- ¹ Two Models of Meaning: Revisiting the Principle of
- ² Compositionality from the Neurocognition of Language
- 3 RUNNING HEAD: Two Models of Meaning
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16 Abstract

A core tenet in linguistic theory is the principle of compositionality, which holds that the meaning of a multi-word utterance directly derives from the meanings of the indi-18 vidual words, and the rules by which they are combined. Semantic theories of lexical 19 word meaning and compositional utterance meaning have, however, developed into surprisingly distinct fields of study. Lexical semantic theories of word meaning focus on 21 modeling conceptual structure and similarity, e.g., the words "tea" and "coffee" are 22 similar in that they both describe drinkable substances. Formal semantic theories fo-23 cusing on compositional utterance meaning, in turn, focus on modeling sentence- and 24 discourse-level entailments and inferences, e.g., "drinking hot coffee" entails "drinking coffee". Critically, attempts at unifying models of lexical and compositional semantics have proven challenging and often yield complex frameworks, in which word- and 27 utterance-level meanings are patched together to form a whole, without fully integrating 28 their semantic contributions. We here revisit the principle of compositionality from the 29 neurocognition of language, which reveals that the human comprehension system har-30 nesses distinct models for lexical and compositional meaning, and that these models are 31 critically intertwined in a cyclic architecture for language comprehension. Within this 32 architecture, compositionality arises from a non-linear mapping of lexical semantic rep-33 resentations into a space for compositional semantic meaning, resulting in a continuous, 34 expectation-based, and spatiotemporally-extended notion of compositional integration. 35 This novel perspective on compositionality, combining linguistic and neurocognitive theory, paves way for more integrative approach towards modeling the meaning of words and utterances.

39 1 Introduction

One of the core topics in linguistic theory has traditionally been the question of how the meaning of complex multi-word utterances is derived from the meaning of the indi-41 vidual words that constitute these utterances. In the traditional view, there is a clear separation between the *syntactic* principles that determine how words can be combined to form complex utterances, and the semantic principles that define how meanings are represented and constructed. This distinction is colorfully illustrated in the famous ex-45 ample "Colorless green ideas sleep furiously", which was introduced as an example of 46 a sentence that is grammatically correct, yet nonsensical (Chomsky, 1957, p.15). This 47 distinction between syntax and semantics has long been a guiding principle in answering the overarching question of how meaning is assigned to linguistic input. Specifically, it has led to the fundamental principle that the meaning of a complex expression is fully 50 determined by the meanings of the individual words that constitute the expression, and 51 the way that they are combined (Partee, 1995). This principle of compositionality lies 52 at the core of current approaches in semantic theory, which presuppose a close relationship between the lexical meanings of individual words and the compositional meanings assigned to sentences and utterances; that is, utterance-level meaning is directly derived from the meanings of the individual words and the syntactic rules by which they are 56 combined. 57

The close formal relationship between lexical and compositional meaning that is
assumed by the principle of compositionality has some desirable properties, as it explains
the observation that human language users are able to produce and understand an
infinitely large number of complex expressions that they have not encountered before
(referred to as *productivity* of language use), and that they can systematically combine
and reorder the constituents of complex expressions into novel utterances (*systematicity*of language use). While the principle of compositionality takes center stage in explaining

these premises of language use, semantic theories that study lexical meaning at the level of words and and those that focus on compositional meaning at the level of sentences and discourses have developed into surprisingly distinct fields of study.

Lexical semantic (LS) theories aim to model the meaning of individual words. In par-68 ticular, distributional approaches to LS model word meaning as vector representations 69 derived from semantic features, capturing the similarities and dissimilarities between concepts in high-dimensional vector spaces: e.g., the concepts "tea" and "coffee" could 71 be modeled with vectors that encode their similarity in that they are both drinkable 72 substances, but also their dissimilarity in that one is made from leaves and the other 73 from beans. To formalize the principle of compositionality, there have been numerous 74 attempts to combine these LS representations into compositional semantic (CS) rep-75 resentations spanning multi-word utterances, for instance through vector averaging or 76 multiplication (e.g., Mitchell and Lapata, 2010). However, these approaches fall short 77 in approximating human-like compositionality, (Pavlick, 2022). Formal semantic frame-78 works, by contrast, fare a lot better in modeling the CS meaning of multi-word ut-79 terances. These formal semantic frameworks are typically grounded in mathematical logic, where LS meanings are modeled as functions—thereby sacrificing their conceptual 81 richness and structure—and composition is modeled as function application (e.g., the 82 meaning of "hot coffee" results from applying the function "hot" to the argument "cof-83 fee"). While these frameworks neatly capture CS meaning in terms of truth-conditional 84 entailment and inference, they do not naturally capture the similarities and dissimilar-85 ities between lexical items, motivating approaches that aim to introduce distributional LS meanings into such frameworks (Garrette et al., 2014; Asher et al., 2016; Beltagy 87 et al., 2016). While these hybrid approaches may conceptually come closest to imple-88 menting the principle of compositionality, they do often yield rather 'Frankensteinian' 89 frameworks in which distributional and formal semantics are patched together to form a whole, while still living in distinct representational spaces, thereby not fully integrating their semantic contributions.

These attempts at implementing the principle of compositionality by combining LS 93 and CS meaning into a single semantic framework raise an important question, namely 94 whether integrating these fundamentally different models of meaning is the right way 95 forward. One way to address this question is to turn to how the human brain represents and constructs meaning. Advances in the neurocognition of language comprehension paint a picture supporting a perspective in which LS and CS meaning do indeed co-exist 98 and interact, and recent neurocomputational modeling work suggests compositionality is 99 achieved by mapping representations from an LS meaning space into a seperate space for 100 CS meaning. Neurocognitive theory, informed by empirical and modeling results, thus 101 suggests that LS and CS meaning do indeed inhabit distinct meaning spaces, but that 102 they are also critically intertwined in the compositional comprehension process: incre-103 mental meaning construction involves retrieval of LS meaning, informed by the unfolding 104 CS utterance context, which is accordingly integrated into an updated representation of 105 the CS utterance meaning (Brouwer et al., 2012, 2017, 2021a). We therefore argue that 106 the traditional notion of compositionality, which is grounded in syntactic combinatory 107 rules, needs to be revised into a more dynamic notion of compositional integration, and 108 we discuss the theoretical and empirical implications of this proposal. 109

The linguistic perspective: How meaning can be modeled

In the study of linguistic meaning, a variety of formal frameworks has been proposed to model meaning at the level of words, sentences, and larger discourses. While these approaches generally agree upon the principle that these levels of meaning are closely related to each other, the core phenomena studied within these frameworks vary widely, ranging from word-level similarity and conceptual structure to sentence-level entailments,

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discourse structure and 'world knowledge'-driven inference. Attempts at implementing
the principle of compositionality by integrating these approaches into a single semantic
framework have proven challenging. This results in a state of affairs that suggests that LS
and CS should instead be treated as complementary, but interacting, models of meaning.

2.1 Lexical semantics: Conceptual knowledge and structure

Semantic formalisms that aim to capture word-level (LS) meaning from a cognitive per-122 spective are typically strongly grounded in the study of human semantic memory: the 123 collection of knowledge that allows humans to not only use and understand language, 124 but also to navigate the world around us, e.g., by recognizing and classifying objects. A 125 core notion that these approaches aim to capture is the observation that the conceptual 126 knowledge associated with individual words is both gradient and structured: concepts 127 are related to each other to different degrees, which is quantified as semantic similarity 128 (e.g., "bird" is more similar to "dog" than to "spoon"), and these relations are hier-129 archical in nature, in the sense that particular concepts are more general than others 130 (e.g., "bird" subsumes both "robin" and "ostrich"). Theories of lexical meaning aim to 131 capture this conceptual knowledge and structure by assuming semantic features as the 132 representational currency for conceptual knowledge (McRae et al., 2005). 133

Semantic features constitute the dimensions of the LS representations and may take different forms (see Frisby et al., 2023). A first set of approaches intuitively conceptualizes these semantic features as identifying discrete categories or local features; for instance, the dimensions of the semantic representation of "bird" may indicate the presence/absence of features such as has wings, can fly, or has eyes. Each semantic representation, then, represents a vector in a high-dimensional semantic space, which can be directly compared to other representations using various vector-based metrics to quantify semantic similarity. The advantage of these approaches is that semantic similarity is not only quantifiable, but that the dimensions are also directly interpretable as independent

categories or features.

An alternative approach to capturing semantic features for LS is grounded in a 144 theoretical foundation that has become known as the Distributional Hypothesis—in 145 the formulation of J. R. Firth: "You shall know a word by the company it keeps!" 146 (Firth, 1957, p.11). Based on the idea that "the meaning of words lies in their use" 147 (Wittgenstein, 1953, pp. 80, 109), the Distributional Hypothesis assumes that words that occur in similar contexts will have similar meanings (see also Turney and Pantel, 2010; 149 Clark, 2012; Erk, 2012; Lenci, 2018). This hypothesis has informed various influential 150 implementations in which the dimensions of the resulting LS representations capture 151 lexical co-occurrence information across linguistic contexts, i.e., sentences or documents 152 (e.g., Latent Semantic Analysis, LSA; Landauer and Dumais, 1997, hyperspace analogue 153 of language, HAL; Burgess, 1998, and dependency vectors, DV; Padó and Lapata, 2007). 154 In more recent instantiations of the Distributional Hypothesis, LS vectors are word 155 embeddings with abstract dimensions that are not directly interpretable, derived for 156 instance from neural prediction models (e.g., word2vec, Mikolov et al., 2013a,b; GloVe, 157 Pennington et al., 2014; ELMo, Peters et al., 2018; BERT, Devlin et al., 2019; GPT, 158 Radford et al., 2019). 159 The resulting distributional lexical semantic (DLS) representations have been ex-160 tremely successful in capturing conceptual knowledge and structure in terms of semantic 161 similarity. This has inspired investigations into how they can be combined composition-162 ally into utterance-level CS representations, for instance, by using vector operations as a 163 proxy for semantic composition (Mitchell and Lapata, 2010), or by combining DLS repre-164 sentations into more complex structures to arrive at CS meaning (Baroni and Zamparelli, 165 2010; Coecke and Clark, 2011; Socher et al., 2012; Grefenstette and Sadrzadeh, 2015). 166 While these approaches have shown some promise, for instance in modeling adjective-167 noun modification (Baroni et al., 2014; Vecchi et al., 2017), it has proven challenging to 168 capture higher level semantic composition, supporting the conclusion that feature-based 169

LS representations are "good at lexical semantics, bad at composition" (Pavlick, 2022, p. 464).

