New Track Fitting

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Abstract

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1. Equation of Motion

Notation.

$step\ length: S$	[cm]
$path\ length:s$	[cm]
$position: ec{p}$	[cm]
$unit\ direction: \hat{u}$	[1]
orthogonal direction : \hat{n}_{τ} and \hat{n}_{ρ}	[1]
$eta: ilde{\eta}= ilde{q}/\left(\gammaeta ight)$	[1]
$rigidity: R = (m/q) \cdot \gamma \beta$	[GV]
mass:m	[GeV]
charge:q	[e]
$charge \ sign: \tilde{q} = q/\big q\big $	[1]
$electron\ mass: m_e = 0.510999$	[MeV]
$electron\ charge: q_e = 1$	[e]
velocity:eta	[1]
$Lorentz\ factor: \gamma = 1/\sqrt{1-\beta^2}$	[1]
$magnetic\ field: ec{B}$	[kGauss]
$lambda: \lambda = 2.99792458 \cdot 10^{-4}$	$[GV \cdot kGauss^{-1} \cdot cm^{-1}]$
$radiation\ length: X_0$	$[g \cdot cm^{-2}]$
$mass\ density: D$	$[g \cdot cm^{-3}]$
$cross\ length: L=D/X_0$	$[cm^{-1}]$
$passage\ length: l$	[cm]
$Rydberg\ constant: C_{\mathrm{Rydberg}} = 0.0136$	[GeV]
K: K = 0.307075	$[MeV \cdot mol^{-1} \cdot cm^2]$
$atomic\ mass: A$	$[g \cdot mol^{-1}]$
$atomic\ number: Z$	[1]
$density\ effect: \delta(\gamma\beta)$	[MeV]
$mean\ excitation\ energy: I$ 3	[eV]
$Landau\ factor: j=0.200$	[1]
	/1

Lorentz Force.

$$\frac{d\hat{u}}{ds} = \Lambda \cdot (\hat{u} \times \vec{B}) \cdot \tilde{\eta}$$

$$\Lambda = \lambda \cdot |q/m|$$

$$(\hat{u} \times \vec{B}) = \begin{pmatrix} \hat{u}_y \vec{B}_z - \hat{u}_z \vec{B}_y \\ \hat{u}_z \vec{B}_x - \hat{u}_x \vec{B}_z \\ \hat{u}_x \vec{B}_y - \hat{u}_y \vec{B}_x \end{pmatrix}$$
(2)

Multiple Scattering.

$$\begin{split} \frac{d\hat{u}}{ds} &= (\omega_{\tau} \cdot \hat{n}_{\tau} + \omega_{\rho} \cdot \hat{n}_{\rho}) \cdot \Omega_{\theta} \\ \hat{n}_{\tau} &= (\vec{B} - (\hat{u} \cdot \vec{B}) \cdot \hat{u}) / |\hat{u} \times \vec{B}| \\ \hat{n}_{\rho} &= (\hat{u} \times \vec{B}) / |\hat{u} \times \vec{B}| \\ \Omega_{\theta} &= C_{\text{Rydberg}} \cdot |q/m| \cdot (|\tilde{\eta}|\sqrt{\tilde{\eta}^{2} + 1}) \cdot \sqrt{l \cdot L} \cdot (1 + 0.038 \cdot \ln(l \cdot L)) \cdot (1/S) \\ \omega_{\tau}, \omega_{\rho} \sim Normal(0, 1) \\ f(\omega) &= \frac{1}{\sqrt{2\pi}} \cdot \exp\left(-\frac{\omega^{2}}{2}\right) \end{split}$$
(3)

Ionisation Energy Loss.

