



**MONASH** University  
Information Technology

**22<sup>nd</sup> and 24<sup>th</sup> April 2015**

**Monash University – Sunway Campus, Malaysia**

# **FIT 2004**

# **Algorithms and Data Structures**

## **Tutorial/ Practical 07**

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# Tutorial07 Task01

- Dynamic programming
  - Optimal sub-structure
  - Sub-problems overlap
- Current problem: Longest Common Subsequence (LCS)

# Tutorial07 Task01

- Given 2 string
  - String01 to be  $s1[1\dots m]$
  - String02 to be  $s2[1\dots n]$
  - Let's have them inside LCS  $[i][j]$  matrix of size  $M \times N$

# Tutorial07 Task01

- 2 possible situation
- Situation 1: If  $s1[i] == s2[j]$ 
  - Then we are able to extend  $LCS[i-1][j-1]$  the character.
  - $LCS[i][j] = LCS[i-1][j-1] + 1$
- Situation 2: If  $s1[i] != s2[j]$ 
  - Then we look for the maximum subsequence of the smaller substring earlier
    - $LCS[i][j-1]$
    - $LCS[i-1][j]$
  - $LCS[i][j] = \max (LCS[i][j-1], LCS[i-1][j])$

# Tutorial07 Task02

- Binary Search Tree (BST)
  - All of you should be familiar now having done Practical06

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  - Given a tree to be `fork(root, left, right)` then we establish that  $\text{Left} < \text{Root} < \text{Right}$

# Tutorial07 Task02

- Binary Search Tree (BST)
  - All of you should be familiar now having done Practical06
  - Given a tree to be fork(root, left, right) then we establish that  $\text{Left} < \text{Root} < \text{Right}$
  - Thus for this question, one can easily establish the need for a recursive algorithm for the traversal of trees
    - > Traversal would be limited to the condition given to be within lo and hi (inclusive)

# Tutorial07 Task02

- Now take some time to come up with the algorithm



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# Tutorial07 Task02

- Solution

```
1  def between(T, lo, hi):
2      if (T is None):
3          return
4      if (lo < T.value) and (T.left is not None):
5          between(T.left, lo, hi)
6      if (T.value < hi) and (T.right is not None):
7          between(T.right, lo, hi)
```

# Tutorial07 Task02

- Solution
  - Not complete because?

```
1  def between(T, lo, hi):  
2      if (T is None):  
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4      if (lo < T.value) and (T.left is not None):  
5          between(T.left, lo, hi)  
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7          between(T.right, lo, hi)
```

# Tutorial07 Task02

- Solution
  - Now complete

```
11  def between(T, lo, hi):
12      if (T is None):
13          return
14      if (lo < T.value) and (T.left is not None):
15          between(T.left, lo, hi)
16      # adds print here to print in order
17      if (lo <= T.value <= hi):
18          print(T.value)
19      if (T.value < hi) and (T.right is not None):
20          between(T.right, lo, hi)
```

# Tutorial07 Task03

- Simple problem
- Try work it out yourself first

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# Tutorial07 Task03

- Insert
  - Just add it in the right position
  - Uphold the requirement that  $\text{left} < \text{root} < \text{right}$

# Tutorial07 Task03

- Insert
  - Just add it in the right position
  - Uphold the requirement that  $\text{left} < \text{root} < \text{right}$
- Delete
  - Slightly more tricky but relatively the same concept
  - Swap the node with the biggest-left leaf or the smallest-right leaf
  - Maintains the requirement that  $\text{left} < \text{root} < \text{right}$



# Tutorial07 Task04

- AVL Trees
  - Slightly more fun and also complex than that of BST in Task03

# Tutorial07 Task04

- Requirement of AVL Trees
  - Given a tree fork(root, left, right)  
 $\text{height}(\text{left}) - \text{height}(\text{right}) \leq \text{abs}(1)$

# Tutorial07 Task04

- Requirement of AVL Trees
  - Given a tree fork(root, left, right)  
 $\text{height}(\text{left}) - \text{height}(\text{right}) \leq \text{abs}(1)$
  - Done in a recursive manner (bottom up from the tree)

