Intro to Statistical Learning with R, Lab 1

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Problem 1

Part A:

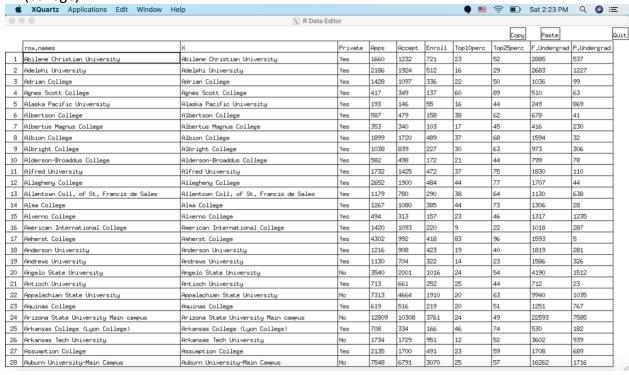
library (ISLR)

Loading Data

college=read.csv("/Users/hbyadav/Desktop/UMKC_spring_2020/Statistical Learning/LAB/Lab1/College.csv", header = TRUE, sep = ",")

rownames (college) = college[,1]

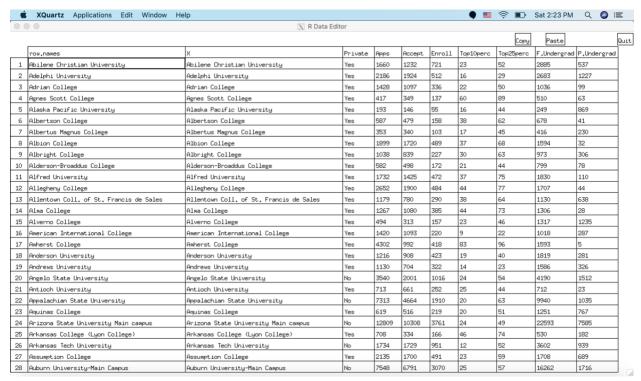
fix (college)



Part B:

college =college [,-1]

fix (college)



Part C:

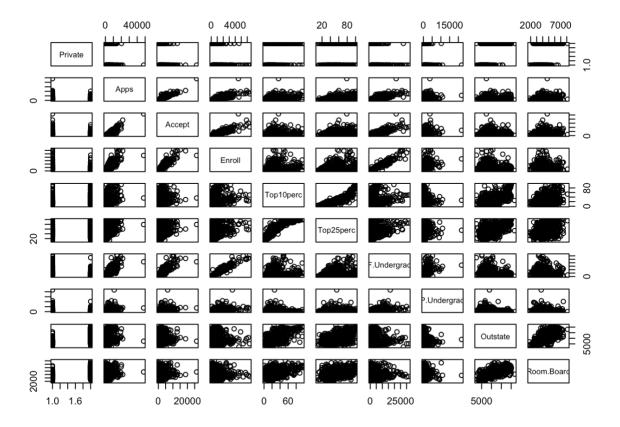
i. Use the summary() function to produce a numerical summary of the variables in the data set.