$$\frac{d\tilde{\eta}}{ds} = \tilde{\eta} \cdot (\omega_I \cdot \Omega_{\delta} + \Omega_{\Delta})$$

$$\Omega_I = (K/2) \cdot (D \cdot l \cdot Z/A) \cdot (q^2) \cdot (\tilde{\eta}^2 + 1)$$

$$\Omega_{\delta} = \Omega_I \cdot (1/m) \cdot (\tilde{\eta}^2 \sqrt{\tilde{\eta}^{-2} + 1}) \cdot (1/S)$$

$$\Omega_{\Delta} = \Omega_{\delta} \cdot \left[\ln \left(\frac{2m_e \cdot \tilde{\eta}^{-2}}{I} \right) + \ln \left(\frac{\Omega_I}{I} \right) + j - \beta^2 - \delta(\gamma\beta) \right]$$

$$\omega_I \sim Landau (0, 1) \ require \ [\omega_I > = (-\Omega_{\Delta}/\Omega_{\delta})]$$

$$f(\omega_I) \simeq \frac{1}{\sqrt{2\pi}} \cdot \exp\left(-\frac{1}{2} \left(\omega_I + \exp\left(-\omega_I \right) \right) \right)$$
(4)

Bremsstrahlung Energy Loss.

$$\frac{d\tilde{\eta}}{ds} = \tilde{\eta} \cdot (\omega_B \cdot \Omega_B)$$

$$\Omega_B = \left(\frac{q}{q_e} \cdot \frac{m_e}{m}\right)^2 \cdot (\sqrt{\tilde{\eta}^{-2} + 1} - 1) \cdot \left(\frac{l \cdot L}{\ln 2}\right) \cdot (\tilde{\eta}^2 \sqrt{\tilde{\eta}^{-2} + 1}) \cdot (1/S)$$

$$\omega_B \sim \Gamma(t, t) \quad require \quad [0 \le \omega_B < \inf]$$

$$f(\omega_B) = \left(\frac{t^t}{\Gamma(t)}\right) \cdot \left(\omega_B^{t-1} \cdot \exp(-\omega_B \cdot t)\right) \quad where \quad t = \left(\frac{l \cdot L}{\ln 2}\right)$$

Summary.

$$\frac{d\vec{p}}{ds} = \hat{u}$$

$$\frac{d\hat{u}}{ds} = \Lambda \cdot (\hat{u} \times \vec{B}) \cdot \tilde{\eta} + (\omega_{\tau} \cdot \hat{n}_{\tau} + \omega_{\rho} \cdot \hat{n}_{\rho}) \cdot \Omega_{\theta}$$

$$\frac{d\tilde{\eta}}{ds} = \tilde{\eta} \cdot [(\omega_{I} \cdot \Omega_{\delta} + \Omega_{\Delta}) + (\omega_{B} \cdot \Omega_{B})]$$
(6)

2. Propagation

Status.

$$\xi_{\vec{p}}^{T} = \begin{pmatrix} x & y & z \end{pmatrix}
\xi_{\hat{u}}^{T} = \begin{pmatrix} \hat{u}_{x} & \hat{u}_{y} & \hat{u}_{z} \end{pmatrix}
\xi_{\hat{\eta}}^{T} = \begin{pmatrix} \hat{\eta} \end{pmatrix}
\xi_{\omega}^{T} = \begin{pmatrix} \omega_{\tau} & \omega_{\rho} & \omega_{I} & \omega_{B} \end{pmatrix}
\xi^{T} = \begin{pmatrix} \xi_{\vec{p}}^{T} & \xi_{\hat{u}}^{T} & \xi_{\tilde{\eta}}^{T} & \xi_{\omega}^{T} \end{pmatrix}
\xi^{T}_{G} = \begin{pmatrix} \xi_{\vec{p}}^{T} & \xi_{\hat{u}}^{T} & \xi_{\tilde{\eta}}^{T} & \xi_{\tilde{\eta}}^{T} \end{pmatrix}
\xi_{L}^{T} = \begin{pmatrix} \xi_{\omega}^{T} \end{pmatrix}$$
(7)

Differential Status.