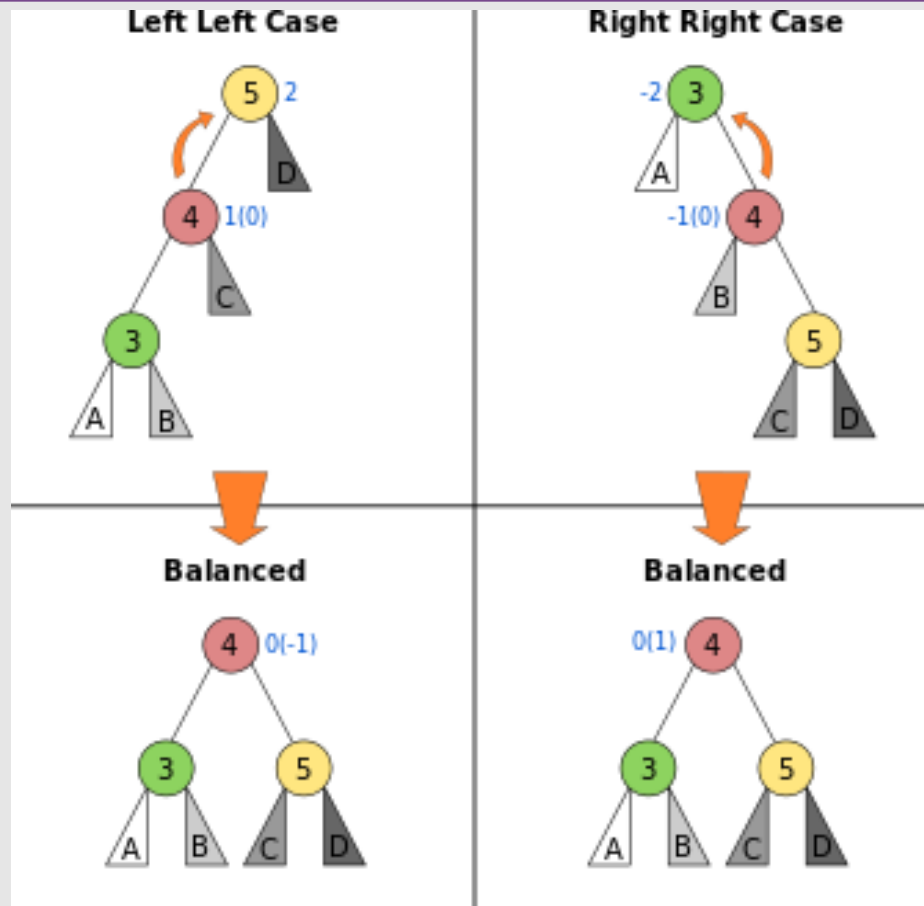
# Tutorial07 Task04

- Requirement of AVL Trees
  - Given a tree fork(root, left, right)  
 $\text{height}(\text{left}) - \text{height}(\text{right}) \leq \text{abs}(1)$
  - Performs rotation to maintain the above rule!
    - LL
    - LR
    - RR
    - RL

# Tutorial07 Task04

- Requirement of AVL Trees
  - Given a tree  $\text{fork}(\text{root}, \text{left}, \text{right})$   
 $\text{height}(\text{left}) - \text{height}(\text{right}) \leq \text{abs}(1)$
  - Performs rotation to maintain the above rule!
    - LL: Simple
    - LR
    - RR: Simple
    - RL

