

HEAP SORT

HEAP SORT

USES A HEAP TO HELP SORT
ELEMENTS IN ASCENDING OR
DESCENDING ORDER

FIRST CONVERTS THE UNSORTED
LIST OR ARRAY INTO A HEAP - THIS
CAN BE DONE IN PLACE

USE THE HEAP TO ACCESS THE
MAXIMUM ELEMENT AND PUT IT
IN THE RIGHT POSITION IN THE
ARRAY

HEAP SORT

HEAPIFY

FIRST CONVERTS THE UNSORTED LIST OR ARRAY INTO A HEAP - THIS CAN BE DONE IN PLACE

TAKE A PORTION OF THE ARRAY - MAKE ALL ELEMENTS IN THAT PORTION SATISFY THE HEAP PROPERTY

KEEP ADDING ADDITIONAL ELEMENTS INTO THE HEAP PORTION ENSURING THAT THESE ADDITIONAL ELEMENTS ALSO SATISFY THE HEAP PROPERTY

THE HEAP WILL GROW TO ENCOMPASS ALL ELEMENTS IN THE ARRAY

SORT

USE THE HEAP TO ACCESS THE MAXIMUM ELEMENT AND PUT IT IN THE RIGHT POSITION IN THE ARRAY

A HEAP OFFERS $O(1)$ ACCESS TO THE LARGEST OR THE SMALLEST ELEMENT

REMOVE THE LARGEST ELEMENT FROM THE HEAP AND POSITION IT AT THE END OF THE SORTED ARRAY

THE SORTED ARRAY WILL GROW TO ENCOMPASS ALL ELEMENTS IN THE ARRAY

HEAP SORT

HEAPIFY

WE'LL USE A **MAXIMUM HEAP**
SO WE CAN ALWAYS ACCESS THE
LARGEST ELEMENT IN $O(1)$ TIME

A HEAP CAN BE REPRESENTED
USING AN ARRAY

HEAPIFY IS THE OPERATION TO CONVERT THE
UNSORTED ARRAY TO A HEAP

WE USE THE SAME ARRAY WITH NO