$$\zeta_{\vec{p}} = \frac{d\xi_{\vec{p}}}{ds} = \hat{u}$$

$$\zeta_{\vec{u}} = \frac{d\xi_{\vec{u}}}{ds} = \Lambda \cdot (\hat{u} \times \vec{B}) \cdot \tilde{\eta} + (\omega_{\tau} \cdot \hat{n}_{\tau} + \omega_{\rho} \cdot \hat{n}_{\rho}) \cdot \Omega_{\theta}$$

$$\zeta_{\tilde{\eta}} = \frac{d\xi_{\tilde{\eta}}}{ds} = \tilde{\eta} \cdot [(\omega_{I} \cdot \Omega_{\delta} + \Omega_{\Delta}) + (\omega_{B} \cdot \Omega_{B})]$$
(8)

 $Transfer\ Status\ A.$

$$\kappa_{\vec{p}} = \frac{d\zeta_{\vec{p}}}{d\xi} = \begin{pmatrix} \frac{d\zeta_{\vec{p}}}{d\xi_{\vec{p}}} & \frac{d\zeta_{\vec{p}}}{d\xi_{\hat{u}}} & \frac{d\zeta_{\vec{p}}}{d\xi_{\hat{u}}} & \frac{d\zeta_{\vec{p}}}{d\xi_{\omega}} \end{pmatrix}$$

$$\kappa_{\hat{u}} = \frac{d\zeta_{\hat{u}}}{d\xi} = \begin{pmatrix} \frac{d\zeta_{\hat{u}}}{d\xi_{\vec{p}}} & \frac{d\zeta_{\hat{u}}}{d\xi_{\hat{u}}} & \frac{d\zeta_{\hat{u}}}{d\xi_{\hat{u}}} & \frac{d\zeta_{\hat{u}}}{d\xi_{\omega}} \end{pmatrix}$$

$$\kappa_{\tilde{\eta}} = \frac{d\zeta_{\tilde{\eta}}}{d\xi} = \begin{pmatrix} \frac{d\zeta_{\tilde{\eta}}}{d\xi_{\vec{p}}} & \frac{d\zeta_{\tilde{\eta}}}{d\xi_{\hat{u}}} & \frac{d\zeta_{\tilde{\eta}}}{d\xi_{\tilde{\eta}}} & \frac{d\zeta_{\tilde{\eta}}}{d\xi_{\omega}} \end{pmatrix}$$

$$\kappa_{\vec{p}} = \frac{d\zeta_{\vec{p}}}{d\xi} = \begin{pmatrix} 0 & \frac{d\zeta_{\vec{p}}}{d\xi_{\hat{u}}} & 0 & 0 \end{pmatrix}$$

$$\kappa_{\hat{u}} = \frac{d\zeta_{\hat{u}}}{d\xi} = \begin{pmatrix} 0 & \frac{d\zeta_{\tilde{u}}}{d\xi_{\hat{u}}} & \frac{d\zeta_{\tilde{u}}}{d\xi_{\tilde{\eta}}} & \frac{d\zeta_{\tilde{u}}}{d\xi_{\omega}} \end{pmatrix}$$

$$\kappa_{\tilde{\eta}} = \frac{d\zeta_{\tilde{\eta}}}{d\xi} = \begin{pmatrix} 0 & 0 & \frac{d\zeta_{\tilde{\eta}}}{d\xi_{\tilde{u}}} & \frac{d\zeta_{\tilde{\eta}}}{d\xi_{\tilde{u}}} & \frac{d\zeta_{\tilde{u}}}{d\xi_{\omega}} \end{pmatrix}$$

Transfer Status B.

$$\frac{d\zeta_{\vec{p}_i}}{d\xi_{\hat{u}_j}} = \delta_{ij}$$

$$\frac{d\zeta_{\hat{u}_i}}{d\xi_{\hat{u}_j}} = \Lambda \cdot \frac{\partial(\hat{u} \times \vec{B})_i}{\partial \hat{u}_j} \cdot \tilde{\eta}$$

$$\frac{d\zeta_{\hat{u}_i}}{d\xi_{\tilde{\eta}}} = \Lambda \cdot (\hat{u} \times \vec{B})_i$$

$$\frac{d\zeta_{\hat{u}_i}}{d\xi_{\omega_{\tau}}} = (\Omega_{\theta} \cdot \hat{n}_{\tau})_i$$

$$\frac{d\zeta_{\hat{u}_i}}{d\xi_{\omega_{\rho}}} = (\Omega_{\theta} \cdot \hat{n}_{\rho})_i$$