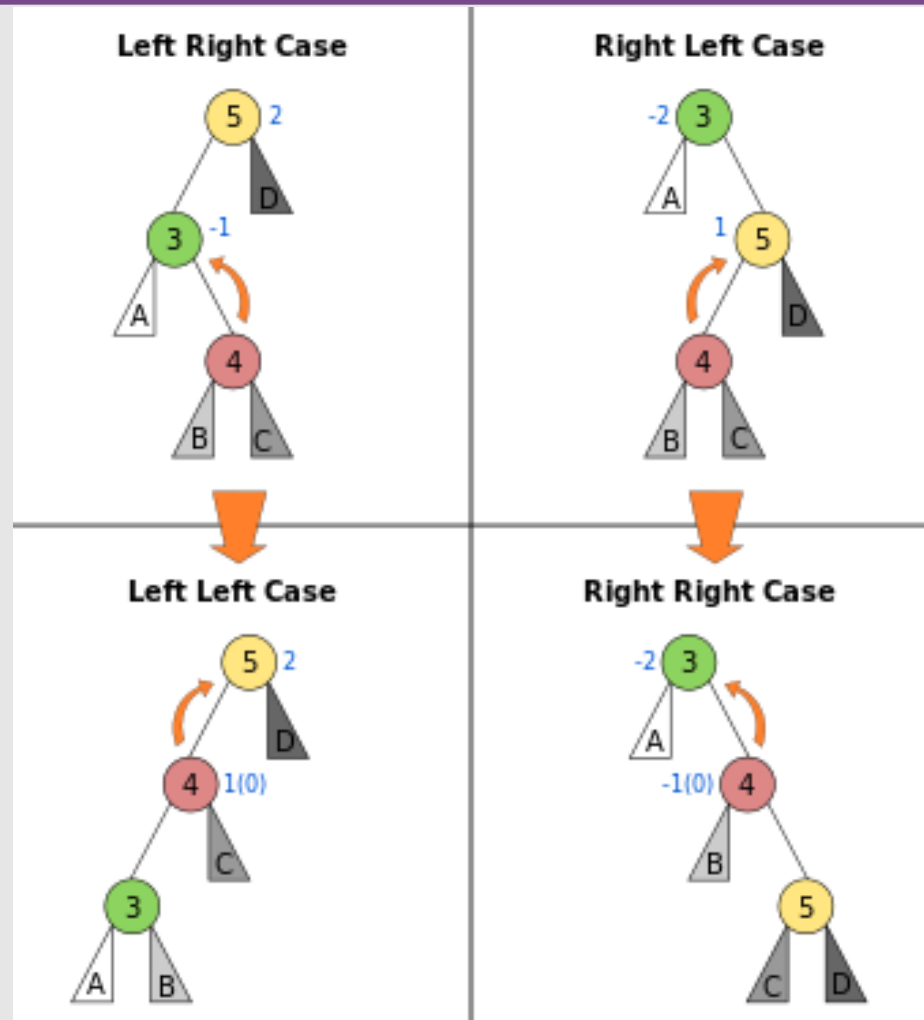
# Tutorial07 Task04



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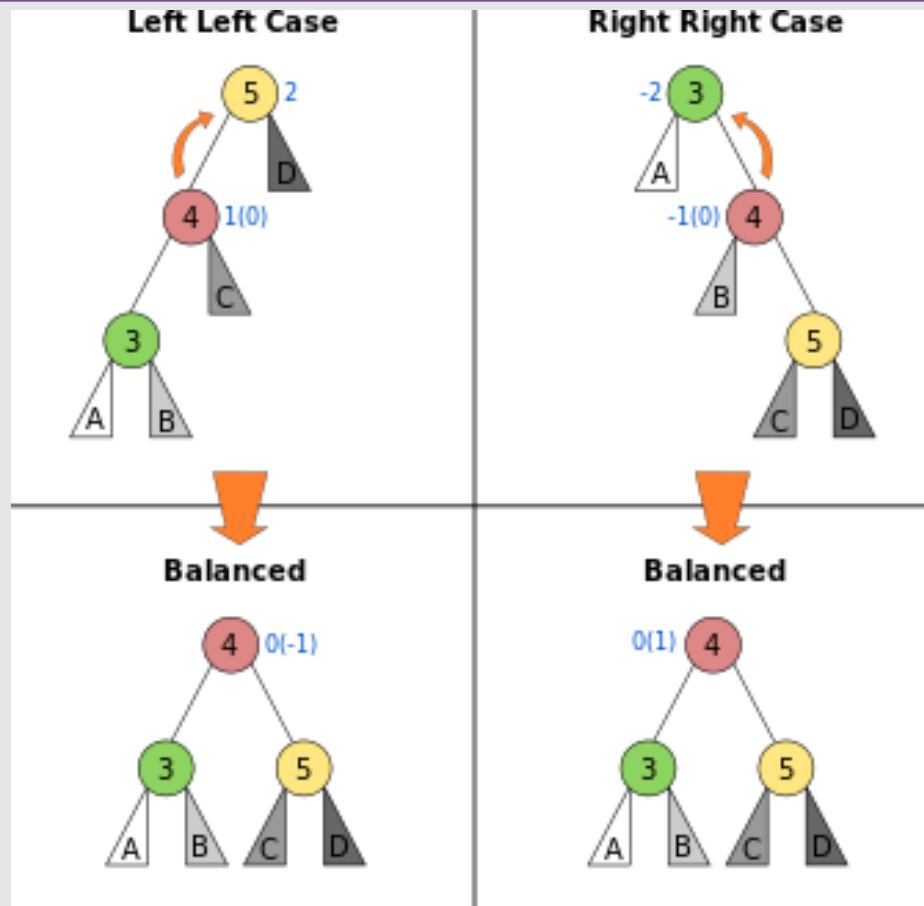
- Requirement of AVL Trees
  - Given a tree fork(root, left, right)  
 $\text{height}(\text{left}) - \text{height}(\text{right}) \leq \text{abs}(1)$
  - Performs rotation to maintain the above rule!
    - LL: Simple
    - LR: Convert to LL first
    - RR: Simple
    - RL: Convert to RR first

