

# Capability-Flavoured Effects

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Many modern applications require developers to build safe systems out of potentially unsafe components, but existing languages are insufficient in the techniques they provide for identifying untrustworthy or unsafe code. This report explores how capability-safety enables a low overhead effect-system that can reason about the authority of unannotated code. We demonstrate this with a capability calculus CC and give several scenarios where it helps developers make more informed choices about whether to trust code.

CCS Concepts: •**Computer systems organization** → **Embedded systems**; *Redundancy*; Robotics; •**Networks** → Network reliability;

General Terms: Capabilities, effects

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## 1 INTRODUCTION

Good software is distinguished from bad software by qualities such as security, maintainability, and performance. We are interested in how the design of a programming language and its type system can make it easier to write secure software.

There are different situations where we may not trust code. One example is in a development environment adhering to ideas of *code ownership*, wherein developers may exercise responsibility for specific components of the system [1]. When a developer writes code to interact with another component, they can make false assumptions about how it should be used. This can break correctness or leave components in a malconfigured state, putting the whole system at risk. Another setting involves applications which allow third-party plug-ins, some of which could be malicious. Such an example is a web mash-up, which brings together several disparate web applications into one unified service. In both cases, despite the presence of untrustworthy components, we want the system to function securely.

It is difficult to determine if a piece of code should be trusted, but a range of approaches can be taken about the issue. One is to *sandbox* untrusted code inside a virtual environment. If anything goes wrong, damage

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is theoretically limited to the virtual environment, but in practice there are many vulnerabilities [3, 7, 15, 19]. Verification gives a comprehensive analysis of the behaviour of code, but the techniques are heavyweight and developers must have a deep understanding of how they work in order to use them [5]. Furthermore, verification requires a complete specification of the system, which may be undefined or evolving throughout the development process. Lightweight analyses, such as type systems, are easy for the developer to use, but existing languages are insufficient in the tools they provide for detecting and isolating untrustworthy components [2, 18]. A qualitative approach might be taken, where software is developed according to best-practice guidelines. One such guideline is the *principle of least authority*: that software components should only have access to the information and resources necessary for their purpose [13]. For example, a logger module, which only needs to append to a file, should not be given arbitrary read-write access. Another is *privilege separation*, where the division of a program into components is informed by what resources are needed and how they are to be propagated [14]. This report focuses on the class of lightweight analyses, and in particular how type systems can be used to reject unsafe programs and put developers in a more informed position to make qualitative assessments.

One approach to privilege separation is the capability model. A *capability* is an unforgeable token granting its bearer permission to perform some operation [4]. For example, a system resource like a file or socket can only be used through a capability granting operations on it. Capabilities also encapsulate the source of *effects*, which describe intensional details about the way in which a program executes [10]. For example, a logger might append to a File, and so executing its code would incur a File.append effect. In the capability model, this requires the logger to possess a capability granting it the ability to append to that particular file.

Although the idea of a capability is an old one, there has been recent interest in its application to programming language design. Miller has identified the ways in which capabilities should proliferate to encourage *robust composition* — a set of ideas summarised by “only connectivity begets connectivity” [9]. As a result, a program’s components are explicitly parameterised by the capabilities they may use; the only effects a component can incur are those for which it has been given a capability. Building on these ideas, Maffeis et. al. formalised the notion of a *capability-safe* language and showed a subset of Caja (a JavaScript implementation) is capability-safe [8]. Another capability-safe language, and one we use in this report, is Wyvern [11].

Effect systems were introduced by Lucassen and Gifford to determine what code can be safely parallelised [6]. They have also been applied to problems such as determining which functions might be invoked in a program [17] or determining which regions in memory may be accessed or updated [16]. Knowing what effects a piece of code might incur allows a developer to determine if code is trustworthy before executing it. This can be qualitatively assessed by comparing the static approximation of its effects to its expected least authority — a “logger” implementation which could write to a Socket is not to be trusted!

Despite these benefits, effect systems have seen little use in mainstream programming languages. Rytz et. al. believe the verbosity of their annotations is the main reason [12]. Successive works have focussed on reducing the developer overhead through techniques such as inference. Inference enables developers to rapidly prototype without annotations, incrementally adding them as their safety needed, but the benefit of capabilities for this has received less attention: because capabilities encapsulate the source of effects, and because capability-safety impose constraints on how they can propagate through the system, the effects of a piece of code can be safely approximated by inspecting what capabilities are passed into it. This is the key contribution of this report: capability-safety facilitates a lightweight, incremental effect discipline.

We begin by discussing preliminary concepts involving the formal definition of programming languages, effect systems, and Miller’s capability model. Chapter 3 introduces the Operation Calculus OC, a typed lambda calculus with a simple notion of capabilities and their operations in which all code is effect-annotated. Relaxing this requirement, we then introduce the Capability Calculus CC, which permits the nesting of unannotated code inside annotated code in a controlled, capability-safe manner. A safe inference about the unannotated code can be made

by inspecting the capabilities passed into it from its annotated surroundings. In chapter 4 we show how CC can model practical examples. We finish with a summary and a literature comparison.

## 2 BACKGROUND

This is the background.

## 3 CALCULI

## 4 APPLICATIONS

## 5 CONCLUSIONS

## A OC PROOFS

LEMMA A.1 (OC CANONICAL FORMS). *Unless the rule used is  $\varepsilon$ -SUBSUME, the following are true:*

- (1) *If  $\Gamma \vdash x : \tau$  with  $\varepsilon$  then  $\varepsilon = \emptyset$ .*
- (2) *If  $\Gamma \vdash v : \tau$  with  $\varepsilon$  then  $\varepsilon = \emptyset$ .*
- (3) *If  $\Gamma \vdash v : \{\bar{r}\}$  with  $\varepsilon$  then  $v = r$  and  $\{\bar{r}\} = \{r\}$ .*
- (4) *If  $\Gamma \vdash v : \tau_1 \rightarrow_{\varepsilon'} \tau_2$  with  $\varepsilon$  then  $v = \lambda x : \tau.e$ .*

PROOF.

