(a) (3 marks) Let \mathcal{F} be a collection of subsets of a set Ω . Provide the three necessary conditions for \mathcal{F} to be an algebra.

- $A \in \mathcal{F} \Rightarrow A^c \in \mathcal{F}$;
- $A, B \in \mathcal{F} \Rightarrow A \cup B \in \mathcal{F}$; and
- $\bullet \ \Omega \in \mathcal{F}$.