# Theory of Multi-Paradigm Programming Languages

Lecture 5-2

# Chapter 3 ML Programming Language

**Overview** 

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## 3.3 FUNCTION

```
fun square(x:int) = x*x;
val square = fn : int -> int
```

<프로그램 3-20> square Example

fun square  $x^{229}$ ) = (x:int)\*x;

<프로그램 3-20-1> square Example

```
1  square(3);
2  val it = 9 : int
```

<프로그램 3-21> square Example

```
fun member(x, nil) = false

member(x, y::ys) =

if x=y then true

else member(x, ys);

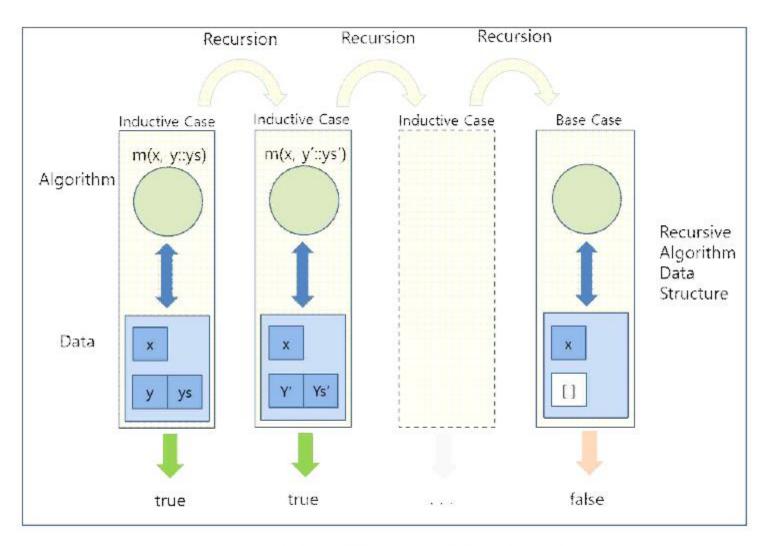
val member= fn : ''a * ''a list -> bool
```

<프로그램 3-22> member Example

```
Base Case
                     Pattern 1
                                                int member (int x, IL * 1)
                                                   if (!1)
fun member (x, nil)
                      = false
                                                      return false;
  | member(x, y::ys)| =
                                                   else
      if x=y
                                                      if (x == 1->y)
         then true
                                                         return true;
         else member(x, ys);
                                                      else
                                                         member (x, 1->next)
   Inductive Case
                     Pattern 2
```

<그림 3-8> Patterns

```
struct Integer_List
{
   int x;
   struct Integer_List * nest;
}
typedef struct Integer List IL;
```