# Tutorial07 Task04





# Tutorial07 Task04



# Tutorial07 Task05

- Suffix Tries.
- Pretty difficult (for me personally) and very tedious.
- Give it a try now pen and paper
- We would discuss it later

# Data Structures

- Abstract Data Type (ADT)
  - Keep this in mind when coding as this is an issue faced by many of you (mainly due to the nature of Python also)
  - Code following the definition of the data structure.
    - Example the `HashTable.insert(key, data)`

# Practical07

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  - Keep this in mind when coding as this is an issue faced by many of you (mainly due to the nature of Python also)
  - Code following the definition of the data structure.
    - Example the `HashTable.insert(key, data)`

# Practical07

- Tries
  - Several ways to implement this
  - You can be creative :3

# Practical07

- AVL Trees
  - What are the main rules to follow?
    - Height balanced
  - Thus the main components
    - Calculate height
    - Calculate balance
    - Right rotate
    - Left rotate

# Practical08

- Anything to clarify or discuss?
- Pretty simple practical
  - So much easier than Practical06 (Prac08 nerfed?)
  - In fact last year's FIT 2004 only have Task02 as their only question so yea, no nerf...

# HashTable

- Will do this when I have time.
- There are a lot of variants



# HashTable

- Insert(key, data)
  - Insert data into the HashTable, using Key to get the position quickly
    - How?

# HashTable

- Insert(key, data)
  - Insert data into the HashTable, using Key to get the position quickly
    - How? By hashing the key
      - Relies on the hash function
    - **Follow this definition! NO OPERATIONS**

# HashTable

- **Insert(key, data)**
  - Insert data into the HashTable, using Key to get the position quickly
    - How? By hashing the key
      - Relies on the hash function
      - Chaining/ probing/ bucketing if required
    - Follow this definition!
  - Roughly  $O(1)$  best and worst case
    - Ensure this with resizing
    - When to resize?
      - When it is getting full
      - When the chain is going too long

# HashTable

- Insert(key, data)
  - No repeated keys
    - Data with the same key can be added as into the bucket with the Entry having a key and a List<Data>

# HashTable

- Lookup(key)
  - Search for the key quickly
    - Via hashing of key
    - With chaining/ probing/ bucketing if required
  - Retrieve
    - Data if the key is found
    - None if key is not found
    - No printout, no return of False etc.
      - Remember, consistent with definition and ADT!

# HashTable

- Delete(key)
  - Delete the Entry with the key
    - Lookup via hashing of key
    - With chaining/ probing/ bucketing if required
  - How to delete? With respect to chaining
    - Remove the Entry
      - Need to ensure the chain is maintained by shifting the other elements in the chain over
      - Pretty simple if you keep the chain short
    - Set Entry to a special Delete flag
      - Maintains the chain for probing
      - Remove/ Ignore when Resize

# HashTable

- **Resize()**
  - Easiest one of all!
  - Save all entries into the a temporary list
    - Ignore all None
    - Ignore all with Delete flag
  - Insert(key, data) for all Entry
    - Totally fine since insert have no operation

# HashTable

- Bonus: Entry
  - Must contain key and data
  - Can optionally contain other information to ease out operations
    - Hash value without chain  $H(\text{key}, 0)$
  - Declared as an inner class that encapsulate information you need





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**Thank You**