The simplest form of the standard 3-stage hierarchical model in the context of MEP size modeling can be described as follows. Let there be N_P exchangle sequences $\{(x_i^j, y_i^j)_{i=1}^{n_j} \mid j=1, 2...N_P\}$ of MEP size y_i^j recorded at stimulus intensity x_i^j from j^{th} participant, for a total of N_P participants.

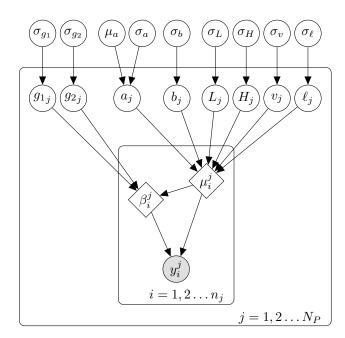
The first stage of hierarchy is the participant-level and specifies parametric model $P(y_i^j \mid x_i^j, \theta_j)$ for each of the N_P sequences and models the MEP size y_i^j as a function of stimulus intensity x_i^j and participant specific parameters θ_j . In the second stage, $\theta_1, \theta_2 \dots \theta_P$ are assumed to be exchangeable and generated from a common distribution $P(\theta_j \mid \gamma)$ with hyper-parameters γ . In the third stage, the hyper-parameters γ are assumed to be unknown and are assigned a non-informative prior density $P(\gamma)$.

$$y_i^j \mid x_i^j, \theta_i, \gamma \sim P(y_i^j \mid x_i^j, \theta_i, \gamma) \tag{4.3.1}$$

$$\theta_j \mid \gamma \sim P(\theta_j \mid \gamma)$$
 (4.3.2)

$$\gamma \sim P(\gamma) \tag{4.3.3}$$

Figure 4.3.1 shows the graphical representation of the basic hierarchical model implemented by hbmep (Section 5.1) for recruitment-curve fitting



$$y_{i}^{j} \mid x_{i}^{j}, \Omega_{1}^{j} \sim \mathcal{G}\left(\mu_{i}^{j} \cdot \beta_{i}^{j}, \beta_{i}^{j}\right)$$

$$\mu_{i}^{j} = \mathcal{F}\left(x_{i}^{j} \mid \Omega_{1}^{j}\right) \quad \beta_{i}^{j} = g_{1j} + \frac{\mu_{i}^{j}}{g_{2j}}$$

$$a_{j} \sim \mathcal{TN}\left(\mu_{a}, \sigma_{a}\right)$$

$$\theta_{j} \sim \mathcal{HN}\left(\sigma_{\theta_{j}}\right) \quad \forall \theta_{j} \in \Omega \setminus \{a_{j}\}$$

$$\mu_{a} \sim \mathcal{TN}\left(50, 20\right) \quad \sigma_{a} \sim \mathcal{HN}\left(30\right)$$

$$\sigma_{\sigma_{L}} \sim \mathcal{HN}\left(.05\right) \quad \sigma_{\theta} \sim \mathcal{HN}\left(5\right) \quad \forall \theta \in \Omega_{2}$$

$$\Omega_{1}^{j} = \{a_{j}, b_{j}, v_{j}, L_{j}, \ell_{j}, H_{j}, g_{1j}, g_{2j}\}$$

$$\Omega_{2} = \{\sigma_{L}, \sigma_{H}, \sigma_{v}, \sigma_{\ell}, \sigma_{q_{1}}, \sigma_{q_{2}}\}$$