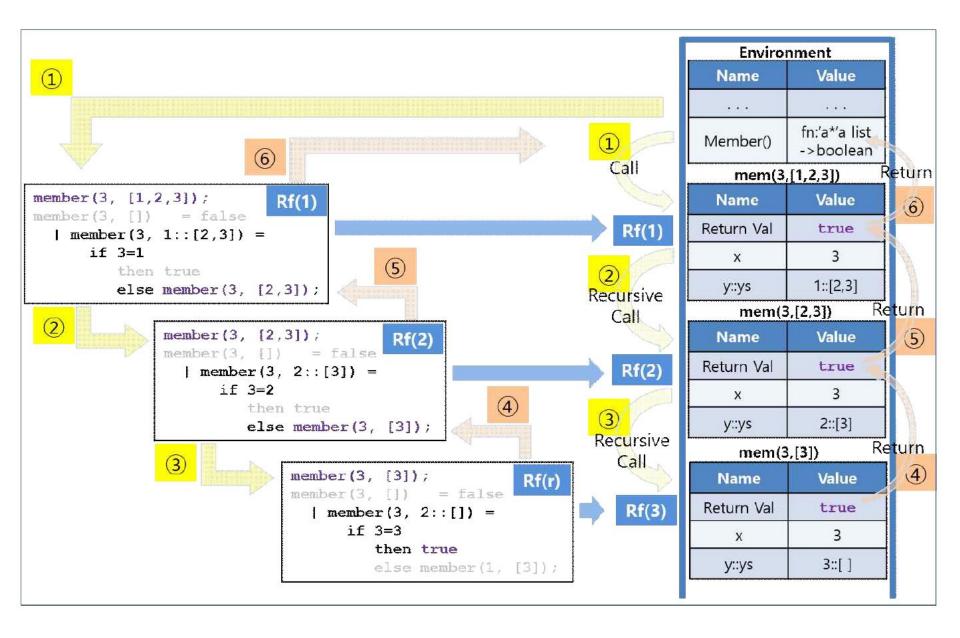


<그림 3-9> rAD 구조: member 함수

<프로그램 3-23> member Example

1	member(3,[1,2,3]);
2	val it = true : bool

<프로그램 3-24> member Example

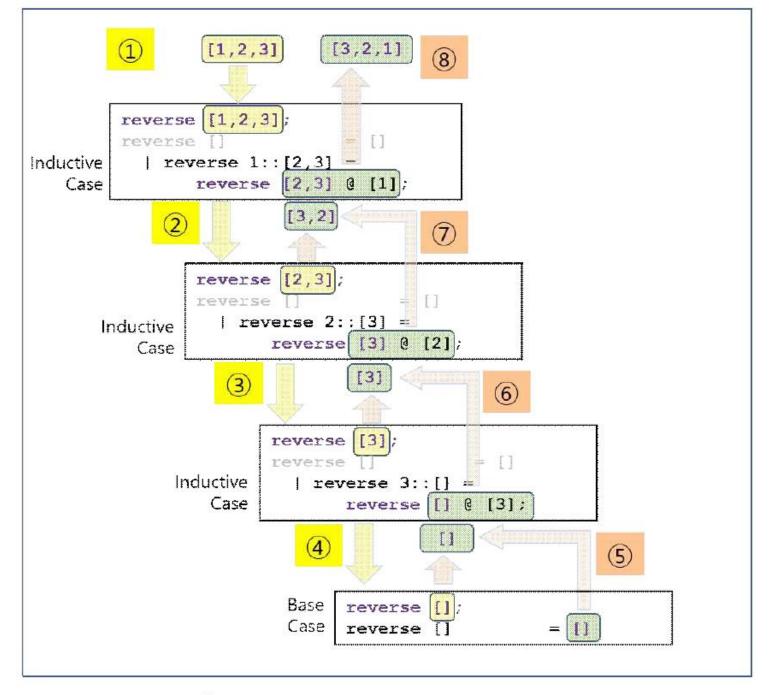


```
1  fun reverse([]) = []
2  | reverse(x::xs) =
3    reverse (xs) @ [x];
4  val reverse = fn : 'a list -> 'a list
```

<프로그램 3-25> reverse Example

```
1 reverse([1,2,3]);
2 val it = [3,2,1] : int list
```

<프로그램 3-26> reverse Example



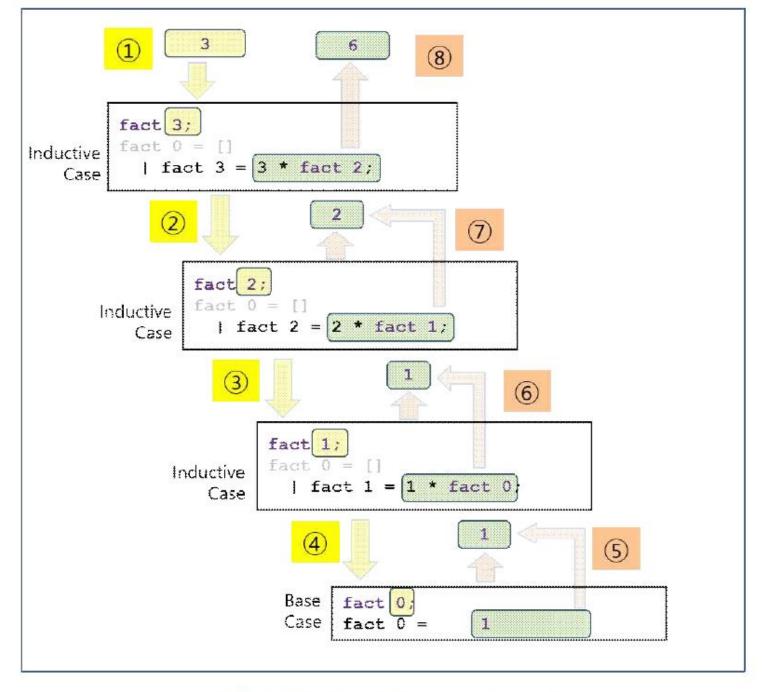
<그림 3-11> Execution for reverse [ 1,2,3]

```
1  fun fact 0 = 1
2  | fact n = n*fact(n-1);
3  val fact = fn : int -> int
```

