1 Grammar

```
types
e ::=
                                                   exprs.
                                                                        \mid X
                                                                                                   type variable
                                                  variable
      \boldsymbol{x}
                                                                                                    effect set
                                                     value
      v
                                                                                                          arrow
                                           operation\ call
      e.\pi
                                                                                                  universal type
                                              application
      e e
                                        type\ application
                                                                     \hat{	au} ::=
                                                                                             annotated types
                                                                                                type variable
v ::=
                                                   values
                                                                                                   resource set
                                         resource literal
     r
                                                                                              annotated\ arrow
                                              abstraction
      \lambda x : \tau . e
                                                                            \forall X<:\hat{\tau}.\hat{\tau}
                                                                                               universal type
      \lambda X <: \tau.e
                                    type polymorphism
                                                                             \forall \phi \subseteq \varepsilon.\hat{\tau} \quad universal \ effect \ set
\hat{e} ::=
                                     annotated exprs.
                                                                                                           effects
                                                                     \varepsilon \; ::= \;
                                                  variable
                                                                                               effect\ variable
      \hat{v}
                                                     value
                                                                                                       effect set
      \hat{e}.\pi
                                           operation call
      \hat{e} \hat{e}
                                              application
                                                                                                       contexts
                                        type application
                                                                       Ø
                                                                                                      empty\ ctx.
                                     effect application
                                                                        \Gamma, x : \tau
                                                                                                 var. binding
      import(\varepsilon_s) \ x = \hat{e} \ in \ e
                                                   import
                                                                           \Gamma, X <: \tau
                                                                                              type var. binding
                                     annotated values
                                                                                         annotated contexts
    r
                                        resource\ literal
                                                                                                    empty \ ctx.
                                                                      \lambda x : \hat{\tau}.\hat{e}
                                              abstraction
     \lambda X <: \tau.\hat{e}
                                    type polymorphism
      \lambda \phi \subseteq \varepsilon.\hat{e}
                                 effect polymorphism
                                                                                           effect var. binding
```

2 Functions

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Definition (annot :: \tau \times \varepsilon \rightarrow \hat{\tau})
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```
 \begin{array}{l} 1. \  \, \operatorname{annot}(X, \square) = X \\ 2. \  \, \operatorname{annot}(\{\bar{r}\}, \square) = \{\bar{r}\} \\ 3. \  \, \operatorname{annot}(\tau_1 \to \tau_2, \varepsilon) = \operatorname{annot}(\tau_1, \varepsilon) \to_{\varepsilon} \operatorname{annot}(\tau_2, \varepsilon) \\ 4. \  \, \operatorname{annot}(\forall X <: \tau_1.\tau_2, \varepsilon) = \forall X <: \operatorname{annot}(\tau_1, \varepsilon).\operatorname{annot}(\tau_2, \varepsilon) \\ 5. \  \, \operatorname{annot}(\forall \phi \subseteq \varepsilon.\tau, \varepsilon) = \forall \phi \subseteq \varepsilon.\operatorname{annot}(\tau, \varepsilon) \end{array}
```

Definition (annot :: $e \times \varepsilon \rightarrow \hat{e}$)

```
 \begin{split} &1. \ \operatorname{annot}(x, \square) = e \\ &2. \ \operatorname{annot}(r, \square) = r \\ &3. \ \operatorname{annot}(\lambda x : \tau.e, \varepsilon) = \lambda x : \operatorname{annot}(\tau, \varepsilon).\operatorname{annot}(e, \varepsilon) \\ &4. \ \operatorname{annot}(e_1 \ e_2, \varepsilon) = \operatorname{annot}(e_1) \ \operatorname{annot}(e_2) \\ &5. \ \operatorname{annot}(e.\pi, \varepsilon) = \operatorname{annot}(e, \varepsilon).\pi \\ &6. \ \operatorname{annot}(\lambda X <: \tau_1.e, \varepsilon) = \lambda X <: \operatorname{annot}(\tau_1, \varepsilon).\operatorname{annot}(e, \varepsilon) \\ &7. \ \operatorname{annot}(e \ \tau, \varepsilon) = \operatorname{annot}(e, \varepsilon) \ \operatorname{annot}(\tau, \varepsilon) \end{split}
```

Definition (annot :: $\Gamma \times \varepsilon \to \hat{\Gamma}$)

```
1. \operatorname{annot}(\varnothing, \bot) = \varnothing
2. \operatorname{annot}((\Gamma, x : \tau), \varepsilon) = \operatorname{annot}(\Gamma, \varepsilon), x : \operatorname{annot}(\tau, \varepsilon)
3. \operatorname{annot}((\Gamma, X <: \tau), \varepsilon) = \operatorname{annot}(\Gamma, \varepsilon), X <: \operatorname{annot}(\tau, \varepsilon)
```

Definition (erase :: $\hat{\tau} \to \tau$)

```
1. \ \mathtt{erase}(X) = X
```

2.
