

# THE BINARY HEAP

WHILE INSERTING OR REMOVING AN ELEMENT INTO THE HEAP HOW DO WE KNOW WHICH IS THE RIGHT POSITION FOR THE ELEMENT TO OCCUPY?

WE PLACE A SINGLE ELEMENT IN THE **WRONG POSITION**

THEN WE TRY AND FIND THE **RIGHT POSITION** FOR THE ELEMENT

THIS PROCESS IS CALLED:

## HEAPIFY

# THE BINARY HEAP

## HEAPIFY

### SIFT DOWN

AN ELEMENT IS IN THE WRONG POSITION WITH RESPECT TO OTHER ELEMENTS **BELOW** IT IN THE HEAP

IT HAS TO BE MOVED **DOWNWARDS** IN THE HEAP TOWARDS THE LEAF NODES TO FIND IT'S RIGHT POSITION

### SIFT UP

AN ELEMENT IS IN THE WRONG POSITION WITH RESPECT TO OTHER ELEMENTS **ABOVE** IT IN THE HEAP

IT HAS TO BE MOVED **UPWARDS** IN THE HEAP TOWARDS THE ROOT NODE TO FIND IT'S RIGHT POSITION

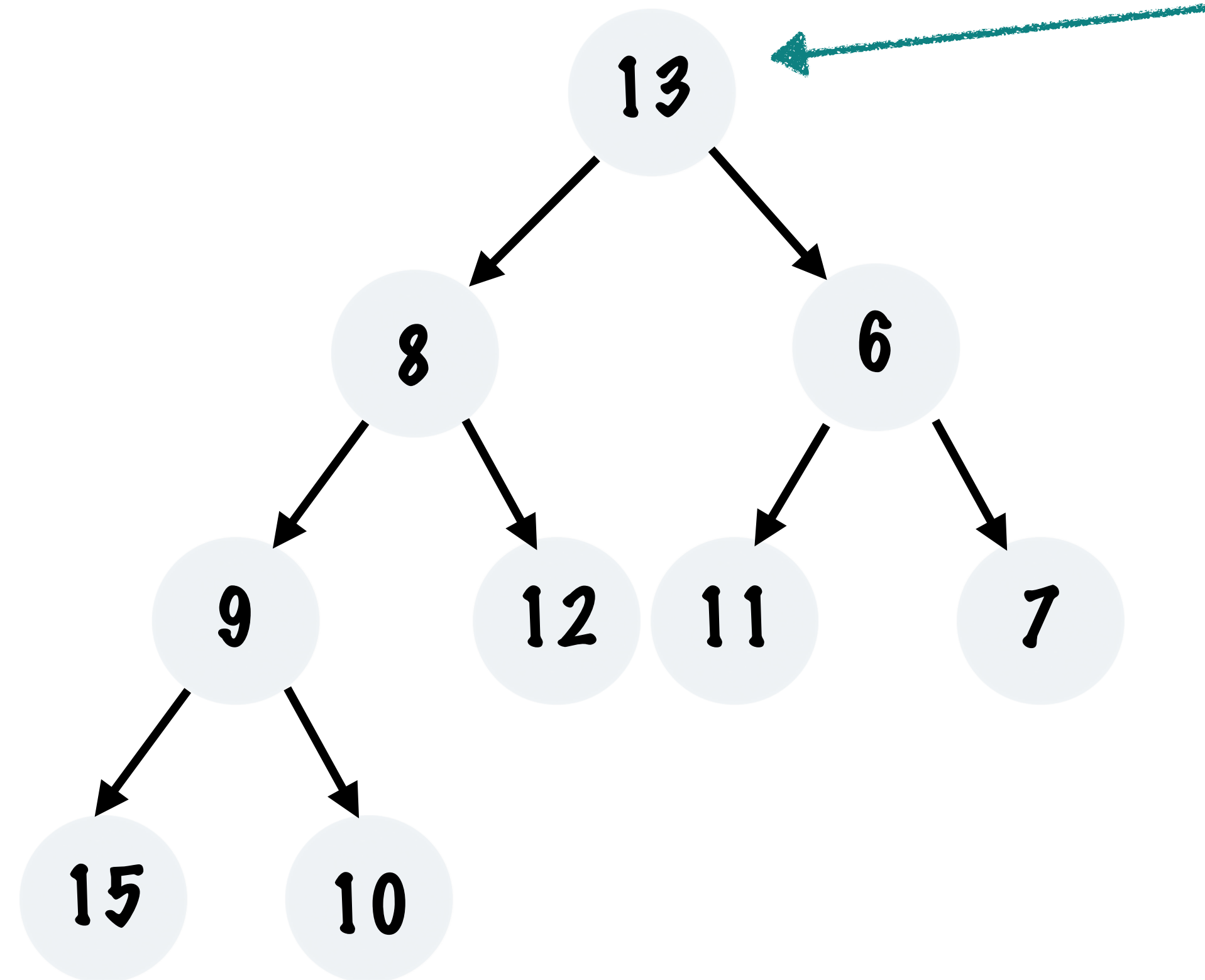
# THE BINARY HEAP

## HEAPIFY

SIFT DOWN

SIFT UP

THIS IS A MINIMUM  
HEAP



THE VALUE 13 IS NOT  
IN THE RIGHT POSITION  
WITH RESPECT TO THE  
NODES BELOW IT

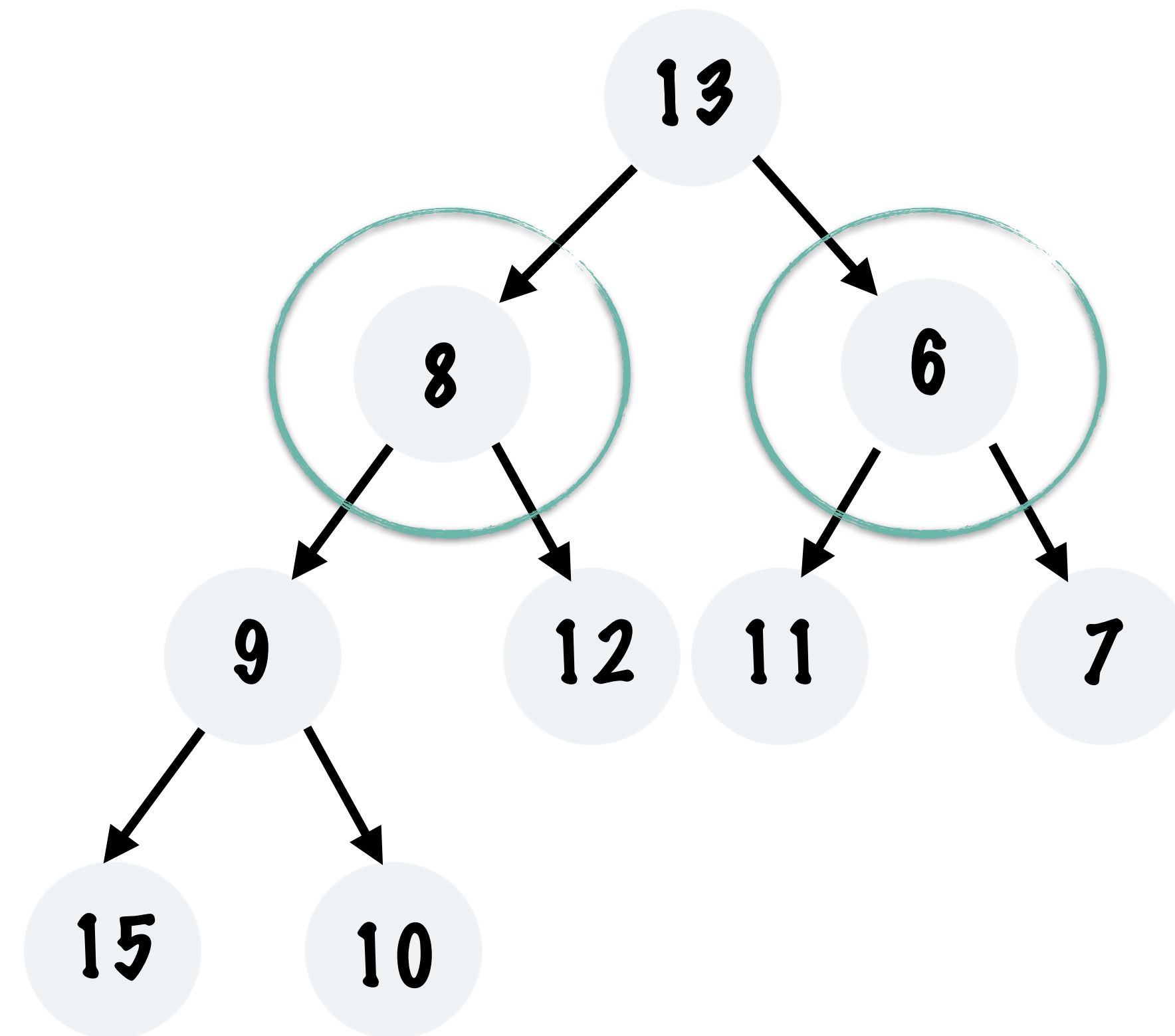
# THE BINARY HEAP

## HEAPIFY

SIFT UP

$6 < 8$  THIS MEANS THAT  
6 IS THE CANDIDATE FOR  
SWAP

SIFT DOWN



SWAP 6 AND 13

6 IS THE MINIMUM  
ELEMENT IN THIS HEAP

# THE BINARY HEAP

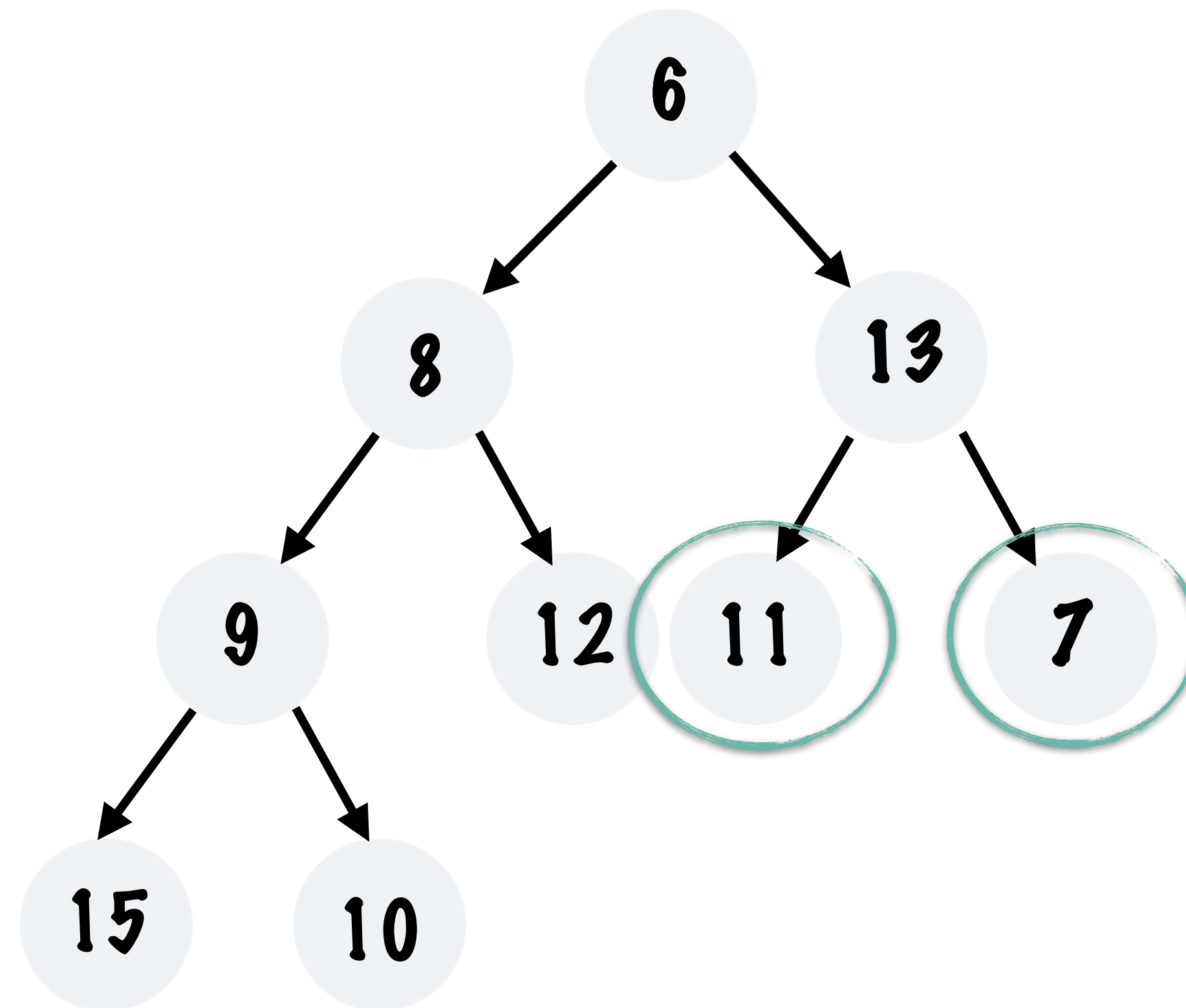
## HEAPIFY

SIFT UP

$7 < 11$  THIS MEANS  
THAT 7 IS THE  
CANDIDATE FOR SWAP

SIFT DOWN

SWAP 7 AND 11

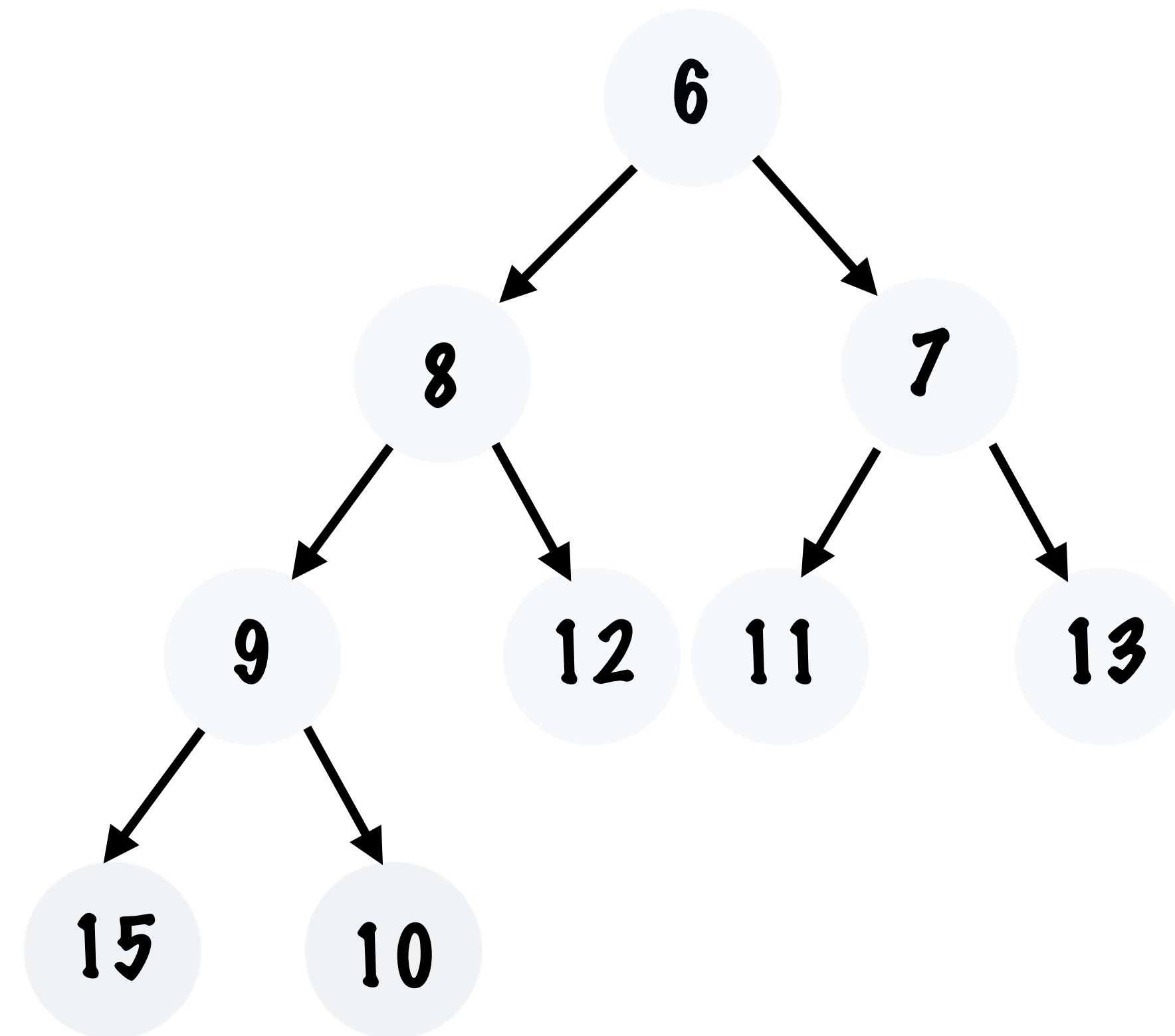


# THE BINARY HEAP

## HEAPIFY

SIFT UP

SIFT DOWN



13 IS NOW IN THE  
CORRECT POSITION -  