2.2 Compositional semantics: The meaning of multi-word utterances

Formal semantic frameworks for CS meaning focus on modeling the construction and 173 interpretation of phrases, sentences and multi-sentence discourses. Starting from the 174 idea that sentences (or: propositional-level meanings) can be either true or false with 175 respect to a state of affairs in the world, approaches in formal semantics focus on de-176 scribing sentence meanings with respect to formal model structures that describe such 177 situations. In its simplest form, a model structure is defined as a set of entities, called 178 the universe U, and an interpretation function I that assigns entities from the universe 179 (or sets thereof) to formal representations of linguistic expressions (e.g., the interpreta-180 tion I(bird) describes the subset of entities in the universe U that are birds). Sentences 181 can thus be assigned truth values within these model structures via a translation to 182 some logical representation of their meaning, which in turn obtains a formal model in-183 terpretation via the interpretation function (e.g., "Tweety is a bird" is true if and only 184 if "Tweety" refers to an entity in the universe that is also in the set of birds). Sentence 185 meaning, then, is defined in terms of the truth conditions with respect to formal model 186 structures: the constraints under which the logical representation of the sentence is as-187 signed the truth value "true" in the model—in other words, the conditions under which 188 the model satisfies the meaning of the sentence. Two sentences are assumed to express 189 the same meaning if they have the same truth conditions, i.e., they are satisfied by the 190 same models. This critically allows for a formalization of the logical entailment relation 191 between individual sentences: Sentence A is logically entailed by sentence B if any model that satisfies the meaning of sentence B also satisfies the meaning of sentence A (e.g., 193 the sentence "Mike paid" is logically entailed by the sentence "Mike ordered and paid"). 194

represent meaning as well as in terms of the complexity of the underlying model structures, which may capture, for instance, event structure (Davidson, 1969) or a notion 197 of time (Kamp, 1980). Furthermore, traditional approaches have formalized composi-198 tional semantic construction in a static manner, assuming independent representations 199 for lexical constituents (e.g., as lambda functions) which are then combined into com-200 positional representations through function application (Montague, 1970). More recent 201 semantic theorizing, however, has embraced a dynamic view toward meaning construc-202 tion, emphasizing the incremental nature of linguistic processing in terms of the growth 203 of semantic information over time (Nouwen et al., 2022). 204

205 2.2.1 Dynamic semantics: Discourse structure and composition

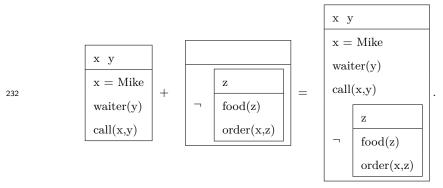
A dynamic semantic framework that is particularly amenable to different variations 206 of model-theoretic complexity is Discourse Representation Theory (DRT; Kamp, 1981; 207 Kamp and Reyle, 1993; Kamp et al., 2011). DRT is a mentalist framework for formal 208 semantics that provides abstract representations corresponding to the types of mental 209 representations assumed to underlie human language comprehension, often referred to 210 as mental models (Johnson-Laird, 1983) or situation models (Zwaan and Radvansky, 211 1998). The basic meaning units in DRT are called Discourse Representation Structures 212 (DRSs), which are formally defined as a tuple $\langle U, C \rangle$ consisting of a set of entities U and 213 a set of conditions on these entities C. The conditions in a DRS may describe simple 214 first-order properties or relations, but may themselves also include logical combinations 215 of DRSs. DRSs are often visualized using box-representations such as in example (1) 216 below, where the universe of the DRS ($\{x,y\}$) is represented in the top of the box and the conditions are described as first-order predicates over these variables: 218

(1) Mike called the waiter.

$$\begin{array}{c} x \ y \\ \\ x = \text{Mike} \\ \\ \text{waiter(y)} \\ \\ \text{call(x,y)} \end{array}$$

Each DRS can be formally assigned truth conditions relative to a model structure, 221 via either a translation to first-order logic or via an embedding function (Kamp, 1981). 222 A critical aspect of DRT is that it formalizes meaning at the discourse rather than the 223 sentence level; each DRS not only defines the truth conditions for a given sentence, 224 but also provides a context for any upcoming semantic content, e.g., in terms of the 225 referents that are available for pronominal reference. For example, a discourse in which the sentence above is continued with a novel sentence containing a referential expression, 227 is formalized as an updated DRS in which the initial meaning representation is extended 228 with the novel semantic information. This is effectuated as a 'merge' operation (+) 229 between DRSs: 230

231 (2) Mike called the waiter. He did not order any food.



The DRS resulting from this merge operation combines the universes of both DRSs, $\{x,y\}$ for the first DRS and the empty set for the second DRS, as well as their conditions.

DRT thus captures discourse-level meaning in terms of formal truth-conditional representations, while at the same time offering a dynamic semantic framework for meaning construction, in which novel semantic information is continuously merged with the

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discourse context established so far. To arrive at these representations in a compositional manner, Muskens (1996) defines a version of DRT that employs lambda calculus 239 to formalize how word-level meanings (formalized as functions in the form of lambda 240 expressions) combine into sentence- and discourse-level DRS representations. Such com-241 positional formulations, however, still assume a relatively static representation of lexical 242 meaning, where a word like "waiter" is interpreted relative to a formal model structure as the set of entities that satisfy this predicate. This means that lexical-level similarities, as 244 for instance modeled in distributional approaches to lexical semantics, are not naturally 245 captured within these representations. Another important limitation of formal semantic 246 approaches such as DRT is that that these logical frameworks do not naturally allow 247 for capturing defeasible inferences that go beyond the literal meaning of the individual 248 expressions—although various extensions of DRT have been proposed that do capture 249 presuppositions and implicatures (e.g., Layered DRT; Geurts and Maier, 2013, Projec-250 tive DRT; Venhuizen et al., 2018), as well as rhetorical structure (Segmented DRT; Asher 251 and Lascarides, 2003). In particular, the interpretation of DRS representations in terms 252 of model-derived truth conditions does not allow for capturing defeasible probabilistic 253 inferences that reflect world knowledge-driven expectations; for instance, the inference 254 that it is likely that "Mike" is in a "restaurant" in example (2) above. In order to capture 255 such world knowledge-driven inferences, recent work has sought to combine insights from 256 model-theoretic semantics with those deriving from distributional approaches to develop 257 a framework for expectation-based semantics, which offers distributional representations 258 of CS meaning at the level of propositions (Venhuizen et al., 2019a, 2022).

2.2.2 Expectation-based semantics: World knowledge-driven inferencing

Distributional Formal Semantics (DFS; Venhuizen et al., 2019a, 2022) is a distributional framework for meaning representation that builds on neurocognitive models of story comprehension (Golden and Rumelhart, 1993; Frank et al., 2009) to capture propositional

meanings in terms of co-occurrences in the world. Conceptually, DFS defines a meaning 264 space in terms of different states-of-affairs in the world, in which propositions such as 265 enter(mike,bar), describing "Mike entering a bar", may or may not co-occur; e.g., en-266 ter(mike,bar) may co-occur with order(mike,cola), but not with enter(mike,restaurant). 267 The DFS meaning representations that derive from this space are vectors that are com-268 positional at the propositional level, in that meanings can be combined using logical 269 operators, as well as probabilistic in the sense that they inherently capture the likeli-270 hood that meanings (co-)occur within the meaning space. 271

More formally, DFS defines meaning relative to a (finite) set of formal model struc-272 tures $\mathbb{M}_{\mathbb{P}}$, which together constitute the meaning space based on a finite set of proposi-273 tions P. Each model constitutes an observation of a state of affairs in the world, in that 274 each $M \in \mathbb{M}_{\mathbb{P}}$ is a first-order model that describes which of the propositions in \mathbb{P} are 275 true in that model. The set of models $\mathbb{M}_{\mathbb{P}}$ can thus be interpreted as a set of possible 276 worlds, in which different constellations of propositions may co-occur (in the tradition 277 of Carnap, 1988). The meaning of an individual proposition, then, is defined relative to 278 this set of models (or possible worlds); that is, the meaning of a (simple or complex) 279 proposition $p \in \mathbb{P}$ is defined by a vector $\llbracket p \rrbracket^{\mathbb{M}_{\mathbb{P}}} = \vec{v}(p)$ that assigns 1 to each $M \in \mathbb{M}_{\mathbb{P}}$ 280 that satisfies p, and 0 otherwise (Venhuizen et al., 2022). 281

Critically, as propositional meaning is directly defined in terms of satisfaction with respect to formal model structures, DFS representations are fully compositional at the propositional level. This means that the meaning of any logical combination of propositions can be derived from the meaning space as operations over the underlying meaning vectors. Specifically, we can define the meaning of the negation of a given proposition p as a vector operation: $\llbracket \neg p \rrbracket^{\mathbb{M}_{\mathbb{P}}} = 1 - \vec{v}(p)$, which results in a vector that is the complement of $\vec{v}(p)$ and that assigns 0 to each $M \in \mathbb{M}_{\mathbb{P}}$ that satisfies p, and 1 otherwise. The conjunction of two propositions p and q, in turn, is defined as component-wise vector multiplication: $\llbracket p \wedge q \rrbracket^{\mathbb{M}_{\mathbb{P}}} = \vec{v}(p)\vec{v}(q)$, such that the resulting vector $\vec{v}(p \wedge q)$ assigns 1 to

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each $M \in \mathbb{M}_{\mathbb{P}}$ that satisfies both p and q, and 0 otherwise. Together, these negation and conjunction operators allow for the derivation of any arbitrarily complex combination of propositions, as well as for definitions of existential quantification (e.g., "someone orders cola") and universal quantification ("everyone pays"); see Venhuizen et al. (2022) for details.

The set of models $\mathbb{M}_{\mathbb{P}}$ constitutes a meaning space that encodes the meaning of (complex) propositions in terms of their co-occurrence with other propositions: propositions that co-occur across a large set of models (observations of states-of-affairs in the world) will result in similar meaning vectors. Critically, while propositional meaning is defined in terms of binary vectors relative to the meaning space $\mathbb{M}_{\mathbb{P}}$, this space actually constitutes a continuous vector space $\mathbb{R}^{\mathbb{M}_{\mathbb{P}}}$. As a result, the meaning space defines meanings not only for binary propositional vectors, but also for real-valued vectors that do not directly correspond to (combinations of) propositions; rather, these vectors can be described as representing meanings that may lie in between the meanings of propositional expressions. As will become apparent below, these real-valued vectors represent sub-propositional meanings (e.g., "bartender brings" which still requires an object) that can be used to express the incremental construction of propositional-level meaning (e.g., by adding "fries" to form bring(bartender, fries), which is a full proposition).

