

# HEAP SORT

## HEAPIFY

NOW LET'S SEE SOME CODE...

# GET LEFT CHILD INDEX

```
private static int getLeftChildIndex(int index, int endIndex) {  
    int leftChildIndex = 2 * index + 1;  
    if (leftChildIndex > endIndex) {  
        return -1;  
    }  
  
    return leftChildIndex;  
}
```

CALCULATE THE LEFT CHILD INDEX  
USING THE FORMULA

CHECK TO SEE IF A LEFT CHILD OF  
THIS NODE IS PRESENT. IF IT'S  
LESS THAN COUNT (THE NUMBER  
OF NODES) THEN IT'S A VALID LEFT  
CHILD

RETURN -1 IF A VALID LEFT CHILD  
WAS NOT FOUND

# GET RIGHT CHILD INDEX

```
private static int getRightChildIndex(int index, int endIndex) {  
    int rightChildIndex = 2 * index + 2;  
    if (rightChildIndex > endIndex) {  
        return -1;  
    }  
    return rightChildIndex;  
}
```

CALCULATE THE RIGHT CHILD INDEX USING THE FORMULA

CHECK TO SEE IF A RIGHT CHILD OF THIS NODE IS PRESENT. IF IT'S LESS THAN COUNT (THE NUMBER OF NODES) THEN IT'S A VALID RIGHT CHILD

RETURN -1 IF A VALID RIGHT CHILD WAS NOT FOUND

# GET PARENT INDEX

```
private static int getParentIndex(int index, int endIndex) {  
    if (index < 0 || index > endIndex) {  
        return -1;  
    }  
  
    return (index - 1) / 2;  
}
```

CHECK THAT THE INDEX IS NOT OUT OF RANGE



USE THE FORMULA TO GET THE PARENT INDEX



# SWAP

```
private static void swap(int index1, int index2) {  
    int tempValue = array[index1];  
    array[index1] = array[index2];  
    array[index2] = tempValue;  
}
```

HOLD THE VALUE OF INDEX1 IN A  
TEMPORARY VARIABLE



SWAP THE VALUES AT THE TWO  
SPECIFIED INDICES





# PERCOLATE DOWN

```
private static void percolateDown(int index, int endIndex) {  
    int leftChildIndex = getLeftChildIndex(index, endIndex);  
    int rightChildIndex = getRightChildIndex(index, endIndex);  
  
    if (leftChildIndex != -1 && array[leftChildIndex] > array[index]) {  
        swap(leftChildIndex, index);  
        percolateDown(leftChildIndex, endIndex);  
    }  
    if (rightChildIndex != -1 && array[rightChildIndex] > array[index]) {  
        swap(rightChildIndex, index);  
        percolateDown(rightChildIndex, endIndex);  
    }  
}
```

GET THE LEFT AND RIGHT  
CHILD INDICES

FOR LEFT CHILD AND RIGHT  
CHILD IN RANGE CHECK IF  
THE MAX HEAP PROPERTY  
IS SATISFIED

NOTE THAT THE CURRENT INDEX  
SHOULD HOLD THE MAX OF THE  
LEFT AND RIGHT CHILD - BOTH  
COMPARISONS NEED TO BE DONE

IF NOT SWAP ELEMENTS AND  
PERCOLATE DOWN FURTHER TO  
ENSURE ALL CHILD NODES  
SATISFY THE MAX HEAP  
PROPERTY

# HEAPIFY

HEAPIFY THE ENTIRE ARRAY

```
public static void heapify(int endIndex) {  
    int index = getParentIndex(endIndex, endIndex);  
    while (index >= 0) {  
        percolateDown(index, endIndex);  
        index--;  
    }  
}
```

