

MERGE SORT

THIS FOLLOWS THE DIVIDE
AND CONQUER APPROACH
TO CREATE SMALLER
SUB-PROBLEMS

A LIST IS BROKEN DOWN INTO
SMALLER AND SMALLER
PARTS RECURSIVELY

AT SOME POINT THERE WILL
BE A LIST OF LENGTH ONE

WE CAN CONSIDER THAT A
SORTED LIST

THEN MERGE THE SORTED LISTS
TOGETHER TO GET THE FULLY
SORTED LIST

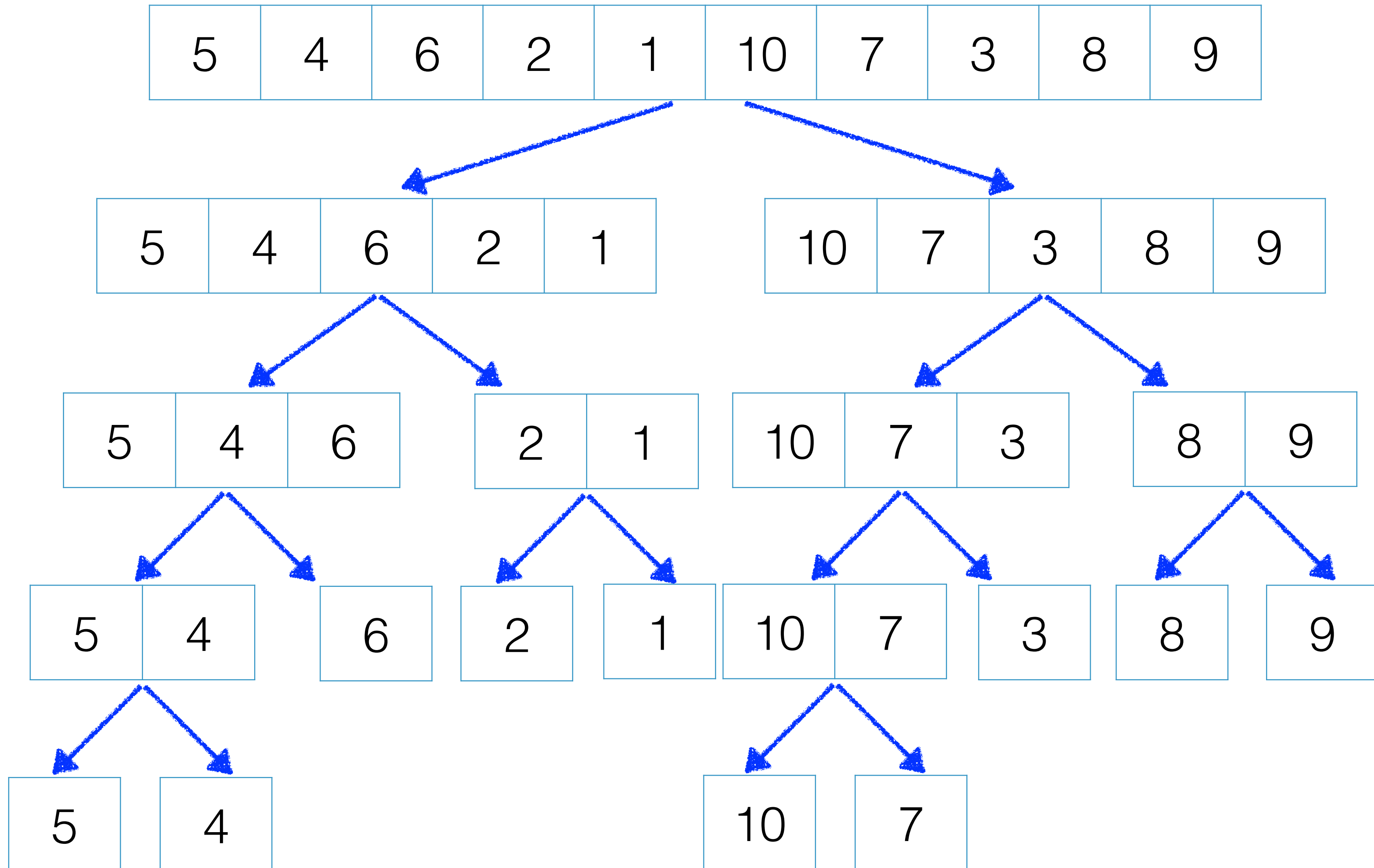
DIVIDE AND CONQUER - THE WEAPON? RECURSION

THIS IS A CLASSIC RECURSION BASED ALGORITHM, DIVIDE TILL THE PROBLEM IS SO SMALL AS TO BE TRIVIAL

