

Lagrange's Interpolation Method/Formula

Applicable even if the values of x are not at equal distance (unlike to Newton's Forward/Backward interpolation formula)

$$y = \frac{(x-x_1)(x-x_2)(x-x_3)\dots(x-x_n)}{(x_0-x_1)(x_0-x_2)(x_0-x_3)\dots(x_0-x_n)} \times y_0 + \frac{(x-x_0)(x-x_2)(x-x_3)\dots(x-x_n)}{(x_1-x_0)(x_1-x_2)(x_1-x_3)\dots(x_1-x_n)} \times y_1 + \dots + \frac{(x-x_0)(x-x_1)(x-x_2)\dots(x-x_{n-1})}{(x_n-x_0)(x_n-x_1)(x_n-x_2)\dots(x_n-x_{n-1})} \times y_n$$

Example 1:

Age in months		Weight in LBS (pound)	
x_0	0	y_0	5
x_1	2	y_1	7
x_2	3	y_2	8
x_3	5	y_3	10
x_4	6	y_4	12

The above table gives normal weight of a baby during six month of life. Estimate the weight of baby at the age of 4 months.

	A	B	C	D	E	F	G	H	I
1	$x = 4$								
2	Age in months		Weight in LBS (pound)		Term ₁	Term ₂	Term ₃	Term ₄	Term ₅
3	x_0	0	y_0	5	0.11111	-2.33333	7.11111	5.33333	-1.33333
4	x_1	2	y_1	7					
5	x_2	3	y_2	8					
6	x_3	5	y_3	10					
7	x_4	6	y_4	12					
8									
9	$y = 8.88889$								
10									