HEAPIFY COMPLETE!

# THE BINARY HEAP

## HEAPIFY

NOW LET'S SEE SOME CODE...




# MINIMUM HEAP

```
public class MinHeap<T extends Comparable> extends Heap<T> {
```

```
    public MinHeap(Class<T> clazz) {  
        super(clazz);  
    }
```

```
    public MinHeap(Class<T> clazz, int size) {  
        super(clazz, size);  
    }
```

EXTEND THE HEAP BASE CLASS TO  
CREATE A MINIMUM HEAP



SET UP THE CONSTRUCTORS





# SIFT DOWN

@Override

```
protected void siftDown(int index) {  
    int leftIndex = getLeftChildIndex(index);  
    int rightIndex = getRightChildIndex(index);  
  
    // Find the minimum of the left and right child elements.  
    int smallerIndex = -1;  
    if (leftIndex != -1 && rightIndex != -1) {  
        smallerIndex = getElementAtIndex(leftIndex).compareTo(getElementAtIndex(rightIndex)) < 0  
            ? leftIndex : rightIndex;  
    } else if (leftIndex != -1) {  
        smallerIndex = leftIndex;  
    } else if (rightIndex != -1) {  
        smallerIndex = rightIndex;  
    }  
  
    // If the left and right child do not exist stop sifting down.  
    if (smallerIndex == -1) {  
        return;  
    }  
  
    // Compare the smaller child with the current index to see if a swap  
    // and further sift down is needed.  
    if (getElementAtIndex(smallerIndex).compareTo(getElementAtIndex(index)) < 0) {  
        swap(smallerIndex, index);  
        siftDown(smallerIndex);  
    }  
}
```