summary(College)						
##	Private	Apps		Accept	Enroll	Top10perc
##	No :212	Min. :	81 Min	. : 72	Min. : 35	Min. : 1.0
##	Yes:565	1st Qu.:	776 1st	Qu.: 604	1st Qu.: 242	1st Qu.:15.0
##		Median :	1558 Med:	ian : 1110	Median : 434	Median :23.0
##		Mean :	3002 Mean	n : 2019	Mean : 780	Mean :27.6
##		3rd Qu.:	3624 3rd	Qu.: 2424	3rd Qu.: 902	3rd Qu.:35.0
##		Max. :4	8094 Max	. :26330	Max. :6392	Max. :96.0
##	Top25pe	rc F.	Undergrad	P.Under	grad Outs	state
##	Min. :	9.0 Min	. : 139	Min. :	1 Min.	: 2340
##	1st Qu.:	41.0 1st	Qu.: 992	1st Qu.:	95 1st Qu.	: 7320
##	Median :	54.0 Med	lian : 1707	Median :	353 Median	: 9990
##	Mean :	55.8 Mea	n : 3700	Mean :	855 Mean	:10441
##	3rd Qu.:	69.0 3rd	Qu.: 4005	3rd Qu.:	967 3rd Qu.	:12925
##	Max. :1	00.0 Max	:31643	Max. :	21836 Max.	:21700

```
##
     Room.Board
                      Books
                                   Personal
                                                    PhD
          :1780
                 Min. : 96
                                     : 250
                                               Min. : 8.0
##
  Min.
                                Min.
   1st Qu.:3597
                  1st Qu.: 470
                                1st Qu.: 850
                                               1st Qu.: 62.0
   Median :4200
                  Median : 500
                                Median :1200
                                               Median: 75.0
   Mean
         :4358
                  Mean
                       : 549
                                Mean
                                       :1341
                                               Mean : 72.7
   3rd Qu.:5050
                  3rd Qu.: 600
                                3rd Qu.:1700
                                               3rd Qu.: 85.0
   Max.
          :8124
                  Max.
                         :2340
                                Max.
                                       :6800
                                               Max.
                                                     :103.0
##
      Terminal
                     S.F.Ratio
                                  perc.alumni
                                                    Expend
   Min.
        : 24.0
                   Min.
                       : 2.5
                                 Min.
                                      : 0.0
                                                Min.
                                                     : 3186
   1st Qu.: 71.0
                   1st Qu.:11.5
                                  1st Qu.:13.0
                                                1st Qu.: 6751
   Median: 82.0
                   Median :13.6
                                 Median :21.0
                                                Median: 8377
   Mean
         : 79.7
                   Mean
                        :14.1
                                  Mean
                                       :22.7
                                                Mean : 9660
   3rd Qu.: 92.0
                   3rd Qu.:16.5
                                  3rd Qu.:31.0
                                                3rd Qu.:10830
   Max.
          :100.0
                   Max.
                         :39.8
                                  Max.
                                        :64.0
                                                Max.
                                                       :56233
     Grad.Rate
##
   Min.
        : 10.0
   1st Qu.: 53.0
   Median: 65.0
   Mean
        : 65.5
   3rd Qu.: 78.0
##
   Max. :118.0
```

ii. Use the pairs() function to produce a scatterplot matrix of the first ten columns or variables of the data. Recall that you can reference the first ten columns of a matrix A using A[,1:10].

```
pairs(College[, 1:10])
```



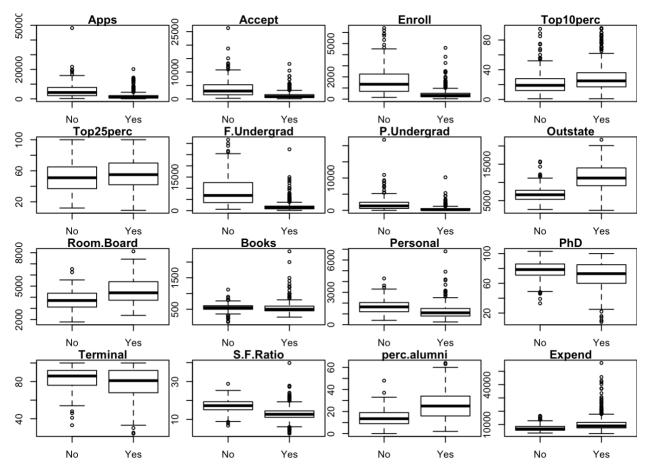
iii. Use the plot() function to produce side-by-side boxplots of Outstate versus Private.

Since the problem doesn't say which variable to make the boxplot for, I use all 16 other quantitative variables. In the par() command, mfrow=c(4, 4) makes a 4x4 panel plot, and mar=c(3,2,0,0) makes smaller margins around each plot - see ?par for explanations of these arguments. See ?boxplot for explanations of xlab, ylab, and main.

```
par(mfrow=c(4,4), mar=c(2, 2, 1, 0))

for (i in 2:17)

boxplot(College[, i] ~ College[, 1], xlab="", main=colnames(College)[i])
```

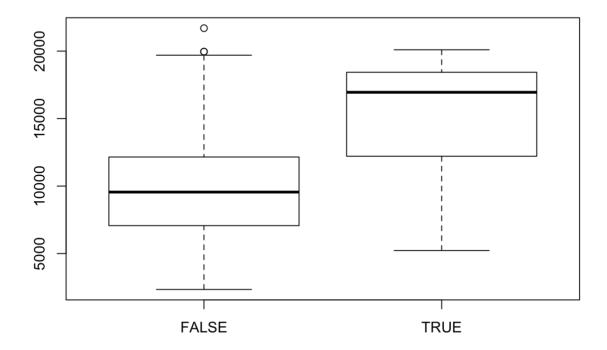


iv. Create a new qualitative variable, called Elite, by binning the Top10perc variable. We are going to divide universities into two groups based on whether or not the proportion of students coming from the top 10% of their high school classes exceeds 50 %. Use the summary() function to see how many elite univer- sities there are.

```
College$Elite <- College$Top10perc > 50
summary(College[, c("Top10perc", "Elite")])
##
      Top10perc
                      Elite
##
    Min.
           : 1.0
                    Mode :logical
    1st Qu.:15.0
                    FALSE: 699
##
##
    Median :23.0
                    TRUE: 78
            :27.6
                    NA's :0
##
    Mean
    3rd Qu.:35.0
##
            :96.0
##
    Max.
```

