1 Grammar

```
types
                                                              exprs.
e ::=
                                                                                                                                 type variable
                                                            variable
                                                                                        \{ar{r}\}
                                                                                                                                     effect set
       v
                                                               value
                                                                                                                                           arrow
       e.\pi
                                                   operation call
                                                                                                                               universal type
                                                       application
                                                type application
                                                                                   \hat{	au} ::=
                                                                                                                          annotated types
                                                                                      \mid X
                                                                                                                                 type variable
v ::=
                                                              values
                                                                                                                                  resource set
                                                                                          \hat{\tau} \to_{\varepsilon} \hat{\tau}
                                                 resource literal
       r
                                                                                                                            annotated arrow
       \lambda x : \tau . e
                                                       abstraction
                                                                                                                               universal type
       \lambda X <: \tau.e
                                           type\ polymorphism
                                                                                           \forall \phi \subseteq \varepsilon. \hat{\tau} \text{ caps } \varepsilon \quad universal \ effect \ set
\hat{e} ::=
                                            annotated exprs.
                                                                                                                                          effects
                                                                                   \varepsilon ::=
       \boldsymbol{x}
                                                            variable
                                                                                                                              effect variable
       \hat{v}
                                                               value
                                                                                                                                      effect set
      \hat{e}.\pi
                                                   operation call
                                                       application
                                                                                                                                       contexts
                                                type application
                                                                                                                                     empty ctx.
                                             effect application
                                                                                      \Gamma, x : \tau
                                                                                                                                   var. binding
       import(\varepsilon_s) \ x = \hat{e} \ in \ e
                                                             import
                                                                                                                           type var. binding
