2)} \text{ 19} \qquad \frac{\Delta; \Phi \vdash \tau_{::S_{\kappa}}(\tau_1)}{\Delta; \Phi \vdash S_{S_{\kappa}(\tau_1)}(\tau) \equiv S_{\kappa}(\tau_1)} \text{ 20}$$

$$\frac{\Delta; \Phi \vdash \tau_{::\Pi_{t::\kappa_1}.\kappa_2}}{\Delta; \Phi \vdash S_{\Pi_{t::\kappa_1}.\kappa_2}(\tau) \equiv \Pi_{t::\kappa_1}.S_{\kappa_2}(\tau t)} \text{ 21} \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}{\Delta; \Phi \vdash \Pi_{t::\kappa_1}.\kappa_2 \equiv \Pi_{t::\kappa_3}.\kappa_4} \text{ 22}$$

 $\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2$ κ_1 is a consistent subkind of κ_2

$$\frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \text{KHole} \lesssim \kappa} 23 \qquad \frac{\Delta; \Phi \vdash \kappa \text{ OK}}{\Delta; \Phi \vdash \kappa \lesssim \text{KHole}} 24$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_2}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2} 25 \qquad \frac{\Delta; \Phi \vdash \kappa_1 \equiv \kappa_3}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2} \qquad \frac{\Delta; \Phi \vdash \kappa_3 \lesssim \kappa_4}{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2} \qquad 26$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2}{\Delta; \Phi \vdash S_\kappa(\tau) \lesssim \kappa} 27 \qquad \frac{\Delta; \Phi \vdash \kappa_3 \lesssim \kappa_1}{\Delta; \Phi \vdash \Pi_{t:::\kappa_1} . \kappa_2 \lesssim \Pi_{t:::\kappa_3} . \kappa_4} \qquad 28$$

$$\frac{\Delta; \Phi \vdash \kappa_1 \lesssim \kappa_2}{\Delta; \Phi \vdash \Pi_{t:::\kappa_1} . \kappa_2 \lesssim \Pi_{t:::\kappa_3} . \kappa_4} \qquad 28$$

 $\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2 \mid \tau_1 \text{ is equivalent to } \tau_2 \text{ at kind } \kappa$

$$\frac{\Delta; \Phi \vdash \tau_1 :: S_{\kappa}(\tau_2)}{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{=} \tau_2} 30$$

$$\frac{\Delta; \Phi \vdash \tau :: \kappa}{\Delta; \Phi \vdash \tau \equiv \tau} \quad 31$$

$$\frac{\Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{\equiv} \tau_1}{\equiv \tau_2} \quad 32$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_3}{\equiv \tau_3} \quad \Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{\equiv} \tau_4$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_3}{\equiv \tau_3} \quad \Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{\equiv} \tau_4$$

$$\frac{\Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_3}{\equiv \tau_3} \quad \Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{\equiv} \tau_4$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3 \oplus \tau_4} \quad 34$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3 \oplus \tau_4} \quad \Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{\equiv} \tau_2$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3} \quad \Delta; \Phi \vdash \tau_2 \stackrel{\kappa}{\equiv} \tau_3$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3 \tau_4} \quad 36$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3 \tau_4} \quad 36$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3 \tau_4} \quad \Delta; \Phi \vdash \tau_2 \oplus \tau_2 t$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_3 \tau_4} \quad \Delta; \Phi \vdash \tau_1 \stackrel{\kappa}{\equiv} \tau_2 t$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_2} \quad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_2} \quad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

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$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_2} \quad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

$$\frac{\Delta; \Phi \vdash \tau_1 \oplus \tau_2}{\equiv \tau_2} \quad \Delta; \Phi \vdash \kappa_1 \equiv \kappa$$

 $\Delta; \Phi \vdash \kappa \text{ OK} \quad \kappa \text{ is well formed}$

$$\frac{\Delta; \Phi \vdash \mathsf{Type}\;\mathsf{OK}}{\Delta; \Phi \vdash \mathsf{KHole}\;\mathsf{OK}} \ \ \frac{\Delta; \Phi \vdash \tau :: \kappa}{\Delta; \Phi \vdash \mathsf{S}_{\kappa}(\tau)\;\mathsf{OK}} \ \ 41}{\frac{\Delta; \Phi \vdash \kappa_1\;\mathsf{OK} \quad \Delta; \Phi \vdash \kappa_2\;\mathsf{OK}}{\Delta; \Phi \vdash \Pi_{t :: \kappa_1} \cdot \kappa_2\;\mathsf{OK}}} \ \ 42}$$