$$erase(\{\bar{r}\}) = \{\bar{r}\}$$

3.
$$\operatorname{erase}(\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = \operatorname{erase}(\hat{\tau}_1) \to \operatorname{erase}(\hat{\tau}_2)$$

4. $\operatorname{erase}(\forall X <: \hat{\tau}_1.\hat{\tau}_2) = \forall X <: \operatorname{erase}(\hat{\tau}_1).\operatorname{erase}(\hat{\tau}_2)$

Definition (erase :: $\hat{e} \rightarrow e$)

- 1. erase(x) = x
- 2. erase(r) = r
- 3. $erase(\lambda x : \hat{\tau}.\hat{e}) = \lambda x : erase(\hat{\tau}).erase(\hat{e})$
- 4. $\operatorname{erase}(\hat{e}_1 \ \hat{e}_2) = \operatorname{erase}(\hat{e}_1)\operatorname{erase}(\hat{e}_2)$
- 5. $\operatorname{erase}(\hat{e}.\pi) = \operatorname{erase}(\hat{e}).\pi$
- 6. $\operatorname{erase}(\lambda X <: \hat{\tau}.\hat{e}) = \lambda X <: \operatorname{erase}(\hat{\tau}).\operatorname{erase}(\hat{e})$

Definition (erase :: $\hat{\Gamma} \rightarrow \Gamma$)

```
1. erase(\emptyset) = \emptyset
```

2.
$$\operatorname{erase}(\hat{\Gamma}, x : \hat{\tau}) = \operatorname{erase}(\hat{\Gamma}), x : \operatorname{erase}(\hat{\tau})$$

3. $\operatorname{erase}(\hat{\Gamma}, X <: \hat{\tau}) = \operatorname{erase}(\hat{\Gamma}), X <: \operatorname{erase}(\hat{\tau})$

Definition (effects :: $\hat{\tau} \rightarrow \varepsilon$)

```
1. effects(X) = \emptyset
```

2. effects(
$$\{\bar{r}\}$$
) = $\{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$

3.
$$\operatorname{effects}(\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = \operatorname{ho-effects}(\hat{\tau}_1) \cup \varepsilon \cup \operatorname{effects}(\hat{\tau}_2)$$

- 4. effects $(\forall \hat{\tau}_1.\hat{\tau}_2)$ = ho-effects $(\hat{\tau}_1)$ \cup effects $(\hat{\tau}_2)$
- 5. effects($\forall \phi \subseteq \varepsilon.\hat{\tau}$) = effects($\hat{\tau}$)

Definition (ho-effects :: $\hat{\tau} \to \varepsilon$)

```
1. ho-effects(t) = \emptyset
```

2. ho-effects
$$(\{\bar{r}\}) = \emptyset$$

- 3. ho-effects $(\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = \texttt{effects}(\hat{\tau}_1) \cup \texttt{ho-effects}(\hat{\tau}_2)$
- 4. ho-effects($\forall \hat{\tau}_1.\hat{\tau}_2$) = effects($\hat{\tau}_1$) \cup ho-effects($\hat{\tau}_2$)
- 5. ho-effects($\forall \phi \subseteq \varepsilon.\hat{\tau}$) = $\varepsilon \cup$ ho-effects($\hat{\tau}$)

Definition (substitution :: $\hat{e} \times \hat{v} \times \hat{v} \rightarrow \hat{e}$)

The notation $[\hat{v}/x]\hat{e}$ is short-hand for substitution (\hat{e},\hat{v},x) . This function is partial, because the third input must be a variable. We adopt the usual renaming conventions to avoid accidental capture.