THE ELEMENT AT THIS INDEX HAS  
TO BE SIFTED DOWN TO THE RIGHT  
POSITION

GET THE LEFT AND RIGHT CHILD INDICES  
TO COMPARE VALUES

STORE THE INDEX AT  
WHICH WE FIND THE  
MINIMUM VALUE IN  
SMALLER INDEX

IF THE NODE HAS BOTH LEFT AND  
RIGHT CHILDREN FIND THE  
SMALLER VALUE BETWEEN THEM

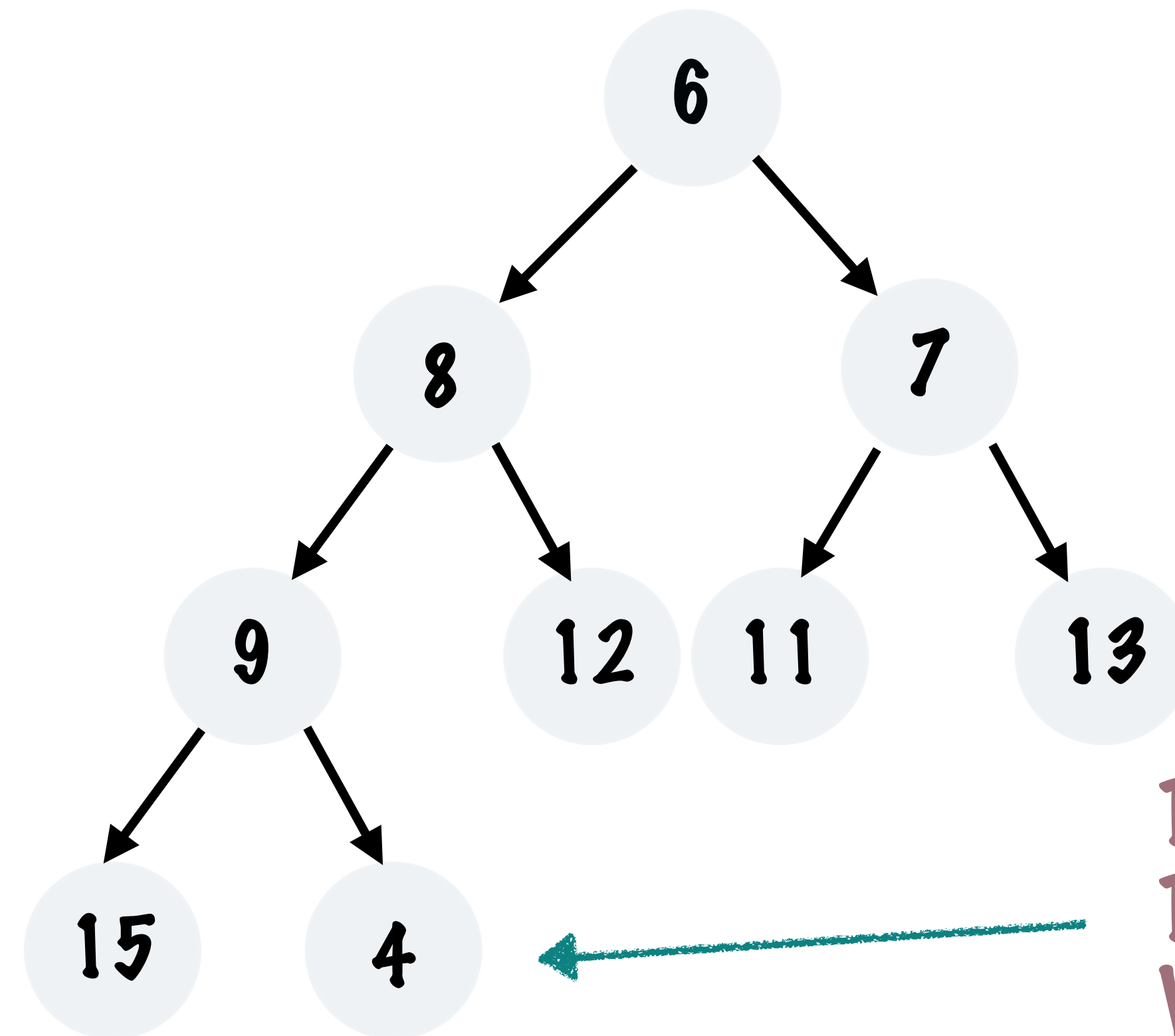
IF THE NODE HAS ONLY A LEFT OR  
ONLY A RIGHT CHILD THAT CHILD  
CAN BE CONSIDERED THE ONE  
WHICH HAS THE SMALLER VALUE