                                            annotated values
                                                                                                                     annotated contexts
  | r
                                                 resource\ literal
                                                                                    \begin{array}{c|c} \ddots & & \\ & \emptyset & \\ & \hat{\varGamma}, x : \hat{\tau} \\ & \hat{\varGamma}, X <: \hat{\tau} \\ & \hat{\varGamma}, \phi \subseteq \varepsilon \end{array} 
                                                                                                                                     empty ctx.
       \lambda x : \hat{\tau}.\hat{e}
                                                       abstraction
                                                                                                                                  var. binding
       \lambda X <: \hat{\tau}.\hat{e}
                                           type polymorphism
                                                                                                                      type var. binding
                                       effect\ polymorphism
                                                                                                                       effect var. binding
```

2 Functions

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Definition (annot :: \tau \times \varepsilon \rightarrow \hat{\tau})
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 \begin{split} &1. \ \operatorname{annot}(X, \square) = X \\ &2. \ \operatorname{annot}(\{\bar{r}\}, \square) = \{\bar{r}\} \\ &3. \ \operatorname{annot}(\tau_1 \to \tau_2, \varepsilon) = \operatorname{annot}(\tau_1, \varepsilon) \to_{\varepsilon} \operatorname{annot}(\tau_2, \varepsilon) \\ &4. \ \operatorname{annot}(\forall X <: \tau_1.\tau_2, \varepsilon) = \forall X <: \operatorname{annot}(\tau_1, \varepsilon). \operatorname{annot}(\tau_2, \varepsilon) \text{ caps } \varepsilon \end{split}
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Definition (annot :: $e \times \varepsilon \rightarrow \hat{e}$)

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 \begin{split} &1. \ \operatorname{annot}(x, \square) = e \\ &2. \ \operatorname{annot}(r, \square) = r \\ &3. \ \operatorname{annot}(\lambda x : \tau.e, \varepsilon) = \lambda x : \operatorname{annot}(\tau, \varepsilon).\operatorname{annot}(e, \varepsilon) \\ &4. \ \operatorname{annot}(e_1 \ e_2, \varepsilon) = \operatorname{annot}(e_1) \ \operatorname{annot}(e_2) \\ &5. \ \operatorname{annot}(e.\pi, \varepsilon) = \operatorname{annot}(e, \varepsilon).\pi \\ &6. \ \operatorname{annot}(\lambda X <: \tau_1.e, \varepsilon) = \lambda X <: \operatorname{annot}(\tau_1, \varepsilon).\operatorname{annot}(e, \varepsilon) \\ &7. \ \operatorname{annot}(e \ \tau, \varepsilon) = \operatorname{annot}(e, \varepsilon) \ \operatorname{annot}(\tau, \varepsilon) \end{split}
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Definition (annot :: $\Gamma \times \varepsilon \to \hat{\Gamma}$)

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 \begin{array}{l} 1. \  \, \mathrm{annot}(\varnothing, \square) = \varnothing \\ 2. \  \, \mathrm{annot}((\varGamma, x : \tau), \varepsilon) = \mathrm{annot}(\varGamma, \varepsilon), x : \mathrm{annot}(\tau, \varepsilon) \\ 3. \  \, \mathrm{annot}((\varGamma, X <: \tau), \varepsilon) = \mathrm{annot}(\varGamma, \varepsilon), X <: \mathrm{annot}(\tau, \varepsilon) \end{array}
```

Definition (erase :: $\hat{\tau} \rightarrow \tau$)

- 1. erase(X) = X
- 2. $erase(\{\bar{r}\}) = \{\bar{r}\}$
- 3. $\operatorname{erase}(\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = \operatorname{erase}(\hat{\tau}_1) \to \operatorname{erase}(\hat{\tau}_2)$
- 4. $\operatorname{erase}(\forall X <: \hat{\tau}_1.\hat{\tau}_2 \operatorname{caps} \varepsilon) = \forall X <: \operatorname{erase}(\hat{\tau}_1).\operatorname{erase}(\hat{\tau}_2)$

Definition (erase :: $\hat{e} \rightarrow e$)

- 1. erase(x) = x
- 2. erase(r) = r
- 3. $\operatorname{erase}(\lambda x : \hat{\tau}.\hat{e}) = \lambda x : \operatorname{erase}(\hat{\tau}).\operatorname{erase}(\hat{e})$
- 4. $\operatorname{erase}(\hat{e}_1 \ \hat{e}_2) = \operatorname{erase}(\hat{e}_1)\operatorname{erase}(\hat{e}_2)$
- 5. $\operatorname{erase}(\hat{e}.\pi) = \operatorname{erase}(\hat{e}).\pi$