```
1. [\hat{v}/y]x = \hat{v}, if x = y
```

2.
$$[\hat{v}/y]x = x$$
, if $x \neq y$

- 3. $[\hat{v}/y](\lambda x : \hat{\tau}.\hat{e}) = \lambda x : \hat{\tau}.[\hat{v}/y]\hat{e}$, if $y \neq x$ and y does not occur free in \hat{e}
- 4. $[\hat{v}/y](\hat{e}_1 \ \hat{e}_2) = ([\hat{v}/y]\hat{e}_1)([\hat{v}/y]\hat{e}_2)$
- 5. $[\hat{v}/y](\hat{e}.\pi) = ([\hat{v}/y]\hat{e}).\pi$
- 6. $[\hat{v}/y](\lambda X.\hat{e}) = \lambda X.[\hat{v}/y]\hat{e}$
- 7. $[\hat{v}/y](\lambda\phi.\hat{e}) = \lambda\phi.[\hat{v}/y]\hat{e}$
- 8. $[\hat{v}/y](\hat{e} \ \hat{\tau}) = [\hat{v}/y]\hat{e} \ \hat{\tau}$
- 9. $[\hat{v}/y](\hat{e} \ \varepsilon) = [\hat{v}/y]\hat{e} \ \varepsilon$
- 10. $[\hat{v}/y](\mathtt{import}(\varepsilon_s) \ x = \hat{e} \ \mathtt{in} \ e) = \mathtt{import}(\varepsilon_s) \ x = [\hat{v}/y]\hat{e} \ \mathtt{in} \ e$

When performing multiple substitutions the notation $[\hat{v}_1/x_1, \hat{v}_2/x_2]\hat{e}$ is used as shorthand for $[\hat{v}_2/x_2]([\hat{v}_1/x_1]\hat{e})$ (note the order of the variables has been flipped; the substitutions occur as they are written, left-to-right).

Definition (substitution :: $\hat{\tau} \times \hat{\tau} \times \hat{\tau} \to \hat{\tau}$)

- 1. $[\hat{\tau}/Y]X = \hat{\tau}$, if X = Y
- 2. $[\hat{\tau}/Y]X = X$, if $X \neq Y$
- 3. $[\hat{\tau}/Y]\{\bar{r}\} = \{\bar{r}\}$
- 4. $[\hat{\tau}/Y](\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = [\hat{\tau}/Y]\hat{\tau}_1 \to_{\varepsilon} [\hat{\tau}/Y]\hat{\tau}_2$ 5. $[\hat{\tau}/Y](\forall X.\hat{\tau}_1) = \forall X.[\hat{\tau}/Y]\tau_1$, if $Y \neq X$ and Y does not occur free in τ_1
- 6. $\left[\hat{\tau}/Y\right](\forall \phi.\hat{\tau}_1) = \forall \phi.\left[\hat{\tau}/Y\right]\tau_1$

Definition (substitution :: $\varepsilon \times \varepsilon \times \varepsilon \to \hat{\tau}$)

- 1. $[\varepsilon/\phi]\Phi = \varepsilon$, if $\phi = \Phi$
- 2. $[\varepsilon/\phi]\Phi = \Phi$, if $\phi \neq \Phi$
- 3. $[\varepsilon/\phi]\{\overline{r.\pi}\}=\{\overline{r.\pi}\}$

Definition (substitution :: $\hat{\tau} \times \varepsilon \times \varepsilon \rightarrow \hat{\tau}$)

- 1. $[\varepsilon/\phi]X = X$
- 2. $[\varepsilon/\phi]\{\bar{r}\}=\{\bar{r}\}$
- 3. $[\varepsilon/\phi](\hat{\tau}_1 \to_{\varepsilon}' \hat{\tau}_2) = [\varepsilon/\phi]\hat{\tau}_1 \to_{[\varepsilon/\phi]\varepsilon'} [\varepsilon/\phi]\hat{\tau}_2$ 4. $[\varepsilon/\phi](\forall X.\hat{\tau}) = \forall X.[\varepsilon/\phi]\hat{\tau}$
- 5. $[\varepsilon/\phi](\forall \Phi.\hat{\tau}) = \forall \Phi.[\varepsilon/\phi]$, if $\phi \neq \Phi$ and ϕ does not occur free in $\hat{\tau}$

Static Rules

$$\Gamma \vdash e : \tau$$

