

TEST 2 – COMPUTATIONAL MATHEMATICS (SECI1113)

30 MAY 2021 (40 minutes) – session 1

Question 1

(15 marks)

Let

$$V = \left\{ \begin{pmatrix} 1 & b \\ c & 1 \end{pmatrix} \mid b, c \in R \right\}$$

Define addition and scalar multiplication as follows.

$$\begin{pmatrix} 1 & b \\ c & 1 \end{pmatrix} + \begin{pmatrix} 1 & e \\ f & 1 \end{pmatrix} = \begin{pmatrix} 1 & b+e \\ c+f & 1 \end{pmatrix}$$

$$k \begin{pmatrix} 1 & b \\ c & 1 \end{pmatrix} = \begin{pmatrix} 1 & kb \\ kc & 1 \end{pmatrix}$$

verify the following axioms:

a) $(u + v) + w = u + (v + w)$

(5 marks)

b) $u + (-u) = -u + u = 0$

(5 marks)

c) $c \cdot (u + v) = (c \cdot u) + (c \cdot v)$

(5 marks)

Note: u, v, w , are vectors and c and d are scalars