Now use the plot() function to produce side-by-side boxplots of Outstate versus Elite.

```
boxplot(Outstate ~ Elite, data=College)
```



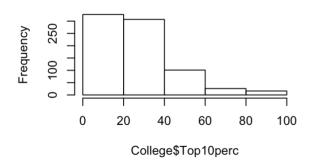
v. Use the hist() function to produce some histograms with differing numbers of bins for a few of the quantitative vari- ables. You may find the command par(mfrow=c(2,2)) useful: it will divide the print window into four regions so that four plots can be made simultaneously. Modifying the arguments to this function will divide the screen in other ways.

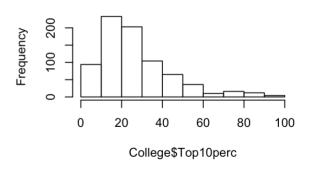
Just one example:

```
par(mfrow=c(2,2))
hist(College$Top10perc, breaks=5)
hist(College$Top10perc, breaks=10)
hist(College$Top10perc, breaks=20)
hist(College$Top10perc, breaks=40)
```

Histogram of College\$Top10perc

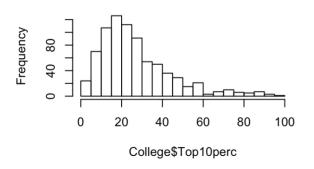
Histogram of College\$Top10perc

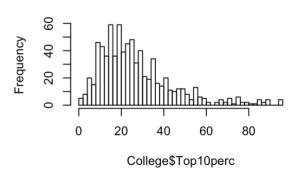




Histogram of College\$Top10perc

Histogram of College\$Top10perc





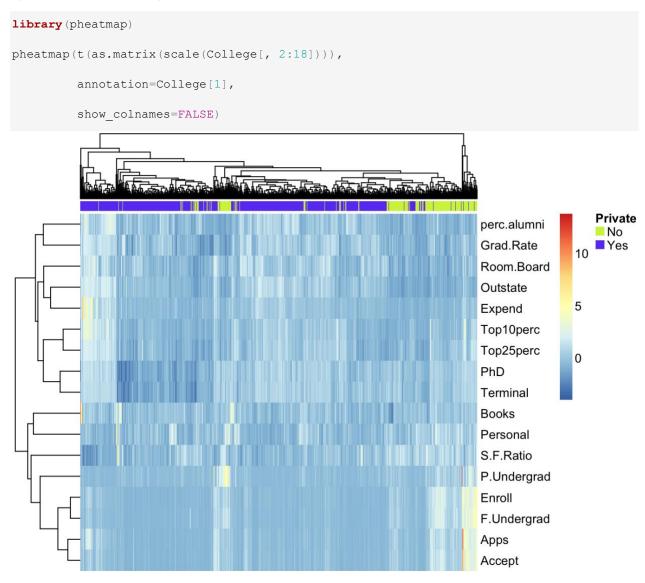
vi. Continue exploring the data, and provide a brief summary of what you discover.

How about a heatmap of the data. To help with interpretation, here's the codebook:

- Private: Public/private indicator
- Apps: Number of applications received
- Accept: Number of applicants accepted
- Enroll: Number of new students enrolled
- *Top10perc*: New students from top 10 % of high school class
- *Top25perc*: New students from top 25 % of high school class
- *F.Undergrad*: Number of full-time undergraduates
- P.Undergrad: Number of part-time undergraduates
- Outstate: Out-of-state tuition
- Room.Board: Room and board costs
- Books: Estimated book costs
- *Personal*: Estimated personal spending
- *PhD*: Percent of faculty with Ph.D.'s
- Terminal: Percent of faculty with terminal degree
- S.F.Ratio: Student/faculty ratio
- perc.alumni: Percent of alumni who donate
- Expend: Instructional expenditure per student

• Grad.Rate: Graduation rate

Note that for this plot, we: 1. standardize each variable to mean 0 and standard deviation 1 using scale(), 2. convert the data.frame to a matrix as required by heatmap functions, 3. transpose the matrix to show the variables as rows rather than columns, just for convenient viewing, 4. use the pheatmap library, just because it by default produces a prettier heatmap than the built-in heatmap, and 5. Annotate the columns by whether the university is private or not.



Problem 2.

