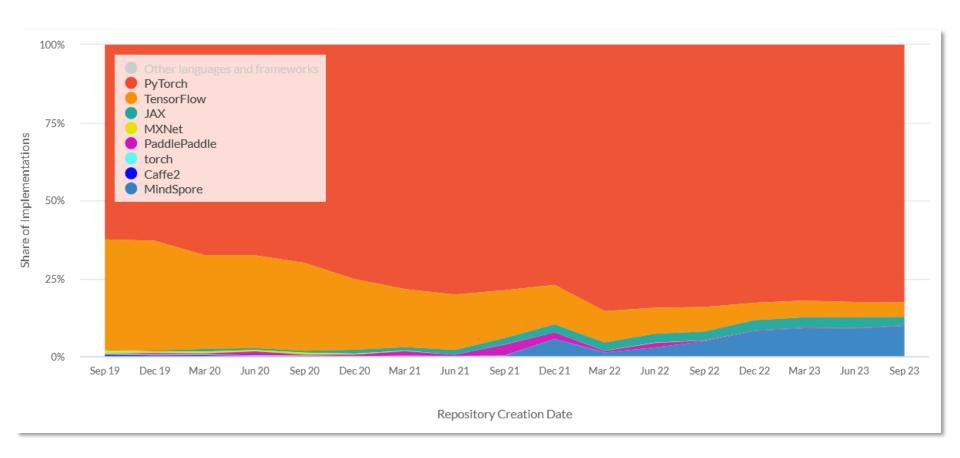
MACHINE LEARNING IN PHYSICS FOUNDATIONS 1

Harrison B. Prosper PHY6937 / PHY4936 Fall 2025

Goals of this Course

- 1. Gain a good understanding of the mathematical basis of machine learning (ML).
- 2. Gain experience building ML models using **PyTorch** to solve data science problems in physics.
- 3. Gain experience with different ML models.
- 4. Gain an appreciation of the power of ML models as well as their (current) limitations.

Why PyTorch?



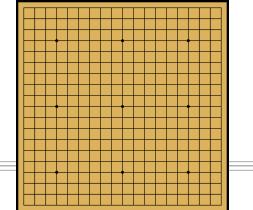
https://viso.ai/deep-learning/pytorch-vs-tensorflow/

What is Artificial Intelligence?

Artificial Intelligence

Algorithms that cause machines to exhibit *human*- or *superhuman*-level intelligence.

ARTICLE



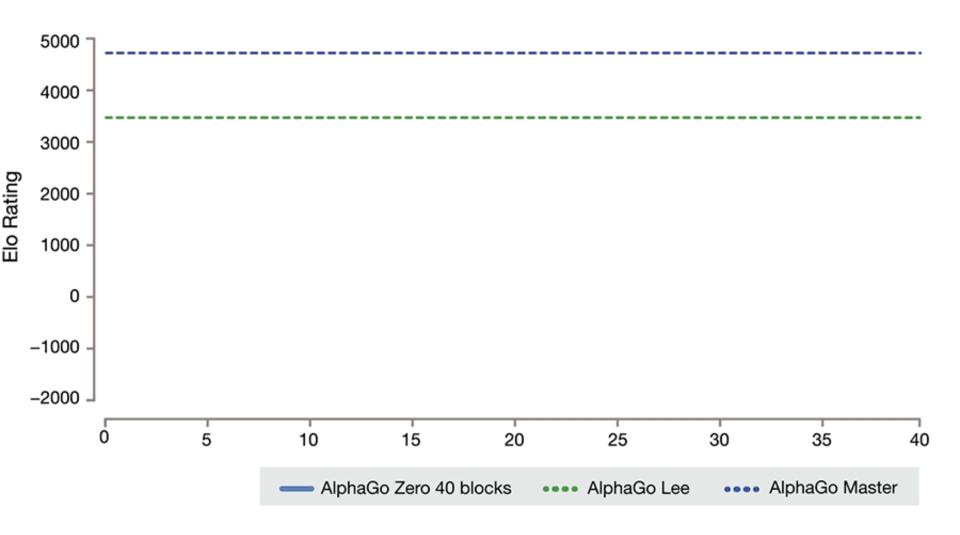
doi:10.1038/nature24270

Mastering the game of Go without human knowledge

David Silver¹*, Julian Schrittwieser¹*, Karen Simonyan¹*, Ioannis Antonoglou¹, Aja Huang¹, Arthur Guez¹, Thomas Hubert¹, Lucas Baker¹, Matthew Lai¹, Adrian Bolton¹, Yutian Chen¹, Timothy Lillicrap¹, Fan Hui¹, Laurent Sifre¹, George van den Driessche¹, Thore Graepel¹ & Demis Hassabis¹

