### 1 Effects

Fix some set of resources R. A resource is some language primitive that has the authority to directly perform I/O operations. Elements of the set R are denoted by r.  $\Pi$  is a fixed set of operations on resources. Its members are denoted  $\pi$ . An effect is a member of the set of pairs  $R \times \Pi$ . A set of effects is denoted by  $\varepsilon$ . In this system we cannot dynamically create resources or resource-operations.

Throughout we refer to the notions of effects and captures. A piece of code C has the effect  $(r, \pi)$  if operation  $\pi$  is performed on resource r during execution of C. C captures the effect  $(r, \pi)$  if it has the authority to perform operation  $\pi$  on resource r at some point during its execution.

We use  $r.\pi$  as syntactic sugar for the effect  $(r,\pi)$ . For example, FileIO.append instead of (FileIO, append).

Types are either resources or structural. Structural types have a set of method declarations. An object of a particular structural type  $\{\bar{\sigma}\}$  can have any of the methods defined by  $\sigma$  invoked on it. The structural type  $\varnothing$  with no methods is called Unit.

We assume there are constructions of the familiar types using the basic structural type  $\varnothing$  and method declarations (for example,  $\mathbb{N}$  could be made using  $\varnothing$  and a successor function, Peano-style).

Note the distinction between methods (usually denoted m) and operations (usually denoted  $\pi$ ). An operation can only be invoked on a resource; resources can only have operations invoked on them. A method can only be invoked on an object; objects can only have methods invoked on them.

We make a simplifying assumption that every method/lambda takes exactly one argument. Invoking some operation  $\pi$  on a resource returns  $\varnothing$ .

# 2 Fully-Annotated Programs

In this first system every method in the program is explicitly annotated with its set of effects.

#### 2.1 Grammar

$$\begin{array}{ll} e ::= x & expressions \\ \mid & r \\ \mid & \text{new } x \Rightarrow \overline{\sigma = e} \\ \mid & e.m(e) \\ \mid & e.\pi(e) \\ \end{array}$$
 
$$\tau ::= \{\bar{\sigma}\} \mid \{\bar{r}\} & types \\ \sigma ::= d \text{ with } \varepsilon & labeled \ decls. \\ d ::= \det m(x:\tau) : \tau \ unlabeled \ decls. \\ \Gamma ::= \varnothing \\ \mid & \Gamma, \ x : \tau \\ \end{array}$$

## Notes:

- Declarations ( $\sigma$ -terms) are annotated by what effects they have.
- d-terms do not appear in programs, except as part of  $\sigma$ -terms.
- All methods (and lambda expressions) take exactly one argument. If a method specifies no argument, then
  the argument is implicitly of type. Unit.
- Although  $e_1.\pi(e_2)$  is a syntactically valid expression, it is only well-formed if  $e_1$  is a resource (so  $e_1$  is only a resource in well-typed programs).

## 2.2 Syntactic Sugar

Programs may also contain let, val, and  $\lambda$  expressions. These can be encoded using the current grammar using transformation rules. We use  $\leadsto$  for this purpose: if the relation  $\Gamma \mid a \leadsto b$  holds if and only if in any piece of code S[a] with context  $\Gamma$ , the dynamic semantics of S[b/a] are exactly the same as S[a].

$$\frac{\varGamma \vdash e_1 : \tau_1 \quad \varGamma, x : \tau_1 \vdash e_2 : \tau_2}{\text{let } x = e_1 \text{ in } e_2 \leadsto (\text{new def } m(x : \tau_1) : \tau_2)).m(e_1)} \text{ (Trans-Let)}$$
 
$$\frac{\varGamma \vdash e_1 : \tau_1}{\text{val } x : \tau_1 = e_1 \leadsto \text{let } \alpha x = (\text{new def } get() : \tau_1 = e_1) \text{ in } (\alpha x.get())} \text{ (Trans-ValDef)}$$
 
$$\frac{x : \tau \in \varGamma}{x \leadsto \alpha x.get()} \text{ (Trans-Val)}$$

#### Notes:

- We use the symbol  $\alpha$  to prefix anonymous objects. These are objects constructed by the application of transformation rule. The variable x is turned into  $\alpha x$ , an object with a single get method that returns the expression defining x.