All meaning vectors that can be defined in the DFS meaning space inherently encode probabilistic knowledge about (co-)occurrence in the world that is defined by the meaning space; propositions that are true in many models can be considered to have a high probability in the world. Hence, the probability P(a) of a (propositional or sub-propositional) expression a in this space is defined as follows:

$$P(a) = \frac{1}{|\mathcal{M}_{\mathbb{P}}|} \sum_{i} \vec{v}_{i}(a) \tag{1}$$

That is, the probability of a is defined as the fraction of models (observations) in which

a is satisfied. This definition can be straightforwardly extended to a definition of the 315 conditional probability of a given b: $P(a|b) = P(a \wedge b)/P(b)$. This means that the repre-316 sentations in DFS allow for calculating the conditional probability of any expression in 317 relation to all other (propositional or sub-propositional) meanings that can be defined 318 within the meaning space. As a result, we can use this probabilistic nature of the mean-319 ing representations to quantify the extent to which expressions are inferred from each 320 other. Specifically, if the conditional probability P(a|b) equals 1 for some propositional 321 meanings a and b, this means that a is satisfied in all the models that satisfy b; in other 322 words, a is entailed by b ($b \models a$). Furthermore, by comparing the conditional proba-323 bility P(a|b) to the prior probability P(a), the degree to which knowing b increases or 324 decreases the certainty in a can be quantified, which gives us a notion of probabilistic 325 inference (Venhuizen et al., 2022; Frank et al., 2009): 326

$$inference(a,b) = \begin{cases} \frac{P(a \mid b) - P(a)}{1 - P(a)} & \text{if } P(a \mid b) > P(a) \\ \frac{P(a \mid b) - P(a)}{P(a)} & \text{otherwise} \end{cases}$$
(2)

This inference score results in a value between -1 and 1, such that negative values indicate that a is negatively inferred from b (or: knowing b decreases the probability 328 that a is the case) and positive values indicate that a is positively inferred from b (or: 329 knowing b increases the probability that a is the case). Hence, an inference score of 0 330 indicates that a is probabilistically independent of b, an inference score of 1 indicates 331 positive entailment $(b \models a)$ and an inference score of -1 indicates negative entailment 332 $(b \vDash \neg a).$ 333 Let us turn to an example to illustrate how this mathematical machinery can be used 334 to quantify the inferences and expectations in a concrete meaning space. Figure 1 plots the inference score for a subset of the propositions that are defined in the meaning space 336 presented in Venhuizen et al. (2022). Propositions take the form of predicated expres-337

sions, such that order(mike, cola) corresponds to the meaning of "Mike orders cola". This

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heatmap shows the value of inference(a,b), ranging from -1 (red) to +1 (green), for each 339 propositional expression a given itself and each other propositional expression b. The green diagonal shows that each proposition is positively entailed by itself. Furthermore, 341 certain propositions are negatively entailed by each other (e.g., enter(mike,bar) given en-342 ter(mike, restaurant), and vice versa), which reflects the fact that in the meaning space 343 these propositions never co-occur. All graded values reflect probabilistic inferences; for instance, enter(mike,bar) is inferred negatively from order(mike,salad). Hence, these 345 inferences reflect how the meaning vectors that derive from the DFS meaning space 346 capture rich world knowledge based on propositional co-occurrences—in other words, 347 to paraphrase the famous formulation of the Distributional Hypothesis by Firth (1957): 348 you shall know a proposition by the company it keeps in the world. 349

An important observation to make here is that the inferences made within such a propositional meaning space do not directly align with word-level LS inferences informed by semantic similarity. For instance, while "bar" and "restaurant" may be elicit similar associations on the lexical level (e.g., about ordering food and drinks), the propositions in which these expressions occur are not semantically similar within the DFS meaning space, due to the (relatively) low co-occurrence of these propositions across the observations of states-of-affairs in the world. This means that the inferences that can be drawn from the DFS meaning space are distinct from those that can be drawn from lexical co-occurrences or componential analysis.

2.3 Two models of meaning?

The linguistic perspective delineates two models of meaning. On the one hand, DLS uses feature-based representations to model conceptual knowledge and structure. While these approaches do indeed successfully capture human intuitions about conceptual similarity, it has proven challenging to define compositionality over such LS representations (Pavlick, 2022). In fact, one can even raise the question if it is possible to express all of

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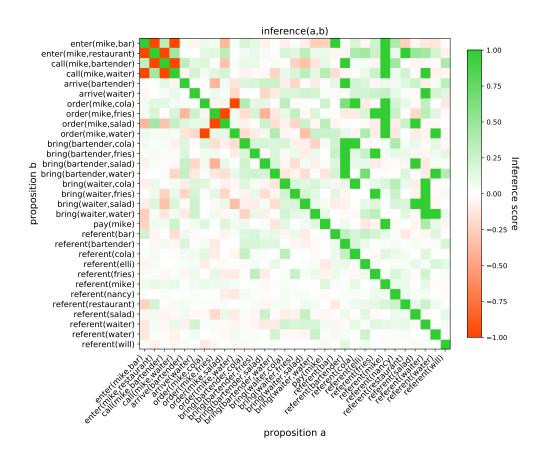


Figure 1: Meaning space with probabilistic inferences. Cells plot the inference score of each proposition a given each proposition b for a subset of propositions in the meaning space presented in Venhuizen et al. (2022). Bright green cells indicate positive entailment between propositions ($b \models a$), bright red cells indicate negative entailment ($b \models \neg a$), and all other intermediate cells indicate probabilistic inferences on this positive-to-negative continuum. Reproduced with permission (CC BY-NC-ND 4.0) from Venhuizen et al. (2022).

the complexities of compositional meaning within a meaning space for LS, of which the dimensions are assumed to represent some form of componential semantic features of in-366 dividual concepts. Dynamic semantic frameworks, like DRT, on the other hand, harness 367 formal model theory to construct CS representations that successfully capture truth-368 conditional entailment relations. More recent expectation-based semantic frameworks, 369 like DFS, extend this truth-conditional approach to capturing 'world knowledge'-driven 370 inferences in terms of probabilistic entailment relations. Neither of these formal semantic 371 approaches to CS, however, captures the conceptual knowledge and structure that DLS 372 approaches capture. 373

Various methods have been developed that aim to incorporate lexical-level distribu-374 tional semantics into formal semantic frameworks (see, e.g., Coecke et al., 2010; Garrette 375 et al., 2014; Asher et al., 2016; Beltagy et al., 2016), which for instance allow LS mean-376 ing to guide the construction of logical form for CS (Asher et al., 2016). What these 377 approaches have in common, however, is that there remains a clear separation between 378 the levels of representation that capture LS-derived properties (e.g., semantic similarity) 379 and those that explain CS-derived properties (e.g., logical inference). Hence, in one way 380 or the other, these frameworks fail to fully integrate the semantic contributions of LS 381 and CS meaning. This raises the question if connecting these two models of meaning 382 in a single formal semantic system is the right way forward. In what follows, we will 383 address this question from the perspective of the neurocognition of language, and derive 384 an architecture for incremental meaning construction that combines models of LS and 385 CS meaning through a compositional integration process.

The neural perspective: How the brain represents meaning

The neurocognition of language comprehension is concerned with how, when, and where 389 in the brain meaning is attributed to incoming linguistic signal as it unfolds in time. 390 Event-Related Potentials (ERPs)—stimulus-locked, scalp-recorded voltage fluctuations 391 caused by post-synaptic neural activity—have been instrumental in addressing questions 392 about the how and when (see Kutas et al., 2006; Kutas and Federmeier, 2011; Hoeks 393 and Brouwer, 2014, for reviews). ERP studies focus on systematic voltage fluctuations, 394 referred to as *components*, which are taken to reflect specific computational operations 395 carried out in given neuro-anatomical networks (Näätänen and Picton, 1987). Of par-396 ticular salience to language comprehension are the N400 and the P600 components (see 397 Brouwer et al., 2012; Kuperberg, 2007; Bornkessel-Schlesewsky and Schlesewsky, 2008, 398 for reviews). Critically, the differential sensitivity of these components to aspects of LS 399 and CS delineates a comprehension architecture in which meaning representations for 400 LS and CS dynamically interact in the construction of compositional meaning. This dy-401 namic interplay between LS and CS forms the core of Retrieval-Integration (RI) theory, 402 an integrated theory of the electrophysiology of language comprehension (Brouwer et al., 403 2012), with an explicit cortical mapping (Brouwer and Hoeks, 2013) and neurocompu-404 tational instantiation (Brouwer et al., 2017, 2021b). 405

406 3.1 The Retrieval-Integration theory of online comprehension

RI theory, as first formulated by Brouwer et al. (2012), provides an explicit account of the processes assumed to underlie the N400 and P600 components. The N400 is a negative deflection in the ERP signal that becomes apparent 200-300ms post-word onset and peaks at about 400 ms (see Figure 2), and was first identified in response to semantically incongruous words, such as the word "socks" in "He spread the warm bread

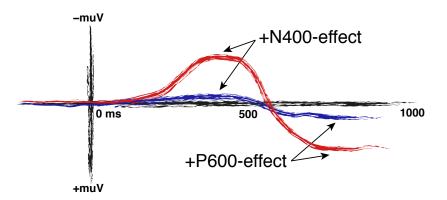


Figure 2: N400 and P600 components in the ERP signal. Hypothesized ERP waveform for a contrast between a target condition (red) compared to a baseline condition (blue). By convention negative voltage is plotted upwards on the y-axis. This contrast elicits both an N400 and a P600 effect for the target relative to the baseline condition, which result from the differential modulations of the N400 and P600 components in the ERP signal, respectively. Reproduced with permission (CC BY 4.0) from Brouwer and Crocker (2017).

with socks/butter" (Kutas and Hillyard, 1980). This component is, however, not just 412 a response to an anomaly, but is in fact inversely proportional to the expectation of a 413 word in context, such that less expected words yield larger N400 amplitudes (Kutas and 414 Hillyard, 1984). N400 amplitude to unexpected words can, however, be attenuated if an 415 incoming word shares semantic (Federmeier and Kutas, 1999) or orthographic features (Federmeier and Laszlo, 2009) with an expected word. Furthermore, the processes un-417 derlying the N400 are also sensitive to the semantic association of a word to its prior 418 context (Aurnhammer et al., 2021), to the degree that strong association may override 419 any effect of expectancy; that is, the word "socks" in the example above will not produce 420 a larger N400 amplitude relative to "butter" when the critical sentence is embedded in a 421 context discussing, for instance, someone trying find a fresh pair of socks before break-422 fast (Aurnhammer et al., 2023). Taken together, these findings pose clear constraints on 423 the computational operations underlying the N400, leading to the now well-established 424 perspective that the N400 is an index of the contextualized retrieval of feature-based LS

representations from long-term semantic memory, such that the more the context primes the LS features of an upcoming word, the more facilitated its retrieval and the more at-427 tenuated N400 amplitude (Kutas and Federmeier, 2000; Lau et al., 2008; Federmeier and 428 Laszlo, 2009; van Berkum, 2009; Brouwer et al., 2012; Federmeier, 2022). 429 The P600, in turn, is a positive deflection in the ERP signal that starts to emerge 430 at about 600ms post-word onset (see Figure 2), and that was first identified in re-431 sponse to syntactically infelicitous words, such as the word "throw" in "The spoilt child 432 $\underline{\text{throw}}/\underline{\text{throws}}$ [...]." This component is, however, not just sensitive to syntactic felicity. 433 P600 amplitude also increases in response to structurally-induced garden-path construc-434 tions and long-distance wh-dependencies (Gouvea et al., 2010), semantic incongruities 435 (Van Petten and Luka, 2012; Brouwer and Crocker, 2017), as well as a wide-range of 436 phenomena requiring pragmatic inferencing (see Hoeks and Brouwer, 2014, for a review). 437 Furthermore, it has recently been shown that the P600 is not just a binary reflection 438 of well-formedness, but that its amplitude rather tracks the plausibility of a word in 439 context in a continuous manner (Aurnhammer et al., 2023). Taken together, this is 440 consistent with a view in which the P600 reflects the integration of incoming linguistic input into a CS representation of the unfolding utterance thus far, such that the more 442 effort it takes to arrive at a coherent CS representation—in terms of construction, re-443 organization, and/or updating—the larger the amplitude of the P600 (Brouwer et al., 444 2012). 445 Indeed, these perspectives on the N400 as LS retrieval and the P600 as CS integration 446 suggest that the brain harnesses two separate models of meaning for LS and CS meaning. This raises the question, however, how these meaning spaces interface in online language comprehension; that is, how do we go from the perception of words through LS to CS? RI 449 theory offers an integrated theory of the electrophysiology of language comprehension 450 that combines the retrieval perspective on the N400 with the integration perspective 451 on the P600 (Brouwer et al., 2012; Brouwer and Hoeks, 2013; Brouwer et al., 2017,