$$\frac{d\zeta_{\hat{\eta}_i}}{d\xi_{\omega_{\rho}}} = (\omega_I \cdot \Omega_{\delta} + \Omega_{\Delta}) + (\omega_B \cdot \Omega_B)$$

$$\frac{d\zeta_{\tilde{\eta}}}{d\xi_{\tilde{\eta}}} = \tilde{\eta} \cdot \Omega_{\delta}$$

$$\frac{d\zeta_{\tilde{\eta}}}{d\xi_{\omega_B}} = \tilde{\eta} \cdot \Omega_B$$

$$\frac{\partial(\hat{u} \times \vec{B})}{\partial \hat{u}} = \begin{pmatrix} 0 & \vec{B}_z & -\vec{B}_y \\ -\vec{B}_z & 0 & \vec{B}_x \\ \vec{B}_y & -\vec{B}_x & 0 \end{pmatrix}$$

 $Euler\ Method.$

$$\xi^{0} = \xi(0)$$

$$\xi^{f} = \xi(S)$$

$$\xi_{G}^{f} = \xi_{G}^{0} + \begin{pmatrix} S \cdot \zeta_{\vec{p}}^{0} + \frac{S^{2}}{2} \cdot \zeta_{\hat{u}}^{0} \\ S \cdot \zeta_{\hat{u}}^{0} \\ S \cdot \zeta_{\hat{\eta}}^{0} \end{pmatrix}$$

$$J^{f} = \begin{pmatrix} J_{GG}^{f} & J_{GL}^{f} \\ S \cdot \kappa_{\vec{p}G}^{0} + \frac{S^{2}}{2} \cdot \kappa_{\hat{u}G}^{0} \\ S \cdot \kappa_{\hat{u}G}^{0} \\ S \cdot \kappa_{\hat{\eta}G}^{0} \end{pmatrix}$$

$$J_{GL}^{f} = \begin{pmatrix} \frac{S^{2}}{2} \cdot \kappa_{\hat{u}L}^{0} \\ S \cdot \kappa_{\hat{u}L}^{0} \\ S \cdot \kappa_{\hat{\eta}L}^{0} \end{pmatrix}$$

$$(11)$$

Euler-Heun Method.

$$\xi^{0} = \xi(0)$$

$$\xi^{1} = \xi(S)$$

$$\xi_{G}^{1} = \xi_{G}^{0} + \begin{pmatrix} S \cdot \zeta_{p}^{0} + \frac{S^{2}}{2} \cdot \zeta_{u}^{0} \\ S \cdot \zeta_{u}^{0} \\ S \cdot \zeta_{\eta}^{0} \end{pmatrix}$$

$$J^{1} = \begin{pmatrix} J_{GG}^{1} & J_{GL}^{1} \\ S \cdot \kappa_{pG}^{0} + \frac{S^{2}}{2} \cdot \kappa_{uG}^{0} \\ S \cdot \kappa_{uG}^{0} \\ S \cdot \kappa_{uG}^{0} \end{pmatrix}$$

$$J_{GG}^{1} = I + \begin{pmatrix} S \cdot \kappa_{pG}^{0} + \frac{S^{2}}{2} \cdot \kappa_{uG}^{0} \\ S \cdot \kappa_{uG}^{0} \\ S \cdot \kappa_{uG}^{0} \\ S \cdot \kappa_{uL}^{0} \end{pmatrix}$$

$$J_{GL}^{1} = \begin{pmatrix} \frac{S^{2}}{2} \cdot \kappa_{uL}^{0} \\ S \cdot \kappa_{uL}^{0} \\ S \cdot \kappa_{uL}^{0} \\ S \cdot \kappa_{uL}^{0} \end{pmatrix}$$

$$\xi^{f} = \xi(S)$$

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$$J^{f} = \begin{pmatrix} J_{GG}^{f} & J_{GL}^{f} \\ \frac{S}{2} \cdot (\zeta_{u}^{0} + \zeta_{u}^{1}) \\ \frac{S}{2} \cdot (\zeta_{\eta}^{0} + \zeta_{u}^{1}) \end{pmatrix}$$