### 2.3 Rules

$$\Gamma \vdash e : au$$
 with  $arepsilon$ 

$$\overline{\Gamma,\ x:\tau\vdash x:\tau\ \text{with}\ \varnothing}\ \left(\varepsilon\text{-Var}\right) \qquad \overline{\Gamma,\ r:\{r\}\vdash r:\{r\}\ \text{with}\ \varnothing}\ \left(\varepsilon\text{-Resource}\right)$$
 
$$\frac{\Gamma,\ x:\{\bar{\sigma}\}\vdash \overline{\sigma}=e\ \text{OK}}{\Gamma\vdash \text{new}\ x\Rightarrow \overline{\sigma}=\overline{e}:\{\bar{\sigma}\}\ \text{with}\ \varnothing}\ \left(\varepsilon\text{-NewObJ}\right)$$
 
$$\frac{\Gamma\vdash e_1:\{\bar{r}\}\ \text{with}\ \varepsilon_1\quad \Gamma\vdash e_2:\tau_2\ \text{with}\ \varepsilon_2\quad \pi\in \varPi}{\Gamma\vdash e_1.\pi(e_2):\varnothing\ \text{with}\ \{\bar{r},m\}\cup\varepsilon_1\cup\varepsilon_2}\ \left(\varepsilon\text{-OperCall}\right) }$$
 
$$\frac{\Gamma\vdash e_1:\{\bar{\sigma}\}\ \text{with}\ \varepsilon_1\quad \Gamma\vdash e_2:\tau_2\ \text{with}\ \varepsilon_2\quad \sigma_i=\text{def}\ m_i(y:\tau_2):\tau\ \text{with}\ \varepsilon}{\Gamma\vdash e_1.m_i(e_2):\tau\ \text{with}\ \varepsilon_1\cup\varepsilon_2\cup\varepsilon}\ \left(\varepsilon\text{-MethCallObJ}\right) }$$
 
$$\frac{\Gamma\vdash \sigma=e\ \text{OK}}{\Gamma\vdash \sigma=e\ \text{OK}}$$
 
$$\frac{\Gamma,\ x:\tau\vdash e:\tau'\ \text{with}\ \varepsilon\quad \sigma=\text{def}\ m(x:\tau):\tau'\ \text{with}\ \varepsilon}{\Gamma\vdash \sigma=e\ \text{OK}}\ \left(\varepsilon\text{-ValidImpl}_{\sigma}\right) }$$

### Notes:

- Every expression in the program must be explicitly annotated; either as  $\sigma$ -terms or by what they capture.
- The rules ε-VAR, ε-RESOURCE, and ε-NEWOBJ have in their consequents an expression typed with no effect: merely having an object or resource is not an effect; you must do something with it, like a call a method on it, in order for it to be an effect.
- $-\varepsilon$ -ValidIMPL says that the return type and effects of the body of a method must agree with what its signature says.
- In  $\varepsilon$ -METHCALLRESOURCE, we may only call a method m on a resource r if m is a predefined operation in the set M. Invoking m returns the resource r you called it upon (which has potentially different state afterwards).

# 3 Partially-Annotated Programs

In this second system methods may either be fully labeled with their effects or have no labels. When they have no labels a conservative effect inference is performed using rules which provide an upper-bound (not necessarily tight) on the effects of the code when executed.

### 3.1 Grammar

$$\begin{array}{lll} e ::= x & expressions \\ \mid & r \\ \mid & \operatorname{new}_{\sigma} x \Rightarrow \overline{\sigma = e} \\ \mid & \operatorname{new}_{d} x \Rightarrow \overline{d = e} \\ \mid & e.m(e) \\ \mid & e.\pi(e) \\ \end{array}$$
 
$$\begin{array}{ll} \tau ::= \{ \overline{\sigma} \} & types \\ \mid & \{ \overline{t} \} \\ \mid & \{ \overline{d} \} \\ \mid & \{ \overline{d} \text{ captures } \varepsilon \} \\ \end{array}$$
 
$$\sigma ::= d \text{ with } \varepsilon \qquad labeled decls.$$
 
$$d ::= \operatorname{def} m(x : \tau) : \tau \text{ unlabeled decls.}$$

## Notes:

- $-\sigma$  denotes a declaration with effect labels. d denotes a declaration without effect labels.
- There are two new expressions:  $\mathbf{new}_{\sigma}$  for objects whose declarations are annotated;  $\mathbf{new}_{d}$  for objects whose declarations aren't.
- $\{\bar{d} \text{ captures } \varepsilon\}$  is a special kind of type that doesn't appear in the source program, but may be assigned as a consequence of the capture rules.