- (1) The only rule that applies to variables is  $\varepsilon$ -VAR which ascribes the type  $\emptyset$ .
- (2) By definition a value is either a resource literal or a lambda. The only rules which can type values are  $\varepsilon$ -RESOURCE and  $\varepsilon$ -ABS. In the conclusions of both,  $\varepsilon = \emptyset$ .
- (3) The only rule ascribing the type  $\{\bar{r}\}$  is  $\varepsilon$ -RESOURCE. Its premises imply the result.
- (4) The only rule ascribing the type  $\tau_1 \rightarrow_{\varepsilon'} \tau_2$  is  $\varepsilon$ -ABS. Its premises imply the result.

□

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THEOREM A.2 (OC PROGRESS). *If  $\Gamma \vdash e : \tau$  with  $\varepsilon$  and  $e$  is not a value or variable, then  $e \longrightarrow e' \mid \varepsilon$ , for some  $e', \varepsilon$ .*

PROOF. By induction on  $\Gamma \vdash e : \tau$  with  $\varepsilon$ .

Case:  $\varepsilon$ -VAR,  $\varepsilon$ -RESOURCE, or  $\varepsilon$ -ABS. Then  $e$  is a value or variable and the theorem statement holds vacuously.

Case:  $\varepsilon$ -APP. Then  $e = e_1 e_2$ . If  $e_1$  is not a value or variable it can be reduced  $e_1 \longrightarrow e'_1 \mid \varepsilon$  by inductive assumption, so  $e_1 e_2 \longrightarrow e'_1 e_2 \mid \varepsilon$  by E-APP1. If  $e_1 = v_1$  is a value and  $e_2$  a non-value, then  $e_2$  can be reduced  $e_2 \longrightarrow e'_2 \mid \varepsilon$  by inductive assumption, so  $e_1 e_2 \longrightarrow v_1 e'_2 \mid \varepsilon$  by E-APP2. Otherwise  $e_1 = v_1$  and  $e_2 = v_2$  are both values. By inversion on  $\varepsilon$ -APP and canonical forms,  $\Gamma \vdash v_1 : \tau_2 \rightarrow_{\varepsilon'} \tau_3$  with  $\emptyset$ , and  $v_1 = \lambda x : \tau_2.e_{body}$ . Then  $(\lambda x : \tau_2.e_{body})v_2 \longrightarrow [v_2/x]e_{body} \mid \emptyset$  by E-APP3.

Case:  $\varepsilon$ -OPERCALL. Then  $e = e_1.\pi$ . If  $e_1$  is a non-value it can be reduced  $e_1 \longrightarrow e'_1 \mid \varepsilon$  by inductive assumption, so  $e_1.\pi \longrightarrow e'_1.\pi \mid \varepsilon$  by E-OPERCALL1. Otherwise  $e_1 = v_1$  is a value. By inversion on  $\varepsilon$ -OPERCALL and canonical forms,  $\Gamma \vdash v_1 : \{r\}$  with  $\{r.\pi\}$ , and  $v_1 = r$ . Then  $r.\pi \longrightarrow \text{unit} \mid \{r.\pi\}$  by E-OPERCALL2.

Case:  $\varepsilon$ -SUBSUME. If  $e$  is a value or variable, the theorem holds vacuously. Otherwise by inversion on  $\varepsilon$ -SUBSUME,  $\Gamma \vdash e : \tau'$  with  $\varepsilon'$ , and  $e \longrightarrow e' \mid \varepsilon$  by inductive assumption.

□

LEMMA A.3 (OC SUBSTITUTION). *If  $\Gamma, x : \tau' \vdash e : \tau$  with  $\varepsilon$  and  $\Gamma \vdash v : \tau'$  with  $\emptyset$  then  $\Gamma \vdash [v/x]e : \tau$  with  $\varepsilon$ .*

PROOF. By induction on the derivation of  $\Gamma, x : \tau' \vdash e : \tau$  with  $\varepsilon$ .

*Case:  $\varepsilon$ -VAR.* Then  $e = y$  is a variable. Either  $y = x$  or  $y \neq x$ . Suppose  $y = x$ . By applying canonical Forms to the theorem assumption  $\Gamma, x : \tau' \vdash e : \tau'$  with  $\emptyset$ , hence  $\tau' = \tau$ .  $[v/x]y = [v/x]x = v$ , and by assumption,  $\Gamma \vdash v : \tau'$  with  $\emptyset$ , so  $\Gamma \vdash [v/x]y : \tau$  with  $\emptyset$ .

Otherwise  $y \neq x$ . By applying canonical forms to the theorem assumption  $\Gamma, x : \tau' \vdash y : \tau$  with  $\emptyset$ , so  $y : \tau \in \Gamma$ . Since  $[v/x]y = y$ , then  $\Gamma \vdash y : \tau$  with  $\emptyset$  by  $\varepsilon$ -VAR.

*Case:  $\varepsilon$ -RESOURCE.* Because  $e = r$  is a resource literal then  $\Gamma \vdash r : \{r\}$  with  $\emptyset$  by canonical forms. By definition  $[v/x]r = r$ , so  $\Gamma \vdash [v/x]r : \{\bar{r}\}$  with  $\emptyset$ .