⁴⁵³ 2021b; Venhuizen and Brouwer, 2025). On RI theory, the processing of an incoming ⁴⁵⁴ word is mechanistically conceptualized as a *process* function, that maps an acoustically ⁴⁵⁵ or orthographically perceived *word form* in the *utterance context* in which it occurs onto ⁴⁵⁶ a *CS representation* of utterance meaning:

process: (word form, utterance context)
$$\rightarrow$$
 CS representation (3)

Critically, this *process* function decomposes into a *retrieve* and *integrate* function, such
that the perceived *word form* in an *utterance context* is first mapped onto a *LS repre- sentation* of word meaning:

retrieve: (word form, utterance context)
$$\rightarrow$$
 LS representation (4)

This contextualized retrieval of word meaning is what underlies the N400 component, and the retrieved LS representation serves as input to an *integrate* function that combines it with the *utterance context* established thus far, to produce an updated *CS representation* of utterance meaning:

integrate: (LS representation, utterance context)
$$\rightarrow$$
 CS representation (5)

This integration of the *LS representation* of the meaning of an incoming word with
the *utterance context* underlies the P600 component. The resultant *CS representation*spanning the entire utterance will determine the *utterance context* for upcoming words;
more specifically, it will serve as the *utterance context* that primes the *LS representation*associated with potential upcoming input.

RI theory thus assumes a cyclic relationship between the retrieval processes underlying the N400 and the integration processes underlying the P600. While ERPs are not directly informative about where these processes are carried out in the brain, aligning

insights from electrophysiology with those on the cortical organization of language e.g., from functional Magnetic Resonance Imaging (fMRI) and lesion studies—results in a minimal functional-anatomic mapping of RI theory that further corroborates its 474 cyclic nature (Brouwer and Hoeks, 2013). This functional-anatomic mapping is centered 475 around the left posterior Middle Temporal Gyrus (lpMTG) as an epicenter/hub for re-476 trieval, and the left Inferior Frontal Gyrus (IIFG) as an epicenter/hub for integration (see Figure 3a). These epicenters/hubs are connected via white matter fibers in both a 478 dorsal pathway (dp) and a ventral (vp) pathway (see Brouwer and Hoeks, 2013, section 479 3.4, for further discussion). Depending on whether the input modality is spoken or writ-480 ten, a perceived word form enters the cortical RI cycle via either the auditory cortex 481 (ac) or visual cortex (vc), respectively. The lpMTG then retrieves its associated LS word 482 meaning representation, which is assumed to be stored across the association cortices, 483 thereby generating the N400 component. The retrieved LS representation is then pro-484 jected to the IIFG where it is integrated with the current utterance context to produce 485 an updated CS utterance representation. This updated CS utterance representation in 486 the IIFG is then connected back to the lpMTG to provide an utterance context that 487 leads to the pre-activation/priming of (aspects of) LS representations associated with 488 potential upcoming words (see Brouwer and Hoeks, 2013, section 4.3, for a discussion 489 on the temporal dynamics of the communication between the lIFG and the lpMTG). 490

3.2 Neural meaning composition

The neurocomputational instantiation of RI theory directly implements the cortical instantiation of RI in a recurrent neural network architecture (see Figure 3b). This architecture consists of five layers, starting with an input ('ac/vc') layer at which the model receives perceived word forms. These perceived word forms are projected through a 'retrieval' (lpMTG) layer, which combines it with a top-down CS utterance context projection, from the later 'integration' (lIFG) layer, to map the perceived word form

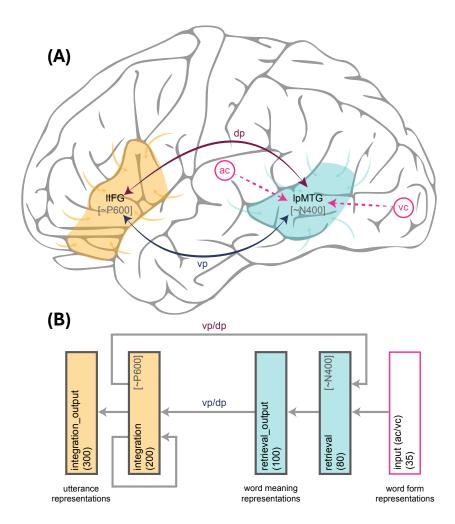


Figure 3: Retrieval-Integration (RI) theory. (A) Functional-anatomic instantiation of RI theory: Perceived word forms enter the RI cycle through the auditory cortex (ac) or the visual cortex (vc), depending on the input modality (spoken versus written). The left posterior Middle Temporal Gyrus (lpMTG) serves as retrieval epicenter/hub and core generator of the N400, while the left Inferior Frontal Gyrus (lIFG) is serves as integration epicenter/hub and core generator of the P600. The epicenters/hubs are connected via white matter fibers in both a dorsal pathway (dp) and ventral pathway (vp). (B) Neurocomputational instantiation of RI theory: A recurrent neural network architecture that progressively maps word forms in context onto a LS word meaning representation, and LS representations into incremental CS utterance representations. N400 amplitude is estimated as the word-induced change in activity the lpMTG layer, and P600 amplitude as the change in activity in the lIFG layer. Reproduced with permission (CC BY-NC 4.0) from Brouwer et al. (2017).

in context onto a LS word meaning representation in the 'retrieval_output' layer. This 498 retrieved LS word meaning representation is then projected through a recurrent 'inte-499 gration' (IIFG) layer, which combines it with the previous utterance context, to produce 500 an updated CS utterance representation in the 'integration_output' layer. The model 501 processes sentences on an incremental, word-by-word basis, and at each word N400 am-502 plitude is estimated as the degree of change induced in the 'retrieval' layer, whereas P600 503 amplitude is estimated as the degree of change induced in the 'integration' layer. Using 504 these explicit linking hypotheses to the N400 and P600, the model has been shown to 505 account for key psycholinguistic processing phenomena (Brouwer et al., 2017, 2021b). 506 Critically, the neurocomputational instantiation of RI theory is not only explicit 507 about its architecture and processing mechanisms, but also about the nature of the 508 neural LS and CS representations that it assumes. The neural LS representations of 509 word meaning are rather straightforwardly modeled as DLS representations (using the 510 Correlated Occurrence Analogue to Lexical Semantics, COALS; Rohde et al., 2009), such 511 that the dimensions of these vectors are proxies for componential semantic features. 512 In the most recent instantiation of the model (Brouwer et al., 2021b), the neural CS 513 representations are modeled using the vector representations from Distributional Formal Semantics (DFS) (Venhuizen et al., 2022). As introduced in Section 2.2.2, DFS assumes 515 a meaning space M_P, consisting of set of formal model structures, such that each model 516 $M \in \mathbb{M}_{\mathbb{P}}$ determines the truth value of each proposition $p \in \mathbb{P}$. Together these models 517 form a continuous vector space $(\mathbb{R}^{\mathbb{M}_{\mathbb{P}}})$, and comprehension in the neurocomputational 518 model involves navigating this vector space on a word-by-word basis to recover utterancefinal propositional meaning. 520 This notion of comprehension as meaning-space navigation is illustrated in Figure 4. 521 The cube in Figure 4a represents the meaning space presented in Venhuizen et al. (2022) 522 (see also Figure 1), mapped from $|\mathbb{M}_{\mathbb{P}}| = 150$ dimensions into three dimensions (using 523

multi-dimensional scaling, MDS). The propositional meanings that are shown represent

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binary vectors for a subset of the propositions in \mathbb{P} , as well as two compositional meanings derived from combining these propositions: $enter(mike,bar) \wedge order(mike,cola)$ and $enter(mike,bar) \land order(mike,fries)$. The position of these vectors relative to each other directly reflects the world knowledge in the meaning space; propositions that are likely to co-occur will be positioned closer to each other in the meaning space, and vice versa. The model learns to navigate this meaning space on a word-by-word basis, producing realvalued CS output vectors (see Figure 3b) that directly reflect world-knowledge driven 531 inferences. Critically, the trajectory through meaning space is directly influenced by the linguistic experience that the model is exposed to, in terms of the frequency of utterancemeaning pairs encountered during training, such that the model favors trajectories for more frequently encountered word sequences (Venhuizen et al., 2019a,b).

This navigation process is illustrated in Figure 4a for the sentence prefix "Mike entered the bar, he ordered ...". After processing this sentence prefix, the model finds itself in a state that is more in line with the sentence-final meaning $enter(mike,bar) \wedge$ order(mike, cola) than with the meaning $enter(mike, bar) \wedge order(mike, fries)$. If the sentence prefix is then continued with either "cola" or "fries", processing the word "cola" results in a more expected transition compared to processing the word "fries"—as measured by the information-theoretic notion of surprisal (Hale, 2001; Levy, 2008), which in DFS is defined as the negative logarithm of the probability of the current point in meaning space given the previous point (see Venhuizen et al., 2019a). After processing the final word, the model arrives at a point in space that approximates the intended sentence-final meaning for each sentence.