START WITH THE PARENT INDEX  
OF THE LAST ELEMENT IN THE  
ARRAY

PERCOLATE THE ELEMENTS DOWN  
THE HEAP TO THE RIGHT LOCATIONS

# HEAP SORT

## SORT



# HEAP SORT

## SORT

THIS IS A MAXIMUM  
HEAP CONSTRUCTED IN-  
PLACE USING HEAPIFY

0	1	2	3	4	5	6	7	8	9	10
56	17	12	5	14	9	4	2	1	10	6




MOVE THE LARGEST  
ELEMENT TO THE CORRECT  
POSITION IN THE SORTED  
ARRAY

# HEAP SORT

## SORT

LEAVE THE LAST ELEMENT  
OUT OF THE HEAP - IT'S  
PART OF THE SORTED  
ARRAY AND NO LONGER  
PART OF THE HEAP

0	1	2	3	4	5	6	7	8	9	10
6	17	12	5	14	9	4	2	1	10	56



NOW THE ELEMENT 6 AT  
INDEX 0 DOES NOT SATISFY  
THE HEAP PROPERTY

PERCOLATE DOWN THE  
ELEMENT TO IT'S CORRECT  
POSITION

# HEAP SORT

## SORT

0	1	2	3	4	5	6	7	8	9	10
17	6	12	5	14	9	4	2	1	10	56



NOW THE ELEMENT 6 AT  
INDEX 1 DOES NOT SATISFY  
THE HEAP PROPERTY

PERCOLATE DOWN THE  
ELEMENT TO IT'S CORRECT  
POSITION

# HEAP SORT

## SORT

0	1	2	3	4	5	6	7	8	9	10
17	14	12	5	6	9	4	2	1	10	56



NOW THE ELEMENT 6 AT  
INDEX 4 DOES NOT SATISFY  
THE HEAP PROPERTY

# HEAP SORT

## SORT

0	1	2	3	4	5	6	7	8	9	10
17	14	12	5	10	9	4	2	1	6	56

WE'VE NOW GOT A VALID  
HEAP ONCE AGAIN!



# HEAP SORT

## SORT

THE LARGEST ELEMENT IS  
ONCE AGAIN AT THE VERY  
FIRST POSITION AT INDEX 0

0	1	2	3	4	5	6	7	8	9	10
17	14	12	5	10	9	4	2	1	6	56



MOVE THE LARGEST  
ELEMENT TO ITS CORRECT  
LOCATION IN THE SORTED  
ARRAY

REMEMBER THE ELEMENT  
56 AT INDEX 10 IS  
ALREADY SORTED

# HEAP SORT

## SORT

0	1	2	3	4	5	6	7	8	9	10
6	14	12	5	10	9	4	2	1	17	56

ONCE AGAIN HEAPIFY ELEMENT  
6 AT INDEX 0

THE LAST 2 ELEMENTS ARE IN  
THE CORRECT SORTED POSITION,  
THEY ARE NO LONGER PART OF  
THE HEAP

REMOVING FROM THE HEAP AND  
MOVING TO THE END OF THE ARRAY  
CONTINUES TILL THE ENTIRE  
ARRAY IS SORTED!

# HEAP SORT

## SORT

0	1	2	3	4	5	6	7	8	9	10
1	2	4	5	6	9	10	12	14	17	56

**A SORTED ARRAY!**

# HEAP SORT

## SORT

NOW LET'S SEE SOME CODE...

# HEAPSORT

```
public static void heapsort() {  
    heapify(array.length - 1);  
  
    int endIndex = array.length - 1;  
    while (endIndex > 0) {  
        swap(0, endIndex);  
        endIndex--;  
        percolateDown(0, endIndex);  
    }  
}
```

HEAPIFY THE ENTIRE  
UNSORTED ARRAY SO IT'S  
NOW A HEAP

START WITH THE VERY  
LAST INDEX, AND PLACE  
THE LARGEST ELEMENT IN  
THE LAST POSITION

REDUCE THE END INDEX  
INDICATING THAT THE HEAP  
NO LONGER INCLUDES THE  
ELEMENTS WHICH ARE IN THE  
CORRECTLY SORTED POSITION



# HEAP SORT

## SORT

HEAP SORT USES OPERATIONS ON A HEAP TO GET A SORTED LIST

INSERTION INTO A HEAP IS DONE N TIMES TO GET ALL THE ELEMENTS IN HEAP FORM

REMOVAL OF THE MAXIMUM ELEMENT IS DONE N TIMES, FOLLOWED BY HEAPIFY

INSERTION AND REMOVAL HAVE  $\log N$  TIME COMPLEXITY SO DOING IT FOR N ELEMENTS MEANS:

THE AVERAGE CASE COMPLEXITY OF HEAP SORT IS  $O(N \log N)$ .

# HEAP SORT

## SORT

HEAP SORT IS NOT ADAPTIVE

IT'S NOT A STABLE SORT

IT DOES NOT NEED ADDITIONAL SPACE  
- SPACE COMPLEXITY IS  $O(1)$