## CE394M: Stress-strain-strength relationship of clay

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#### Overview

Stress-strain-strength relationship

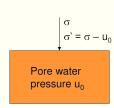
Simple shear

#### L-soil v D-soil

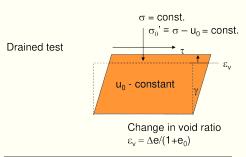
L-soils:

D-soils:

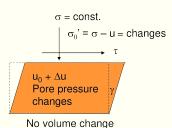
#### Simple shear



Initial consolidation Void ratio e<sub>0</sub>



Undrained test





## NCL: L-soil (drained v undrained)

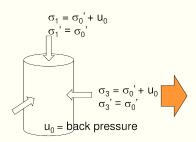
# SS: LOC-soil (L-soils)

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# SS: HOC-soil (D-soils)

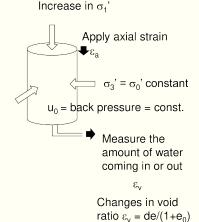
# SS: HOC-soil (D-soils) (drained v undrained)

### TXC: Drained strength and volume at failure using CS

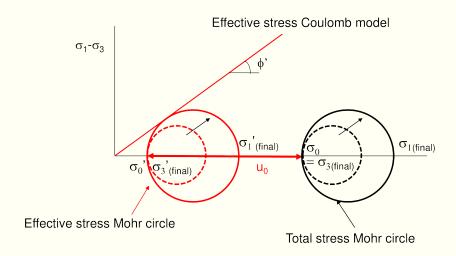


Initial consolidation condition

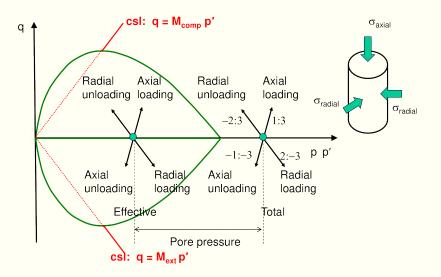
$$e_0 = Gsw_0$$



## TXC: Drained (Mohr-Coulomb ESA)



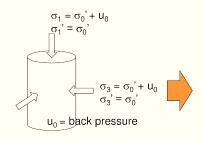
### TXC: Drained Cam-Clay yield and failure



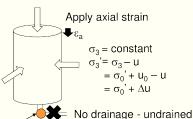
# TXC Drained (axial loading)

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#### TXC: Undrained strength and excess PWP at failure



Increase in  $\sigma_1$  and  $\sigma_1$ '=  $\sigma_1$ -u



Measure pore pressure (u) by a pressure transducer

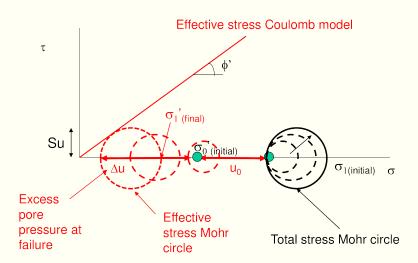
Excess pore pressure  $\Delta u = u - u_0$ 

e<sub>0</sub> or w<sub>0</sub> is kept constant

Initial consolidation condition

$$e_0 = Gsw_0$$

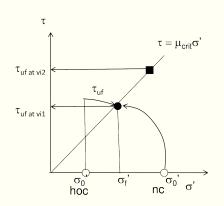
## TXC: Undrained (Mohr-Coulomb ESA)

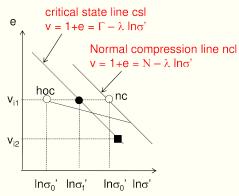


## TXC Undrained (axial loading)

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#### Critical state concept





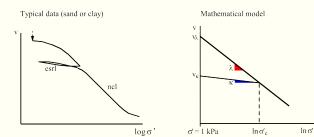
#### Critical state concept

Interchangeable parameters for stress at yield and  $d\varepsilon^p$ .

System	Effective	Plastic	Effective	Plastic	Critical	Plastic	Critical
	normal	normal	shear	shear	stress	normal	normal
	stress	strain	stress	strain	ratio	stress	stress
General	σ*	ε*	τ*	γ*	μ* <sub>crit</sub>	σ* <sub>c</sub>	σ* <sub>crit</sub>
SSA	σ΄	3	τ	γ	tan φ <sub>crit</sub>	σ' <sub>c</sub>	$\sigma'_{ m crit}$
BA-PS	s'	$\epsilon_{ m v}$	t	$\epsilon_{\gamma}$	sin φ <sub>crit</sub>	s′ c	s' crit
TA-AS	p'	$\epsilon_{\rm v}$	q	$\epsilon_{\rm s}$	M	p'c	p' <sub>crit</sub>

Plastic work and dissipation:  $\sigma^*\partial \varepsilon^* + \tau^*\partial \gamma^* = \mu^*_{\it crit}\sigma^*\partial \gamma^*$ . General yield surface:  $\frac{\tau^*}{\sigma^*} = \mu^* = \mu^*_{\it crit} \ln \left[\frac{\sigma^*_{\it c}}{\sigma}\right]$ 

#### Critical state concept: 1D compression



Plastic compression stress  $\sigma_c'$  is taken as the larger of the initial aggregate crushing stress and the historic maximum effective vertical stress. Clay muds are taken to begin with  $\sigma_c'=1$ kPa.

Plastic compression (normal compression line):  $v = v_l ambda - \lambda \ln \sigma'$  for  $\sigma' = \sigma'_c$ .

Elastic swelling and recompression line  $(\kappa$ -line):  $v = v_c + \kappa (\ln \sigma'_c - \ln \sigma'_v)$ .