SOLVE FOR THE TRIVIAL CASE AND THEN BUILD UP THE COMPLETE SOLUTION AS RECURSION UNWINDS

RECURSION CAN SEEM LIKE MAGIC, SO MAKE SURE YOU UNDERSTAND RECURSION BEFORE TACKLING THIS

MERGE SORT



MERGE SORT

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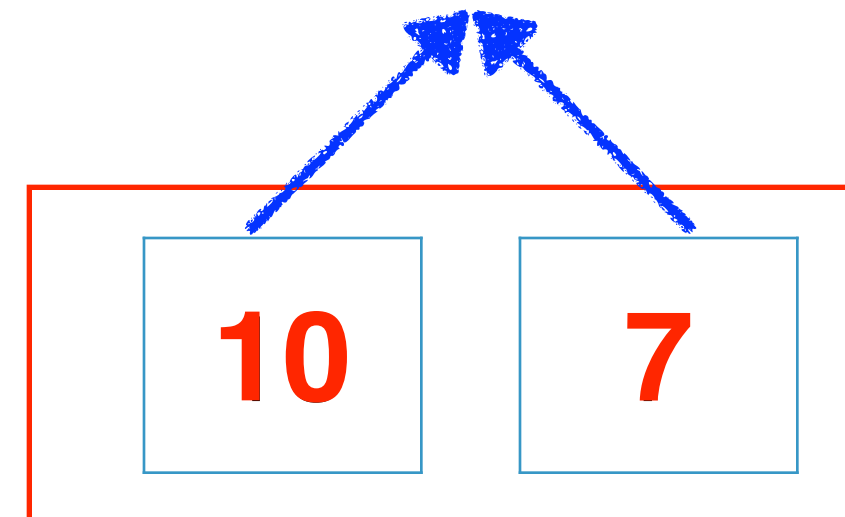
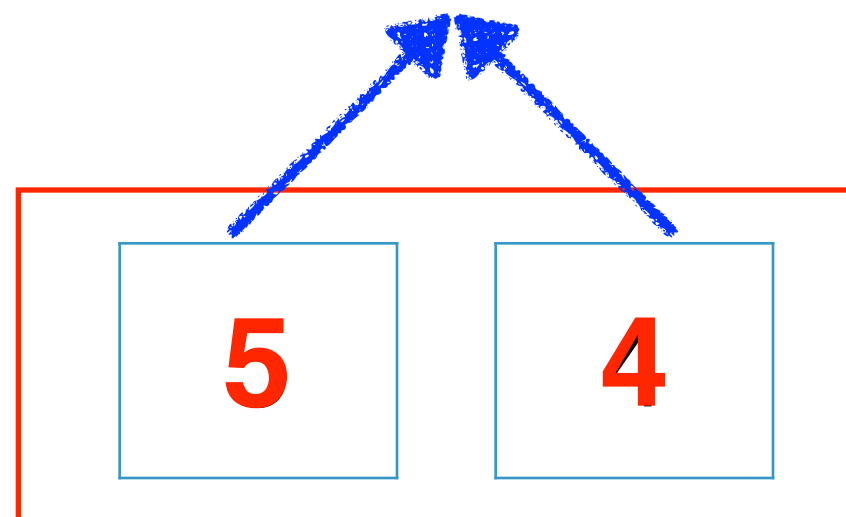
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MERGE SORT