$$\begin{split} \frac{\Gamma, x : \tau \vdash x : \tau}{\Gamma, x : \tau \vdash x : \tau} & \text{(T-VAR)} \quad \frac{\Gamma, r : \{r\} \vdash r : \{r\}}{\Gamma, r : \{r\} \vdash r : \{r\}} & \text{(T-RESOURCE)} \quad \frac{\Gamma \vdash e : \{\bar{r}\}}{\Gamma \vdash e . \pi : \text{Unit}} & \text{(T-OPERCALL)} \\ & \frac{\Gamma, x : \tau_1 \vdash e : \tau_2}{\Gamma \vdash \lambda x : \tau_1 . e : \tau_1 \to \tau_2} & \text{(T-ABS)} \quad \frac{\Gamma \vdash e_1 : \tau_2 \to \tau_3}{\Gamma \vdash e_1 : e_2 : \tau_3} & \text{(T-APP)} \\ & \frac{\Gamma, X <: \tau_1 \vdash e : \tau_2}{\Gamma \vdash \lambda X <: \tau_1 . e : \tau_2} & \text{(T-POLYTYPEABS)} \quad \frac{\Gamma \vdash e : \forall X <: \tau_1 . \tau_2 \quad \tau' <: \tau_1}{\Gamma \vdash e \; \tau' : [\tau'/X] \tau_2} & \text{(T-POLYTYPEAPP)} \end{split}$$

$$\hat{\varGamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon$$

$$\frac{\hat{\varGamma},x:\tau\vdash x:\tau \text{ with }\varnothing}{\hat{\varGamma},x:\tau\vdash\hat{r}:\{r\}\vdash r:\{r\} \text{ with }\varnothing} \ (\varepsilon\text{-Resource})$$

$$\frac{\hat{\varGamma}\vdash\hat{e}:\{\bar{r}\}}{\hat{\varGamma}\vdash\hat{e}.\pi:\text{Unit with }\{r.\pi\mid r\in\bar{r}\}} \ (\varepsilon\text{-OperCall}) \ \ \frac{\hat{\varGamma}\vdash e:\tau \text{ with }\varepsilon\quad \tau<:\tau'\quad \varepsilon\subseteq\varepsilon'}{\hat{\varGamma}\vdash e:\tau' \text{ with }\varepsilon'} \ (\varepsilon\text{-Subsume})$$

$$\frac{\hat{\varGamma}, x: \hat{\tau}_2 \vdash \hat{e}: \hat{\tau}_3 \text{ with } \varepsilon_3}{\hat{\varGamma} \vdash \lambda x: \tau_2. \hat{e}: \hat{\tau}_2 \rightarrow_{\varepsilon_3} \hat{\tau}_3 \text{ with } \varnothing} \ (\varepsilon\text{-Abs}) \quad \frac{\hat{\varGamma} \vdash \hat{e}_1: \hat{\tau}_2 \rightarrow_{\varepsilon} \hat{\tau}_3 \text{ with } \varepsilon_1 \quad \hat{\varGamma} \vdash \hat{e}_2: \hat{\tau}_2 \text{ with } \varepsilon_2}{\hat{\varGamma} \vdash \hat{e}_1 \hat{e}_2: \hat{\tau}_3 \text{ with } \varepsilon_1 \cup \varepsilon_2 \cup \varepsilon} \ (\varepsilon\text{-App})$$

$$\frac{\hat{\Gamma}, X <: \hat{\tau}_1 \vdash \hat{e} : \hat{\tau}_2 \text{ with } \varepsilon}{\hat{\Gamma} \vdash \lambda X <: \hat{\tau}_1.\hat{e} : \hat{\tau}_2 \text{ with } \varnothing} \ \left(\varepsilon\text{-PolyTypeAbs}\right) \quad \frac{\hat{\Gamma} \vdash \hat{e} : \forall X <: \hat{\tau}_1.\hat{\tau}_2 \text{ with } \varepsilon_1 \quad \hat{\tau}' <: \hat{\tau}_1}{\hat{\Gamma} \vdash \hat{e} : \hat{\tau}' : [\hat{\tau}'/X]\hat{\tau}_2 \text{ with } \varepsilon_1 \cup \text{effects}(\hat{\tau}')} \ \left(\varepsilon\text{-PolyTypeApp}\right)$$