Critically, as each point in the meaning space carries its own probability in relation each other point in meaning space, the model updates its inferences about the communicated state-of-affairs on a word-by-word basis. This is illustrated in Figure 4b, which plots the inference scores (see Equation 2) for a subset of propositions pertaining to referential presuppositions, as derived from the CS representation at the output layer of

the model at each word of the sentence "someone called the waiter, she ordered cola". While the sentence-initial meaning vectors show no strong inferences regarding these 553 presuppositions, the introduction of "waiter" leads to the strong inference (entailment) 554 that a waiter is present in the described state-of-affairs. Furthermore, linguistic expe-555 rience leads the model to infer the presence of female referents (elli and nancy) at the 556 word "she". At the sentence-final word "cola", the set of probabilistic inferences reflects 557 the 'world knowledge'-driven, non-literal interpretation that the model assigns to this 558 sentence, namely that elli is a referent in the described situation (driven by the high 559 probability of elli ordering cola in the meaning space; see Venhuizen et al., 2022 for 560 details). 561

This comprehension as meaning-space navigation has several important implications. 562 First of all, meaning composition in the model is an incremental process in which the LS 563 meaning associated with a perceived word, in context of the CS representation estab-564 lished thus far, effectively triggers a transition in CS meaning-space. This transition is 565 effectuated by the "integration" (IIFG) layer of the model, which updates its state based 566 on its current activity pattern—its current state—and the LS of an incoming word. The 567 degree to which this state changes as a result of processing an incoming word is an 568 estimate of P600 amplitude in the model. Secondly, the retrieval of word meaning is ef-569 fectively the activation of a word-associated LS representation in a DLS meaning-space, 570 and this retrieval is directly affected by the state of the "integration" (IIFG) layer; that 571 is, the "retrieval" (lpMTG) updates its state based on a word form perceived in the 572 "ac/vc" layer, as well as the top-down state of the "integration" (IIFG) layer to retrieve the word-associated LS representation. The degree of change in this state is an estimate 574 of N400 amplitude in the model. LS and CS meaning thus inhabit distinct meaning 575 spaces, but are critically intertwined: compositional meaning construction involves in-576 tegrating LS representations into CS space, and the current point in CS space directly 577 affects the anticipation of aspects of upcoming LS representations.

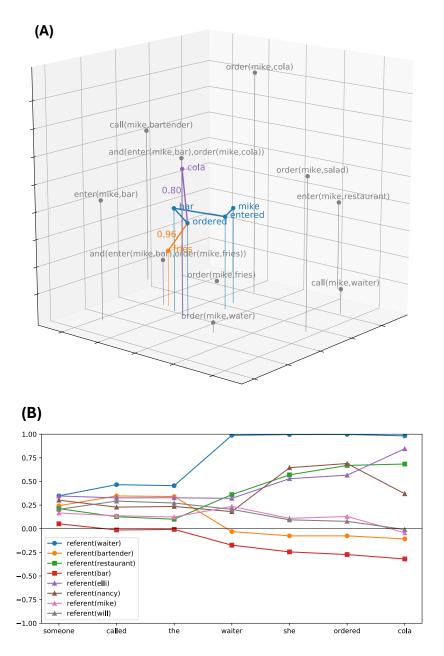


Figure 4: Comprehension as meaning-space navigation. (A) Three-dimensional mapping of the meaning-space presented in Venhuizen et al. (2022). The gray points show a subset of the propositions that define the meaning space, as well as two complex propositions derived from combining them. The colored points show the word-by-word trajectories for the sentences "Mike entered the bar, he ordered [cola/fries]". The numbers represented the expectancy (information-theoretic surprisal) of the sentence final words "cola" and "fries". (B) Word-by-word inference scores for propositions pertaining to referential presupposition at each word of the sentence "someone called the waiter, she ordered cola". Reproduced with permission (CC BY-NC-ND 4.0) from Venhuizen et al. (2022).

579 3.3 Decoding meaning representations from neural activity

According to RI theory, the construction of compositional utterance meaning involves a dynamic interplay between two distinct models of meaning. Conceptual meaning, on the one hand, is captured by an LS space, with representations stored across the association cortices, and the lpMTG serving has an epicenter/hub for their retrieval. Compositional utterance meaning, on the other hand, is captured by a CS space, with the lIFG serv-ing as an epicenter/hub for the construction of an unfolding CS representation, which involves compositionally integrating LS representations into this CS space. While the neurocomputational instantiation of RI theory is both representationally explicit about LS and CS, as well as mechanistically explicit about their interplay in the compositional process, these representations and mechanisms are only simplified abstractions of those underlying comprehension in the brain. Indeed, the ultimate aim is to investigate these representations and mechanisms in the brain more directly.

Recent advances in neuroscience and artificial intelligence have led to the development of mapping models that do enable the direct investigation of neural meaning representation and computation in the brain through either decoding or encoding (Poldrack, 2011; King and Dehaene, 2014). These mapping models traditionally start from a set of words, LS representations for these words (of which the dimensions may or may not be directly interpretable; see Frisby et al., 2023), and neural activity patterns elicited by the perception of these words, such as individual voxel activation levels from fMRI. Decoding models then seek to accurately predict each LS dimension from these voxel activation levels, effectively yielding models that quantify the degree to which each individual voxel contributes to a particular LS dimension. Encoding models, in turn, start from the LS representations, and aim to predict each voxel activation level from the LS dimensions, yielding models that quantify the degree to which each dimension contributes to a given voxel. Critically, these encoding models can also be used for decoding, by finding the most likely cause for a pattern of observed activity, which can for instance be achieved

through informed search (see Tang et al., 2023, for such an approach).

While early mapping models using static LS representations—constructed using lan-607 guage models or human ratings—have shown that it is possible to successfully decode 608 the meaning of words or sentences from neural activity (e.g., Mitchell et al., 2008; Pereira 609 et al., 2018), more recent models have pushed the state-of-the-art to the decoding of con-610 tinuous language by using the contextualized representations from large language models 611 (Tang et al., 2023). Beyond practical implications of such models for brain-computer 612 interfaces, they also provide a toolkit for directly investigating the representation and 613 computation of meaning in the brain. However, before mapping models can be harnessed 614 to address such fundamental questions, important methodological and and theoretical 615 challenges need to be addressed. These challenges include the inconsistency of extant 616 mapping results (e.g., Frisby et al., 2023) and the difficulty in reconciling these results 617 with neurocognitive theory (e.g., compare the decoding results by Tang et al., 2023 618 to the cortical instantiation of RI by Brouwer and Hoeks, 2013). Furthermore, these 619 models predominantly focus on LS and are challenged by the theoretical difficulties of 620 the large-scale modeling of multi-word CS representations, as well as the difficulties im-621 posed by the spatiotemporal dynamics of LS and CS representation and computation in 622 the compositional process (see also the discussion below). While these challenges may 623 not be straightforwardly overcome, mapping models do hold the promise to be instru-624 mental in answering fundamental, fine-grained questions about the representation and 625 computation of meaning in the brain. 626

627 4 The principle of compositionality revisited

The principle of compositionality assumes a close formal relationship between word-level LS and utterance-level CS meaning, since in its standard formulation, the CS meaning of an expression directly derives from the LS meanings of its constituents and the (syn-

tactic) rules by which they are combined (Partee, 1995). Despite this assumed close rela-631 tionship, semantic theories of LS and CS meaning have developed into rather disparate 632 fields of study. Models of LS meaning focus on representations that capture concep-633 tual knowledge and structure, but attempts at introducing compositionality into these 634 models—e.g., through vector averaging or multiplication (Mitchell and Lapata, 2010)— 635 have had limited success (see Pavlick, 2022, for discussion). Models of CS meaning, on 636 the other hand, focus on representations that capture truth-conditional entailment rela-637 tions, but treat LS meaning in terms of mathematical functions, which do not capture 638 any conceptual structure or similarity. While there have been attempts to incorporate 639 (distributional) LS representations into such CS models, these often result in frameworks 640 in which LS and CS representations are patched together through complex mathematical machinery, but do not fully integrate their semantic contributions (e.g., Garrette et al., 642 2014; Asher et al., 2016; Beltagy et al., 2016). Taken together, this raises the question of 643 whether connecting models of LS and CS meaning in a single, unified semantic system 644 is the right way forward. 645

646 4.1 Compositionality as a non-linear mapping between meaning spaces

Experimental findings and theoretical modeling within the neurocognition of language 647 reveal that the human comprehension system does indeed harness both a model for LS meaning as well as a model for CS meaning. Electrophysiological research on lan-649 guage comprehension has shown that the N400 and the P600—the two most salient 650 language-related components of the ERP signal—are differentially sensitive to aspects 651 of LS and CS meaning, respectively. That is, the degree to which word-associated LS 652 meaning is contextually anticipated has been shown to result in a reduction of N400 amplitude (e.g., Kutas, 1993; Federmeier and Kutas, 1999), while expectations regarding 654 utterance-level CS meaning result in a reduction of P600 amplitude (e.g., Aurnhammer 655 et al., 2023). This differential sensitivity of the N400 and P600 forms the core of the 656

Retrieval-Integration theory of language comprehension (Brouwer et al., 2012; Venhuizen and Brouwer, 2025), an integrated theory of language electrophysiology with an explicit 658 functional-anatomic mapping (Brouwer and Hoeks, 2013) and neurocomputational in-659 stantiation (Brouwer et al., 2017, 2021b). On RI theory, the N400 component of the 660 ERP signal indexes the retrieval of the LS meaning of a word, a process that is directly 661 modulated by top-down CS utterance context. The P600 component, in turn, indexes 662 the integration of this retrieved LS word meaning into an unfolding CS representation 663 of utterance meaning. Hence, RI theory assumes LS and CS meaning to coexist and 664 interact during language comprehension. Furthermore, the functional-anatomic map-665 ping of RI assumes two distinct cortical epicenters/hubs, with the lpMTG serving as 666 an epicenter/hub for the retrieval of LS representations that are assumed to be stored 667 across the association cortices, and the lIFG as an epicenter/hub for CS meaning con-668 struction. These epicenters are wired together through dorsal and ventral white matter 669 pathways, supporting the cyclic circuit required for top-down CS context to modulate 670 the retrieval of incoming LS word meaning, and bottom-up LS meaning to be integrated 671 into a representation of CS meaning. 672

The neurocomputational instantiation of RI theory representationally and mechanistically explicates this functional-anatomic mapping, and suggests that rather than connecting LS and CS meaning in a rule-based, formal semantic system that mathematically conflates their distinct representational currencies, compositionality may be achieved through a non-linear mapping integrating representations from an LS meaning space into a meaning space for CS; that is, the neurocomputational instantiation of RI suggests that compositionality may be an emergent epiphenomenon of the neural machinery implementing the comprehension system. Fundamentally, this is, however, still consistent with the assumption underlying the principle of compositionality that the meaning of a complex expression is determined by the meanings of the individual words that constitute the expression, and the way that they are combined.