<프로그램 3-27> fact Example

1	fact 3;
2	val it = 6 : int

<프로그램 3-28> fact Example

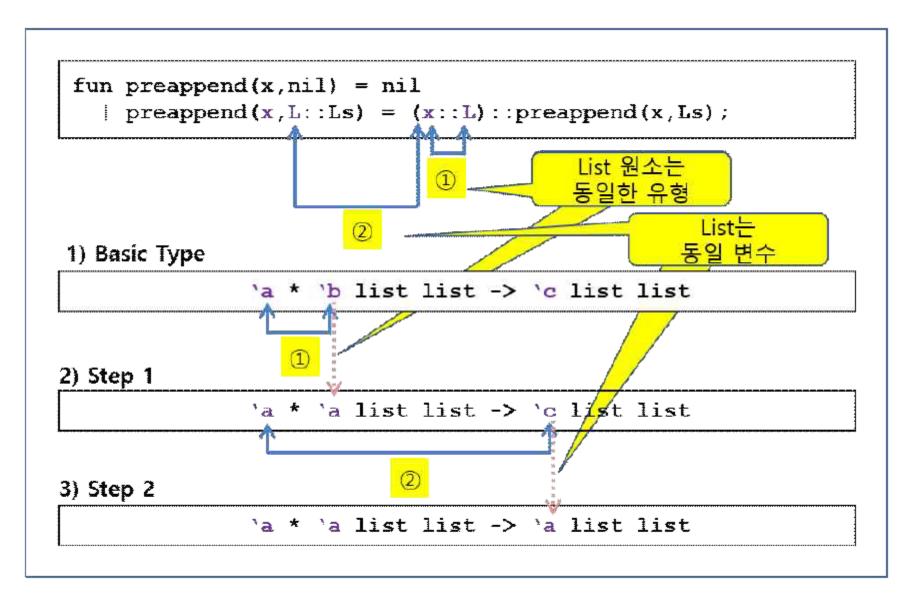


<그림 3-12> Execution for fact 3

```
let
   val <1st variable> = <1st expression>;
   val <2nd variable> = <2nd expression>;
        . . .
   val <1ast variable> = <1ast expression>
in
        <expression>
end
```

```
fun preappend(x,nil) = nil
    | preappend(x,L::Ls) = (x::L)::preappend(x,Ls);
    val preappend = fn : 'a * 'a list list -> 'a list list
```

<프로그램 3-29> preappend Example



<그림 3-13> Type Checking for preappend

```
preappend(1, [[],[2,3], [4,5,6]]);

val it = [[1], [[1,2,3], [1,4,5,6]] : int list list
```

<프로그램 3-30> preappend Example

```
[[1],[1,2,3],[1,4,5,6]]
       (1,[[],[2,3],[4,5,6]])
                                                                  8
preappend (1,[[],[2,3],[4,5,6]]);
fun preappend(x,nil) = nil
| preappend(1,[]::[[2,3],[4,5,6]]=(1::[])::preappend(1,[[2,3],[4,5,6]])
                                               [[1,2,3],[1,4,5,6]]
    (2)
       preappend (1,[[2,3],[4,5,6]]);
       fun preappend(x,nil) = nil
       | preappend(1, [2,3]::[[4,5,6]]=(1::[2,3])::preappend(1,[[4,5,6]]);
                                                          [[1,4,5,6]]
          (3)
                                                                                6
              preappend (1, [[4,5,6]]);
              fun preappend(x, nil) = nil
                                                           (1::[4,5,6])::preappend(1,[]);
              | preappend(1,[4,5,6]::[]=
                                                                                      (5)
                     preappend (1,[]);
                     fun preappend(x,nil)
                                                                                      nil.
```

<그림 3-14> Execution for preappend(1, [[],[2,3], [4,5,6]])

<프로그램 3-31> power\_set Example

```
1 power_set([1,2,3]);
2 val it = [[],[3],[2],[2,3],[1],[1,3],[1,2],[1,2,3]] : int list list
```

