

Recreating Market Conditions for Vote-Selling and Vote-Buying in the Lab: The Chilean Case

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Abstract

The literature asserts that Chilean parties no longer buy votes. While those are good news, the bad news are that we are rather ignorants about a number of other interesting, and yet, unanswered questions. First and foremost, the approach used by most scholars focuses exclusively on vote-buying. That is, parties offering to buy votes, completely ignoring the ones who sell their votes (i.e. voters). This is a rather important distinction. What would voters do if offered the chance to sell their votes? Would they sell them? And if so, at what price? Would voters still sell their votes to their own party of preference, or would they sell it to the opposing party? Do voters set a higher selling price if selling to the opposing party, while lowering the price if selling to the party they would have supported anyways? Another important question is who political parties target: party supporters, opposers, or swing voters? By recreating market conditions that exist between vote-buyers and vote-sellers implemented in the lab, the paper sheds light on these issues.

Please consider downloading the last version of the paper [here](#).

Keywords— clientelism; vote-buying; vote-selling; experimental economics; formal modeling.

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Thank you paragraph.

I. INTRODUCTION

Nice introduction here.

II. THE MODEL

We consider an electorate of n citizens which have to elect a leader to implement a common policy γ from the set $\Gamma = \{1, 2, \dots, 100\}$. Each citizen i has an ideal point x_i that is an iid draw from an uniform distribution over Γ . The payoff of citizen i when the policy γ is implemented is given by $u(D, x_i, \gamma) = D - |x_i - \gamma|$, where D represents **completar ac** \tilde{A} **j**. This payoff can be incremented by transferences from parties to the voter.

In this election there are two candidates, one from the left party and other from to the right party. The left (right) candidate represent a policy γ_L (γ_R) which is an iid draw from an uniform distribution over $\{1, \dots, 50\}$ ($\{51, \dots, 100\}$). The location of this policy give us the number of citizens n_L that eventually prefer the left party candidate, and n_R citizens that prefer right party candidate ($n_L + n_R = n$).

In this setting, both party can negotiate with one of this n citizens. This citizen is randomly selected from the total population n . Observe that, the higher the n , the lower the representation in the election of this voter, while if n is smaller, negotiating with this voter may be more attractive to political parties. We assume that each candidate has a budget (B) that they can use to buy votes. If a party decides not to negotiate with the voter or the voter does no accept the payment, this budget remains on the payoff of the party. The profits of party i is given by,

$$\pi_i(W, e_i, s_i) = W \cdot e_i + (1 - s_i \cdot a_j) \cdot B$$

where W ($W \geq B$) is a constant that represents how much each party values to win the election, $e_i = 1$ if party i wins the election and 0 otherwise, s_i is the fraction of B that the party offers to the citizen j who can accept the offer ($a_j = 1$) or not ($a_j = 0$). We study two versions of this party-citizen interaction: one where both parties can make simultaneous offers to the voter and he decides which offer accept (vote buying case), and other in which the voter can make private offers to each party, and the party decides if to pay or not the offer (vote selling case).

The timing of the game is as follows: at the beginning of the game n citizens and two candidates

are randomly located on their ideal point: citizens along Γ , the left candidate along $\{1, \dots, 50\}$ and the right on $\{51, \dots, 100\}$. This location is public information as well the budget B , the number of citizens (n), and supporters of each party (n_L and n_R). Then the timing depends on the case. On the vote-buying case, each party simultaneously decides if make an offer to the voter. If a party decides to negotiate with the voter, privately sends him the offer. Then the voter decides if take or not the offer, or which one accept if he receives two offers. If he takes up an offer, he should vote for this candidate. On the vote-selling case, the voter may privately proposes a certain amount to each party in exchange for his vote, the parties decide if to pay or not the offer, and then the voter decides which one to accept. In this case, the voter can ask to one or both parties, and each proposal might be different.