A long-standing goal of artificial intelligence is an algorithm that learns, *tabula rasa*, superhuman proficiency in challenging domains. Recently, AlphaGo became the first program to defeat a world champion in the game of Go. The tree search in AlphaGo evaluated positions and selected moves using deep neural networks. These neural networks were trained by supervised learning from human expert moves, and by reinforcement learning from self-play. Here we introduce an algorithm based solely on reinforcement learning, without human data, guidance or domain knowledge beyond game rules. AlphaGo becomes its own teacher: a neural network is trained to predict AlphaGo's own move selections and also the winner of AlphaGo's games. This neural network improves the strength of the tree search, resulting in higher quality move selection and stronger self-play in the next iteration. Starting *tabula rasa*, our new program AlphaGo Zero achieved superhuman performance, winning 100–0 against the previously published, champion-defeating AlphaGo.

https://deepmind.com/blog/alphago-zero-learning-scratch/



Symbolic Mathematics

In December 2019, Guillaume Lample and François Charton* (Meta fka Facebook AI Research, Paris) claimed: "We achieve results that outperform commercial Computer Algebra Systems such as Matlab or Mathematica."







Charton

^{*} G. Lample and F. Charton, Deep Learning for Symbolic Mathematics, arXiv: 1912.01412v1





OPEN ACCESS

RECEIVED

21 September 2022

REVISED

8 December 2022

ACCEPTED FOR PUBLICATION

12 January 2023

PUBLISHED

27 January 2023

Original Content from this work may be used under the terms of the Creative Commons Attribution 4.0 licence.

Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.



PAPER

SYMBA: symbolic computation of squared amplitudes in high energy physics with machine learning

Abdulhakim Alnuqaydan^{1,2,*}, Sergei Gleyzer³ and Harrison Prosper⁴

- ¹ Department of Physics and Astronomy, University of Kentucky, Lexington, KY, United States of America
- ² Department of Physics, College of Science, Qassim University, Qassim, Saudi Arabia
- ³ Department of Physics and Astronomy, The University of Alabama, Tuscaloosa, AL, United States of America
- ⁴ Department of Physics, Florida State University, Talllahassee, FL, United States of America
- * Author to whom any correspondence should be addressed.

E-mail: aal700@uky.edu

Keywords: physics, high energy physics, machine learning

Abstract

The cross section is one of the most important physical quantities in high-energy physics and the most time consuming to compute. While machine learning has proven to be highly successful in numerical calculations in high-energy physics, analytical calculations using machine learning are still in their infancy. In this work, we use a sequence-to-sequence model, specifically, a transformer, to compute a key element of the cross section calculation, namely, the squared amplitude of an interaction. We show that a transformer model is able to predict correctly 97.6% and 99% of squared amplitudes of quantum chromodynamics and quantum electrodynamics processes, respectively, at a speed that is up to orders of magnitude faster than current symbolic computation frameworks. We discuss the performance of the current model, its limitations and possible future directions for this work.

ChatGPT



Developer(s) OpenAl

Initial release November 30, 2022

(2 years ago)^[1]

Stable release August 7, 2025

(16 days ago)[2]

Engine GPT-5

What is Machine Learning?

Artificial Intelligence

Algorithms that cause machines to exhibit human- or *super-human* level intelligence.

Machine Learning

Algorithms for modeling data.

What is Machine Learning?

Supervised Learning

Unsupervised Learning

Data: (x, y)

y are labels

Task: $x \rightarrow y$

Use cases:

Classification, regression, translation, etc. Data: x

no labels

Task: find structure in,

and/or model, data

Use cases:

Clustering, data
 compression, solving
 differential equations, etc.

What is Machine Learning?

Generative Learning

Reinforcement Learning

Data: x

may or may not be associated with labels

Task: $x \to p(x) \to x$

Use cases:

➤ fast simulators, image/text generation, chatbots, etc.

Data: (x, a, r) x state of the environment a action taken on environment r reward arising from action

Task: find optimal $x \rightarrow a$

Use cases:

➤ Game playing, robotics, accelerator controls, etc.

What is Deep Learning?

Artificial Intelligence

Algorithms that cause machines to exhibit human- or *super-human*-level intelligence.

Machine Learning

Algorithms for modeling data

Deep Learning

ML using (large) neural networks

What is Deep Learning?