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Indeed, this is highly reminiscent of the way in which large language models (LLMs) 684 construct meaning. LLMs also start from LS representations, in terms of word em-685 beddings, which they progressively and non-linearly map into deeper, contextualized 686 embeddings. The impressive human-like comprehension behavior of such LLMs has led 687 to suggestions that they implement mechanisms that are highly similar to those im-688 plemented by the comprehension system in the human brain (Goldstein et al., 2022; 689 Schrimpf et al., 2021). While such conclusions may be premature (see, e.g., Krieger 690 et al., 2024), LLMs do offer interesting systems for further investigation. For one, the 691 contextualized embeddings that these models construct may be the closest thing we have 692 to wide-coverage CS representations. Hence, a better understanding of these representa-693 tions by grounding them in linguistic theory and relating them to neural activity through 694 mapping models, may further our understanding of how CS meaning is represented in the 695 brain. Furthermore, as LLMs also start from LS representations, they serve as examples 696 of systems that construct approximate CS representations trough non-linear mappings 697 rather than formal, rule-based mathematical machinery, offering a means to investigate 698 such mappings on a large scale. 699

4.2 Compositionality is continuous

The LS and CS models of meaning that are assumed by RI theory account for fundamen-701 tally distinct types of knowledge. The LS model is assumed to capture the conceptual 702 structure and similarity that is associated with semantic memory. This includes con-703 ceptual knowledge regarding semantic categories and features, for instance regarding 704 taxonomy (e.g., is animate, is mammal), function (e.g., is edible, cutting tool), and 705 visual form (e.g., has legs, made of steel) (McRae et al., 2005). While RI theory is agnostic about the precise nature of these LS representations, the neurocomputational 707 instantiation employs DLS representations deriving from word co-occurrences to capture 708 conceptual similarity (based on Rohde et al., 2009; see Brouwer et al., 2017). RI theory 709

does, however, critically assume the LS meaning space to be continuous in nature; that is, since the N400 has also been shown to be sensitive in a graded manner to the degree of semantic similarity (in terms of features and/or categories; see e.g., Boddy, 1981; Bentin et al., 1985; Federmeier and Kutas, 1999), the LS meaning space should capture gradient conceptual similarity. More concretely, concepts such as *bar* and *restaurant* should have a certain degree of similarity within the LS meaning space, capturing that both have shared semantic features like *is location*, *sells food*, but also that they are associated with different features such as *bar tender* and *has waiter*, respectively.

RI theory asserts that retrieved LS meaning is integrated into an utterance-wide CS representation on a word-by-word basis. More formally, utterance representations are assumed to be dynamic in the sense that the CS meaning is captured in terms of 'context-change potential' (Nouwen et al., 2022); CS representations provide both a representation of the utterance so far, as well as a context for the retrieval of LS meaning associated with incoming words and the integration of this meaning into an updated CS representation. As such, RI assumes that the CS model allows for incremental composition of utterance-level meaning — similar to the way in which a dynamic semantic framework such as Discourse Representation Theory formalizes meaning construction.

Furthermore, the CS representations assumed by RI should not only capture literal utterance-level entailments that are the focus of standard truth-conditional semantic theories, but should also support probabilistic inferences that reflect 'world knowledge'-driven expectations; that is, since the P600 has been shown to have graded sensitivity to 'world knowledge'-driven plausibility manipulations (Aurnhammer et al., 2023), the integrative composition of CS representations should capture this gradedness. Indeed, the representations from the DFS framework (Venhuizen et al., 2022), which formalize CS meaning in the most recent computational instantiation of RI theory (Brouwer et al., 2021b), have been shown to capture graded 'world knowledge'-driven inferences as part of a high-dimensional propositional meaning space. Comprehension in the model can be

conceptualized as navigating this meaning space on a word-by-word basis, and trajectories through this space are influenced by the linguistic experience that the model is
exposed to, such that gradedness can also arise from differences in utterance frequencies.

In this model, CS meaning reflects propositional structure and similarity independent of
feature-based LS similarity; that is, in the CS meaning space, sub-propositional meaning
representations that pertain to concepts such as bar and restaurant are highly dissimilar,
since the proposition enter(mike,bar), for instance, leads to a probabilistic inference that call(mike,bartender), while it entails the negation $\neg enter(mike,restaurant)$.

Critically, RI assumes that LS and CS meaning reside in distinct, but interacting 745 meaning spaces, and that both of these meaning spaces are continuous in nature. As 746 a result, the non-linear mapping from LS representations into a CS meaning space is in itself taken to be a continuous process, in that changes in contextually activated 748 conceptual LS knowledge during comprehension will affect utterance-level CS meaning 749 in a non-linear manner. Furthermore, the non-linear mapping from LS representations 750 into a CS space may generalize beyond the concepts and propositional state-of-affairs 751 that the comprehension system has experienced, thereby providing a basis for produc-752 tivity and systematicity of language use, within the confines of these spaces themselves. 753 That is, because the meaning spaces themselves are structured and capture word- and 754 utterance-level inferences, models that describe compositional comprehension as a map-755 ping between these spaces can map novel combinations of LS representations into the 756 CS meaning space (productivity), and also construct novel CS meanings (systematicity), 757 under the assumption that these meanings can be interpreted within the CS meaning space (see also Frank et al., 2009; Calvillo et al., 2021). 759

760 4.3 Compositionality is expectation-based

Expectation-based theories of language comprehension hypothesize that the comprehension system continuously generates predictions about upcoming words given the unfold-

ing context, be it implicitly or explicitly. On Surprisal Theory, these predictions are directly related to processing effort, such that the more unexpected an incoming word 764 is, the higher its processing difficulty, e.g., as measured using reading times (Hale, 2001; 765 Levy, 2008). Indeed, the cyclic nature of RI theory renders it inherently expectation-766 based: the top-down CS context affects both expectations about the conceptual LS 767 meaning associated with an incoming word, as well as expectations about CS meaning 768 resulting from integrating this LS meaning (see also Aurnhammer et al., 2021; Venhuizen 769 and Brouwer, 2025). The degree of contextual expectations leads to graded predictions 770 regarding N400 and P600 modulations, where the retrieval processes underlying the N400 771 are modulated by the degree to which LS features are pre-activated by the context, and 772 the integration processes underlying the P600 by what can effectively be conceptualized 773 as "comprehension-centric" surprisal—the likelihood of the current state in CS space 774 given the previous state (Venhuizen et al., 2019a; Brouwer et al., 2021b). 775

The expectation-based nature of RI theory raises the question of what drives expectations about LS and CS meaning. Starting with CS meaning, expectations are directly conditioned on the current state in the CS meaning space. As each state inherently carries its own probability in the world, as well as its co-occurrence probability with other points in the meaning space, each word-induced transition in meaning space may be more or less expected within the CS space itself. In other words, world knowledge determines which states in the meaning space are positioned close to each other, thereby driving expectations regarding upcoming linguistic input. Critically, however, these transitions in meaning space are also modulated by the linguistic experience that is captured by the mapping from LS to CS representations in terms of the frequency with which certain combinations of LS meanings are mapped onto CS meanings (Venhuizen et al., 2019a). This linguistic experience reflects how often states-of-affairs are talked about in language, independent of their probability in the world. Expectations deriving from linguistic experience may often be in agreement with those deriving from

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world knowledge, e.g., when describing a canonical situation like "John entered the cinema and ordered steak/popcorn", where the continuation "steak" is unexpected both in terms of our knowledge of the world and in terms of how frequently this situation would be described. Critically, however, world knowledge and linguistic experience may also disagree; that is, there are highly likely states-of-affairs (expected according to world knowledge) that are very uninformative and unlikely to be talked about (unexpected according to linguistic experience), e.g., "Mary drove through a green light". Indeed, it is far more likely to hear someone state that "Mary drove through a red light", as this indicates a state-of-affairs that less probable to occur in the world (assuming Mary re-spects traffic laws). This shows that expectations about CS meaning are thus driven by the propositional co-occurrence structure of the CS space itself, as well as by bottom-up linguistic experience (see Venhuizen et al., 2019a, for discussion).

Expectations about LS meaning, in turn, derive from an interplay between the top-down propositional co-occurrence structure of the CS space, bottom-up linguistic experience, as well as world knowledge-driven conceptual structure of semantic memory. First of all, the mapping of word form onto a LS meaning representation—i.e., retrieval of word meaning—is modulated by top-down CS context, meaning that similar CS contexts will lead to the anticipation of similar LS meanings. Which LS meanings are anticipated in a given CS context, however, is determined by linguistic experience; that is, it is linguistic experience that shapes the relative strength of the association between a given CS context and specific LS meanings. Finally, LS meanings that are positioned relatively close in the conceptual meaning space will share activation patterns and may therefore also influence lexical-level expectations. Hence, expectations about both LS and CS meaning are modulated by the linguistic experience that the system is exposed to, as well as both conceptual and propositional world knowledge (see also Troyer and Kutas, 2020a,b, for direct empirical investigations of the influence of world knowledge on word processing).

4.4 Compositionality is spatiotemporally extended

The functional-anatomic mapping of RI theory assumes a spatial segregation between 818 the epicenters/hubs for retrieval and integration in terms of the lpMTG (plus association 819 cortices) and IFG, respectively (Brouwer and Hoeks, 2013). This spatial segregation can 820 be addressed using mapping models, as discussed in Section 3.3. At a bare minimum, 821 this means that mapping model investigations into LS meaning, CS meaning, and the 822 compositional process should honor this segregation: the lpMTG and association cor-823 tices are predicted to be more involved in LS retrieval, whereas the IIFG is predicted to be more focally involved in CS integration. This state of affairs is, however, further com-825 plicated by the temporal dynamics of the assumed retrieval and integration processes; 826 that is, the retrieval and integration processes are known to be active simultaneously, 827 leading the N400 and P600 to spatiotemporally overlap in the scalp-recorded ERP sig-828 nal (see Delogu et al., 2019, 2021; Brouwer et al., 2021a; Delogu et al., 2025). Beyond 829 complications for interpreting this scalp-recorded ERP signal (see Brouwer and Crocker, 2017, for discussion), this implies that the compositional process is also spatiotemporally 831 extended. As a consequence, mapping models should take both the spatial and tempo-832 ral dynamics of the compositional process into account. Going forward, we should thus 833 disentangle LS and CS representation in space, by building mapping models that target 834 data from neuroimaging methods with high spatial resolution such as fMRI, as well as 835 in time, through mapping models targeting data from neuroimaging methods with high 836 temporal resolution such as electroencephalography (EEG). To synthesize the results on 837 space and time, mapping models could be complemented by neurocomputational models 838 that explicate the spatiotemporal dynamics underlying compositionality in comprehen-839 sion, such as a temporally-extended version of the neurocomputational instantiation of 840 RI theory (see Brouwer et al., 2017, section 5.4, for discussion).