I. Equilibrium in Vote-Buying Case

On this case, both parties can offer certain amount on exchange for political support. Note that the parties only have incentives to negotiate with the voter if he has the pivotal vote, it means $|n_L - n_R| \leq 1$ and the voter (i) supports to ex-ante winner of the election ($i \in \max\{n_L, n_R\}$). The voter prefers the party which is closer to his ideal point, if both parties are located at the same distance, the voter is indifferent. Denote by $i^* \in \{L, R\}$ the preferred party of the voter, and $-i^*$ the other party.

Note that, naturally, both parties want to make different bids. If the voter is the pivotal, the less prefer party has incentives to offer a certain amount m_{-i^*} such that the voter has more utility voting by him than to the opposite party, that is:

$$\begin{aligned} m_{-i^*} &\geq (D - |x_{i^*} - \gamma_{i^*}|) - (D - |x_{i^*} - \gamma_{-i^*}|) \\ &= |x_{i^*} - \gamma_{-i^*}| - |x_{i^*} - \gamma_{i^*}|. \end{aligned}$$

The parties expect to win the election but have a limited budget, more precisely they want to win the election at minimum cost. If the party $-i^*$ offers the voter $m_{-i^*} = |x_{i^*} - \gamma_{-i^*}| - |x_{i^*} - \gamma_{i^*}|$, he is indifferent between vote for the party i^* or $-i^*$. The offers $m_{i^*} = 0$ and $m_{-i^*} = |x_{i^*} - \gamma_{-i^*}| - |x_{i^*} - \gamma_{i^*}|$ are the minimum bid that may give led to each party the winning of the election, letting indifferent to the pivotal voter between the two political options. This voter indifference gives rise to two possible Nash equilibria. In one equilibrium, the voter reject the offer and vote for i^* . On the

other equilibrium, the voter accepts the offer and the elected party is $-i^*$. If individuals are utility maximizers, they would effectively be indifferent between these two equilibria. However, if we frequently observe that voters reject offers, this would give us light that the players have other motivations. For example, more politicized players may be more likely to reject offers from the less preferred party.

II. Equilibrium in Vote-Selling Case

On the case that the voter can set the price of his vote, he may negotiate with one or both parties setting the price that he is willing to embrace in order to support a political option. In the instance that the voter has to set the offer, he has incentives to set the maximum offer that each party can pay, in our model this is B . When the voter is pivotal, he may change his vote to the party $-i^*$ only if the budget is enough big to compensate that he loose voting for his less prefer policy, that is, $B > |x_{i^*} - \gamma_{-i^*}| - |x_{i^*} - \gamma_{i^*}|$. When the voter decide to negotiate with both parties and both accept to pay the price set by him, he has to select just one offer and vote for this candidate. Thus, in equilibrium, the voter set his offer in B for each party, and then they decide if to pay it or not. Finally, the voter decides which offer accept, if both parties are willing to pay B , he will prefer his ex-ante option, it means i^* . It is important to highlight that, in this latter case the vote-selling is not effective to the party side, because the negotiation do not change the result of the political election. When a party win the election accepting to pay the voter, its payoff is $\pi_i(W, 1, 1) = W$, and the loser party obtains $\pi_i(W, 0, 0) = B$. If the pivotal voter decide negotiate with both political forces, the parties i^* and $-i^*$ have to decide if accept to pay B to the voter or not, this strategic situation is represented by¹,

		$-i^*$	
		Accept	Reject
i^*	Accept	W, B	W, B
	Reject	B, W	$W + B, B$

We can observe that there exist an unique equilibrium where both parties are willing to pay B to the voter.

¹This situation is considering that, if both parties accept to pay the price set by the voter, he prefers the party i^* .

III. EXPERIMENTAL DESIGN

The experiment was conducted at Centre for Experimental Social Sciences (CESS) of Universidad de Santiago. A total of XX student participated on XX sessions of XX participants. Each session lasting about XX hours.

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