

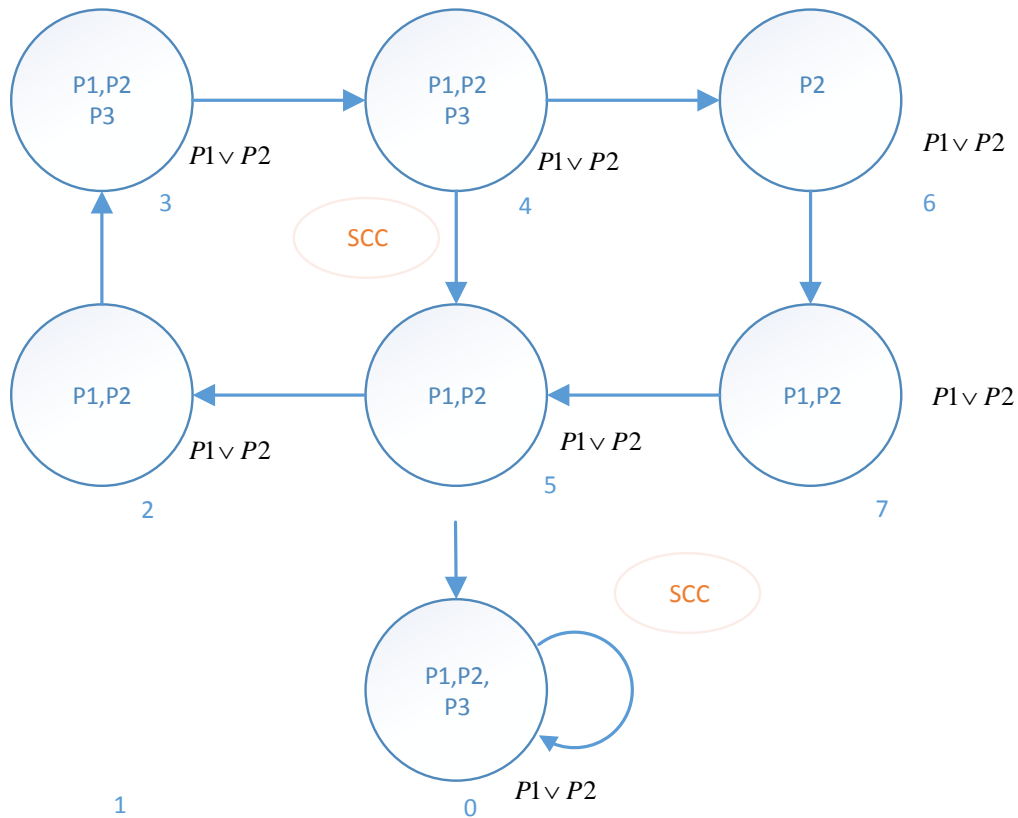
Q1:

1. Answer:

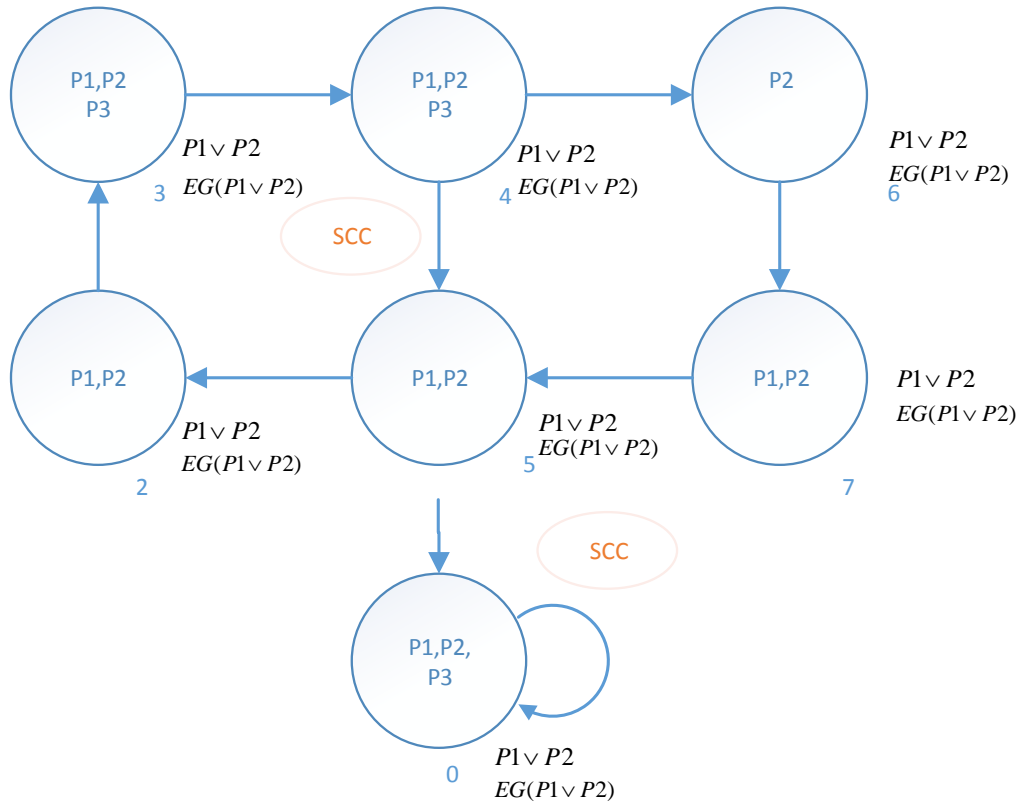
$$AF(f) = \neg EG(\neg f) \Rightarrow AF(\neg P1 \wedge \neg P2) = \neg EG(\neg(\neg P1 \wedge \neg P2)) = \neg EG(P1 \wedge P2)$$

The following diagrams are the steps to check $\neg EG(P1 \wedge P2)$

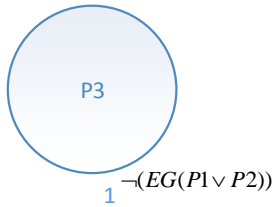
Step1: check $P1 \wedge P2$



Step 2: check $EG(P1 \wedge P2)$



Step 3: check $\neg EG(P1 \wedge P2)$



Therefore, the initial state does not satisfy the requirement $AF(\neg P1 \wedge \neg P2)(\neg EG(P1 \wedge P2))$. It means that this model cannot meet requirement $AF(\neg P1 \wedge \neg P2)$.

2.

(1). To any two different processes, the state of them will not be "critical" at the same time.

$$\forall i, j: n \bullet i \neq j \text{ imply } AG(\neg(critical(i) \wedge critical(j)))$$