*Case:  $\varepsilon$ -APP.* By inversion  $\Gamma, x : \tau' \vdash e_1 : \tau_2 \rightarrow_{\varepsilon_3} \tau_3$  with  $\varepsilon_A$  and  $\Gamma, x : \tau' \vdash e_2 : \tau_2$  with  $\varepsilon_B$ , where  $\varepsilon = \varepsilon_A \cup \varepsilon_B \cup \varepsilon_3$  and  $\tau = \tau_3$ . From inversion on  $\varepsilon$ -APP and inductive assumption,  $\Gamma \vdash [v/x]e_1 : \tau_2 \rightarrow_{\varepsilon_3} \tau_3$  with  $\varepsilon_A$  and  $\Gamma \vdash [v/x]e_2 : \tau_2$  with  $\varepsilon_B$ . By  $\varepsilon$ -APP  $\Gamma \vdash ([v/x]e_1)([v/x]e_2) : \tau_3$  with  $\varepsilon_A \cup \varepsilon_B \cup \varepsilon_3$ . By simplifying and applying the definition of substitution, this is the same as  $\Gamma \vdash [v/x](e_1 e_2) : \tau$  with  $\varepsilon$ .

*Case:  $\varepsilon$ -OPERCALL.* By inversion  $\Gamma, x : \tau' \vdash e_1 : \{\bar{r}\}$  with  $\varepsilon_1$  and  $\tau = \text{Unit}$  and  $\varepsilon = \varepsilon_1 \cup \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$ . By inductive assumption,  $\Gamma \vdash [v/x]e_1 : \{\bar{r}\}$  with  $\varepsilon_1$ . Then by  $\varepsilon$ -OPERCALL,  $\Gamma \vdash ([v/x]e_1).\pi : \text{Unit}$  with  $\varepsilon_1 \cup \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$ . By simplifying and applying the definition of substitution, this is the same as  $\Gamma \vdash [v/x](e_1.\pi) : \tau$  with  $\varepsilon$ .

*Case:  $\varepsilon$ -SUBSUME.* By inversion,  $\Gamma, x : \tau' \vdash e : \tau_2$  with  $\varepsilon_2$ , where  $\tau_2 < \tau$  and  $\varepsilon_2 \subseteq \varepsilon$ . By inductive hypothesis,  $\Gamma \vdash [v/x]e : \tau_2$  with  $\varepsilon_2$ . Then  $\Gamma \vdash [v/x]e : \tau$  with  $\varepsilon$  by  $\varepsilon$ -SUBSUME. □

THEOREM A.4 (OC PRESERVATION). *If  $\Gamma \vdash e_A : \tau_A$  with  $\varepsilon_A$  and  $e_A \rightarrow e_B \mid \varepsilon$ , then  $\tau_B < \tau_A$  and  $\varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$ , for some  $e_B, \varepsilon, \tau_B, \varepsilon_B$ .*

PROOF. By induction on the derivation of  $\Gamma \vdash e_A : \tau_A$  with  $\varepsilon_A$  and then the derivation of  $e_A \rightarrow e_B \mid \varepsilon$ .

*Case:  $\varepsilon$ -VAR,  $\varepsilon$ -RESOURCE,  $\varepsilon$ -UNIT,  $\varepsilon$ -ABS.* Then  $e_A$  is a value and cannot be reduced, so the theorem holds vacuously.

*Case:  $\varepsilon$ -APP.* Then  $e_A = e_1 e_2$  and  $\Gamma \vdash e_1 : \tau_2 \rightarrow_{\varepsilon_3} \tau_3$  with  $\varepsilon_1$  and  $\Gamma \vdash e_2 : \tau_2$  with  $\varepsilon_2$  and  $\tau_B = \tau_3$  and  $\varepsilon_A = \varepsilon_1 \cup \varepsilon_2 \cup \varepsilon_3$ . In each case we choose  $\tau_B = \tau_A$  and  $\varepsilon_B \cup \varepsilon = \varepsilon_A$ .

**Subcase: E-APP1.** Then  $e_1 e_2 \rightarrow e'_1 e_2 \mid \varepsilon$ . By inversion on E-APP1,  $e_1 \rightarrow e'_1 \mid \varepsilon$ . By inductive hypothesis and  $\varepsilon$ -SUBSUME  $\Gamma \vdash v_1 : \tau_2 \rightarrow_{\varepsilon_3} \tau_3$  with  $\varepsilon_1$ . Then  $\Gamma \vdash e'_1 e_2 : \tau_3$  with  $\varepsilon_1 \cup \varepsilon_2 \cup \varepsilon_3$  by  $\varepsilon$ -APP.

**Subcase: E-APP2.** Then  $e_1 = v_1$  is a value and  $e_2 \rightarrow e'_2 \mid \varepsilon$ . By inversion on E-APP2,  $e_2 \rightarrow e'_2 \mid \varepsilon$ . By inductive hypothesis and  $\varepsilon$ -SUBSUME  $\Gamma \vdash e'_2 : \tau_2$  with  $\varepsilon_2$ . Then  $\Gamma \vdash v_1 e'_2 : \tau_3$  with  $\varepsilon_1 \cup \varepsilon_2 \cup \varepsilon_3$  by  $\varepsilon$ -APP.

**Subcase: E-APP3.** Then  $e_1 = \lambda x : \tau_2.e_{body}$  and  $e_2 = v_2$  are values and  $(\lambda x : \tau_2.e_{body}) v_2 \rightarrow [v_2/x]e_{body} \mid \emptyset$ . By inversion on the rule  $\varepsilon$ -APP used to type  $\lambda x : \tau_2.e_{body}$ , we know  $\Gamma, x : \tau_2 \vdash e_{body} : \tau_3$  with  $\varepsilon_3$ .  $e_1 = v_1$  and  $e_2 = v_2$  are values, so  $\varepsilon_1 = \varepsilon_2 = \emptyset$  by canonical forms. Then by the substitution lemma,  $\Gamma \vdash [v_2/x]e_{body} : \tau_3$  with  $\varepsilon_3$  and  $\varepsilon_A = \varepsilon_B = \varepsilon$ .

