For  $a, b, L, \ell, H > 0$ , define  $\mathcal{F} : \mathbb{R} \to \mathbb{R}^+$  such that

$$\mathcal{F}(x) = L + \max \left\{ 0, -\ell + \frac{H + \ell}{1 + \left(\frac{H}{\ell}\right)e^{-b(x-a)}} \right\}$$

$$(4.2.1)$$

For  $c_1, c_2 > 0$ 

$$y \mid x, \Omega, c_1, c_2 \sim \text{Gamma}(\mu \cdot \beta, \beta)$$
 (4.2.2)

$$\mu = \mathcal{F}(x \mid \Omega) = \mathbb{E}(y \mid x, \Omega, c_1, c_2)$$
(4.2.3)

$$\beta = \frac{1}{c_1} + \frac{1}{c_2 \cdot \mu} \tag{4.2.2}$$

$$\Omega = \{a, b, L, \ell, H\} \tag{4.2.4}$$