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5 Conclusions

Formal modeling approaches in linguistic theory and the neurocognition of language 843 comprehension are both concerned with the question of how meaning is represented and 844 constructed from linguistic signal. The principle of compositionality, which assumes 845 that the meaning of a complex expression is defined as a function of the meaning of its parts and the way they are combined, has long been a hallmark of formal semantic ap-847 proaches. Extant models of semantic theory, however, focus on either capturing lexical 848 semantic meaning in terms of the conceptual knowledge and structure, or compositional 849 meaning in terms of truth-conditional entailments and inferences. Attempts at directly 850 integrating these models of lexical semantics with models of utterance-level composi-851 tional semantics—to formalize a single semantic framework for compositional meaning 852 representation and construction—have proven challenging, and question the validity of 853 this endeavor. On the other hand, recent neurocognitive theorizing and modeling reveals 854 an architecture for language comprehension that assumes Retrieval-Integration cycles, in 855 which word-by-word processing involves the retrieval of lexical semantic word meaning 856 from long-term memory, and the integration of these lexical semantic meanings into a 857 coherent representation of compositional semantic utterance meaning. 858

Combining insights from linguistic theory regarding the nature of the representations for lexical semantics and utterance-level compositional semantics with the computational mechanisms assumed to underlie Retrieval-Integration cycles, paints a picture in which compositional meaning construction harnesses two separate, but interacting models of meaning—one for lexical semantics and one for compositional semantics—that dynamically interact during the incremental process of word-by-word meaning construction. Within this architecture, compositionality arises from a non-linear mapping of lexical semantic representations into a space for utterance-level compositional meaning. This results in a notion of compositional integration, which emphasizes the continuous nature

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of the compositional process and its underlying representations, the expectation-based dynamics of word-by-word meaning composition, as well as the observation that incremental meaning construction is a spatiotemporally-extended process in the brain. This novel perspective on compositionality—centered around two models of meaning—thus combines insights from linguistic and neurocognitive theory, and serves as a starting point for more integrative, interdisciplinary approaches towards modeling the representation and computation of the meaning of words, sentences, and larger discourses.

References

- Asher, N. and Lascarides, A. (2003). *Logics of Conversation*. Cambridge University
 Press.
- Asher, N., Van de Cruys, T., Bride, A., and Abrusán, M. (2016). Integrating type
 theory and distributional semantics: a case study on adjective—noun compositions.

 Computational Linguistics, 42(4):703–725.
- Aurnhammer, C., Delogu, F., Brouwer, H., and Crocker, M. W. (2023). The P600 as a continuous index of integration effort. *Psychophysiology*, 60:e14302.
- Aurnhammer, C., Delogu, F., Schulz, M., Brouwer, H., and Crocker, M. W. (2021).

 Retrieval (N400) and integration (P600) in expectation-based comprehension. *PLOS*ONE, 16(9):e0257430.
- Baroni, M., Bernardi, R., and Zamparelli, R. (2014). Frege in space: A program of compositional distributional semantics. Linguistic Issues in Language Technology (LiLT),
 9:241–346.
- Baroni, M. and Zamparelli, R. (2010). Nouns are vectors, adjectives are matrices: Representing adjective-noun constructions in semantic space. In *Proceedings of the 2010*

- 891 Conference on Empirical Methods in Natural Language Processing, pages 1183–1193.
- Association for Computational Linguistics.
- Beltagy, I., Roller, S., Cheng, P., Erk, K., and Mooney, R. J. (2016). Representing
- meaning with a combination of logical and distributional models. Computational
- linguistics, 42(4):763–808.
- 896 Bentin, S., McCarthy, G., and Wood, C. C. (1985). Event-related potentials, lexical
- decision and semantic priming. Electroencephalography and clinical Neurophysiology,
- 60(4):343-355.
- Boddy, J. (1981). Evoked potentials and the dynamics of language processing. Biological
- 900 Psychology, 13:125–140.
- 901 Bornkessel-Schlesewsky, I. and Schlesewsky, M. (2008). An alternative perspective on
- "semantic P600" effects in language comprehension. Brain research reviews, 59(1):55–
- 903 73.
- 904 Brouwer, H. and Crocker, M. W. (2017). On the proper treatment of the N400 and P600
- in language comprehension. Frontiers in Psychology, 8:1327.
- 906 Brouwer, H., Crocker, M. W., Venhuizen, N. J., and Hoeks, J. C. (2017). A neurocom-
- putational model of the N400 and the P600 in language processing. Cognitive Science,
- 908 41:1318-1352.
- Brouwer, H., Delogu, F., and Crocker, M. W. (2021a). Splitting event-related potentials:
- Modeling latent components using regression-based waveform estimation. European
- Journal of Neuroscience, 53(4):974-995.
- Brouwer, H., Delogu, F., Venhuizen, N. J., and Crocker, M. W. (2021b). Neurobehav-
- 913 ioral correlates of surprisal in language comprehension: A neurocomputational model.
- 914 Frontiers in Psychology, 12:615538.

- Brouwer, H., Fitz, H., and Hoeks, J. (2012). Getting real about semantic illusions:
- Rethinking the functional role of the P600 in language comprehension. Brain Research,
- 917 1446:127–143.
- Brouwer, H. and Hoeks, J. C. (2013). A time and place for language comprehension:
- Mapping the N400 and the P600 to a minimal cortical network. Frontiers in Human
- 920 Neuroscience, 7:758.
- 921 Burgess, C. (1998). From simple associations to the building blocks of language: Mod-
- eling meaning in memory with the HAL model. Behavior Research Methods, Instru-
- ments, & Computers, 30(2):188-198.
- ⁹²⁴ Calvillo, J., Brouwer, H., and Crocker, M. W. (2021). Semantic systematicity in con-
- nectionist language production. *Information*, 12(8):329.
- 926 Carnap, R. (1988). Meaning and necessity: A study in semantics and modal logic,
- volume 30. University of Chicago Press.
- ⁹²⁸ Chomsky, N. (1957). Syntactic Structures. Mouton & Co., N.V., 's-Gravenhage, Nether-
- 929 lands.
- 930 Clark, S. (2012). Vector space models of lexical meaning. In Lappin, S. and Fox, C.,
- editors, Handbook of Contemporary Semantics-second edition, pages 493–522. Wiley-
- 932 Blackwell.
- 933 Coecke, B., Sadrzadeh, M., and Clark, S. (2010). Mathematical foundations for a com-
- positional distributional model of meaning. arXiv preprint arXiv:1003.4394.
- 935 Coecke, M. S. B. and Clark, S. (2011). Mathematical foundations for a compositional
- distributional model of meaning. In Festschrift for Joachim Lambek, volume 36 of
- 937 Linguistic Analysis, pages 345–384. Linguistic Analysis.

- Davidson, D. (1969). The individuation of events. In Essays in honor of Carl G. Hempel:
- A tribute on the occasion of his sixty-fifth birthday, pages 216–234. Springer.
- Delogu, F., Aurnhammer, C., Brouwer, H., and Crocker, M. W. (2025). On the biphasic
- nature of the n400-p600 complex underlying language comprehension. Brain and
- 942 Cognition, 186:106293.
- Delogu, F., Brouwer, H., and Crocker, M. W. (2019). Event-related potentials index
- lexical retrieval (N400) and integration (P600) during language comprehension. Brain
- and Cognition, 135:103569.
- Delogu, F., Brouwer, H., and Crocker, M. W. (2021). When components collide: Spa-
- tiotemporal overlap of the N400 and P600 in language comprehension. Brain Research,
- 948 1766:147514.
- Devlin, J., Chang, M.-W., Lee, K., and Toutanova, K. (2019). Bert: Pre-training of
- 950 deep bidirectional transformers for language understanding. In *Proceedings of the*
- 951 2019 conference of the North American chapter of the association for computational
- 952 linguistics: human language technologies, volume 1 (long and short papers), pages
- 953 4171-4186.
- ⁹⁵⁴ Erk, K. (2012). Vector space models of word meaning and phrase meaning: A survey.
- Language and Linguistics Compass, 6(10):635-653.
- 956 Federmeier, K. D. (2022). Connecting and considering: Electrophysiology provides in-
- 957 sights into comprehension. *Psychophysiology*, 59(1):e13940.
- 958 Federmeier, K. D. and Kutas, M. (1999). A rose by any other name: Long-term memory
- 959 structure and sentence processing. Journal of memory and Language, 41(4):469–495.
- Federmeier, K. D. and Laszlo, S. (2009). Time for meaning: Electrophysiology provides

- insights into the dynamics of representation and processing in semantic memory. Psy-
- chology of learning and motivation, 51:1-44.
- Firth, J. (1957). A synopsis of linguistic theory, 1930-1955. Studies in linguistic analysis,
- 964 pages 10–32.
- 965 Frank, S. L., Haselager, W. F., and van Rooij, I. (2009). Connectionist semantic sys-
- 966 tematicity. Cognition, 110(3):358–379.
- 967 Frisby, S. L., Halai, A. D., Cox, C. R., Ralph, M. A. L., and Rogers, T. T. (2023).
- Decoding semantic representations in mind and brain. Trends in Cognitive Sciences,
- 27(3):258-281.
- 970 Garrette, D., Erk, K., and Mooney, R. (2014). A formal approach to linking logical form
- and vector-space lexical semantics. In *Computing meaning*, pages 27–48. Springer.
- 972 Geurts, B. and Maier, E. (2013). Layered Discourse Representation Theory. In Capone,
- A., Piparo, F. L., and Carapezza, M., editors, Perspectives on Linguistic Pragmatics,
- pages 311–327. Springer International Publishing.
- 975 Golden, R. M. and Rumelhart, D. E. (1993). A parallel distributed processing model of
- story comprehension and recall. Discourse processes, 16(3):203–237.
- 977 Goldstein, A., Zada, Z., Buchnik, E., Schain, M., Price, A., Aubrey, B., Nastase, S. A.,
- Feder, A., Emanuel, D., Cohen, A., et al. (2022). Shared computational principles
- for language processing in humans and deep language models. Nature neuroscience,
- 25(3):369-380.
- Gouvea, A. C., Phillips, C., Kazanina, N., and Poeppel, D. (2010). The linguistic
- processes underlying the p600. Language and cognitive processes, 25(2):149–188.
- 983 Grefenstette, E. and Sadrzadeh, M. (2015). Concrete models and empirical evaluations

- for the categorical compositional distributional model of meaning. Computational
 Linguistics, 41(1):71–118.
- 986 Hale, J. T. (2001). A probabilistic Earley parser as a psycholinguistic model. In Pro-
- ceedings of the second meeting of the North American Chapter of the Association for
- ⁹⁸⁸ Computational Linquistics on Language technologies, pages 1–8, Stroudsburg, PA. As-
- 989 sociation for Computational Linguistics.
- 990 Hoeks, J. C. J. and Brouwer, H. (2014). Electrophysiological research on conversation
- and discourse processing. In Holtgraves, T. M., editor, The Oxford Handbook of Lan-
- guage and Social Psychology, pages 365–386. New York: Oxford University Press.
- Johnson-Laird, P. N. (1983). Mental models: Towards a cognitive science of language,
- inference, and consciousness. Harvard University Press, Cambridge, MA.
- 895 Kamp, H. (1980). Some remarks on the logic of change, Part I. In Rohrer, C., editor,
- 996 Time, Tense, and Quantifiers: Proceedings of the Stuttgart Conference on the Logic of
- 7997 Tense and Quantification,, pages 135–180. Max Niemeyer Verlag, Berlin, New York.
- 998 Kamp, H. (1981). A theory of truth and semantic representation. In Groenendijk, J.
- A. G., Janssen, T. M. V., and Stokhof, M. B. J., editors, Formal Methods in the
- study of Language, Proceedings of the Third Amsterdam Colloquium, pages 277–322,
- 1001 Amsterdam. Mathematisch Centrum.
- 1002 Kamp, H. and Reyle, U. (1993). From discourse to logic: Introduction to modeltheoretic
- semantics of natural language, formal logic and Discourse Representation Theory.
- Kluwer, Dordrecht.
- Kamp, H., van Genabith, J., and Reyle, U. (2011). Discourse Representation Theory.
- In Gabbay, D. M. and Guenthner, F., editors, Handbook of Philosophical Logic, vol-
- ume 15, pages 125–394. Springer Netherlands.