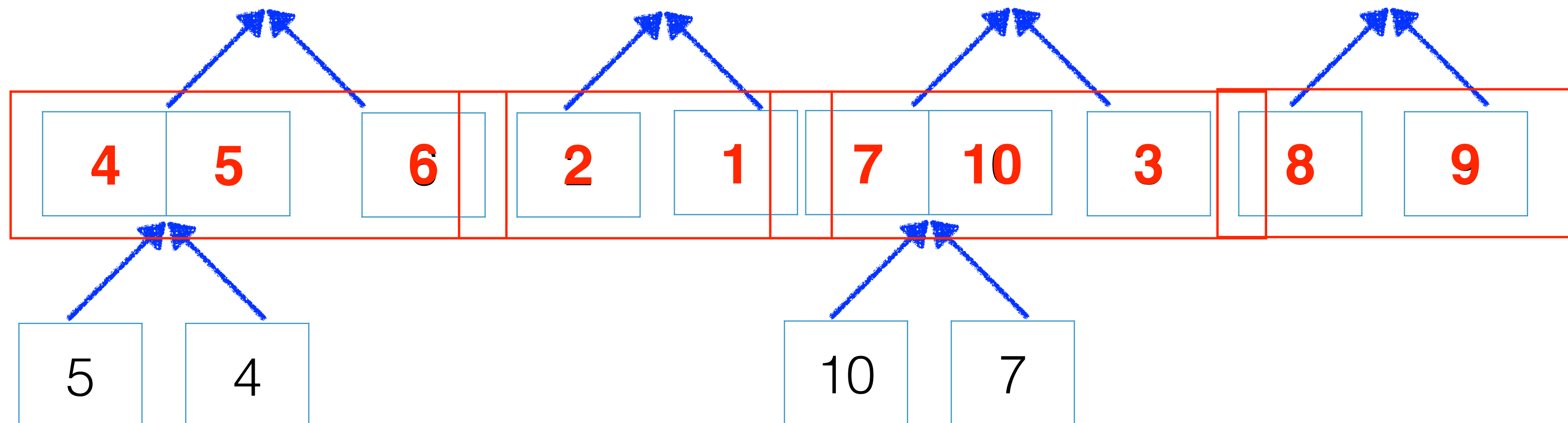
MERGE THE LISTS
KEEPING THE SORTED
ORDER



MERGE SORT