$$J^{f} = \begin{pmatrix} J_{GG}^{f} & J_{GL}^{f} \\ S \cdot \kappa_{pG}^{0} + \kappa_{uG}^{1} J_{GG}^{f} \\ \frac{S}{2} \cdot (\kappa_{uG}^{0} + \kappa_{uG}^{1} J_{GG}^{f}) \\ \frac{S}{2} \cdot (\kappa_{uG}^{0} + \kappa_{uG}^{1} J_{GG}^{f} + \kappa_{uL}^{1}) \end{pmatrix}$$

$$J_{GL}^{f} = \begin{pmatrix} \frac{S^{2}}{6} \cdot (2\kappa_{uL}^{0} + (\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1})) \\ \frac{S}{2} \cdot (\kappa_{uL}^{0} + (\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1})) \\ \frac{S}{2} \cdot (\kappa_{uL}^{0} + (\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1})) \end{pmatrix}$$

 $Runge ext{-}Kutta ext{-}Nystrom\ Method\ A.$

$$\xi^{0} = \xi(0)$$

$$\xi^{1} = \xi\left(\frac{S}{2}\right)$$

$$\xi_{G}^{1} = \xi_{G}^{0} + \left(\frac{\frac{S}{2} \cdot \zeta_{p}^{0} + \frac{S^{2}}{8} \cdot \zeta_{u}^{0}}{\frac{S}{2} \cdot \zeta_{u}^{0}}\right)$$

$$\xi_{G}^{1} = \xi_{G}^{0} + \left(\frac{\frac{S}{2} \cdot \zeta_{u}^{0}}{\frac{S}{2} \cdot \zeta_{u}^{0}}\right)$$

$$J^{1} = \left(J_{GG}^{1} J_{GL}^{1}\right)$$

$$J_{GG}^{1} = I + \left(\frac{\frac{S}{2} \cdot \kappa_{pG}^{0} + \frac{S^{2}}{8} \cdot \kappa_{uG}^{0}}{\frac{S}{2} \cdot \kappa_{uG}^{0}}\right)$$

$$J_{GL}^{1} = \left(\frac{\frac{S^{2}}{8} \cdot \kappa_{uL}^{0}}{\frac{S}{2} \cdot \kappa_{uL}^{0}}\right)$$

$$\xi^{2} = \xi\left(\frac{S}{2}\right)$$

$$\xi^{2} = \xi\left(\frac{S}{2}\right)$$

$$\xi^{2} = \xi_{G}^{i} + \left(\frac{\frac{S}{2} \cdot \zeta_{p}^{0} + \frac{S^{2}}{8} \cdot \zeta_{u}^{0}}{\frac{S}{2} \cdot \zeta_{u}^{1}}\right)$$

$$J^{2} = \left(J_{GG}^{2} J_{GL}^{2}\right)$$

$$J^{2} = \left(J_{GG}^{2} J_{GL}^{2}\right)$$

$$J_{GG}^{2} = I + \left(\frac{\frac{S}{2} \cdot \kappa_{uG}^{0} + \frac{S^{2}}{8} \cdot \kappa_{uG}^{0}}{\frac{S}{2} \cdot \kappa_{uG}^{1} J_{GG}^{1}}\right)$$

$$J_{GL}^{2} = \left(\frac{S^{2}}{8} \cdot \kappa_{uL}^{0}}{\frac{S}{2} \cdot \kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1}}\right)$$

$$\frac{S}{2} \cdot \left(\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1}}\right)$$

$$\frac{S}{2} \cdot \left(\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1}}\right)$$

Runge-Kutta-Nystrom Method B.