ADDITIONAL SPACE TO DO THE HEAPIFY

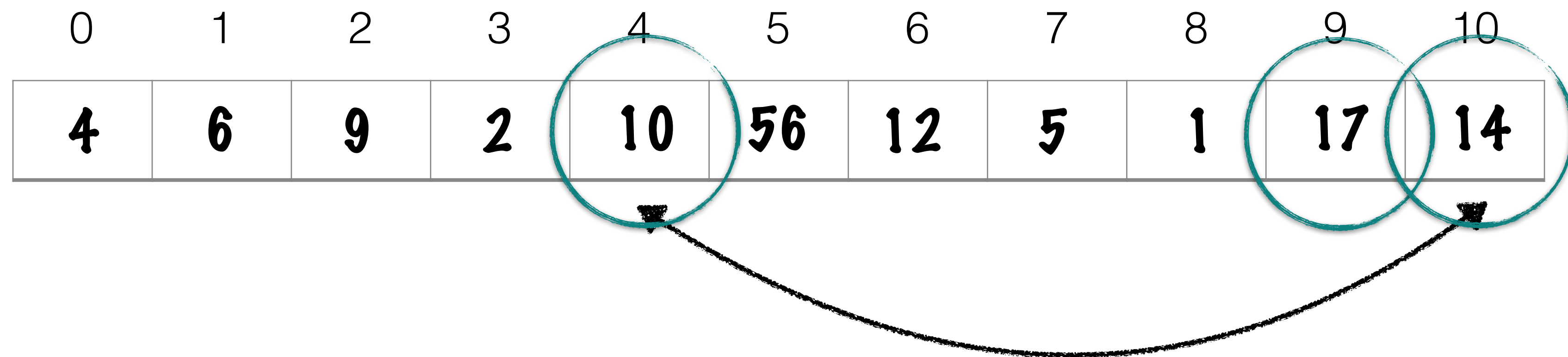
HEAP SORT

HEAPIFY

HEAP SORT

HEAPIFY

START WITH THE PARENT OF THE
LAST ELEMENT IN THIS
UNSORTED ARRAY



NODE AT INDEX: i

HAS PARENT AT INDEX: $(i - 1) / 2$

ENSURE THAT ELEMENT AT
INDEX 4 AND ALL CHILDREN
BELOW IT SATISFY THE HEAP
PROPERTY

HEAP SORT

HEAPIFY

MOVE TO THE PREVIOUS PARENT
AT INDEX 3

THERE ARE NO FURTHER
CHILDREN TO CONSIDER

0	1	2	3	4	5	6	7	8	9	10
4	6	9	2	17	56	12	5	1	10	14

ENSURE THAT ELEMENT AT
INDEX 3 AND ALL CHILDREN
BELOW IT SATISFY THE HEAP
PROPERTY

HEAP SORT

HEAPIFY

MOVE TO THE PREVIOUS PARENT
AT INDEX 2

THERE ARE NO FURTHER
CHILDREN TO CONSIDER

0	1	2	3	4	5	6	7	8	9	10
4	6	9	5	17	56	12	2	1	10	14

ENSURE THAT ELEMENT AT
INDEX 2 AND ALL CHILDREN
BELOW IT SATISFY THE HEAP
PROPERTY

HEAP SORT

HEAPIFY

MOVE TO THE PREVIOUS PARENT
AT INDEX 1

THERE ARE NO FURTHER
CHILDREN TO CONSIDER

0	1	2	3	4	5	6	7	8	9	10
4	6	5	6	17	9	12	2	1	10	14

ENSURE THAT ELEMENT AT
INDEX 1 AND ALL CHILDREN
BELOW IT SATISFY THE HEAP
PROPERTY

HEAP SORT

HEAPIFY

CONSIDER THE CHILDREN OF
ELEMENTS AT INDEX 3 AND 4 AS
WELL, STARTING WITH 3

0	1	2	3	4	5	6	7	8	9	10
4	17	56	5	6	9	12	2	1	10	14