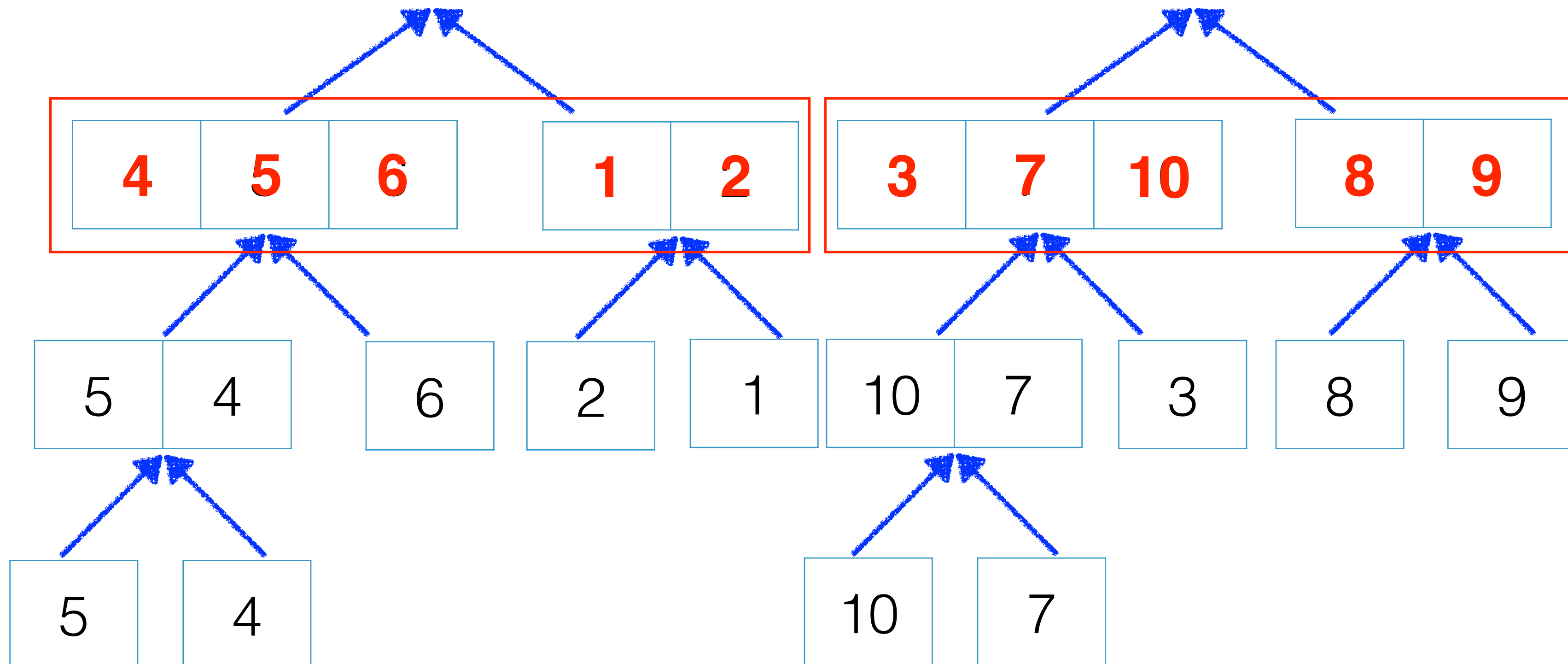
EACH LIST IS SORTED
WHETHER IT IS A
SINGLE ELEMENT LIST
OR LISTS WITH 2
ELEMENTS