Deep learning is the science and art of fitting models to data using functions formed by *composing* nonlinear parameterized functions,

$$f(x) = f_m \circ f_{m-1} \circ \cdots f_1$$

$$= f_m (f_{m-1} (\dots f_1(x)) \dots)$$

$$f(x)$$

$$f_m \qquad f_{m-1} \qquad f_1 \qquad x$$

Each of these functions is referred to as a **layer**. The ChatGPT3 function has **96** layers and **175 billion** parameters!

What is Deep Learning? Example

Here is a simple example of a quark/gluon classifier:

```
f(x) = \operatorname{softmax} \left( \operatorname{dropout}(\operatorname{linear}(\operatorname{flatten} \left( g(c(h(c(x)))) \right)) \right)
y = c(x)
y = \operatorname{flatten}(y)

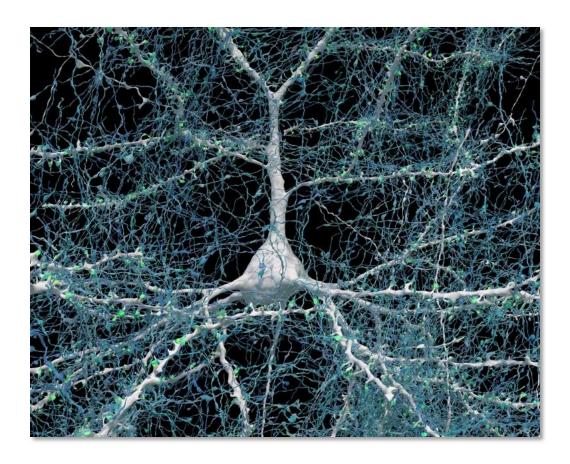
Here is an algorithm-level view: y = h(y)
y = \operatorname{dropout}(y)

And here is a code-level view: y = g(y)
f = \operatorname{softmax}(y)
```

```
Sequential(
  (0): Conv2d(1, 4, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
  (1): MaxPool2d(kernel_size=(2, 2), stride=2, padding=0, dilation=1, ceil_mode=False)
  (2): ReLU()
  (3): Conv2d(4, 4, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
  (4): MaxPool2d(kernel_size=(2, 2), stride=2, padding=0, dilation=1, ceil_mode=False)
  (5): ReLU()
  (6): Flatten(start_dim=1, end_dim=-1)
  (7): Linear(in_features=64, out_features=2, bias=True)
  (8): Dropout(p=0.2, inplace=False)
  (9): Softmax(dim=1)
)
number of parameters: 318
```

BASIC BUILDING BLOCK: THE PERCEPTRON

The Brain's Computational Unit



https://www.nature.com/articles/d41586-024-01387-9

Artificial Comp. Unit: The Perceptron

$$y = g(xA^{T} + b)$$
(Frank Rosenblatt, 1958)
 x is a (row) matrix of input data
 A is a matrix of weights
 b is a (row) matrix of biases
 g is a nonlinear function
$$x_{2}$$

$$y = g(z) = \text{relu}(z) = \max(0, z)$$

$$g(z) = \tanh(z)$$

$$g(z) = \text{sigmoid}(z) = 1 / (1 + \exp(-z))$$

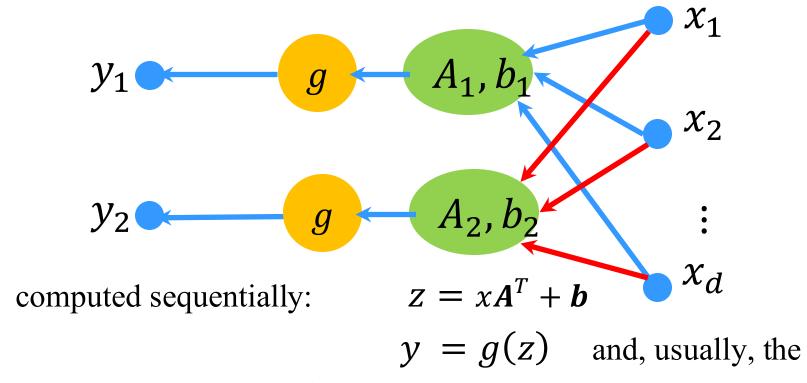
https://news.cornell.edu/stories/2019/09/professors-perceptron-paved-way-ai-60-years-too-soon

