The design of PID is basically same as what was being described in the online class material. I used the array K[3] to store my P, I, and D components. The P (proportional) component is coming directly from cte. The D (derivative) component is basically the delta of cte. The calculation of D is simply the current cte substract the previous cte. And the I (Intergral) is sum of all cte since time zero. To smooth out the derivative noise, I have implemented a low pass filter to smooth out the derivative. I used the std vector to store the previour D component and take the average. Here is the implementation detail

```
void PID::UpdateError(double cte) {
  double diff = cte - error[0];

lowpass.push_back(diff);

if (lowpass.size() > 3){
   lowpass.erase(lowpass.begin());
}

error[1] = std::accumulate( lowpass.begin(), lowpass.end(),
0.0)/lowpass.size();
  error[0] = cte;
  error[2] += cte;

std::cout<<"K value: "<<K[0]<<" : "<<K[1]<<" : "<<K[2]<<std::endl;
  if ( is_twiddle ){
    twiddle();
  }
}</pre>
```

I basically keep a buffer of 3 and take the average of it for the D component. Standard library vector and accumulate functions are used to get the average. For the P component, I assign cte directly into my error[0] variable. And for the I component, I add cte into error[2].

I did not try to fine tune the hyper parameters for the PID coefficient. I use twiddle algorithm to fine out the PID coefficient. I used 0 for the default values in the init() function for my PID coefficient. When the default values are used, twiddle algorithms will automatically trigger. The twiddle algorithms collect a data samples of 1000. Algorithms is simply and work exactly the way how the online class material described. However, to speed up thing a little, I did not use square errors. I do double square (error to the power of fourth). Here is the code that do that:

```
double square = error[0] * error[0];
square *= square; // square it again to speed up the computation a
```

```
little
    err_squ += square;
    // Let's see if we can speed up the twiddle process by checking if
err_squ is already larger than best_err
    if (state == 1 && err_squ > best_err){
      K[index] -= 2*dp[index];
      state = 2;
      iteration = 0;
      error[2] = 0;
      return;
    }
    else if (state == 2 && err_squ > best_err){
      K[index] += dp[index];
      dp[index] *=0.9;
      index = (index+1) % 3;
      state = 0;
      iteration = 0;
      error[2] = 0;
      return;
    }
```

So if the cte input is 4, and I take it to the power of four, it will be 64, This will speed up the rate of err_squ increase its value and we can discover earlier that it is larger than the best error.

After using twiddle, I found the PID coefficient to be P for 0.137611, I = 0 and D = 2.89388. Since I = 0, I did not bother implement integral wind-up.