## 3.2 Rules

In addition to the rules from the previous system, the partially-annotated system has the following rules.

$$\frac{\varGamma\vdash d=e\ \mathtt{OK}}{\Gamma\vdash d=e\ \mathtt{OK}}$$
 
$$\frac{d=\det\ m(x:\tau_1):\tau_2\quad \varGamma\vdash e:\tau_2}{\varGamma\vdash d=e\ \mathtt{OK}}\ \left(\varepsilon\text{-ValidImpl}_d\right)$$

$$\varGamma \vdash e : \tau \text{ with } \varepsilon$$

$$\frac{\varepsilon = effects(\varGamma') \quad \varGamma' \subseteq \varGamma \quad \varGamma', x : \{\bar{d} \text{ captures } \varepsilon\} \vdash \overline{d = e} \text{ OK}}{\varGamma \vdash \text{ new}_d \ x \Rightarrow \overline{d = e} : \{\bar{d} \text{ captures } \varepsilon\} \text{ with } \varnothing} \ (\text{C-NewObJ})$$

$$\frac{\varGamma \vdash e_1 : \{\bar{d} \text{ captures } \varepsilon\} \text{ with } \varepsilon_1 \quad \varGamma \vdash e_2 : \tau_2 \text{ with } \varepsilon_2 \quad d_i := \text{ def } m_i(y : \tau_2) : \tau}{\varGamma \vdash e_1.m_i(e_2) : \tau \text{ with } \varepsilon_1 \cup \varepsilon_2 \cup effects(\tau_2) \cup \varepsilon} \text{ (C-METHCALL)}$$

## Notes:

- The  $\varepsilon$  judgements are to be applied to annotated parts of the program; the C rules for unannotated parts.
- The rules  $\varepsilon$ -VAR,  $\varepsilon$ -RESOURCE, and  $\varepsilon$ -NEWOBJ have in their antecedents an expression typed with no effect. Merely having an object or resource is not an effect; you must do something with it, like a call a method on it, in order for your program to have effects.
- The T judgements before standard typechecking, but they operate on annotated terms. They are needed to apply the  $\varepsilon$ -VALIDIMPL<sub>d</sub>) rule.
- In applying C-NewObj the variable  $\Gamma$  is the current context. The variable  $\Gamma'$  is some sub-context. A good choice of sub-context is  $\Gamma$  restricted to the free variables in the method-body being typechecked. This means we only consider the effects used in the method-body and gives a better approximation of its effects.
- When an unannotated d-declaration is encountered it is first assigned a  $\gamma$ -type by C-NEWOBJ. This annotates it as capturing a certain set of effects. C-METHCALL can then conclude its effects to be what it captures.

## 3.3 Effects Function

The effects function returns the set of effects in a particular typing context.

A method m can return a resource r (directly or via some enclosing object). Returning a resource isn't an effect but it means any unannotated program using m also captures r. To account for this, when the effects function is operating on a type  $\tau$  it must analyse the return type of the method declarations in  $\tau$ .

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\begin{array}{l} -\text{ effects}(\varnothing)=\varnothing\\ -\text{ effects}(\{\bar{r}\})=\{(r,m)\mid r\in\bar{r}, m\in M\}\\ -\text{ effects}(\{\bar{\sigma}\})=\bigcup_{\sigma\in\bar{\sigma}}\text{ effects}(\sigma)\\ -\text{ effects}(\{\bar{d}\})=\bigcup_{d\in\bar{d}}\text{ effects}(d)\\ -\text{ effects}(d\text{ with }\varepsilon)=\varepsilon\cup\text{ effects}(d)\\ -\text{ effects}(\text{def m}(x:\tau_1)\;\tau_2)=\text{effects}(\tau_2) \end{array}
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