COMPARE THE SMALLER OF THE CHILDREN  
WITH THE PARENT INDEX AND SWAP IF  
NEEDED, SIFT THE PARENT DOWN FURTHER

# THE BINARY HEAP

## HEAPIFY

SIFT DOWN  
SIFT UP



THE VALUE 4 IS NOT IN  
THE RIGHT POSITION  
WITH RESPECT TO THE  
NODES ABOVE IT

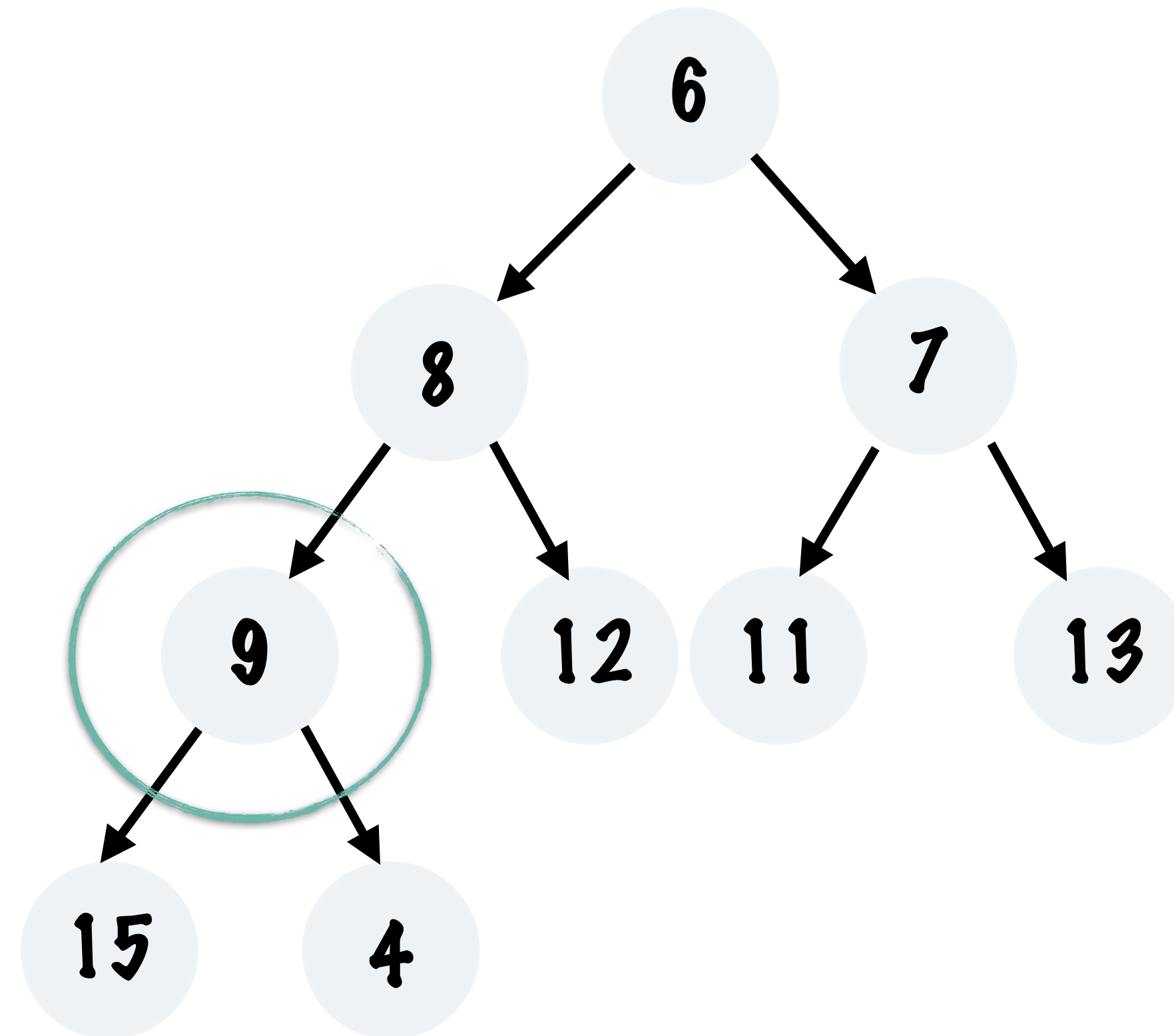
# THE BINARY HEAP

## HEAPIFY

SIFT DOWN

$4 < 9$  THIS MEANS THAT  
4 SHOULD BE SWAPPED  
WITH ITS PARENT

SIFT UP





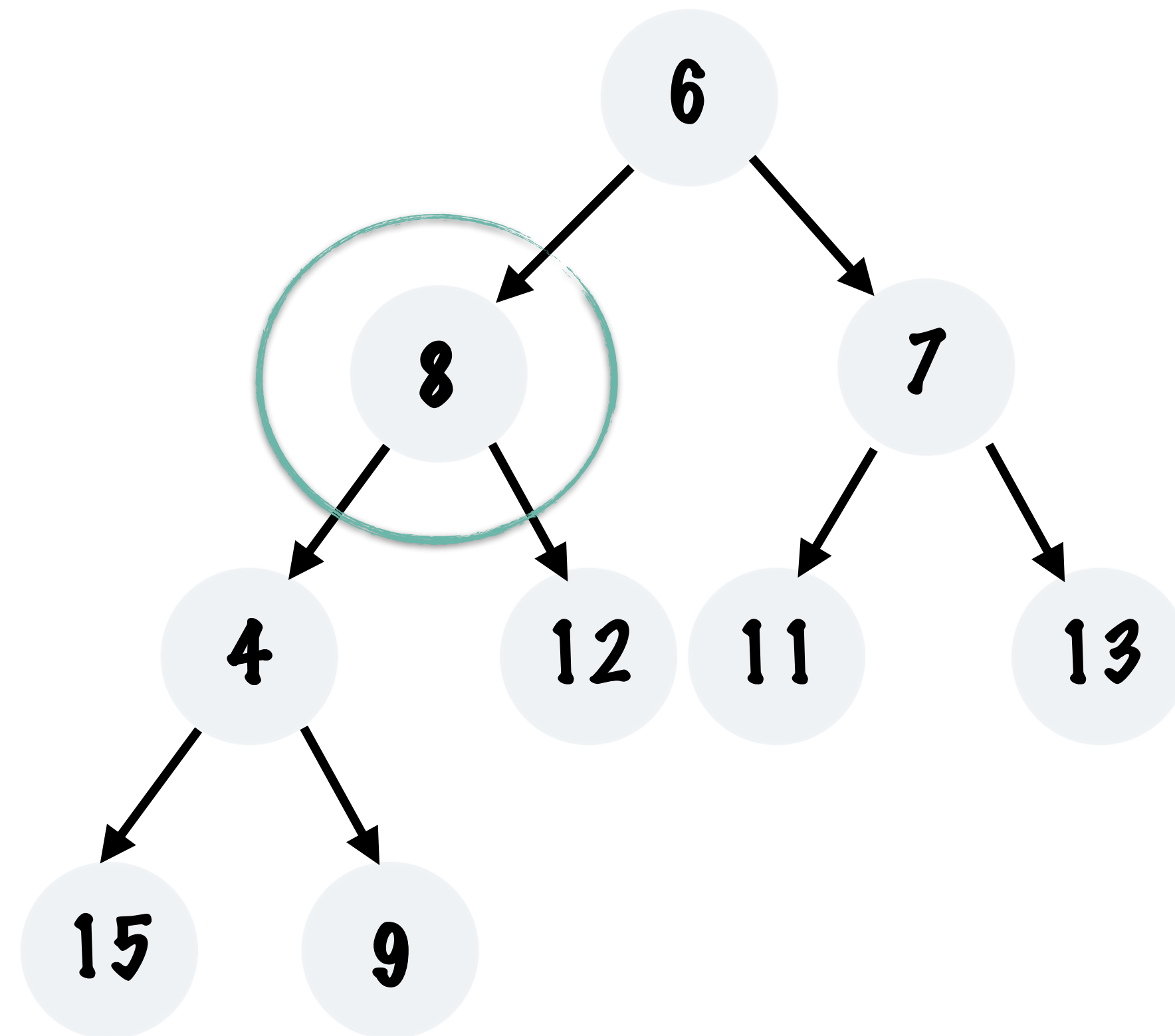
# THE BINARY HEAP

## HEAPIFY

SIFT DOWN

$4 < 8$  THIS MEANS THAT  
