

Problem 3

$$f_c = 1000 \text{ Hz} \quad \omega_c = 2000 \text{ rad/s}$$

$$f_{st} = 350 \text{ Hz} \quad \omega_{st} = 700 \text{ rad/s}$$

$$f_s = 5000 \text{ Hz}$$

$$T_s = \frac{1}{f_s} = 2 \times 10^{-4} \text{ s}$$

$$\begin{aligned} \text{Prewarping } \omega_c &= \frac{2}{T_s} \tan \frac{\omega_c T_s}{2} \\ &= \cancel{7065 \text{ rad/s}} \quad 7265 \text{ rad/s} \end{aligned}$$

$$\omega_{st} = \frac{2}{T_s} \tan \frac{\omega_{st} T_s}{2} = 2235 \text{ rad/s}$$

Order $N=1$

$$H(s) = \frac{1}{s+1} \Big|_{s=\frac{7265}{s}} \quad \text{For HPF with order 1}$$

$$= \frac{s}{s+7265}$$

$$H(z) = H(s) \Big|_{s=\frac{2}{T_s} \left(\frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$\frac{s}{s+7265} \Big|_{s=\frac{2}{T_s} \left(\frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$= 10000 \left(\frac{1 - z^{-1}}{1 + z^{-1}} \right)$$

$$10000 \left(\frac{1 - z^{-1}}{1 + z^{-1}} \right) + 7265$$

$$= \frac{0.5792 (1 - z^{-1})}{1 - 0.1584 z^{-1}}$$

$$Y(z) = 0.1584 z^{-1} Y(z) + 0.5792 X(z) - 0.5792 z^{-1} X(z)$$