This exercise involves the Auto data set studied in the lab. Make sure that the missing values have been removed from the data.

```
data(Auto)
```

Are there any missing values? No:

```
summary(complete.cases(Auto))
```

Mode TRUE NA's

logical 392 0

(a) Which of the predictors are quantitative, and which are qualitative?

```
sapply(Auto, class)
```

```
cylinders displacement
##
            mpg
                                               horsepower
                                                                 weight
      "numeric"
                    "numeric"
                                  "numeric"
##
                                                "numeric"
                                                              "numeric"
## acceleration
                                     origin
                         year
                                                     name
##
      "numeric"
                    "numeric"
                                  "numeric"
                                                 "factor"
```

Name is qualitative, the rest are quantitative. However, looking at summary(), we notice that the "origin" variable takes only values of 1, 2, 3 and should probably be treated as factor:

```
summary(Auto)
```

```
##
         mpg
                     cylinders
                                    displacement
                                                    horsepower
   Min. : 9.0
                                   Min. : 68
##
                   Min.
                           :3.00
                                                  Min.
                                                         : 46.0
    1st Qu.:17.0
                   1st Qu.:4.00
                                   1st Qu.:105
                                                  1st Qu.: 75.0
   Median :22.8
                   Median :4.00
                                   Median :151
                                                  Median: 93.5
   Mean
           :23.4
                   Mean
                          :5.47
                                   Mean
                                           :194
                                                  Mean
                                                        :104.5
##
    3rd Qu.:29.0
                   3rd Qu.:8.00
                                   3rd Qu.:276
                                                  3rd Qu.:126.0
##
   Max.
           :46.6
                   Max.
                           :8.00
                                   Max.
                                           :455
                                                  Max.
                                                         :230.0
##
##
        weight
                    acceleration
                                        year
                                                     origin
   Min.
           :1613
                   Min.
                          : 8.0
                                   Min.
                                          :70
                                                 Min.
                                                        :1.00
    1st Qu.:2225
##
                   1st Qu.:13.8
                                   1st Qu.:73
                                                 1st Qu.:1.00
                                                 Median :1.00
   Median :2804
                   Median :15.5
                                   Median :76
           :2978
##
   Mean
                   Mean
                           :15.5
                                   Mean
                                           :76
                                                Mean
                                                        :1.58
    3rd Qu.:3615
                   3rd Qu.:17.0
                                   3rd Qu.:79
                                                 3rd Qu.:2.00
##
   Max.
           :5140
                   Max.
                           :24.8
                                   Max.
                                           :82
                                                Max.
                                                        :3.00
##
```

name

```
## amc matador : 5
## ford pinto : 5
## toyota corolla : 5
## amc gremlin : 4
## amc hornet : 4
## chevrolet chevette: 4
## (Other) :365
```

Looking at some representative names for each origin, it's clear that origin=1 is U.S.-made, origin=2 is European, and origin=3 is Japanese:

```
head(unique(Auto$name[Auto$origin==1]), 10)
   [1] chevrolet chevelle malibu buick skylark 320
   [3] plymouth satellite amc rebel sst
  [5] ford torino
                          ford galaxie 500
   [7] chevrolet impala
                               plymouth fury iii
   [9] pontiac catalina amc ambassador dpl
## 304 Levels: amc ambassador brougham ... vw rabbit custom
head(unique(Auto$name[Auto$origin==2]), 10)
   [1] volkswagen 1131 deluxe sedan peugeot 504
   [3] audi 100 ls
                                  saab 99e
   [5] bmw 2002
                                 opel 1900
   [7] peugeot 304
                                 fiat 124b
   [9] volkswagen model 111 volkswagen type 3
## 304 Levels: amc ambassador brougham ... vw rabbit custom
head(unique(Auto$name[Auto$origin==3]), 10)
  [1] toyota corona mark ii datsun pl510
   [3] toyota corona
                                toyota corolla 1200
   [5] datsun 1200
                                 toyota corona hardtop
  [7] mazda rx2 coupe
                                 datsun 510 (sw)
  [9] toyouta corona mark ii (sw) toyota corolla 1600 (sw)
```

```
## 304 Levels: amc ambassador brougham ... vw rabbit custom
```

So let's fix this and turn it into a factor:

```
Auto$origin <- factor(Auto$origin, levels=1:3, labels=c("U.S.", "Europe", "Japan"))
```

Now we've corrected origin so that both origin and name are factors:

```
sapply(Auto, class)
##
                    cylinders displacement
                                               horsepower
                                                                  weight
             mpg
      "numeric"
                    "numeric"
                                  "numeric"
                                                 "numeric"
                                                               "numeric"
##
## acceleration
                          year
                                      origin
                                                      name
      "numeric"
                    "numeric"
                                    "factor"
                                                  "factor"
##
```