MERGE THE LISTS
TOGETHER KEEPING
THE SORTED ORDER



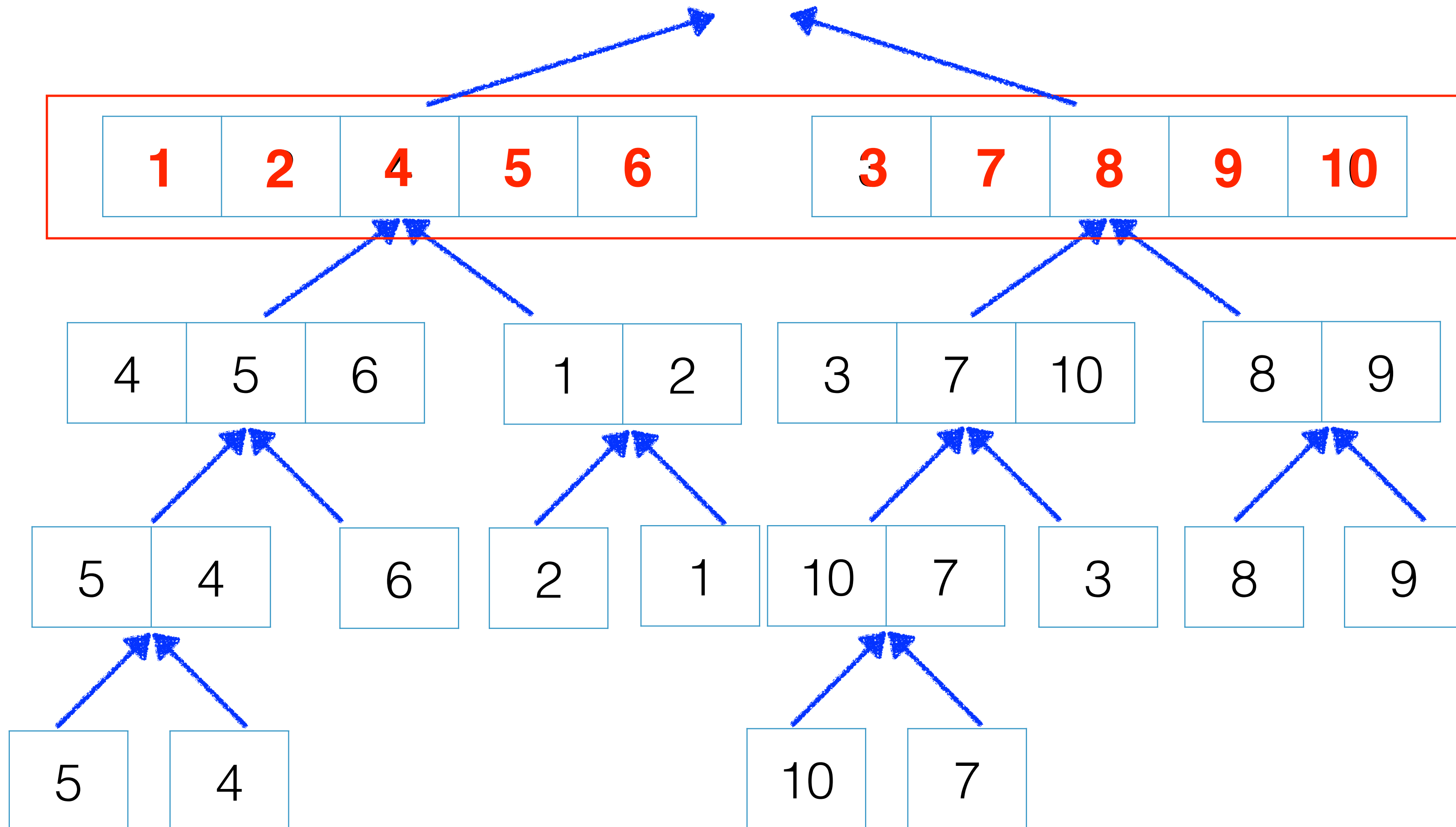
MERGE SORT

OUR LISTS ARE LONGER AND STILL
SORTED, CONTINUE MERGING



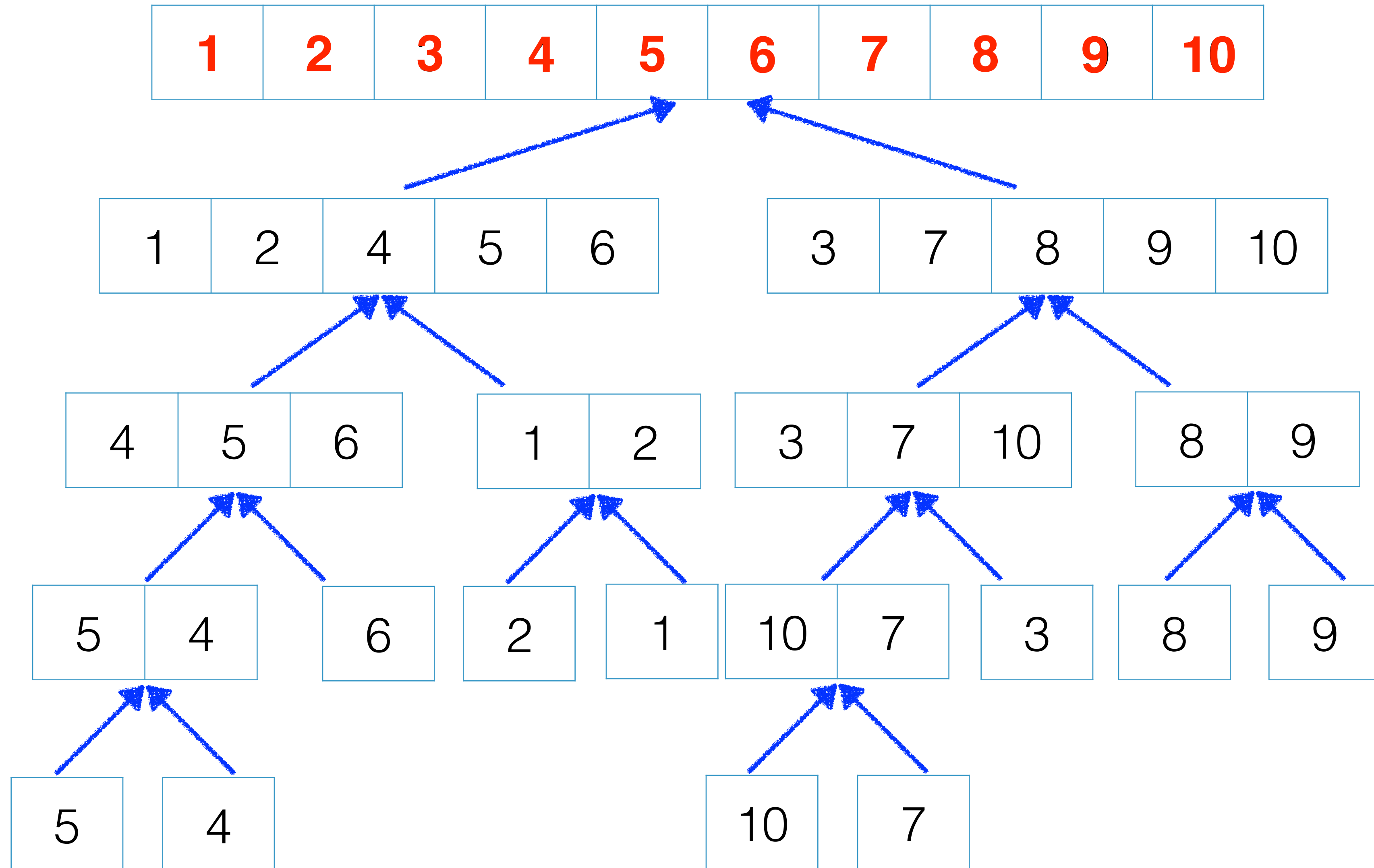
MERGE SORT

ONE FINAL MERGE TO GET THE ORIGINAL LIST IN
SORTED ORDER



MERGE SORT

A SORTED LIST!



NOW FOR SOME CODE...

MERGE SORT USES A NUMBER
OF HELPER METHODS

WE'LL SEE 2 FUNCTIONS IMPLEMENTED:

- 1: THE "SPLIT" METHOD TO SPLIT THE LIST INTO 2 SUB-LISTS
- 2: THE "MERGE" METHOD TO MERGE 2 SORTED LISTS
INTO ONE SORTED LIST
- 3: THE "MERGESORT" METHOD WHICH DOES THE FINAL
RECURSIVE SORT

THE "SPLIT"

THE TWO LISTS FOR THE FIRST AND SECOND HALVES HAVE BEEN SETUP AND SPLIT SIMPLY COPIES THE ELEMENTS FROM THE FIRST LIST OVER

```
public static void split(int[] listToSort, int[] listFirstHalf, int[] listSecondHalf) {  
    int index = 0;  
    int secondHalfStartIndex = listFirstHalf.length;  
    for (int elements : listToSort) {  
        if (index < secondHalfStartIndex) {  
            listFirstHalf[index] = listToSort[index];  
        } else {  
            listSecondHalf[index - secondHalfStartIndex] = listToSort[index];  
        }  
        index++;  
    }  
}
```