- 6. $\operatorname{erase}(\lambda X <: \hat{\tau}.\hat{e}) = \lambda X <: \operatorname{erase}(\hat{\tau}).\operatorname{erase}(\hat{e})$

Definition (erase :: $\hat{\Gamma} \rightarrow \Gamma$)

- 1. $erase(\emptyset) = \emptyset$
- 2. $\operatorname{erase}(\hat{\Gamma}, x : \hat{\tau}) = \operatorname{erase}(\hat{\Gamma}), x : \operatorname{erase}(\hat{\tau})$
- 3. $\operatorname{erase}(\hat{\Gamma}, X <: \hat{\tau}) = \operatorname{erase}(\hat{\Gamma}), X <: \operatorname{erase}(\hat{\tau})$

Definition (effects :: $\hat{\tau} \to \varepsilon$)

- 1. $effects(X) = \emptyset$
- 2. $effects(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$
- 3. $\operatorname{effects}(\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = \operatorname{ho-effects}(\hat{\tau}_1) \cup \varepsilon \cup \operatorname{effects}(\hat{\tau}_2)$
- $4. \ \mathtt{effects}(\forall X <: \hat{\tau}_1.\hat{\tau}_2 \ \mathtt{caps} \ \varepsilon_1) = \mathtt{ho\text{-effects}}(\hat{\tau}_1) \cup \mathtt{effects}(\hat{\tau}_2) \cup \varepsilon_1$
- 5. effects($\forall \phi \subseteq \varepsilon.\hat{\tau} \text{ caps } \varepsilon_1$) = effects($\hat{\tau}$) $\cup \varepsilon_1$

Definition (ho-effects :: $\hat{\tau} \to \varepsilon$)

- 1. $ho\text{-effects}(X) = \emptyset$
- 2. ho-effects($\{\bar{r}\}$) = \emptyset
- 3. ho-effects($\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2$) = effects($\hat{\tau}_1$) \cup ho-effects($\hat{\tau}_2$)
- $4.\ \operatorname{ho-effects}(\forall \hat{\tau}_1.\hat{\tau}_2\ \operatorname{caps}\ \varepsilon) = \operatorname{effects}(\hat{\tau}_1) \cup \operatorname{ho-effects}(\hat{\tau}_2)$
- 5. ho-effects($\forall \phi \subseteq \varepsilon.\hat{\tau} \text{ caps } \varepsilon_1$) = $\varepsilon \cup \text{ho-effects}(\hat{\tau})$

3 Static Rules

$$\Gamma \vdash e : \tau$$

$$\frac{\Gamma, x : \tau \vdash x : \tau}{\Gamma, x : \tau \vdash x : \tau} \text{ (T-VAR)} \quad \frac{\Gamma, r : \{r\} \vdash r : \{r\}}{\Gamma, r : \{r\} \vdash r : \{r\}} \text{ (T-RESOURCE)} \quad \frac{\Gamma \vdash e : \{\bar{r}\}}{\Gamma \vdash e.\pi : \text{Unit}} \text{ (T-OPERCALL)}$$

$$\frac{\Gamma, x : \tau_1 \vdash e : \tau_2}{\Gamma \vdash \lambda x : \tau_1.e : \tau_1 \to \tau_2} \text{ (T-ABS)} \quad \frac{\Gamma \vdash e_1 : \tau_2 \to \tau_3}{\Gamma \vdash e_1 : e_2 : \tau_3} \quad \text{(T-APP)}$$

$$\frac{\Gamma, X <: \tau_1 \vdash e : \tau_2}{\Gamma \vdash \lambda X <: \tau_1.e : \forall X <: \tau_1.\tau_2} \text{ (T-POLYTYPEABS)} \quad \frac{\Gamma \vdash e : \forall X <: \tau_1.\tau_2 \quad \tau' <: \tau_1}{\Gamma \vdash e : \tau' : [\tau'/X]\tau_2} \text{ (T-POLYTYPEAPP)}$$

$$\hat{ec{\Gamma}} dash \hat{e} : \hat{ au}$$
 with $arepsilon$

4 Dynamic Rules

$$\hat{e} \longrightarrow \hat{e} \mid \varepsilon$$

$$\begin{split} \frac{\hat{e}_1 \longrightarrow \hat{e}_1' \mid \varepsilon}{\hat{e}_1 \hat{e}_2 \longrightarrow \hat{e}_1' \hat{e}_2 \mid \varepsilon} & \text{(E-APP1)} \qquad \frac{\hat{e}_2 \longrightarrow \hat{e}_2' \mid \varepsilon}{\hat{v}_1 \hat{e}_2 \longrightarrow \hat{v}_1 \hat{e}_2' \mid \varepsilon} & \text{(E-APP2)} \qquad \frac{(\lambda x : \hat{\tau}. \hat{e}) \hat{v}_2 \longrightarrow [\hat{v}_2/x] \hat{e} \mid \varnothing} \\ \frac{\hat{e} \to \hat{e}' \mid \varepsilon}{\hat{e}.\pi \longrightarrow \hat{e}'.\pi \mid \varepsilon} & \text{(E-OPERCALL1)} \qquad \frac{r \in R \quad \pi \in \varPi}{r.\pi \longrightarrow \text{unit} \mid \{r.\pi\}} & \text{(E-OPERCALL2)} \\ \frac{\hat{e} \longrightarrow \hat{e}' \mid \varepsilon}{\hat{e} \mid \hat{\tau} \longrightarrow \hat{e}' \mid \hat{\tau} \mid \varepsilon} & \text{(E-POLYTYPEAPP1)} \qquad \frac{(\lambda X. \hat{e}) \hat{\tau} \longrightarrow [\hat{\tau}/X] \hat{e} \mid \varnothing} & \text{(E-POLYTYPEAPP2)} \\ \frac{\hat{e} \longrightarrow \hat{e}' \mid \varepsilon}{\hat{e} \mid \hat{\tau} \longrightarrow \hat{e}' \mid \hat{\tau} \mid \varepsilon} & \text{(E-POLYFXAPP1)} \qquad \frac{(\lambda \phi. \hat{e}) \varepsilon \longrightarrow [\varepsilon/\phi] \hat{e} \mid \varnothing} & \text{(E-POLYFXAPP2)} \\ \frac{\hat{e} \longrightarrow \hat{e}' \mid \varepsilon}{\hat{e} \mid \hat{\tau} \longrightarrow \hat{e}' \mid \hat{\tau} \mid \varepsilon} & \text{(E-POLYFXAPP1)} \qquad \frac{\hat{e} \longrightarrow \hat{e}' \mid \varepsilon'}{\text{import}(\varepsilon_s) \mid x = \hat{e} \mid \text{in} \mid e \longrightarrow \text{import}(\varepsilon_s) \mid x = \hat{e}' \mid \text{in} \mid e \mid \varepsilon'} & \text{(E-IMPORT1)} \end{split}$$