

2. Without coding, how would you change ThreeSumFast to become FourSumFast?

We would add a fourth integer l and a third for loop for k and call binarySearch() with the new integer l.

3.

- a. 5 different classes of time complexities and an example of each
  - i. Constant time ( $O(1)$ ): print statement, calculating addition, subtraction, or other simple math
  - ii. Logarithmic time ( $O(\log n)$ ): binary search
  - iii. Linear time ( $O(n)$ ): finding the largest/smallest element of an array
  - iv. Cubic time ( $O(n^3)$ ): array multiplication
  - v. Quadratic time ( $O(n^2)$ ): bubble sort
- b. Code snippet showing a loop of constant time complexity

```
for (int i = 1; i <= a; i++) {  
    System.out.println("Hello World!");  
}
```

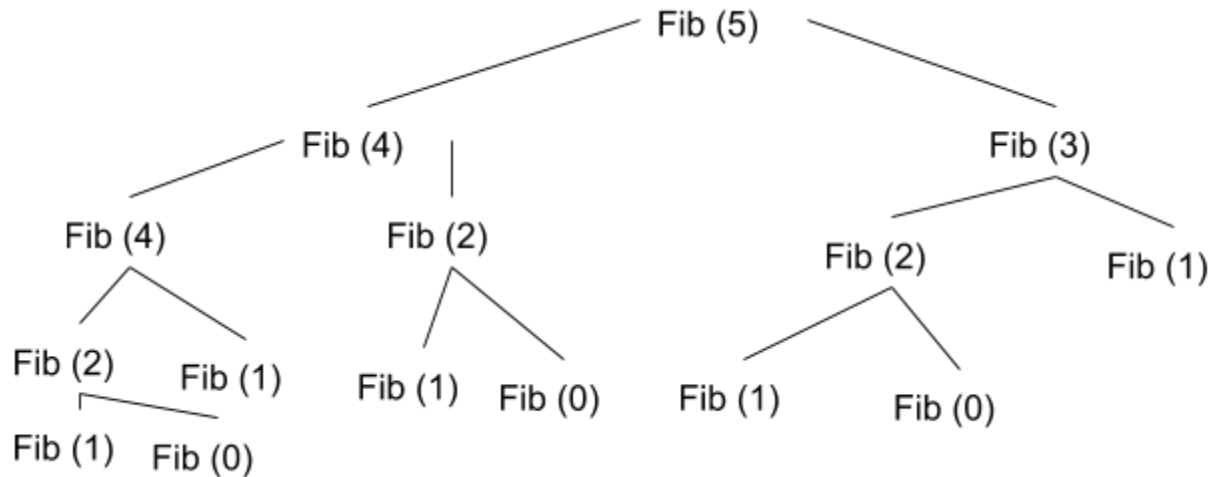
- c. If an algorithm executes  $O(\log n)$  time computation for each entry of an array storing n elements, what is the big O for storing the entire array?

$n * (\log n)$

- d. Using an n of 5, show that time complexity of the recursive fibonacci algorithm is  $O(2^n)$  - write it out

The time complexity is exponential because each time the function is called, you are calling the function two more times. When the function is called n times, you get a time complexity of  $O(2^n)$ .

For an n of 5, the tree has 5 levels:



- e. Using the running time and big o from your programming assignment, predict what the running time of 8000 items would be

Since the time complexity of ThreeSum was  $O(n^3)$ , the time complexity of our new program would be  $O(n^4)$ . Our program ran in 87 seconds with 1000 integers. We predicted that it would take 5939.2 minutes. Since, 1000 goes into 8000 8 times we multiplied our runtime for 1000 integers by  $8^4$ .

- f. Give me the big O of the algorithms with the following worst case runtimes ( $T(N)$ ):
- i.  $T(N) = 3N^2 + 10N + 17$   
 $O(n^2)$
  - ii.  $T(N) = N + 9999$   
 $O(n)$
  - iii.  $T(N) = 734N$   
 $O(n)$