$$\begin{split} \xi_{G}^{3} &= \xi(S) \\ \xi_{G}^{3} &= \xi_{G}^{0} + \begin{pmatrix} S \cdot \zeta_{p}^{0} + \frac{S^{2}}{2} \cdot \zeta_{u}^{2} \\ S \cdot \zeta_{u}^{2} \\ S \cdot \zeta_{u}^{2} \end{pmatrix} \\ J^{3} &= \begin{pmatrix} J_{GG}^{3} & J_{GL}^{3} \\ S \cdot \kappa_{pG}^{3} + \frac{S^{2}}{2} \cdot \kappa_{uG}^{2} J_{GG}^{2} \\ S \cdot \kappa_{pG}^{2} J_{GG}^{2} \\ S \cdot \kappa_{uG}^{2} J_{GG}^{2} \end{pmatrix} \\ J^{3}_{GG} &= I + \begin{pmatrix} S \cdot \kappa_{pG}^{0} + \frac{S^{2}}{2} \cdot \kappa_{uG}^{2} J_{GG}^{2} \\ S \cdot \kappa_{uG}^{2} J_{GG}^{2} \\ S \cdot \kappa_{uG}^{2} J_{GG}^{2} \\ S \cdot \kappa_{uG}^{2} J_{GG}^{2} \end{pmatrix} \\ J^{3}_{GL} &= \begin{pmatrix} \frac{S^{2}}{2} \cdot (\kappa_{uG}^{2} J_{GL}^{2} + \kappa_{uL}^{2}) \\ S \cdot (\kappa_{uG}^{2} J_{GL}^{2} + \kappa_{uL}^{2}) \\ S \cdot (\kappa_{uG}^{2} J_{GL}^{2} + \kappa_{uL}^{2}) \end{pmatrix} \\ \xi^{f} &= \xi(S) \\ \xi^{f}_{G} &= \xi(S) \\ \xi^{f}_{G} &= \xi(S) \\ \xi^{f}_{G} &= (\zeta_{u}^{0} + 2\zeta_{u}^{1} + 2\zeta_{u}^{2} + 2\zeta_{u}^{2} + \zeta_{u}^{3}) \\ \frac{S}{6} \cdot (\zeta_{u}^{0} + 2\zeta_{u}^{1} + 2\zeta_{u}^{2} + 2\zeta_{u}^{2} + \zeta_{u}^{3}) \end{pmatrix} \\ J^{f}_{G} &= I + \begin{pmatrix} S \cdot \kappa_{pG}^{0} + \frac{S^{2}}{6} \cdot (\kappa_{uG}^{0} + \kappa_{uG}^{1} J_{GG}^{1} + \kappa_{uG}^{2} J_{GG}^{2} + \kappa_{uG}^{2} J_{GG}^{2}) \\ \frac{S}{6} \cdot (\kappa_{uG}^{0} + 2\kappa_{uG}^{1} J_{GG}^{1} + 2\kappa_{uG}^{2} J_{GG}^{2} + \kappa_{uG}^{3} J_{GG}^{3}) \\ \frac{S}{6} \cdot (\kappa_{uG}^{0} + 2\kappa_{uG}^{1} J_{GG}^{1} + 2\kappa_{uG}^{2} J_{GG}^{2} + \kappa_{uG}^{3} J_{GG}^{3}) \end{pmatrix} \\ J^{f}_{GL} &= \begin{pmatrix} \frac{S^{2}}{6} \cdot (\kappa_{uL}^{0} + (\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1}) + (\kappa_{uG}^{2} J_{GL}^{2} + \kappa_{uL}^{2}) \\ \frac{S}{6} \cdot (\kappa_{uL}^{0} + 2(\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1}) + (\kappa_{uG}^{2} J_{GL}^{2} + \kappa_{uL}^{2}) \end{pmatrix} \\ \frac{S}{6} \cdot (\kappa_{uL}^{0} + 2(\kappa_{uG}^{1} J_{GL}^{1} + \kappa_{uL}^{1}) + (\kappa_{uG}^{2} J_{GL}^{2} + \kappa_{uL}^{2}) + (\kappa_{uG}^{3} J_{GL}^{3} + \kappa_{uL}^{3})) \end{pmatrix}$$