Let's create a logical vector indicating which variables are quantitative (numeric):

```
quant <- sapply(Auto, is.numeric)</pre>
quant
##
                     cylinders displacement
                                                 horsepower
                                                                    weight
             mpq
##
            TRUE
                          TRUE
                                        TRUE
                                                       TRUE
                                                                      TRUE
## acceleration
                                      origin
                          year
                                                       name
            TRUE
                          TRUE
                                        FALSE
                                                      FALSE
```

(b) What is the range of each quantitative predictor? You can answer this using the range() function.

```
sapply(Auto[, quant], range)
         mpg cylinders displacement horsepower weight acceleration year
## [1,]
        9.0
                      3
                                  68
                                              46
                                                   1613
                                                                  8.0
                                                                        70
## [2,] 46.6
                                 455
                                             230
                                                   5140
                                                                 24.8
                                                                        82
```

(c) What is the mean and standard deviation of each quantitative predictor?

I'll round to two significant digits using signif(). Note first row is mean, second is sd:

```
sapply(Auto[, quant], function(x) signif(c(mean(x), sd(x)), 2))

## mpg cylinders displacement horsepower weight acceleration year

## [1,] 23.0 5.5 190 100 3000 16.0 76.0

## [2,] 7.8 1.7 100 38 850 2.8 3.7
```

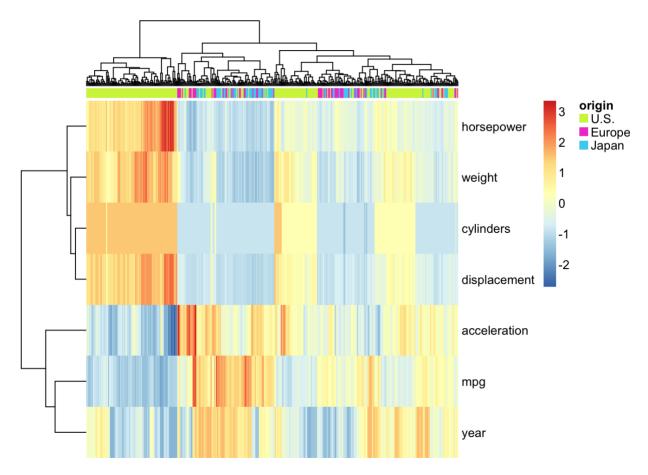
(d) Now remove the 10th through 85th observations. What is the range, mean, and standard deviation of each predictor in the subset of the data that remains?

For the heck of it, I'll add rownames. And round to two decimal places, rather than two significant digits (using round() instead of signif()):

```
\texttt{output} \leftarrow \texttt{sapply}(\texttt{Auto[-10:-85, quant], function}(\texttt{x}) \ \texttt{round}(\texttt{c}(\texttt{range}(\texttt{x}), \texttt{mean}(\texttt{x}), \texttt{sd}(\texttt{x})),
2))
rownames(output) <- c("min", "max", "mean", "sd")</pre>
output
            mpg cylinders displacement horsepower weight acceleration year
##
## min 11.00
                     3.00
                                     68.00
                                                 46.00 1649.0
                                                                           8.50 70.00
## max 46.60
                                    455.00
                                             230.00 4997.0
                     8.00
                                                                           24.80 82.00
                                              100.72 2936.0
## mean 24.40
                      5.37
                                    187.24
                                                                           15.73 77.15
          7.87
                                                   35.71 811.3
## sd
                     1.65
                                     99.68
                                                                             2.69 3.11
```

(e) Using the full data set, investigate the predictors graphically, using scatterplots or other tools of your choice. Create some plots highlighting the relationships among the predictors. Comment on your findings.

How about a heatmap again:



(f) Suppose that we wish to predict gas mileage (mpg) on the basis of the other variables. Do your plots suggest that any of the other variables might be useful in predicting mpg? Justify your answer.

Yes, it would appear that year, acceleration, and origin would be decent predictors of mpg.

Problem 3.

