

S. 2.27 : a) $\lambda t = \left(\frac{1 \text{ calls}}{\text{minute}} \right) \cdot \left(\frac{1}{1} \text{ minute} \right) = 1$

$$Pr(X < 3) = \sum_{k=0}^2 \frac{1}{k!} e^{-1} = \frac{1}{e} \left(1 + 1 + \frac{1}{2} \right) = \frac{5}{2e}$$

$= 0.9197$

b) $\lambda t = \left(\frac{1 \text{ calls}}{\text{minute}} \right) \cdot 6 \text{ minutes} = 60$

$$Pr(X < 3) = \sum_{k=0}^2 \frac{60^k}{k!} e^{-60} = e^{-60} \left(1 + 60 + \frac{3600}{2} \right)$$

$$= 1861 \cdot e^{-60} = 1.627 \times 10^{-23}$$

S. 2.32 WP to ea 2, 3 in Page 30

$$P_X(k) = Pr(A) = \binom{n}{k} p^k (1-p)^{n-k} \quad k=0, 1, 2$$

a) $\rightarrow t = 2 \Rightarrow$ if more than 2 error

occurs in 7-bit data block, decoder will be in error; thus the decoder probability is

$$P_e = \sum_{i=2}^7 \binom{7}{i} (0.03)^i (1-0.03)^{7-i} = 0.0171$$

more than $t \leftarrow i=2$

b) \rightarrow similarly $\rightarrow t = 2 \rightarrow P_e = \sum_{i=3}^{15} \binom{15}{i} (0.03)^i (1-0.03)^{15-i}$

c) similarly $\rightarrow t = 3 \rightarrow P_e = \sum_{i=4}^{31} \binom{31}{i} (0.03)^i (1-0.03)^{31-i}$

$$= 0.0133$$

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Year. Month. Date.

with math Subject:

S-2.37

I'll do it in future
if necessary

S. Homework 3.3:

a) since this is a pdf the following

integral lead to 2: $\int_{-\infty}^{\infty} f(x) dx = 2$

up to $f(x)$ $\Rightarrow \int_{-\infty}^{\infty} f(x) dx = 2 \rightarrow \frac{-a^{-bx}}{b \ln(a)} \Big|_{-\infty}^{\infty} = 1$

$$\Rightarrow \frac{1}{b \ln(a)} + \lim_{x \rightarrow \infty} \left(\frac{-a^{-bx}}{b \ln(a)} \right) = 2$$

Here is two case arise $a > 1$ and $a < 1$

• the case $a < 1$ is not possible

because then $f(x)$ can become
negative $\rightarrow f(x)$ is pdf so it is

impossible \rightarrow first consider case $a > 1$

this lead to finite value if
only if $b < 0$.

* second case: $a < 1$ the limit will
be finite only if $b > 0$

In both cases the limits to 0

and above eq. reduces to $\frac{-1}{b \ln(a)} = 1$

$$\boxed{a = e^{-\frac{1}{b}}}$$

$$\Rightarrow f(x) = a^{-bx} = \left(e^{-\frac{1}{b}}\right)^{bx} \rightarrow f(x) = e^{-x}$$

b). the CDF is given by

$$F(x) = \int_{-\infty}^{\infty} f(x) dx = \int_{-\infty}^{\infty} e^{-x} dx$$

$$\Rightarrow F(x) = \begin{cases} e^{-x} & x \leq 0 \\ 1 & 0 \leq x \end{cases}$$

S. Home work 5

$$Pr(|S - 20| > 1.075) = 2 \int_{9.9}^{9.925} f(s) ds$$

$$= 2 \int_{9.9}^{9.925} 100(s - 9.9) ds = 2 \int_0^{0.025} 100u du$$

$$= 100 \cdot 2(0.025)^2 = 0.125$$

Home work 6:

let $Pr(M=0) = P_0$ and $Pr(M=1) = P_1$

$$f_{X|M=0}(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

$$f_{X|M=1}(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(x-1)^2}{2\sigma^2}\right)$$

$$= \frac{P_0}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{x^2}{2\sigma^2}\right) + \frac{P_1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(x-1)^2}{2\sigma^2}\right)$$

$$Pr(M=0|X=x) = \frac{f_{X|M=0}(x)}{f_X(x)}$$

$$= \frac{P_0 \exp\left(-\frac{x^2}{2\sigma^2}\right)}{P_0 \exp\left(-\frac{x^2}{2\sigma^2}\right) + P_1 \exp\left(-\frac{(x-1)^2}{2\sigma^2}\right)}$$

$$= \frac{1}{1 + \frac{P_1}{P_0} \exp\left(-\frac{(x-1)^2}{2\sigma^2} + \frac{x^2}{2\sigma^2}\right)}$$

$$= \frac{1}{1 + \frac{P_1}{P_0} \exp\left(\frac{x}{\sigma^2} - \frac{1}{2\sigma^2}\right)}$$

we have to plot this

function for the following

combinations

$$(a) \quad P_0 = \frac{1}{2}, P_1 = \frac{1}{2}, \sigma^2 = 1$$

$$Pr(M=0 | X=a) = \frac{1}{1 + \exp(a - \frac{1}{2})}$$

$$P_0 = \frac{1}{2}, P_1 = \frac{1}{5}, \sigma^2 = 5$$

$$P(M=0 | X=a) = \frac{1}{1 + \exp(\frac{a}{5} - \frac{1}{5})}$$

$$(b) \quad P_0 = \frac{1}{4}, P_1 = \frac{3}{4}, \sigma^2 = 1$$

$$Pr(M=0 | X=a) = \frac{1}{1 + 3 \exp(a - \frac{1}{2})}$$

$$P_0 = \frac{1}{4}, P_1 = \frac{3}{4}, \sigma^2 = 5$$

$$Pr(M=0 | X=a) = \frac{1}{1 + 3 \exp(\frac{a}{5} - \frac{1}{5})}$$

Plot of all distributions