3. Track Fitting

 $Negative ext{-}Log ext{-}Likelihood.$

$$\mathcal{L} = -\ln\left(all\ probability\ density\ function\ multiply\right) + Constant \tag{15}$$

$$\mathcal{L} = \left(\frac{1}{2}\right) \cdot \sum \left(\left(\xi_{\vec{p}} - m_{\vec{p}}\right)^T \sigma_{\vec{p}}^{-1} \left(\xi_{\vec{p}} - m_{\vec{p}}\right) \right)
+ \left(\frac{1}{2}\right) \cdot \sum \omega_{\tau}^2
+ \left(\frac{1}{2}\right) \cdot \sum \omega_{\rho}^2
+ \left(\frac{1}{2}\right) \cdot \sum \left(\omega_I + \exp(-\omega_I)\right)
+ \sum \left(\omega_B t + (1 - t) \cdot \ln(\omega_B)\right)$$
(16)

 $Negative ext{-}Log ext{-}Likelihood.$

$$H_{\xi} = \frac{\partial \mathcal{L}}{\partial \xi^{T}} = \sum \left(\left(\frac{d\vec{p}_{\xi}}{d\xi} \right)^{T} \sigma_{m}^{-1} (\vec{p}_{\xi} - \vec{p}_{m}) \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{L}}{\partial \xi} \right)^{T} \cdot \omega_{L} \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{\theta}}{\partial \xi} \right)^{T} \cdot \omega_{\theta} \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{I}}{\partial \xi} \right)^{T} \cdot \left(\frac{1}{2} \right) (1 - \exp(-\omega_{I})) \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{B}}{\partial \xi} \right)^{T} \cdot \left(t + (1 - t) \cdot \omega_{B}^{-1} \right) \right)$$

$$(17)$$

Negative-Log-Likelihood.

$$C_{\xi}^{-1} = \frac{\partial \mathcal{L}}{\partial \xi^{T} \partial \xi} = \sum \left(\left(\frac{d\vec{p}_{\xi}}{d\xi} \right)^{T} \sigma_{m}^{-1} \left(\frac{d\vec{p}_{\xi}}{d\xi} \right) \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{L}}{\partial \xi} \right)^{T} \cdot \left(\frac{\partial \omega_{L}}{\partial \xi} \right) \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{\theta}}{\partial \xi} \right)^{T} \cdot \left(\frac{\partial \omega_{\theta}}{\partial \xi} \right) \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{I}}{\partial \xi} \right)^{T} \cdot \left(\frac{1}{2} \right) \exp(-\omega_{I}) \cdot \left(\frac{\partial \omega_{I}}{\partial \xi} \right) \right) +$$

$$\sum \left(\left(\frac{\partial \omega_{B}}{\partial \xi} \right)^{T} \cdot \left((t - 1) \cdot \omega_{B}^{-2} \right) \cdot \left(\frac{\partial \omega_{B}}{\partial \xi} \right) \right)$$

$$(18)$$

Minimization. The Gradient Descent Method

$$\Delta \xi = c \cdot H_{\xi} \text{ where } c \text{ is constant}$$
 (19)

The Gauss-Newton Method

$$\Delta \xi = C_{\xi} \cdot H_{\xi} \tag{20}$$

The Levenberg-Marquardt Method

$$\Delta \xi = (C_{\xi} + c \cdot diag(C_{\xi})) \cdot H_{\xi} \text{ where } c \text{ is constant}$$
 (21)

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- front matter

20

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 - theorems, definitions and proofs

- lables of enumerations
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Propagation. It uses RK4 method.

References

- [1] R. Feynman, F. Vernon Jr., The theory of a general quantum system interacting with a linear dissipative system, Annals of Physics 24 (1963) 118–173. doi:10.1016/0003-4916(63)90068-X.
- [2] P. Dirac, The lorentz transformation and absolute time, Physica 19 (1--12) (1953) 888-896. doi:10.1016/S0031-8914(53)80099-6.
- [3] A. Strandlie, R. Frühwirth, Track and vertex reconstruction: From classical to adaptive methods, Reviews of Modern Physics 82 (2) (2010) 1419–1458.
- doi:10.1103/RevModPhys.82.1419.

URL http://link.aps.org/doi/10.1103/RevModPhys.82.1419