(2) To any process, if request happens, critical will always eventually happen

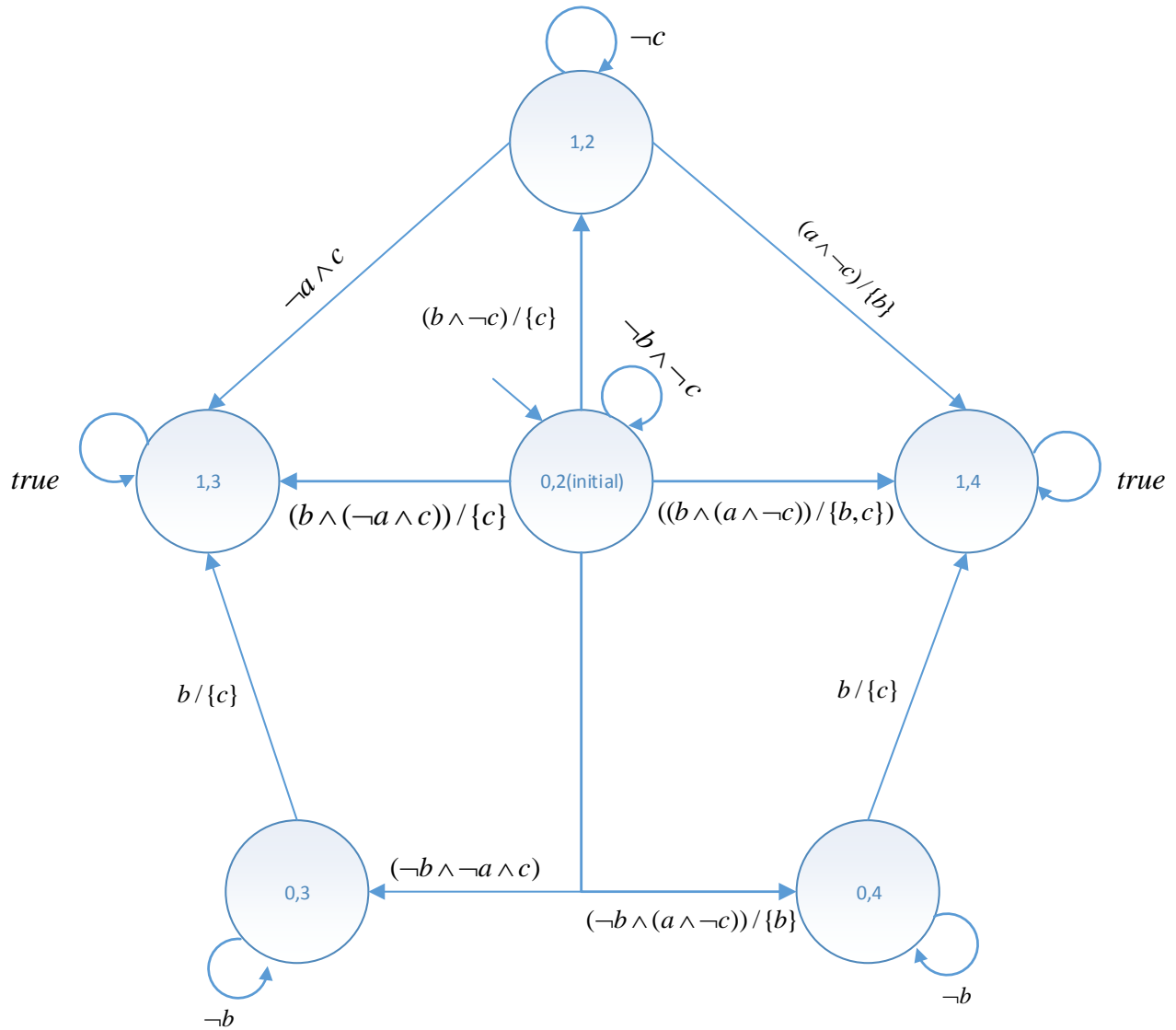
$$\forall i: n \bullet AG(request(i) \Rightarrow AF(critical(i))))$$