<프로그램 3-32> power\_set Example

```
[1,2,3]
                       [[],[3],[2],[2,3],[1],[1,3],[1,2],[1,2,3]]
                               8
PO(1)
power set [1,2,3]
    power set(1::[2,3]) =
                                              PO(2)
     let
                                              power set [2,3]
       val ps = power set([2,3]); (2)
                → [[],[3],[2],[2,3]];
     in
                                                   power set(2::[3]) =
                                                                                       PO(3)
       ps @ preappend(1,ps)
                                                    let
                                                                                       power set [3]
      preappend(1,[],[1,3],[2],[2,3]]
                                                      val ps = power set([3]);
          [3],[2],[2,3]] @
                                                                [[],[3]]
          [1], [1,3], [1,2], [1,2,3]]
                                                    in
                                                                                           power set(3::[]) =
    \rightarrow [[[, [3], [2], [2,3],
                                                                                            let
                                                                                                                              PO(4)
                                                              preappend (2, ps)
          [1],[1,3],[1,2],[1,2,3]]
                                                                                                                              power set []
                                                          preappend(2, [[], [3]])
                                                                                              val ps = power set([])
end:
                                                   → [[], [3]]@[[2], [2,3]]
                                                                                                         [[]];
                                                                                                                              fun power set([]) = [[]]
  (1)-①
                                                   \rightarrow [[[],[3],[2],[2,3]]]
                              (1)-10
                                                                                            in
                                                    end;
                                                                                              ps @ preappend(3, ps)
  (1,[[],[3],[2],[2,3])] [[],[3],[2],[2,3]))
                                                 (2)-①
                                                                                                    preappend(3,[[]])
                                                                   (2)-6
  PR(1,1)
                                                                                              [[]] 3 [[3]]
                                                (2,[[],[3]])
                                                                 [[2],[2,3]]
  or(1,[[],[3],[2],[2,3]]);
                                                                                           \rightarrow [[[],[3]]]
  pr(1,[]::[[3],[2],[2,3]]=
                                               PR(2,1)
                                                                                            end;
            (1::[])::pstl,[[3],[2],[2,3]]);
                                               cr(2,[[],[[3]]);
                                                                                                          (3)-(4)
                                                                                             (3)-①
          → [1]:: [[1,3],[1,2],[1,2,3]]
                                                or (2,0::[3]]=(2::0)::pr(2,[3]);
  PR(1,2) (1)-(2)
                                                                                              (3, [[]])
                                                             → [2]:: [[2,3]]
                                                                                                           [[3]]
                              (1)-9
  or(1,[[3],[2],[2,3]]);
                                                         (2)-2
                                                                        (2)-(5)
                                               PR(2,2)
  pr(1, [3] :: [[2], [2,3]] =
                                                                                         PR(3.1)
                                               cr(2,[[3]]);
            (1::[3])::mr(1,[ [2],[2,3]]);
                                                                                         or (3,[[]]);
                                               or (2,[3]::[=(2::[3])::pr(2,[]);
           _ [1,3]:: [[1,2],[1,2,3]]
                                                                                         pr (3,[]::[]=(3::[])::pr (3,[]);
                                                            → [[2,3]::
                                                                        []
  PR(1.3) (1)-3
                               (1)-(8)
                                                                                                        [3]::
                                                  PR(2,3) (2)-(3)
                                                                         (2)-4
  pr(1,[[2],[2,3]]);
                                                                                                       (3)-(2)
  pr(1,[2]::[[2,3]]=
                                                   pr(2,[]);
                                                                                            PR(3,2)
                                                                                                                      (3)-(3)
            (1::[2])::pr(1,[ [2,3]]);
                                                                     10
                                                   pr (2,[]=
                                                                                            pr(3,[]);
            [1,2]:: [1,2,3]]
                                                                                                                    117
                                                                                            pr (3, []=
  PR(1,4)
            (1)-(4)
                             (1)-7
  pr(1,[[2,3]]);
  pr(1, [2,3]::[]=
            (1::[2,3])::pr(1,5);
          _ [1,2,3]:
                          (1)-(3)
                             (1)-6
  PR(1,5)
  pr(1, []);
                       D;
  per (2, [])=
```