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varnothing}{\hat{\Gamma} \vdash \lambda \phi \subseteq \varepsilon. \hat{e} : \forall \phi \subseteq \varepsilon. \hat{\tau} \text{ with } \varnothing} \ (\varepsilon\text{-PolyFxAbs}) \quad \frac{\hat{\Gamma} \vdash \hat{e} : \forall \phi \subseteq \varepsilon. \hat{\tau} \text{ with } \varepsilon_1}{\hat{\Gamma} \vdash \hat{e} \in \varepsilon: [\varepsilon'/\phi] \hat{\tau} \text{ with } \varepsilon_1 \cup \varepsilon} \ (\varepsilon\text{-PolyFxApp})$$

$$\mathtt{effects}(\hat{\tau}) \cup \mathtt{ho\text{-effects}}(\mathtt{annot}(\tau,\varnothing)) \subseteq \varepsilon$$

$$\frac{\hat{\varGamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \qquad \text{ho-safe}(\hat{\tau}, \varepsilon) \qquad x : \texttt{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\varGamma} \vdash \texttt{import}(\varepsilon) \ x = \hat{e} \ \text{in } e : \texttt{annot}(\tau, \varepsilon) \ \text{with } \varepsilon \cup \varepsilon_1} \ \left(\varepsilon\text{-IMPORT}\right)$$

$$\mathtt{safe}(au,arepsilon)$$

$$\frac{}{\mathsf{safe}(\{\bar{r}\},\varepsilon)} \text{ (SAFE-RESOURCE)} \qquad \frac{}{\mathsf{safe}(\mathsf{Unit},\varepsilon)} \text{ (SAFE-UNIT)}$$

$$\frac{\varepsilon \subseteq \varepsilon' \quad \mathsf{ho\text{-}safe}(\hat{\tau}_1,\varepsilon) \quad \mathsf{safe}(\hat{\tau}_2,\varepsilon)}{\mathsf{safe}(\hat{\tau}_1 \to_{\varepsilon'} \hat{\tau}_2,\varepsilon)} \text{ (SAFE-ARROW)}$$

$$\mathtt{ho\text{-}safe}(\widehat{\tau},\varepsilon)$$

$$\frac{}{\mathsf{ho\text{-}safe}(\{\bar{r}\},\varepsilon)} \ (\mathsf{HOSAFE\text{-}RESOURCE}) \qquad \frac{}{\mathsf{ho\text{-}safe}(\mathsf{Unit},\varepsilon)} \ (\mathsf{HOSAFE\text{-}UNIT}) \\ \\ \frac{\mathsf{safe}(\hat{\tau}_1,\varepsilon) \quad \mathsf{ho\text{-}safe}(\hat{\tau}_2,\varepsilon)}{\mathsf{ho\text{-}safe}(\hat{\tau}_1 \to_{\varepsilon'} \hat{\tau}_2,\varepsilon)} \ (\mathsf{HOSAFE\text{-}ARROW}) \\ \\$$

 $\hat{\tau} <: \hat{\tau}$

$$\frac{\varepsilon \subseteq \varepsilon' \quad \hat{\tau}_2 <: \hat{\tau}_2' \quad \hat{\tau}_1' <: \hat{\tau}_1}{\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2 <: \hat{\tau}_1' \to_{\varepsilon'} \hat{\tau}_2'} \text{ (S-EFFECTS)} \quad \frac{r \in \bar{r}_2 \implies r \in \bar{r}_1}{\{\bar{r}_2\} <: \{\bar{r}_1\}} \text{ (S-RESOURCESET)}$$

4 Dynamic Rules

$$\hat{e} \longrightarrow \hat{e} \mid \varepsilon$$