This exercise involves the Boston housing data set. (a) To begin, load in the Boston data set. The Boston data set is part of the MASS library in R.

```
library (MASS)
```

```
## Warning: package 'MASS' was built under R version 3.1.1
```

Now the data set is contained in the object Boston. Read about the data set: (note I use eval=FALSE in this code chunk so it isn't actually evaluated by R, just shown on the screen)

```
?Boston
```

How many rows are in this data set? How many columns? What do the rows and columns represent?

```
dim(Boston)
```

```
## [1] 506 14
```

506 rows, 14 columns.

summary(Boston) crim chas ## zn indus Min. : 0.01 Min. : 0.0 Min. : 0.46 Min. :0.0000 1st Qu.: 0.08 1st Qu.: 0.0 1st Qu.: 5.19 1st Qu.:0.0000 Median : 0.26 Median : 0.0 Median: 9.69 Median: 0.0000 Mean : 3.61 Mean :11.14 Mean :0.0692 ## Mean : 11.4 3rd Qu.: 3.68 3rd Qu.: 12.5 3rd Qu.:18.10 3rd Qu.:0.0000 ## Max. :88.98 Max. :100.0 Max. :27.74 Max. :1.0000 dis ## nox rm age Min. : 2.9 Min. :0.385 Min. :3.56 Min. : 1.13 ## 1st Qu.:5.89 1st Qu.: 45.0 ## 1st Qu.:0.449 1st Qu.: 2.10 Median: 3.21 Median :0.538 Median :6.21 Median: 77.5 Mean :0.555 Mean :6.29 Mean : 68.6 Mean : 3.79 3rd Qu.:0.624 3rd Qu.:6.62 3rd Qu.: 94.1 3rd Qu.: 5.19 ## :0.871 Max. :8.78 Max. :100.0 Max. :12.13 ## Max. ## rad tax ptratio black Min. : 1.00 Min. :187 Min. :12.6 Min. : 0.3 ## 1st Qu.:17.4 1st Qu.:375.4 1st Qu.: 4.00 1st Qu.:279 Median :330 ## Median : 5.00 Median :19.1 Median :391.4 Mean : 9.55 Mean :408 Mean :18.5 Mean :356.7 3rd Qu.:666 3rd Qu.:24.00 ## 3rd Qu.:20.2 3rd Qu.:396.2 Max. :24.00 Max. :711 Max. :22.0 Max. :396.9 medv ## lstat Min. : 1.73 Min. : 5.0 1st Qu.: 6.95 1st Qu.:17.0 ## Median :11.36 Median :21.2

Mean :22.5

Mean :12.65

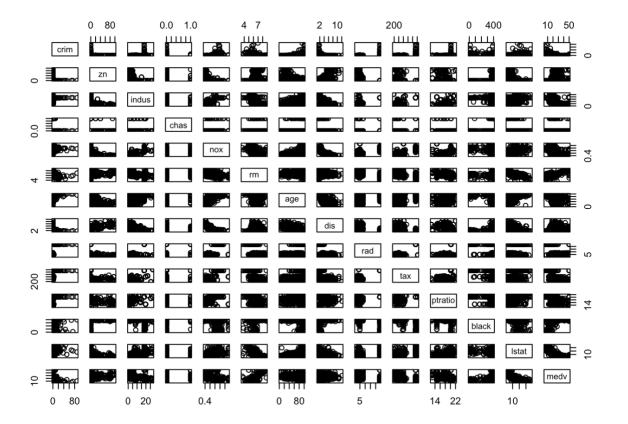
3rd Qu.:16.95 3rd Qu.:25.0

```
## Max. :37.97 Max. :50.0
```

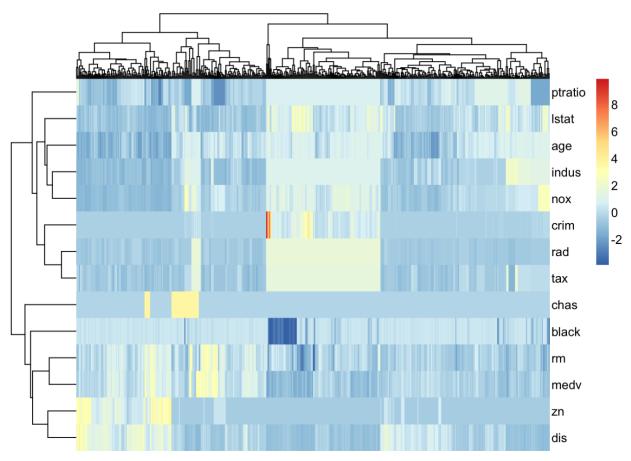
Columns are variables, rows are observations.