*Case:  $\varepsilon$ -OPERCALL.* Then  $e_A = e_1.\pi$  and  $\Gamma \vdash e_1 : \{\bar{r}\}$  with  $\varepsilon_1$  and  $\tau_A = \text{Unit}$  and  $\varepsilon_A = \varepsilon_1 \cup \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$ .

**Subcase:** E-OPERCALL1. Then  $e_1.\pi \longrightarrow e'_1.\pi \mid \varepsilon$ . By inversion on E-OPERCALL1,  $e_1 \longrightarrow e'_1 \mid \varepsilon$ . By inductive hypothesis and application of  $\varepsilon$ -SUBSUME,  $\Gamma \vdash e'_1 : \{\bar{r}\}$  with  $\varepsilon_1$ . Then  $\Gamma \vdash e'_1.\pi : \{\bar{r}\}$  with  $\varepsilon_1 \cup \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$  by  $\varepsilon$ -OPERCALL.

**Subcase:** E-OPERCALL2. Then  $e_1 = r$  is a resource literal and  $r.\pi \longrightarrow \text{unit} \mid \{r.\pi\}$ . By canonical forms,  $\varepsilon_1 = \emptyset$ . By  $\varepsilon$ -UNIT,  $\Gamma \vdash \text{unit} : \text{Unit}$  with  $\emptyset$ . Therefore  $\tau_B = \tau_A$  and  $\varepsilon \cup \varepsilon_B = \{r.\pi\} = \varepsilon_A$ .  $\square$

**THEOREM A.5 (OC SINGLE-STEP SOUNDNESS).** *If  $\Gamma \vdash e_A : \tau_A$  with  $\varepsilon_A$  and  $e_A$  is not a value, then  $e_A \longrightarrow e_B \mid \varepsilon$ , where  $\Gamma \vdash e_B : \tau_B$  with  $\varepsilon_B$  and  $\tau_B <: \tau_A$  and  $\varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$ , for some  $e_B, \varepsilon, \tau_B, \varepsilon_B$ .*

**PROOF.** If  $e_A$  is not a value then the reduction exists by the progress theorem. The rest follows by the preservation theorem.  $\square$

**THEOREM A.6 (OC MULTI-STEP SOUNDNESS).** *If  $\Gamma \vdash e_A : \tau_A$  with  $\varepsilon_A$  and  $e_A \longrightarrow^* e_B \mid \varepsilon$ , where  $\Gamma \vdash e_B : \tau_B$  with  $\varepsilon_B$  and  $\tau_B <: \tau_A$  and  $\varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$ .*

**PROOF.** By induction on the length of the multi-step reduction.

*Case:* Length 0. Then  $e_A = e_B$  and  $\tau_A = \tau_B$  and  $\varepsilon = \emptyset$  and  $\varepsilon_A = \varepsilon_B$ .

*Case:* Length  $n + 1$ . By inversion the multi-step can be split into a multi-step of length  $n$ , which is  $e_A \longrightarrow^* e_C \mid \varepsilon'$ , and a single-step of length 1, which is  $e_C \longrightarrow e_B \mid \varepsilon''$ , where  $\varepsilon = \varepsilon' \cup \varepsilon''$ . By inductive assumption and preservation theorem,  $\Gamma \vdash e_C : \tau_C$  with  $\varepsilon_C$  and  $\Gamma \vdash e_B : \tau_B$  with  $\varepsilon_B$ , where  $\tau_C <: \tau_A$  and  $\varepsilon_C \cup \varepsilon' \subseteq \varepsilon_A$ . By single-step soundness,  $\tau_B <: \tau_C$  and  $\varepsilon_B \cup \varepsilon'' \subseteq \varepsilon_C$ . Then by transitivity,  $\tau_B <: \tau$  and  $\varepsilon_B \cup \varepsilon' \cup \varepsilon'' = \varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$ .  $\square$

## B CC PROOFS

**LEMMA B.1 (CC CANONICAL FORMS).** *Unless the rule used is  $\varepsilon$ -SUBSUME, the following are true:*

- (1) *If  $\hat{\Gamma} \vdash x : \hat{\tau}$  with  $\varepsilon$  then  $\varepsilon = \emptyset$ .*
- (2) *If  $\hat{\Gamma} \vdash \hat{v} : \hat{\tau}$  with  $\varepsilon$  then  $\varepsilon = \emptyset$ .*
- (3) *If  $\hat{\Gamma} \vdash \hat{v} : \{\bar{r}\}$  with  $\varepsilon$  then  $\hat{v} = r$  and  $\{\bar{r}\} = \{r\}$ .*
- (4) *If  $\hat{\Gamma} \vdash \hat{v} : \hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2$  with  $\varepsilon$  then  $\hat{v} = \lambda x : \tau. \hat{e}$ .*

**PROOF.** Same as for OC.  $\square$

**THEOREM B.2 (CC PROGRESS).** *If  $\hat{\Gamma} \vdash \hat{e} : \hat{\tau}$  with  $\varepsilon$  and  $\hat{e}$  is not a value, then  $\hat{e} \longrightarrow \hat{e}' \mid \varepsilon$ , for some  $\hat{e}', \varepsilon$ .*

**PROOF.** By induction on the derivation of  $\hat{\Gamma} \vdash \hat{e} : \hat{\tau}$  with  $\varepsilon$ .

*Case:*  $\varepsilon$ -MODULE. Then  $\hat{e} = \text{import}(\varepsilon_s) x = \hat{e}_i$  in  $e$ . If  $\hat{e}_i$  is a non-value then  $\hat{e}_i \longrightarrow \hat{e}'_i \mid \varepsilon$  by inductive assumption and  $\text{import}(\varepsilon_s) x = \hat{e}_i$  in  $e \longrightarrow \text{import}(\varepsilon_s) x = \hat{e}'_i$  in  $e \mid \varepsilon$  by E-MODULE1. Otherwise  $\hat{e}_i = \hat{v}_i$  is a value and  $\text{import}(\varepsilon_s) x = \hat{v}_i$  in  $e \longrightarrow [\hat{v}_i/x] \text{annot}(e, \varepsilon_s) \mid \emptyset$  by E-MODULE2.  $\square$