$$\frac{\hat{e}_1 \longrightarrow \hat{e}_1' \mid \varepsilon}{\hat{e}_1 \hat{e}_2 \longrightarrow \hat{e}_1' \hat{e}_2 \mid \varepsilon} \text{ (E-APP1)} \qquad \frac{\hat{e}_2 \longrightarrow \hat{e}_2' \mid \varepsilon}{\hat{v}_1 \hat{e}_2 \longrightarrow \hat{v}_1 \hat{e}_2' \mid \varepsilon} \text{ (E-APP2)} \qquad \frac{(\lambda x : \hat{\tau}. \hat{e}) \hat{v}_2 \longrightarrow [\hat{v}_2/x] \hat{e} \mid \varnothing}{(\lambda x : \hat{\tau}. \hat{e}) \hat{v}_2 \longrightarrow [\hat{v}_2/x] \hat{e} \mid \varnothing} \text{ (E-APP3)}$$

$$\frac{\hat{e} \to \hat{e}' \mid \varepsilon}{\hat{e}.\pi \longrightarrow \hat{e}'.\pi \mid \varepsilon} \text{ (E-OPERCALL1)} \qquad \frac{r \in R \quad \pi \in \Pi}{r.\pi \longrightarrow \text{unit} \mid \{r.\pi\}} \text{ (E-OPERCALL2)}$$

$$\frac{\hat{e} \longrightarrow \hat{e}' \mid \varepsilon}{\hat{e}.\hat{\tau} \longrightarrow \hat{e}'.\hat{\tau} \mid \varepsilon} \text{ (E-POLYTYPEAPP1)} \qquad \frac{(\lambda X. \hat{e}) \hat{\tau} \longrightarrow [\hat{\tau}/X] \hat{e} \mid \varnothing}{(\lambda X. \hat{e}) \hat{\tau} \longrightarrow \hat{e}'.\hat{\tau} \mid \varepsilon} \text{ (E-POLYTYPEAPP2)}$$

$$\frac{\hat{e} \longrightarrow \hat{e}' \mid \varepsilon}{\hat{e}.\hat{\tau} \longrightarrow \hat{e}'.\hat{\tau} \mid \varepsilon} \text{ (E-POLYFXAPP1)} \qquad \frac{(\lambda \phi. \hat{e}) \varepsilon \longrightarrow [\varepsilon/\phi] \hat{e} \mid \varnothing}{(\lambda \phi. \hat{e}) \varepsilon \longrightarrow [\varepsilon/\phi] \hat{e} \mid \varnothing} \text{ (E-IMPORT1)}$$

$$\frac{\hat{e} \longrightarrow \hat{e}'.\hat{\tau} \mid \varepsilon}{\text{import}(\varepsilon_s) \ x = \hat{e}. \text{in} \ e \longrightarrow \text{import}(\varepsilon_s) \ x = \hat{e}'. \text{in} \ e \mid \varepsilon'} \text{ (E-IMPORT2)}$$

5 Encodings

5.1 ⊥

The bottom type is defined as $\perp \stackrel{\mathsf{def}}{=} \varnothing$, which is the literal for an empty set of resources.

$$\frac{}{\varGamma\vdash\bot:\varnothing}\ (\text{T-}\bot)\qquad \frac{}{\varGamma\vdash\bot:\varnothing\ \text{with}\ \varnothing}\ (\varepsilon\text{-}\bot)$$

5.2 unit, Unit

Define $\mathtt{unit} = \lambda \mathtt{x} : \varnothing.\mathtt{x}$, i.e. the function which takes an empty set of resources and returns it. We shall refer to its type, which is $\varnothing \to_\varnothing \varnothing$, as Unit. It has various properties befitting unit.

- 1. unit cannot be invoked as \emptyset is uninhabited.
- 2. unit is a value.
- 3. The only term with type Unit is unit.
- 4. \vdash unit : Unit by using ε -ABS and ε -VAR.
- 5. $effects(Unit) = ho-effects(Unit) = \emptyset$
- 6. $safe(Unit, \varepsilon)$ and $ho-safe(Unit, \varepsilon)$

$$\frac{}{\varGamma\vdash \mathtt{unit}:\mathtt{Unit}} \ (\mathrm{T\text{-}UNIT}) \qquad \frac{}{\varGamma\vdash \mathtt{unit}:\mathtt{Unit} \ \mathtt{with} \ \varnothing} \ (\varepsilon\text{-}\mathrm{UNIT})$$