(3) The system is deadlock free

$\forall i : n \bullet \text{AG EX true}$

Q2

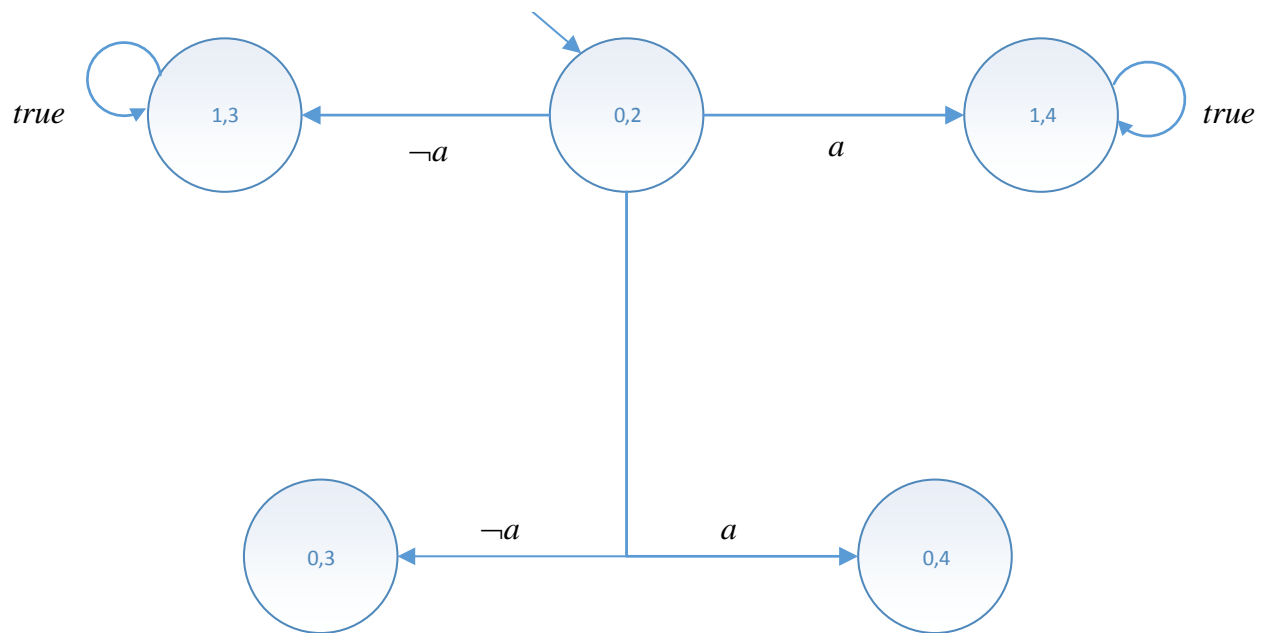
1. $A_1 \parallel A_2$



Deterministic: No, considering the input $(a \wedge \neg b \wedge \neg c)$ to the initial state, states $(0,4)$ and $(0,2)$ are all possible next state. So it is not deterministic.

Reactive: No, considering the input $(a \wedge b \wedge c)$ to the initial state, it will not react. So it is not reactive.

2. $A_1 \parallel A_2 \setminus \{b, c\}$



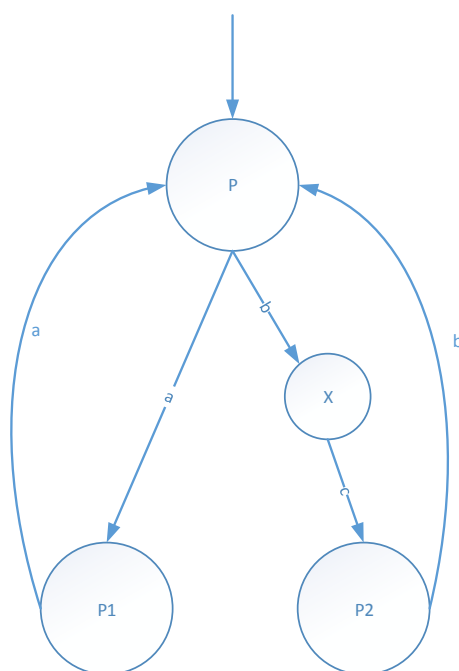
Deterministic: No, considering the input ($\neg a$) to the initial state, states (1,3) and (0,3) are all possible next state. So it is not deterministic.

Reactive: No, considering state (0, 4), it will not react any action. So it is not reactive.

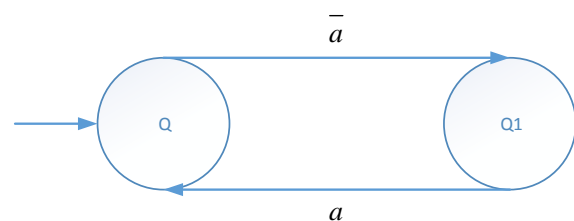
Q3

P and Q can be drawn like below(X is a middle state):