THE FIRST HALF HOLDS EVERYTHING UP TO THE MID-POINT

THE SECOND HALF HOLDS THE REMAINDER OF THE ELEMENTS

THE "MERGE"

SET UP INDICES INTO THE FINAL
MERGED LIST AND THE TWO HALVES
WHICH ARE TO BE MERGED TOGETHER

```
public static void merge(int[] listToSort, int[] listFirstHalf, int[] listSecondHalf) {  
    int mergeIndex = 0;  
    int firstHalfIndex = 0;  
    int secondHalfIndex = 0;  
  
    while (firstHalfIndex < listFirstHalf.length && secondHalfIndex < listSecondHalf.length) {  
        if (listFirstHalf[firstHalfIndex] < listSecondHalf[secondHalfIndex]) {  
            listToSort[mergeIndex] = listFirstHalf[firstHalfIndex];  
            firstHalfIndex++;  
        } else if (secondHalfIndex < listSecondHalf.length) {  
            listToSort[mergeIndex] = listSecondHalf[secondHalfIndex];  
            secondHalfIndex++;  
        }  
        mergeIndex++;  
    }  
  
    if (firstHalfIndex < listFirstHalf.length) {  
        while (mergeIndex < listToSort.length) {  
            listToSort[mergeIndex++] = listFirstHalf[firstHalfIndex++];  
        }  
    }  
    if (secondHalfIndex < listSecondHalf.length) {  
        while (mergeIndex < listToSort.length) {  
            listToSort[mergeIndex++] = listSecondHalf[secondHalfIndex++];  
        }  
    }  
}
```

COPY OVER THE REMAINING
ELEMENTS LEFT IN EITHER
ONE OF THE LISTS

COMPARE THE ELEMENT AT THE
CURRENT INDEX OF EACH OF THE
LISTS AND CHOOSE THE SMALLER
ONE TO GO INTO THE FINAL LIST

FINALLY "MERGESORT"

A LIST OF LENGTH 1 IS A
SORTED LIST! THIS IS THE
BASE CASE OF RECURSION

```
public static void mergeSort(int[] listToSort) {  
    if (listToSort.length == 1) {  
        return;  
    }  
  
    int midIndex = listToSort.length / 2 + listToSort.length % 2;  
    int[] listFirstHalf = new int[midIndex];  
    int[] listSecondHalf = new int[listToSort.length - midIndex];  
    split(listToSort, listFirstHalf, listSecondHalf);  
  
    mergeSort(listFirstHalf);  
    mergeSort(listSecondHalf);  
  
    merge(listToSort, listFirstHalf, listSecondHalf);  
    print(listToSort);  
}
```

GET THE MID-POINT
AT WHICH TO SPLIT
THE LIST

MERGE THE SORTED LIST
TO GET THE ORIGINAL
LIST IN SORTED ORDER

RECURSIVE CALL, MERGE
SORT THE TWO SMALLER
SUB-LISTS CREATED

**MERGE SORT USES DIVIDE AND CONQUER
TO CREATE SMALLER PROBLEMS WHICH
ARE EASIER TO TACKLE**

**TO CALCULATE THE COMPLEXITY WE NEED
TO CONSIDER THE RECURSIVE STEP WHERE
THE PROBLEM IS DIVIDED INTO 2 AND THE
MERGE OF TWO LISTS OF $N/2$ LENGTH**

**THE EXACT DERIVATION IS NOT
REALLY RELEVANT TO
PROGRAMMING INTERVIEWS**

**THE COMPLEXITY OF MERGE
SORT IS $O(N \log N)$**

MERGE SORT IS NOT
ADAPTIVE

IT TAKES $O(N)$ EXTRA SPACE
WHEN WE USE ARRAYS (ALL THE
SMALLER LISTS WE CREATE IN
THE DIVIDE PHASE)

IT IS A STABLE SORT