**LEMMA B.3 (CC SUBSTITUTION).** *If  $\hat{\Gamma}, x : \hat{\tau}' \vdash \hat{e} : \hat{\tau}$  with  $\varepsilon$  and  $\hat{\Gamma} \vdash \hat{v} : \hat{\tau}'$  with  $\emptyset$  then  $\hat{\Gamma} \vdash [\hat{v}/x] \hat{e}_A : \hat{\tau}$  with  $\varepsilon$ .*

PROOF. By induction on the derivation of  $\hat{\Gamma}, x : \hat{\tau}' \vdash \hat{e} : \hat{\tau}$  with  $\varepsilon$ .

Case:  $\varepsilon$ -MODULE. Then the following are true.

- (1)  $\hat{e} = \text{import}(\varepsilon_s) x = \hat{e}_i$  in  $e$
- (2)  $\hat{\Gamma}, y : \hat{\tau}' \vdash \hat{e}_i : \hat{\tau}_i$  with  $\varepsilon_i$
- (3)  $y : \text{erase}(\hat{\tau}_i) \vdash e : \tau$
- (4)  $\hat{\Gamma}, y : \hat{\tau}' \vdash \text{import}(\varepsilon_s) x = \hat{e}_i$  in  $e : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s \cup \varepsilon_i$
- (5)  $\varepsilon_s = \text{effects}(\hat{\tau}_i) \cup \text{ho-effects}(\text{annot}(\tau, \emptyset))$
- (6)  $\hat{\tau}_A = \text{annot}(\tau, \varepsilon)$
- (7)  $\hat{\varepsilon}_A = \varepsilon_s \cup \varepsilon_i$

By applying inductive assumption to (2)  $\hat{\Gamma} \vdash [\hat{v}/x]\hat{e}_i : \hat{\tau}_i$  with  $\varepsilon_i$ . Then by  $\varepsilon$ -MODULE  $\hat{\Gamma} \vdash \text{import}(\varepsilon_s) y = [\hat{v}/x]\hat{e}_i$  in  $e : \text{annot}(\tau_i, \varepsilon_s)$  with  $\varepsilon_s \cup \varepsilon_i$ . By definition of substitution, the form in this judgement is the same as  $[\hat{v}/x]\hat{e}$ .  $\square$

LEMMA B.4 (CC APPROXIMATION 1). *If  $\text{effects}(\hat{\tau}) \subseteq \varepsilon$  and  $\text{ho-safe}(\hat{\tau}, \varepsilon)$  then  $\hat{\tau} <: \text{annot}(\text{erase}(\hat{\tau}), \varepsilon)$ .*

LEMMA B.5 (CC APPROXIMATION 2). *If  $\text{ho-effects}(\hat{\tau}) \subseteq \varepsilon$  and  $\text{safe}(\hat{\tau}, \varepsilon)$  then  $\text{annot}(\text{erase}(\hat{\tau}), \varepsilon) <: \hat{\tau}$ .*

PROOF. By simultaneous induction on derivations of safe and ho-safe.

Case:  $\hat{\tau} = \{\bar{\tau}\}$  Then  $\hat{\tau} = \text{annot}(\text{erase}(\hat{\tau}), \varepsilon)$  and the results for both lemmas hold immediately.

Case:  $\hat{\tau} = \hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2$ ,  $\text{effects}(\hat{\tau}) \subseteq \varepsilon$ ,  $\text{ho-safe}(\hat{\tau}, \varepsilon)$  It is sufficient to show  $\hat{\tau}_2 <: \text{annot}(\text{erase}(\hat{\tau}_2), \varepsilon)$  and  $\text{annot}(\text{erase}(\hat{\tau}_1), \varepsilon) <: \hat{\tau}_1$ , because the result will hold by S-EFFECTS. To achieve this we shall inductively apply lemma 1 to  $\hat{\tau}_2$  and lemma 2 to  $\hat{\tau}_1$ .

From  $\text{effects}(\hat{\tau}) \subseteq \varepsilon$  we have  $\text{ho-effects}(\hat{\tau}_1) \cup \varepsilon' \cup \text{effects}(\hat{\tau}_2) \subseteq \varepsilon$  and therefore  $\text{effects}(\hat{\tau}_2) \subseteq \varepsilon$ . From  $\text{ho-safe}(\hat{\tau}, \varepsilon)$  we have  $\text{ho-safe}(\hat{\tau}_2, \varepsilon)$ . Therefore we can apply lemma 1 to  $\hat{\tau}_2$ .

From  $\text{effects}(\hat{\tau}) \subseteq \varepsilon$  we have  $\text{ho-effects}(\hat{\tau}_1) \cup \varepsilon' \cup \text{effects}(\hat{\tau}_2) \subseteq \varepsilon$  and therefore  $\text{ho-effects}(\hat{\tau}_1) \subseteq \varepsilon$ . From  $\text{ho-safe}(\hat{\tau}, \varepsilon)$  we have  $\text{ho-safe}(\hat{\tau}_1, \varepsilon)$ . Therefore we can apply lemma 2 to  $\hat{\tau}_1$ .