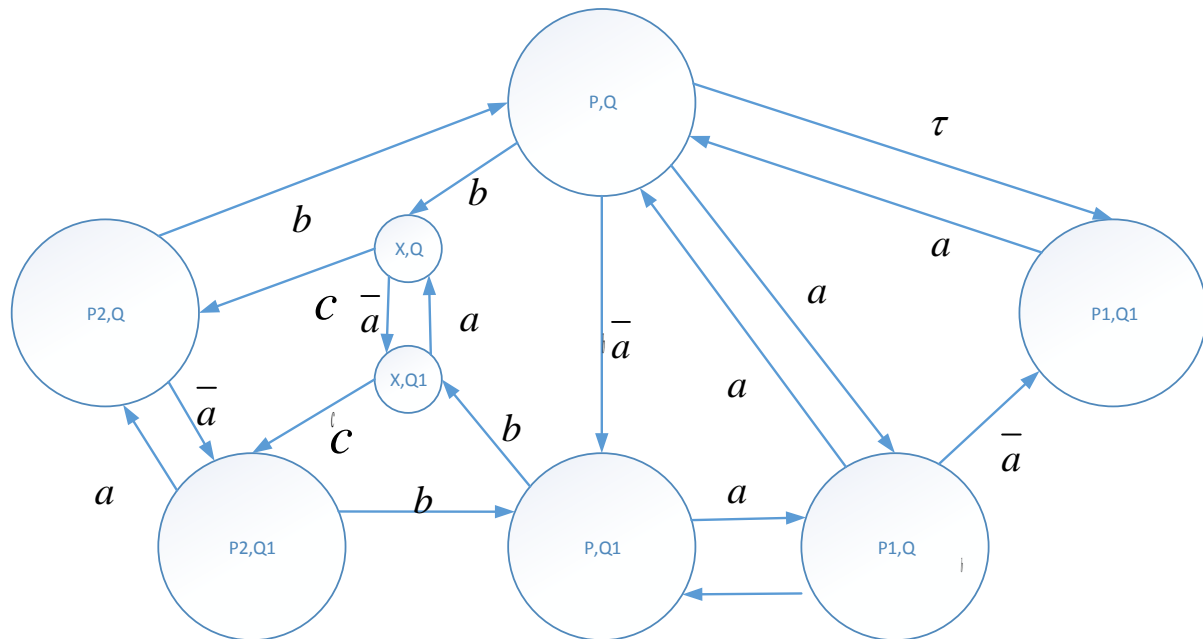
P.



Q.



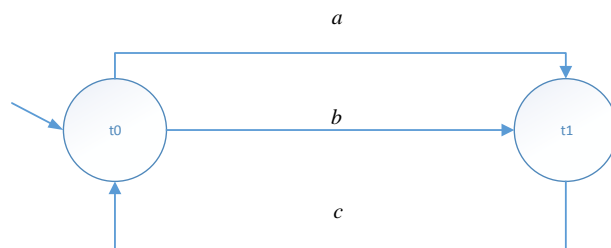
$P \parallel Q$ can be drawn like below:



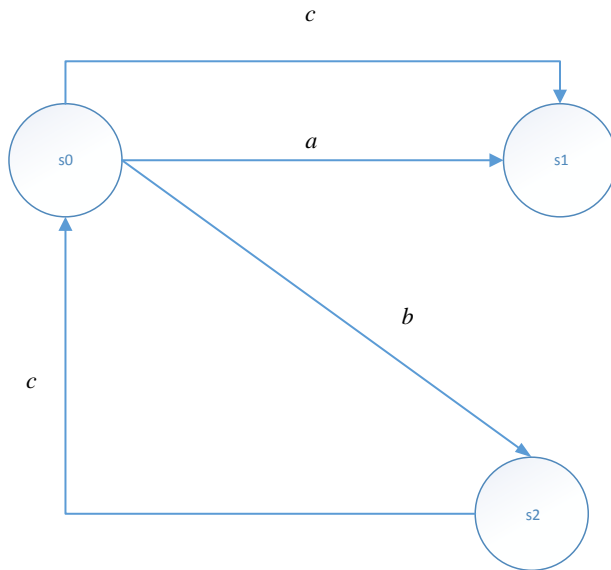
Q4

We can define 2 processes T,S as below:

T



S



(1) Bisimulation

We can use the algorithm to check Bisimulation.

We need to compute the greatest fixpoint (gfp): we do it by computing approximates starting from the Cartesian product:

- $R_0 = \{(t_0, s_0), (t_0, s_1), (t_0, s_2), (t_1, s_0), (t_1, s_1), (t_1, s_2)\}$ – Cartesian product
- $R_1 = \{(t_0, s_0), (t_1, s_0), (t_1, s_1), (t_1, s_2)\}$ – removed those pairs that violate local condition on final (if T final then S final)
- $R_2 = \{(t_0, s_0), (t_1, s_1), (t_1, s_2)\}$ – removed (t_1, s_0) , since t_1 can do c and s_0 cannot
- $R_3 = \{(t_0, s_0), (t_1, s_1), (t_1, s_2)\}$ – nothing is further removed
- $R_2 = R_3$

greatest fixpoint reached, S and T are bisimilar

(2) Simulation

We can use the algorithm to check Simulation.