4 SHOULD BE SWAPPED  
WITH ITS PARENT

SIFT UP



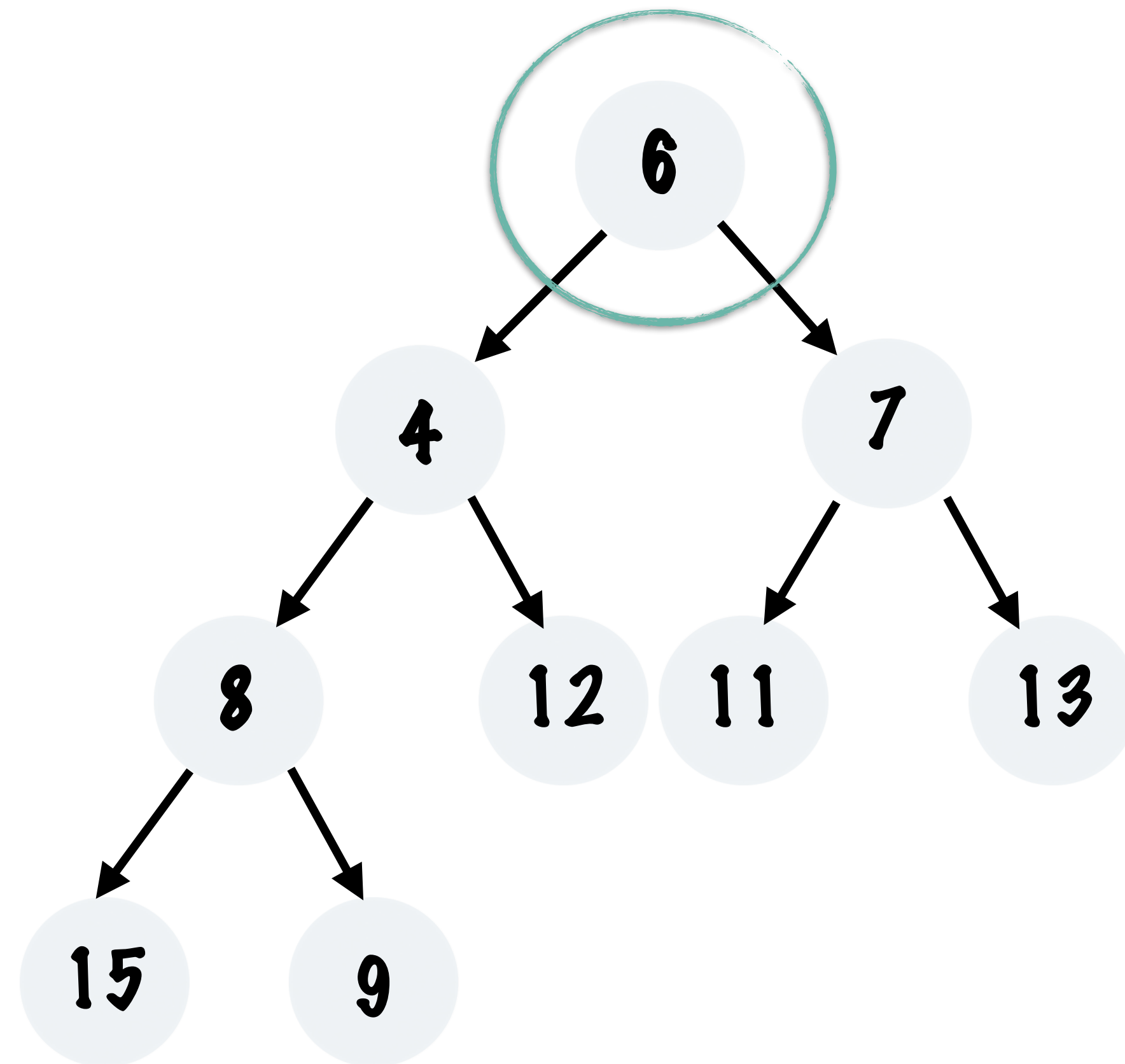
# THE BINARY HEAP

## HEAPIFY

SIFT DOWN

$4 < 6$  THIS MEANS THAT  
4 SHOULD BE SWAPPED  
WITH ITS PARENT

SIFT UP



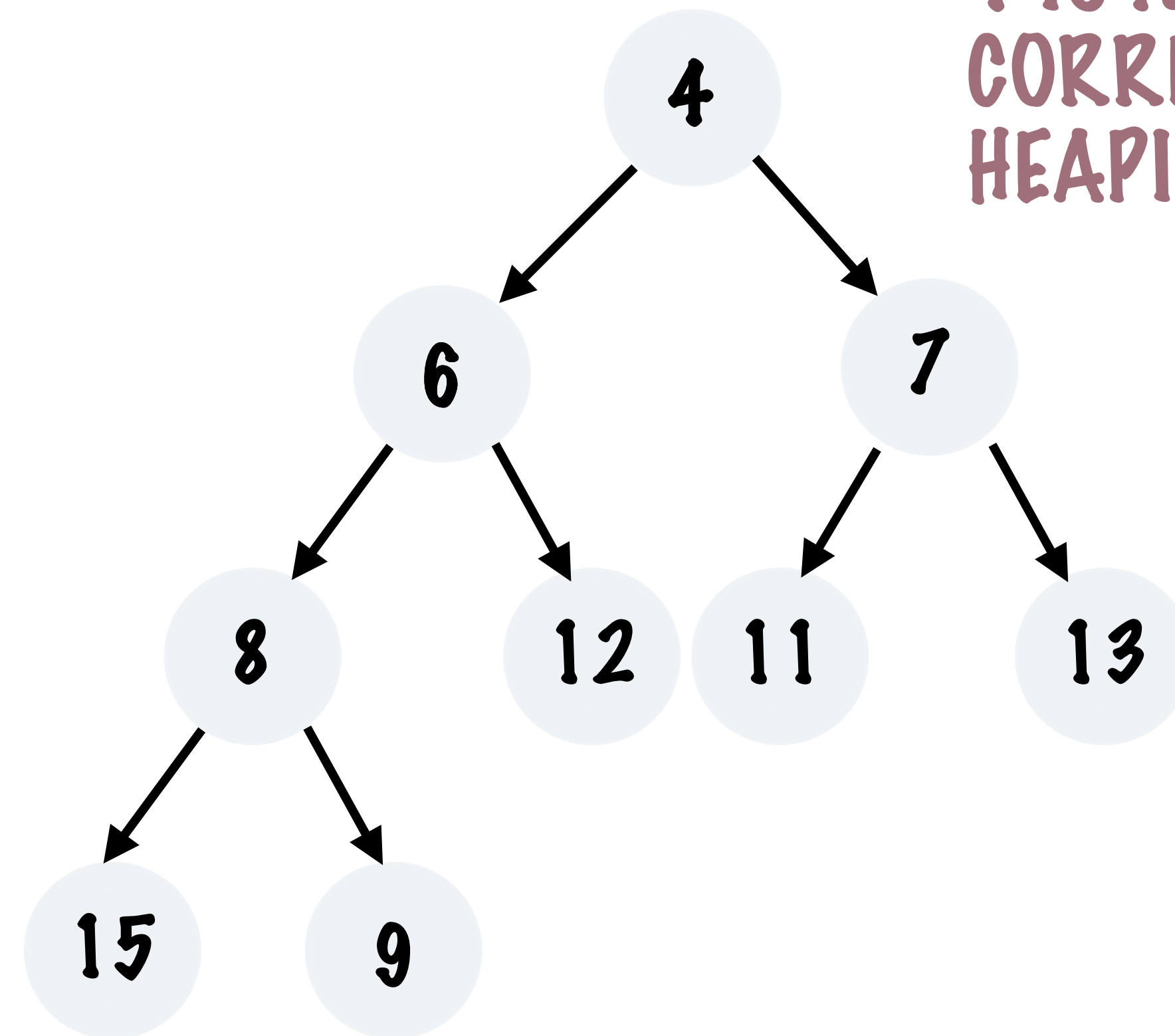
# THE BINARY HEAP

## HEAPIFY

SIFT DOWN

SIFT UP

4 IS NOW IN THE  
CORRECT POSITION -  
HEAPIFY COMPLETE!



# THE BINARY HEAP

## HEAPIFY

NOW LET'S SEE SOME CODE...



# SIFT UP

```
@Override
protected void siftUp(int index) {
    int parentIndex = getParentIndex(index);

    if (parentIndex != -1 &&
        getElementAtIndex(index).compareTo(getElementAtIndex(parentIndex)) < 0) {
        swap(parentIndex, index);
        siftUp(parentIndex);
    }
}
```

THE ELEMENT AT THIS INDEX HAS TO BE SIFTED UP TO THE RIGHT POSITION

FIND THE PARENT ELEMENT OF THE CURRENT NODE AND COMPARE VALUES

IF THE PARENT IS SMALLER THAN THE CURRENT NODE VALUE THEN PERFORM THE SWAP

CONTINUE TO SIFT UP - AS LONG AS ELEMENTS ARE SWAPPED THE RIGHT POSITION FOR THE ORIGINAL ELEMENT HAS NOT BEEN FOUND