(b) Make some pairwise scatterplots of the predictors (columns) in this data set. Describe your findings.

```
pairs (Boston)
```



That's a lot of small scatterplots. Maybe a heatmap will be easier to read:



Notice "chas" is a binary variable. "crim" has outliers. There are some collinear variables, like rad/tax, and rad/tax have a lot of constant values:

```
summary (Boston$rad)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                 Max.
##
      1.00
               4.00
                       5.00
                                9.55
                                                24.00
                                       24.00
table (Boston$rad)
##
            38 110 115 26 17 24 132
```

It's those 24's that stand out in the heatmap - I'll bet these are some kind of weird coding and not real values of 24. Let's set those to NA:

```
Boston$rad[Boston$rad==24] <- NA
```

tax has a lot of "666" values that I don't believe are really 666:

```
table (Boston$tax)
```

```
## 187 188 193 198 216 222 223 224 226 233 241 242 243 244 245 247 252 254
                             5
                                10
                                                  2
                                                               3
  255 256 264 265 270 273 276 277 279 280 281 284 285 287 289 293 296 300
                          5
                             9
         1
           12
                                11
                                      4
                                                      1
  304 305 307 311 313 315 329 330 334 335 337 345 348 351 352 358 370 384
                         2
                                          2
            40
                               10
  391 398 402 403 411 422 430 432 437 469 666 711
       12
                30
                             3
                                  9 15
                                         1 132
```

so let's set those to NA as well:

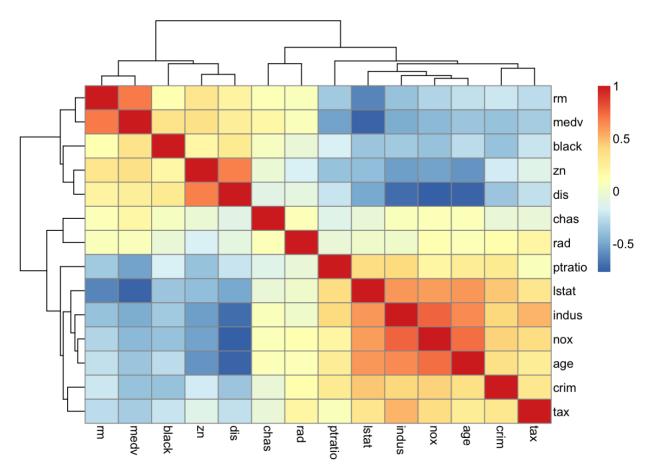
```
Boston$tax[Boston$tax==666] <- NA
```

There are no doubt other variables that need to be cleaned as well (like ptratio for sure) but you get the picture... Data cleaning is hard.

(c) Are any of the predictors associated with per capita crime rate? If so, explain the relationship.

Let's make a heatmap of correlations, calculating correlations using pairwise complete observations (for a given pair of variables, neither has a missing value). It looks like there are a number of variables associated with "crim": ptratio, rad, tax, lstat, age, indus and nox.

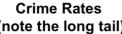
```
pheatmap(cor(Boston, use="pairwise.complete.obs"))
```



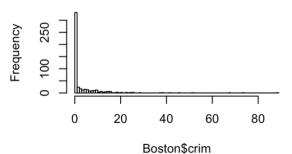
(d) Do any of the suburbs of Boston appear to have particularly high crime rates? Tax rates? Pupil-teacher ratios? Comment on the range of each predictor.

Make histograms of each. breaks="FD" tends to result in more bins in the histogram than the default:

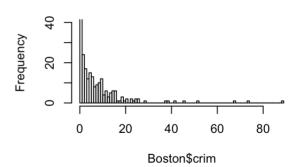
```
par(mfrow=c(2,2))
hist(Boston$crim, main="Crime Rates\n (note the long tail)",breaks="FD")
hist(Boston$crim, main="Crime Rates with y-axis limited",
    ylim=c(0, 40), breaks="FD")
hist(Boston$tax, main="Tax rates\n (note some high-tax outliers)", breaks="FD")
hist(Boston$ptratio, main="Pupil-teacher ratio\n (no real outliers)", breaks="FD")
```



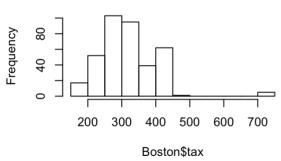
(note the long tail)



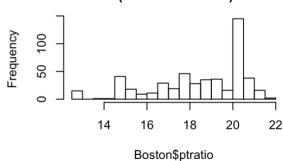
Crime Rates with y-axis limited



Tax rates (note some high-tax outliers)



Pupil-teacher ratio (no real outliers)



(e) How many of the suburbs in this data set bound the Charles river?

```
(=1 if tract bounds river; 0 otherwise)
summary (Boston$chas==1)
##
      Mode
              FALSE
                        TRUE
                                NA's
                          35
## logical
                471
                                    0
```

(f) What is the median pupil-teacher ratio among the towns in this data set?

```
median(Boston$ptratio)
```

[1] 19.05

(g) Which suburb of Boston has lowest median value of owner- occupied homes?