Case:  $\hat{\tau} = \hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2$ ,  $\text{ho-effects}(\hat{\tau}) \subseteq \varepsilon$ ,  $\text{safe}(\hat{\tau}, \varepsilon)$  It is sufficient to show  $\text{annot}(\text{erase}(\hat{\tau}_2), \varepsilon) <: \hat{\tau}_2$  and  $\hat{\tau}_1 <: \text{annot}(\text{erase}(\hat{\tau}_1), \varepsilon)$ , because the result will hold by S-EFFECTS. To achieve this we shall inductively apply lemma 2 to  $\hat{\tau}_2$  and lemma 1 to  $\hat{\tau}_1$ .

From  $\text{ho-effects}(\hat{\tau}) \subseteq \varepsilon$  we have  $\text{effects}(\hat{\tau}_1) \cup \text{ho-effects}(\hat{\tau}_2) \subseteq \varepsilon$  and therefore  $\text{ho-effects}(\hat{\tau}_2) \subseteq \varepsilon$ . From  $\text{safe}(\hat{\tau}, \varepsilon)$  we have  $\text{safe}(\hat{\tau}_2, \varepsilon)$ . Therefore we can apply lemma 2 to  $\hat{\tau}_2$ .

From  $\text{ho-effects}(\hat{\tau}) \subseteq \varepsilon$  we have  $\text{effects}(\hat{\tau}_1) \cup \text{ho-effects}(\hat{\tau}_2) \subseteq \varepsilon$  and therefore  $\text{effects}(\hat{\tau}_1) \subseteq \varepsilon$ . From  $\text{safe}(\hat{\tau}, \varepsilon)$  we have  $\text{ho-safe}(\hat{\tau}_1, \varepsilon)$ . Therefore we can apply lemma 1 to  $\hat{\tau}_1$ .  $\square$

LEMMA B.6 (CC ANNOTATION). *If the following are true:*

- (1)  $\hat{\Gamma} \vdash \hat{v}_i : \hat{\tau}_i$  with  $\emptyset$
- (2)  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e : \tau$
- (3)  $\text{effects}(\hat{\tau}_i) \cup \text{ho-effects}(\text{annot}(\tau, \emptyset)) \cup \text{effects}(\text{annot}(\Gamma, \emptyset)) \subseteq \varepsilon_s$
- (4)  $\text{ho-safe}(\hat{\tau}_i, \varepsilon_s)$

Then  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ .

PROOF. By induction on the derivation of  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e : \tau$ . When applying the inductive assumption,  $e$ ,  $\tau$ , and  $\Gamma$  may vary, but the other variables are fixed.

Case: *T-VAR*. Then  $e = x$  and  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash x : \tau$ . Either  $x = y$  or  $x \neq y$ .

**Subcase 1:**  $x = y$ . Then  $y : \text{erase}(\hat{\tau}_i) \vdash y : \tau$  so  $\tau = \text{erase}(\hat{\tau}_i)$ . By  $\varepsilon$ -VAR,  $y : \hat{\tau}_i \vdash x : \hat{\tau}_i$  with  $\emptyset$ . By definition  $\text{annot}(x, \varepsilon_s) = x$ , so (5)  $y : \hat{\tau}_i \vdash \text{annot}(x, \varepsilon_s) : \hat{\tau}_i$  with  $\emptyset$ . By (3) and (4) we know  $\text{effects}(\hat{\tau}_i) \subseteq \varepsilon_s$  and  $\text{ho-safe}(\hat{\tau}_i, \varepsilon_s)$ . By the approximation lemma,  $\hat{\tau}_i <: \text{annot}(\text{erase}(\hat{\tau}_i), \varepsilon_s)$ . We know  $\text{erase}(\hat{\tau}_i) = \tau$ , so this judgement can be rewritten as  $\hat{\tau}_i <: \text{annot}(\tau, \varepsilon_s)$ . From this we can use  $\varepsilon$ -SUBSUME to narrow the type of (5) and widen the approximate effects of (5) from  $\emptyset$  to  $\varepsilon_s$ , giving  $y : \hat{\tau}_i \vdash \text{annot}(x, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ . Finally, by widening the context,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), \hat{\tau}_i \vdash \text{annot}(x, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ .

**Subcase 2:**  $x \neq y$ . Because  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash x : \tau$  and  $x \neq y$  then  $x : \tau \in \Gamma$ . Then  $x : \text{annot}(\tau, \varepsilon_s) \in \text{annot}(\Gamma, \varepsilon_s)$  so  $\text{annot}(\Gamma, \varepsilon_s) \vdash x : \text{annot}(\tau, \varepsilon_s)$  with  $\emptyset$  by  $\varepsilon$ -VAR. By definition  $\text{annot}(x, \varepsilon_s) = x$ , so  $\text{annot}(\Gamma, \varepsilon_s) \vdash \text{annot}(x, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\emptyset$ . Applying  $\varepsilon$ -SUBSUME gives  $\text{annot}(\Gamma, \varepsilon_s) \vdash \text{annot}(x, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ . By widening the context  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(x, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ .

Case: *T-RESOURCE*. Then  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash r : \{r\}$ . By  $\varepsilon$ -RESOURCE,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon), y : \hat{\tau}_i \vdash r : \{r\}$  with  $\emptyset$ . Applying definitions,  $\text{annot}(r, \varepsilon) = r$  and  $\text{annot}(\{r\}, \varepsilon_s) = \{r\}$ , so this judgement can be rewritten as  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon), y : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\emptyset$ . By  $\varepsilon$ -SUBSUME,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ .

Case: *T-ABS*. Then  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash \lambda x : \tau_2. e_{\text{body}} : \tau_2 \rightarrow \tau_3$ . Applying definitions, (5)  $\text{annot}(e, \varepsilon_s) = \text{annot}(\lambda x : \tau_2. e_{\text{body}}, \varepsilon_s) = \lambda x : \text{annot}(\tau_2, \varepsilon_s). \text{annot}(e_{\text{body}}, \varepsilon_s)$  and  $\text{annot}(\tau, \varepsilon_s) = \text{annot}(\tau_2 \rightarrow \tau_3, \varepsilon_s) = \text{annot}(\tau_2, \varepsilon_s) \rightarrow_{\varepsilon_s} \text{annot}(\tau_3, \varepsilon_s)$ . By inversion on T-ABS, we get the sub-derivation (6)  $\Gamma, y : \text{erase}(\hat{\tau}_i), x : \tau_2 \vdash e_{\text{body}} : \tau_2$ . We shall apply the inductive assumption to this judgement with an unannotated context consisting of  $\Gamma, x : \tau_2$ . To be a valid application of the lemma, it is required that  $\text{effects}(\text{annot}(\Gamma, x : \tau_2, \emptyset)) \subseteq \varepsilon_s$ . We already know  $\text{effects}(\text{annot}(\Gamma, \emptyset)) \subseteq \varepsilon_s$  by assumption (3). Also by assumption (3),  $\text{ho-effects}(\text{annot}(\tau_2 \rightarrow \tau_3, \emptyset)) \subseteq \varepsilon_s$ ; then by definition of ho-effects,  $\text{effects}(\text{annot}(\tau_2, \emptyset)) \subseteq \text{ho-effects}(\text{annot}(\tau_2 \rightarrow \tau_3, \emptyset))$ , so  $\text{effects}(\text{annot}(x : \tau_2, \emptyset)) \subseteq \varepsilon_s$  by transitivity. Then by applying the inductive assumption to (6),  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), \text{annot}(x : \tau_2, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e_{\text{body}}, \varepsilon_s) : \text{annot}(\tau_3, \varepsilon_s)$  with  $\varepsilon_s$ . By  $\varepsilon$ -ABS,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \lambda x : \text{annot}(\hat{\tau}_2, \varepsilon_s). \text{annot}(e_{\text{body}}, \varepsilon_s) : \text{annot}(\hat{\tau}_2, \varepsilon_s) \rightarrow_{\varepsilon_s} \text{annot}(\hat{\tau}_3, \varepsilon_s)$  with  $\emptyset$ . By applying the identities from (5), this judgement can be rewritten as  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\emptyset$ . Finally, by applying  $\varepsilon$ -SUBSUME,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ .

Case: *T-APP*. Then  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e_1 e_2 : \tau_3$  and by inversion  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e_1 : \tau_2 \rightarrow \tau_3$  and  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e_2 : \tau_2$ . By applying the inductive assumption to these judgements,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e_1, \varepsilon_s) : \text{annot}(\tau_2, \varepsilon_s) \rightarrow_{\varepsilon_s} \text{annot}(\tau_3, \varepsilon_s)$  with  $\varepsilon_s$  and  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e_2, \varepsilon_s) : \text{annot}(\tau_2, \varepsilon_s)$  with  $\varepsilon_s$ . Then by  $\varepsilon$ -APP, we get  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e_1, \varepsilon_s) \text{annot}(e_2, \varepsilon_s) : \text{annot}(\tau_3, \varepsilon)$  with  $\varepsilon$ . Unfolding the definition of  $\text{annot}$ , this judgement can be rewritten as  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e_1 e_2, \varepsilon_s) : \text{annot}(\tau_3, \varepsilon)$  with  $\varepsilon$ . Finally, because  $e = e_1 e_2$  and  $\tau = \tau_3$ , this is the same as  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon_s), y : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon)$  with  $\varepsilon$ .

Case: *T-OPERCALL*. Then  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e_1. \pi : \text{Unit}$ . By inversion we get the sub-derivation  $\Gamma, y : \text{erase}(\hat{\tau}_i) \vdash e_1 : \{\bar{r}\}$ . Applying the inductive assumption,  $\hat{\Gamma}, \text{annot}(\Gamma, \varepsilon), y : \hat{\tau}_i \vdash \text{annot}(e_1, \varepsilon_s) : \text{annot}(\{\bar{r}\}, \varepsilon_s)$  with  $\varepsilon_s$ . By definition,  $\text{annot}(\{\bar{r}\}, \varepsilon_s) = \{\bar{r}\}$ , so this judgement can be rewritten as  $\hat{\Gamma}, \text{annot}(\Gamma, \emptyset), y : \hat{\tau}_i \vdash e_1 : \{\bar{r}\}$  with  $\varepsilon_s$ . By

$\varepsilon$ -OPERCALL,  $\hat{\Gamma}, \text{annot}(\Gamma, \emptyset), y : \hat{\tau} \vdash \text{annot}(e_1.\pi, \varepsilon_s) : \{\bar{r}\}$  with  $\varepsilon_s \cup \{\bar{r}.\pi\}$ . All that remains is to show  $\{\bar{r}.\pi\} \subseteq \varepsilon$ . We shall do this by considering which subcontext left of the turnstile is capturing  $\{\bar{r}\}$ . Technically,  $\hat{\Gamma}$  may not have a binding for every  $r \in \bar{r}$ : the judgement for  $e_1$  might be derived using S-RESOURCES and  $\varepsilon$ -SUBSUME. However, at least one binding for some  $r \in \bar{r}$  must be present in  $\hat{\Gamma}$  to get the original typing judgement being subsumed, so we shall assume without loss of generality that  $\hat{\Gamma}$  contains a binding for every  $r \in \bar{r}$ .

**Subcase 1:**  $\{\bar{r}\} = \hat{\tau}$ . By assumption (3),  $\text{effects}(\hat{\tau}) \subseteq \varepsilon_s$ , so  $\bar{r}.\pi \subseteq \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\} = \text{effects}(\{\bar{r}\}) \subseteq \varepsilon_s$ .