- King, J.-R. and Dehaene, S. (2014). Characterizing the dynamics of mental representa-
- tions: the temporal generalization method. Trends in cognitive sciences, 18(4):203–
- 1010 210.
- Krieger, B., Brouwer, H., Aurnhammer, C., and Crocker, M. W. (2024). On the limits of
- llm surprisal as functional explanation of erps. In Proceedings of the Annual Meeting
- of the Cognitive Science Society, volume 46.
- Kuperberg, G. R. (2007). Neural mechanisms of language comprehension: Challenges
- to syntax. Brain Research, 1146:23–49.
- Kutas, M. (1993). In the company of other words: Electrophysiological evidence for
- single-word and sentence context effects. Language and cognitive processes, 8(4):533–
- 1018 572.
- 1019 Kutas, M. and Federmeier, K. D. (2000). Electrophysiology reveals semantic memory
- use in language comprehension. Trends in Cognitive Sciences, 4(12):463–470.
- 1021 Kutas, M. and Federmeier, K. D. (2011). Thirty years and counting: finding meaning
- in the N400 component of the event-related brain potential (ERP). Annual Review of
- 1023 Psychology, 62:621–647.
- 1024 Kutas, M. and Hillyard, S. A. (1980). Reading senseless sentences: Brain potentials
- reflect semantic incongruity. Science, 207(4427):203–205.
- 1026 Kutas, M. and Hillyard, S. A. (1984). Brain potentials during reading reflect word
- expectancy and semantic association. *Nature*, 307(5947):161–163.
- 1028 Kutas, M., van Petten, C., and Kluender, R. (2006). Psycholinguistics electrified II:
- 1994–2005. In Traxler, M. J. and Gernsbacher, M. A., editors, Handbook of Psy-
- cholinquistics, 2nd Edition, pages 659–724. Elsevier, New York.

- Landauer, T. K. and Dumais, S. T. (1997). A solution to Plato's problem: The latent
- semantic analysis theory of acquisition, induction, and representation of knowledge.
- Psychological Review, 104(2):211-240.
- Lau, E. F., Phillips, C., and Poeppel, D. (2008). A cortical network for semantics:
- (de)constructing the N400. Nature Reviews Neuroscience, 9(12):920–933.
- Lenci, A. (2018). Distributional models of word meaning. Annual review of Linguistics,
- 1037 4:151–171.
- Levy, R. (2008). Expectation-based syntactic comprehension. Cognition, 106(3):1126–
- 1039 1177.
- McRae, K., Cree, G. S., Seidenberg, M. S., and McNorgan, C. (2005). Semantic feature
- production norms for a large set of living and nonliving things. Behavior Research
- Methods, 37(4):547-559.
- Mikolov, T., Chen, K., Corrado, G., and Dean, J. (2013a). Efficient estimation of word
- representations in vector space. arXiv preprint arXiv:1301.3781.
- Mikolov, T., Sutskever, I., Chen, K., Corrado, G. S., and Dean, J. (2013b). Distributed
- representations of words and phrases and their compositionality. Advances in neural
- information processing systems, 26.
- 1048 Mitchell, J. and Lapata, M. (2010). Composition in distributional models of semantics.
- Cognitive Science, 34(8):1388-1429.
- Mitchell, T. M., Shinkareva, S. V., Carlson, A., Chang, K.-M., Malave, V. L., Mason,
- R. A., and Just, M. A. (2008). Predicting human brain activity associated with the
- meanings of nouns. science, 320(5880):1191–1195.
- 1053 Montague, R. (1970). Universal grammar. *Theoria*, 36(3):373–398.

- Muskens, R. (1996). Combining Montague semantics and discourse representation. *Lin-*guistics and Philosophy, 19(2):143–186.
- Näätänen, R. and Picton, T. (1987). The N1 wave of the human electric and magnetic
- response to sound: a review and an analysis of the component structure. Psychophys-
- iology, 24(4):375-425.
- Nouwen, R., Brasoveanu, A., van Eijck, J., and Visser, A. (2022). Dynamic Semantics.
- In Zalta, E. N. and Nodelman, U., editors, The Stanford Encyclopedia of Philosophy.
- Metaphysics Research Lab, Stanford University, Fall 2022 edition.
- Padó, S. and Lapata, M. (2007). Dependency-based construction of semantic space models. *Computational linguistics*, 33(2):161–199.
- Partee, B. H. (1995). Lexical semantics and compositionality. In Gleitman, L., Liberman,
- M., and Osherson, D. N., editors, An Invitation to Cognitive Science, Volume 1:
- Language, pages 311–360. The MIT press, Cambridge, MA, 2nd edition.
- Pavlick, E. (2022). Semantic structure in deep learning. Annual Review of Linguistics, 8:447–471.
- Pennington, J., Socher, R., and Manning, C. D. (2014). Glove: Global vectors for word
- 1070 representation. In Proceedings of the 2014 conference on empirical methods in natural
- language processing (EMNLP), pages 1532–1543.
- Pereira, F., Lou, B., Pritchett, B., Ritter, S., Gershman, S. J., Kanwisher, N., Botvinick,
- M., and Fedorenko, E. (2018). Toward a universal decoder of linguistic meaning from
- brain activation. Nature communications, 9(1):963.
- Peters, M. E., Neumann, M., Iyyer, M., Gardner, M., Clark, C., Lee, K., and Zettle-
- moyer, L. (2018). Deep contextualized word representations. In Walker, M., Ji, H., and

- Stent, A., editors, Proceedings of the 2018 Conference of the North American Chap-
- 1078 ter of the Association for Computational Linguistics: Human Language Technologies,
- Volume 1 (Long Papers), pages 2227–2237, New Orleans, Louisiana. Association for
- 1080 Computational Linguistics.
- Poldrack, R. A. (2011). Inferring mental states from neuroimaging data: from reverse inference to large-scale decoding. *Neuron*, 72(5):692–697.
- Radford, A., Wu, J., Child, R., Luan, D., Amodei, D., and Sutskever, I. (2019). Language models are unsupervised multitask learners. *OpenAI*. Accessed: 2024-11-15.
- Rohde, D. L. T., Gonnerman, L. M., and Plaut, D. C. (2009). An improved model of semantic similarity based on lexical co-occurrence. *Cognitive Science*, pages 1–33.
- Schrimpf, M., Blank, I. A., Tuckute, G., Kauf, C., Hosseini, E. A., Kanwisher, N.,
- Tenenbaum, J. B., and Fedorenko, E. (2021). The neural architecture of language:
- Integrative modeling converges on predictive processing. Proceedings of the National
- 1090 Academy of Sciences, 118(45):e2105646118.
- Socher, R., Huval, B., Manning, C. D., and Ng, A. Y. (2012). Semantic compositionality
- through recursive matrix-vector spaces. In Proceedings of the 2012 joint conference on
- empirical methods in natural language processing and computational natural language
- learning, pages 1201–1211. Association for Computational Linguistics.
- Tang, J., LeBel, A., Jain, S., and Huth, A. G. (2023). Semantic reconstruction of continu-
- ous language from non-invasive brain recordings. Nature Neuroscience, 26(5):858–866.
- Troyer, M. and Kutas, M. (2020a). Harry potter and the chamber of what?: The impact
- of what individuals know on word processing during reading. Language, cognition and
- neuroscience, 35(5):641-657.

- 1100 Troyer, M. and Kutas, M. (2020b). To catch a snitch: Brain potentials reveal variability
- in the functional organization of (fictional) world knowledge during reading. Journal
- of Memory and Language, 113:104111.
- Turney, P. D. and Pantel, P. (2010). From frequency to meaning: Vector space models
- of semantics. Journal of artificial intelligence research, 37:141–188.
- van Berkum, J. J. A. (2009). The 'neuropragmatics' of simple utterance comprehension:
- An ERP review. In Sauerland, U. and Yatsushiro, K., editors, Semantics and Prag-
- matics: From experiment to theory, pages 276–316. Palgrave Macmillan, Basingstoke.
- Van Petten, C. and Luka, B. J. (2012). Prediction during language comprehension: Ben-
- efits, costs, and erp components. International journal of psychophysiology, 83(2):176–
- 1110 190.
- 1111 Vecchi, E. M., Marelli, M., Zamparelli, R., and Baroni, M. (2017). Spicy adjectives
- and nominal donkeys: Capturing semantic deviance using compositionality in distri-
- butional spaces. Cognitive science, 41(1):102–136.
- Venhuizen, N. J., Bos, J., Hendriks, P., and Brouwer, H. (2018). Discourse semantics
- with information structure. Journal of Semantics, 35(1):127–169.
- Venhuizen, N. J. and Brouwer, H. (2025). Referential retrieval and integration in lan-
- guage comprehension: An electrophysiological perspective. *Psychological Review*.
- ¹¹¹⁸ Venhuizen, N. J., Crocker, M. W., and Brouwer, H. (2019a). Expectation-based com-
- prehension: Modeling the interaction of world knowledge and linguistic experience.
- $Discourse \ Processes, 56(3):229-255.$
- Venhuizen, N. J., Crocker, M. W., and Brouwer, H. (2019b). Semantic entropy in
- language comprehension. Entropy, 21(12):1159.

- ¹¹²³ Venhuizen, N. J., Hendriks, P., Crocker, M. W., and Brouwer, H. (2022). Distributional
- formal semantics. Information and Computation, 287:104763. Special Issue: Selected
- Papers from WoLLIC 2019, the 26th Workshop on Logic, Language, Information and
- 1126 Computation.
- Wittgenstein, L. (1953). Philosophical Investigations. Basil Blackwell, Oxford.
- ¹¹²⁸ Zwaan, R. A. and Radvansky, G. A. (1998). Situation models in language comprehension
- and memory. Psychological Bulletin, 123(2):162-185.