We don't have suburb names, but it's #399:

```
which.min(Boston$medv)
## [1] 399
```

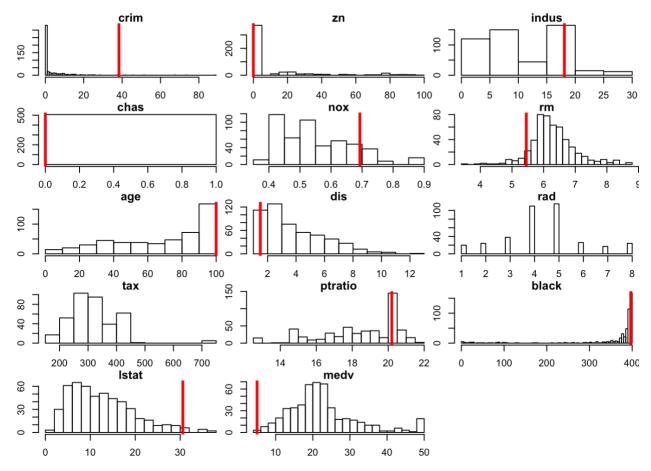
What are the values of the other predictors for that suburb, and how do those values compare to the overall ranges for those predictors? Comment on your findings.

From the ?Boston codebook to help interpret these histograms:

- **crim**: per capita crime rate by town.
- **zn**: proportion of residential land zoned for lots over 25,000 sq.ft.
- **indus**: proportion of non-retail business acres per town.
- **chas**: Charles River dummy variable (= 1 if tract bounds river; 0 otherwise).
- **nox**: nitrogen oxides concentration (parts per 10 million).
- **rm**: average number of rooms per dwelling.
- age: proportion of owner-occupied units built prior to 1940.
- **dis**: weighted mean of distances to five Boston employment centres.
- rad: index of accessibility to radial highways.
- tax: full-value property-tax rate per \$10,000.
- **ptratio**: pupil-teacher ratio by town.
- black: 1000(Bk-0.63)21000(Bk-0.63)2 where Bk is the proportion of blacks by town.
- **lstat**: lower status of the population (percent).
- **medv**: median value of owner-occupied homes in \$1000s.

```
par(mfrow=c(5,3), mar=c(2, 2, 1, 0))

for (i in 1:ncol(Boston)) {
   hist(Boston[, i], main=colnames(Boston)[i], breaks="FD")
   abline(v=Boston[399, i], col="red", lw=3)
}
```



(h) In this data set, how many of the suburbs average more than seven rooms per dwelling?

```
summary(Boston$rm > 7)

## Mode FALSE TRUE NA's

## logical 442 64 0
```

More than eight rooms per dwelling?

```
summary(Boston$rm > 8)

## Mode FALSE TRUE NA's

## logical 493 13 0
```

Comment on the suburbs that average more than eight rooms per dwelling.

First, create a logical index for which suburbs these are:

```
idx <- Boston$rm > 8
summary(idx)

## Mode FALSE TRUE NA's

## logical 493 13 0
```

Let's repeat the histograms again, and show red lines for these (subset rows using idx instead of 399:

```
par(mfrow=c(5,3), mar=c(2, 2, 1, 0))
for (i in 1:ncol(Boston)) {
  hist(Boston[, i], main=colnames(Boston)[i], breaks="FD")
  abline(v=Boston[idx, i], col="red", lw=1)
                  crim
                                                                                         indus
                                                       zn
                                    200
                                                                        100
150
    0
          20
                 40
                        60
                                        0
                                                    40
                                                          60
                                                                80
                                                                     100
                                                                                      10
                                                                                           15
                                                                                                20
                                                                                                     25
                               80
                                              20
                                                                                                          30
                 chas
                                                      nox
500
                                                                        80
200
                                    40
                                                                        40
                                    0
    0.0
         0.2
                0.4
                     0.6
                           8.0
                                 1.0
                                                0.5
                                                     0.6
                                                          0.7
                                                                8.0
                                                                     0.9
                                                                                     5
                  age
                                                                                          rad
                                                                        100
100
                                    09
                                                                        40
    0
          20
                40
                      60
                           80
                                                          8
                                                              10
                                                                   12
                                                                                     3
                                                                                             5
                                                                                                 6
                                 100
                  tax
                                                     ptratio
                                                                                         black
                                    150
80
                                                                        100
40
                                    20
      200 300
               400 500
                          600 700
                                                         18
                                                                      22
                                                                                   100
                                                                                           200
                                                                                                  300
                                                                                                         400
                                                               20
                                                     medv
                  Istat
9
                                    9
30
                                    30
```