MULTI-NODE PERCEPTRON

$$g(z) = \text{relu}(z)$$

 $y_1 = g(xA_1^T + b_1)$
 x_2
 $y_1 = g(xA_1^T + b_1)$
 x_2
 $y_1 = g(xA_1^T + b_1)$
 x_2
 $x_3 = g(xA_1^T + b_2)$
 $y_2 = g(xA_2^T + b_2)$
 $y_2 = g(xA_2^T + b_2)$
 $y_3 = g(xA_2^T + b_2)$
 $y_4 = g(xA_2^T + b_2)$
 $y_5 = g(xA_2^T + b_2)$
 $y_6 = g(xA_2^T + b_2)$
 $y_7 = g(xA_1^T + b_2)$

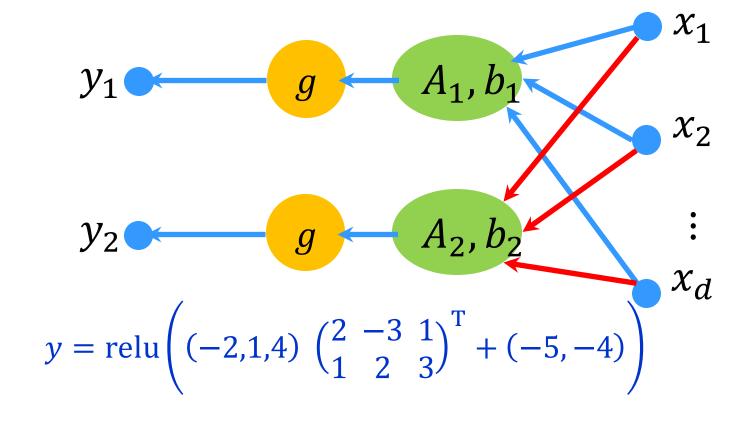
A multi-node perceptron is often drawn as follows,



activation function g(z) is applied *elementwise*, that is, to every element of its matrix input.

Multi-Node Perceptron: Example

$$x = (-2, 1, 4),$$
 $A = \begin{pmatrix} 2 & -3 & 1 \\ 1 & 2 & 3 \end{pmatrix},$ $b = (-5, -4)$



Consider the task of modeling the data triplets

$$D = \{(x_1, x_2, y)_{i=1}^N\}$$
 with a function of the form

 $y = f(x_1, x_2, \omega)$. Let's begin with a 2-input 4-node perceptron

with
$$g(z) = z\sigma(z)$$
,



where,

$$\sigma(z) = \frac{1}{(1+e^{-z})}$$



 χ_1

 χ_2

 $z\sigma(z)$ is called a silu.

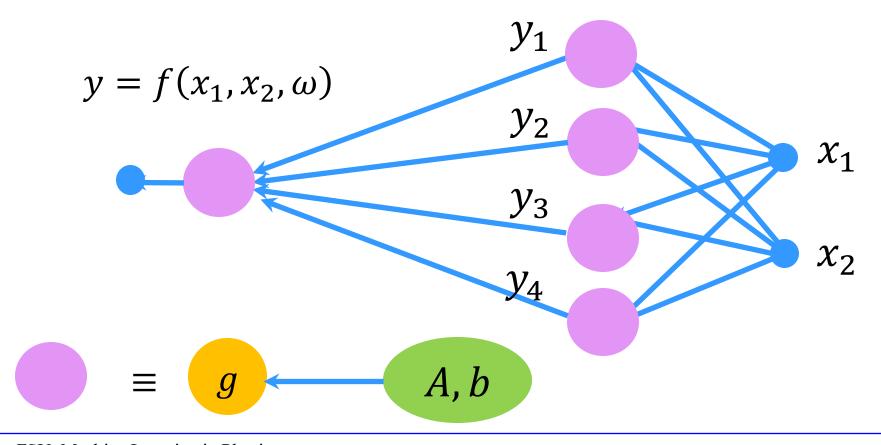
 ω are free parameters.





$$\equiv g$$

Then, let's feed the output of the multi-node perceptron into a 4-input 1-node perceptron:

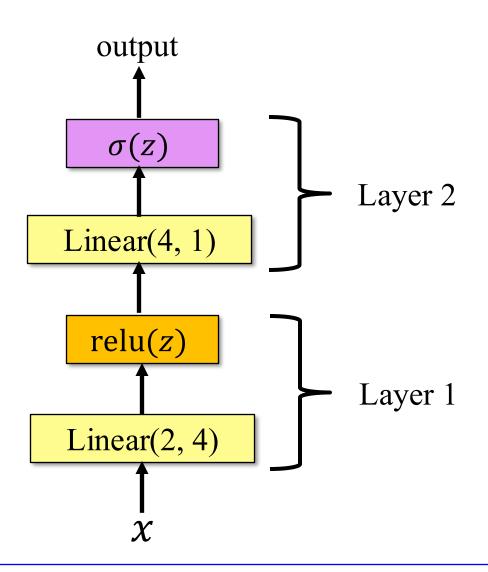


Given the complexity of ML models (i.e., ML functions), it is now common to use a graphical representation of ML models that uses higher-level components.