We need to compute the greatest fixpoint (gfp): we do it by computing approximates starting from the Cartesian product:

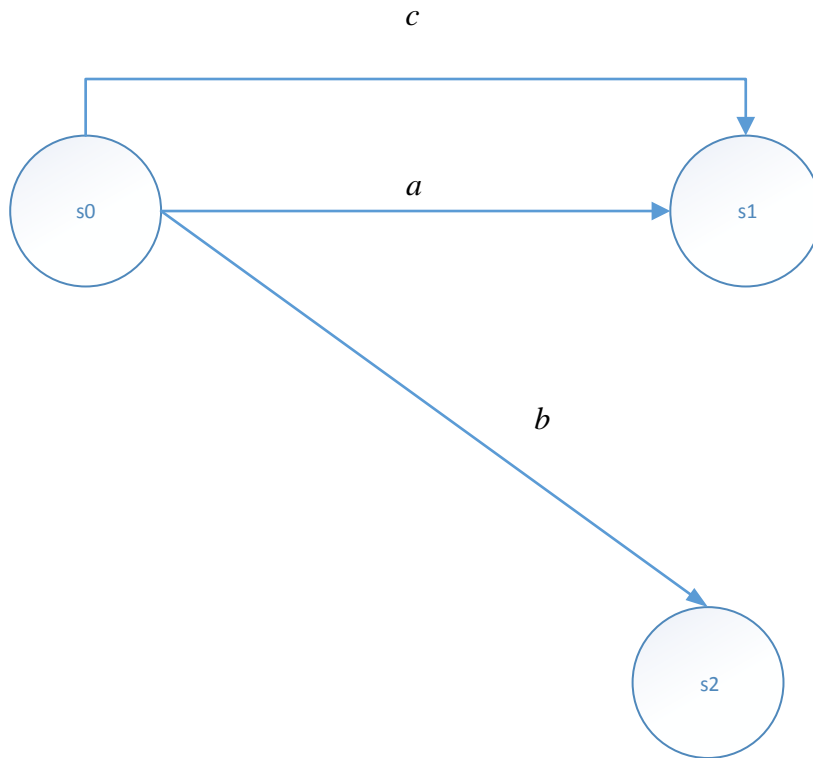
- $R_0 = \{(t_0, s_0), (t_0, s_1), (t_0, s_2), (t_1, s_0), (t_1, s_1), (t_1, s_2)\}$ – Cartesian product
- $R_1 = \{(t_0, s_0), (t_1, s_0), (t_1, s_1), (t_1, s_2)\}$ – removed those pairs that violate local condition on final (if T final then S final)
- $R_2 = \{(t_0, s_0), (t_1, s_1), (t_1, s_2)\}$ – removed (t_1, s_0) , since t_1 can do c and s_0 cannot
- $R_3 = \{(t_0, s_0), (t_1, s_1), (t_1, s_2)\}$ – nothing is further removed

- $R_2 = R_3$

Fixed point reached!

S simulates T and similarly vice versa

However if S performs like below:



(1). Bisimulation

As the algorithm, we can see that S and T are not Bisimilar.

(2). Simulation

We can use the algorithm to check Simulation.

We need to compute the greatest fixpoint: we do it by computing approximates starting from the Cartesian product:

- $R_0 = \{(s_0, t_0), (s_0, t_1), (s_1, t_0), (s_1, t_1), (s_2, t_0), (s_2, t_1)\}$ – Cartesian product
- $R_1 = \{(s_0, t_0), (s_1, t_0), (s_1, t_1), (s_2, t_0), (s_2, t_1)\}$ – removed those pairs that violate local condition on final (if S final then T final)
- $R_2 = \{(s_0, t_0), (s_1, t_1), (s_2, t_0), (s_2, t_1)\}$ – removed (s_1, t_0) , since s_1 can do c but t_0 cannot; removed (t_1, s_2) since t_1 can do c but s_2 cannot
- $R_3 = \{(s_0, t_0), (s_1, t_1), (s_2, t_0), (s_2, t_1)\}$ – nothing is removed $R_2 = R_3$

greatest fixpoint reached, so T simulates S.

However, as we can see S2 cannot accept C action, so S does not simulates T.