THE NODE REPRESENTED BY
INDEX 3 SATISFIES THE HEAP
PROPERTY

HEAP SORT

HEAPIFY

NOW FOR THE NODE AT INDEX 4

0	1	2	3	4	5	6	7	8	9	10
4	17	56	5	6	9	12	2	1	10	14

THIS NEEDS TO BE HEAPIFIED
FURTHER - THE MAX HEAP
PROPERTY IS NOT SATISFIED

HEAP SORT

HEAPIFY

MOVE TO THE PREVIOUS PARENT
AT INDEX 0

0	1	2	3	4	5	6	7	8	9	10
4	17	56	5	14	9	12	2	1	10	6

ENSURE THAT ELEMENT AT
INDEX 0 AND ALL CHILDREN
BELOW IT SATISFY THE HEAP
PROPERTY

HEAP SORT

HEAPIFY

CONTINUE CHECKING THE NODES
AT INDEX 1 AND 2 STARTING
WITH 1

0	1	2	3	4	5	6	7	8	9	10
56	17	4	5	14	9	12	2	1	10	6

THE ELEMENT AT INDEX 1
SATISFIES THE MAX HEAP
PROPERTY

HEAP SORT

HEAPIFY

CHECK INDEX 2

0	1	2	3	4	5	6	7	8	9	10
56	17	4	5	14	9	12	2	1	10	6

THIS DOES NOT SATISFY
THE MAX HEAP PROPERTY
AND HAS TO BE HEAPIFIED
FURTHER

HEAP SORT

HEAPIFY

0	1	2	3	4	5	6	7	8	9	10
56	17	12	5	14	9	4	2	1	10	6

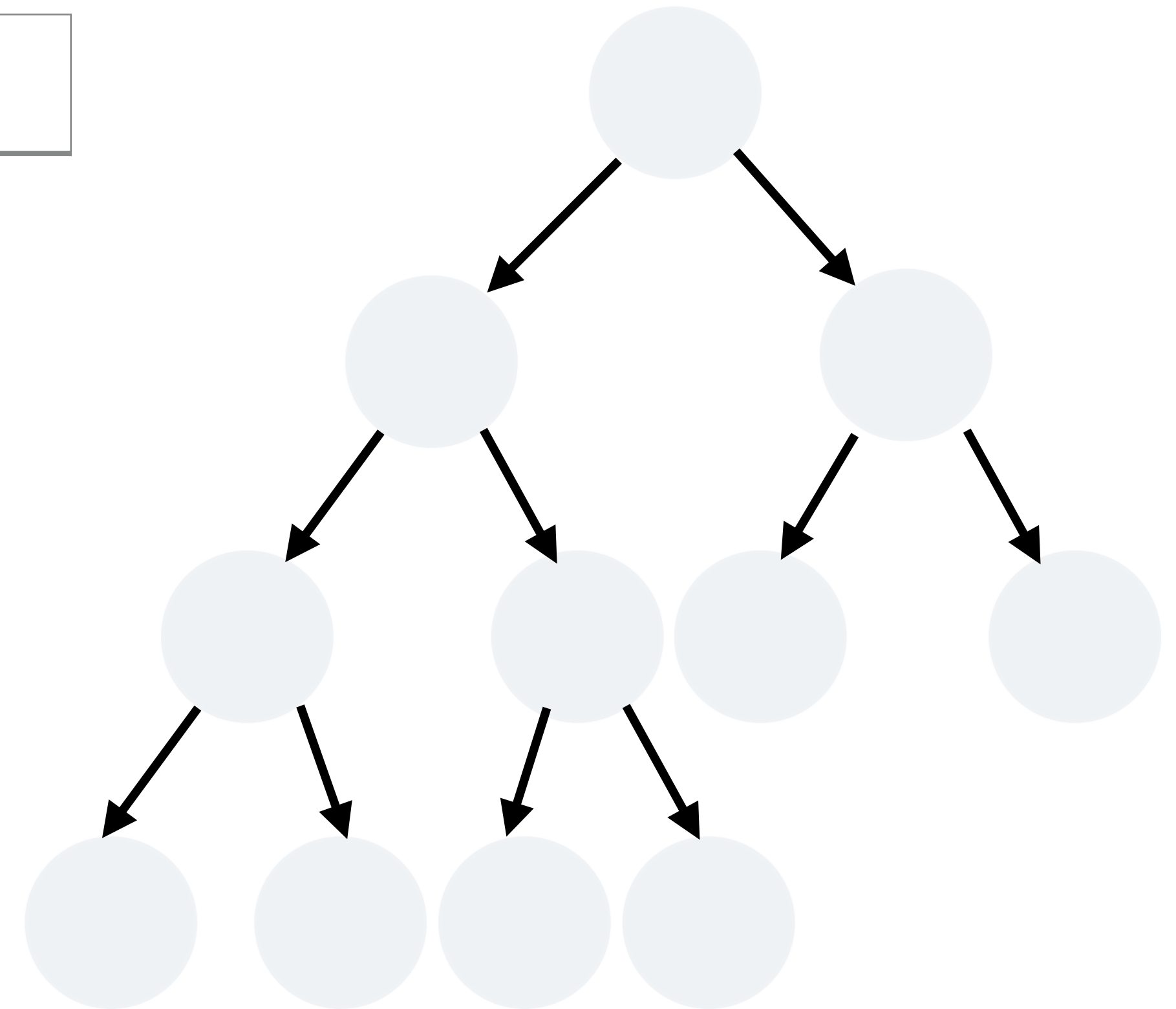
THE HEAP PROPERTY IS
SATISFIED

NO FURTHER CHECKS NEED
TO BE DONE - THIS IS A
MAXIMUM HEAP!

HEAP SORT

HEAPIFY

0	1	2	3	4	5	6	7	8	9	10
56	17	12	5	14	9	4	2	1	10	6



HEAP SORT

HEAPIFY

0 1 2 3 4 5 6 7 8 9 10

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**A MAXIMUM HEAP USING
IN-PLACE HEAPIFY!**