$$f(z) = zA^T + b$$

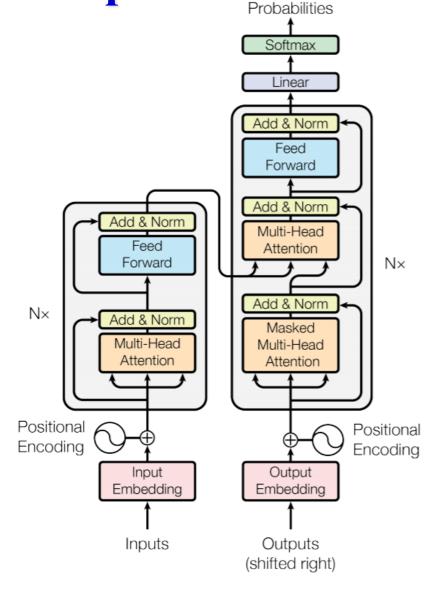
$$relu(z) = \max(0, z)$$

$$\sigma(z) = (1 + e^{-z})^{-1}$$



Here, for example, is a graphical representation of a **transformer**, the model that powers ChatGPT.

In ChatGPT 3, there are 2 x 96 of these "layers"!



Output

LOSS FUNCTION AND EMPIRICAL RISK

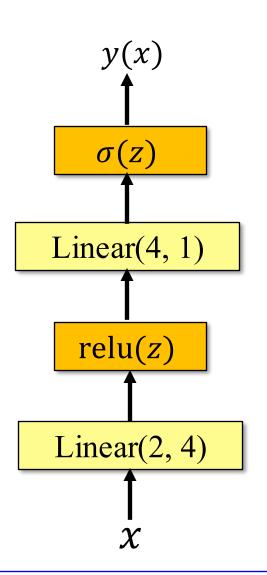
Loss Function

Suppose our goal is to approximate an unknown function

$$y = f(x_1, x_2)$$

given a dataset $D = \{(x_1, x_2, y)_{i=1}^N\},\$

using the *model* on the right.



Loss Function

A well-known approach is to approximate $f(x_1, x_2)$ with a parameterized function $f(x_1, x_2, \omega)$ and find the *best-fit* values ω^* by minimizing

$$R(\omega) = \frac{1}{N} \sum_{i=1}^{N} (y_i - f_i)^2$$

with respect to the parameters ω , where $f_i = f(x_{1i}, x_{2i}, \omega)$.

This is referred to as a least-squared fit.

Loss Function

In machine learning, the least-squares fit is generalized to

$$R(\omega) = \frac{1}{N} \sum_{i=1}^{N} L(y_i, f_i)$$

where the function, $L(y_i, f_i)$, called the **loss function**, measures the discrepancy between the desired **target** y and the model f.

The quantity $R(\omega)$ is called the **empirical risk** and the task of minimizing it is called **empirical risk minimization**.

Warning: In ML, $R(\omega)$ is often referred to as the "loss".

Empirical Risk: Landscape

The empirical risk defines a highly corrugated very high-dimensional "landscape" in the space of parameters.

The goal of an **optimizer** is to navigate the landscape $(R(\omega))$ associated with a *finite* amount of data to find a *good* approximation of the lowest point of the landscape associated with an *infinite* amount of data.

When ML researchers say that a model *generalizes* this is what they mean.

Risk Functional

In mathematics, one can often gain insight by taking some limit of an expression. Let's take the limit of

$$R(\omega) = \frac{1}{N} \sum_{i=1}^{N} L(y_i, f_i)$$

as $N \to \infty$, that is, as the amount of data grows without limit.

In that limit, the empirical risk becomes the risk functional,

$$R[f] = \int dx \int dy L(y, f) p(x, y)$$

where p(x, y)dxdy is the probability distribution of the data.

Summary (1)

General Approaches

> Supervised, unsupervised, generative, and reinforcement learning.

Deep Learning

> Uses functions constructed through deep composition.

> The Perceptron

➤ Basic computational unit: matrix multiplication and addition and (typically) an element-wise nonlinear map.

Summary (2)

- We described the multi-node perceptron and how machine learning models are represented graphically.
- ➤ We illustrated the calculation of the output of a perceptron.
- ➤ We discussed the generalization of least-squared fitting to empirical risk minimization.