**Subcase 2:**  $r : \{\bar{r}\} \in \text{annot}(\Gamma, \varepsilon_s)$ . Then  $\bar{r}.\pi \in \text{effects}(\{\bar{r}\}) \subseteq \text{effects}(\text{annot}(\Gamma, \emptyset))$ , and by assumption (3)  $\text{effects}(\text{annot}(\Gamma, \emptyset)) \subseteq \varepsilon_s$ , so  $\bar{r}.\pi \in \varepsilon_s$ .

**Subcase 3:**  $r : \{\bar{r}\} \in \hat{\Gamma}$ . Because  $\Gamma, y : \text{erase}(\hat{\tau}) \vdash e_1 : \{\bar{r}\}$ , then  $\bar{r} \in \Gamma$  or  $r = \tau$ . If  $r \in \text{annot}(\Gamma, \emptyset)$  then subcase 2 holds. Else  $r = \text{erase}(\hat{\tau})$ . Because  $\hat{\tau} = \{\bar{r}\}$ , then  $\text{erase}(\{\bar{r}\}) = \{\bar{r}\}$ , so  $\hat{\tau} = \tau$ ; therefore subcase 1 holds.  $\square$

**THEOREM B.7 (CC PRESERVATION).** *If  $\hat{\Gamma} \vdash \hat{e}_A : \hat{\tau}_A$  with  $\varepsilon_A$  and  $\hat{e}_A \longrightarrow \hat{e}_B \mid \varepsilon$ , then  $\hat{\Gamma} \vdash \hat{e}_B : \hat{\tau}_B$  with  $\varepsilon_B$ , where  $\hat{e}_B <: \hat{e}_A$  and  $\varepsilon \cup \varepsilon_B \subseteq \varepsilon_A$ , for some  $\hat{e}_B, \varepsilon, \hat{\tau}_B, \varepsilon_B$ .*

**PROOF.** By induction on the derivation of  $\hat{\Gamma} \vdash \hat{e}_A : \hat{\tau}_A$  with  $\varepsilon_A$  and then the derivation of  $\hat{e}_A \longrightarrow \hat{e}_B \mid \varepsilon$ .

*Case:  $\varepsilon$ -IMPORT.* Then by inversion on the rules used, the following are true:

- (1)  $\hat{e}_A = \text{import}(\varepsilon_s) x = \hat{e}_i$  in  $e$
- (2)  $x : \text{erase}(\hat{\tau}_i) \vdash e : \tau$
- (3)  $\hat{\Gamma} \vdash \hat{e}_i : \hat{\tau}_i$  with  $\varepsilon_1$
- (4)  $\hat{\Gamma} \vdash \hat{e}_A : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s \cup \varepsilon_1$
- (5)  $\text{effects}(\hat{\tau}_i) \cup \text{ho-effects}(\text{annot}(\tau, \emptyset)) \subseteq \varepsilon_s$
- (6)  $\text{ho-safe}(\hat{\tau}_i, \varepsilon_s)$

**Subcase 1:** E-IMPORT1. Then  $\text{import}(\varepsilon_s) x = \hat{e}_i$  in  $e \longrightarrow \text{import}(\varepsilon_s) x = \hat{e}'_i$  in  $e \mid \varepsilon$  and by inversion,  $\hat{e}_i \longrightarrow \hat{e}'_i \mid \varepsilon$ . By inductive assumption and subsumption,  $\hat{\Gamma} \vdash \hat{e}'_i : \hat{\tau}'_i$  with  $\varepsilon_1$ . Then by  $\varepsilon$ -IMPORT,  $\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e}'_i$  in  $e : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ .

**Subcase 2:** E-IMPORT2. Then  $\hat{e}_i = \hat{v}_i$  is a value and  $\varepsilon_1 = \emptyset$  by canonical forms. Apply the annotation lemma with  $\Gamma = \emptyset$  to get  $\hat{\Gamma}, x : \hat{\tau}_i \vdash \text{annot}(e, \varepsilon_s) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ . From assumption (4) and canonical forms we have  $\hat{\Gamma} \vdash \hat{v} : \hat{\tau}_i$  with  $\emptyset$ . Applying the substitution lemma,  $\hat{\Gamma} \vdash [\hat{v}_i/x] \text{annot}(e, \varepsilon) : \text{annot}(\tau, \varepsilon_s)$  with  $\varepsilon_s$ . Then  $\varepsilon \cup \varepsilon_B = \varepsilon_A = \varepsilon_s$  and  $\tau_A = \tau_B = \text{annot}(\tau, \varepsilon_s)$ .  $\square$

**THEOREM B.8 (CC SINGLE-STEP SOUNDNESS).** *If  $\hat{\Gamma} \vdash \hat{e}_A : \hat{\tau}_A$  with  $\varepsilon_A$  and  $\hat{e}_A$  is not a value, then  $\hat{e}_A \longrightarrow \hat{e}_B \mid \varepsilon$ , where  $\hat{\Gamma} \vdash \hat{e}_B : \hat{\tau}_B$  with  $\varepsilon_B$  and  $\hat{\tau}_B <: \hat{\tau}_A$  and  $\varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$ , for some  $\hat{e}_B, \varepsilon, \hat{\tau}_B$ , and  $\varepsilon_B$ .*

**THEOREM B.9 (CC MULTI-STEP SOUNDNESS).** *If  $\hat{\Gamma} \vdash \hat{e}_A : \hat{\tau}_A$  with  $\varepsilon_A$  and  $\hat{e}_A \longrightarrow^* e_B \mid \varepsilon$ , then  $\hat{\Gamma} \vdash \hat{e}_B : \hat{\tau}_B$  with  $\varepsilon_B$ , where  $\hat{\tau}_B <: \hat{\tau}_A$  and  $\varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$ , for some  $\hat{\tau}_B, \varepsilon_B$ .*

**PROOF.** The same as for OC.  $\square$



## C DESUGARING

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