

# assignment8

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```
library(Benchmarking)
```

```
## Loading required package: lpSolveAPI
```

```
## Loading required package: ucminf
```

```
## Loading required package: quadprog
```

```
##  
## Loading Benchmarking version 0.30h, (Revision 244, 2022/05/05 16:31:31) ...
```

```
## Build 2022/05/05 16:31:40
```

```
library(lpSolveAPI)  
library(quadprog)  
library(ucminf)
```

#setting up matrix

```
inputs = matrix(c(150, 400, 320, 520, 350, 320, 0.2, 0.7, 1.2, 2.0, 1.2, 0.7), ncol = 2)  
#inputs  
outputs = matrix(c(14000, 14000, 42000, 28000, 19000, 14000, 3500, 21000, 10500, 42000,  
25000, 15000), ncol = 2)  
colnames(inputs) <- c("staff hours/day", "supplies/day")  
colnames(outputs) <- c("reimbursed", "privately paid")
```

#VRS

```
hv_vrs = dea(inputs, outputs, RTS = "vrs") #solve lp problem  
e_vrs = eff(hv_vrs)  
e_vrs
```

```
## [1] 1.0000000 1.0000000 1.0000000 1.0000000 1.0000000 0.8963283
```

```
peers(hv_vrs)
```

```
##      peer1 peer2 peer3
## [1,]      1    NA    NA
## [2,]      2    NA    NA
## [3,]      3    NA    NA
## [4,]      4    NA    NA
## [5,]      5    NA    NA
## [6,]      1     2     5
```

```
lambda(hv_vrs)
```

```
##           L1           L2 L3 L4           L5
## [1,] 1.0000000 0.0000000  0  0 0.0000000
## [2,] 0.0000000 1.0000000  0  0 0.0000000
## [3,] 0.0000000 0.0000000  1  0 0.0000000
## [4,] 0.0000000 0.0000000  0  1 0.0000000
## [5,] 0.0000000 0.0000000  0  0 1.0000000
## [6,] 0.4014399 0.3422606  0  0 0.2562995
```

```
#FDH
```

```
hv_fdh = dea(inputs, outputs, RTS = "fdh") #solve lp problem
e_fdh = eff(hv_fdh)
e_fdh
```

```
## [1] 1 1 1 1 1 1
```

```
peers(hv_fdh)
```

```
##      peer1
## [1,]      1
## [2,]      2
## [3,]      3
## [4,]      4
## [5,]      5
## [6,]      6
```

```
lambda(hv_fdh)
```

```
##      L1 L2 L3 L4 L5 L6
## [1,]  1  0  0  0  0  0
## [2,]  0  1  0  0  0  0
## [3,]  0  0  1  0  0  0
## [4,]  0  0  0  1  0  0
## [5,]  0  0  0  0  1  0
## [6,]  0  0  0  0  0  1
```

```
#CRS
```

```

hv_crs = dea(inputs, outputs, RTS = "crs") #solve lp problem
e_crs = eff(hv_crs)
e_crs

```

```
## [1] 1.0000000 1.0000000 1.0000000 1.0000000 0.9774987 0.8674521
```

```
peers(hv_crs)
```

```

##      peer1 peer2 peer3
## [1,]      1    NA    NA
## [2,]      2    NA    NA
## [3,]      3    NA    NA
## [4,]      4    NA    NA
## [5,]      1     2     4
## [6,]      1     2     4

```

```
lambda(hv_crs)
```

```

##           L1           L2 L3           L4
## [1,] 1.0000000 0.0000000  0 0.0000000
## [2,] 0.0000000 1.0000000  0 0.0000000
## [3,] 0.0000000 0.0000000  1 0.0000000
## [4,] 0.0000000 0.0000000  0 1.0000000
## [5,] 0.2000000 0.08048142  0 0.5383307
## [6,] 0.3428571 0.39499264  0 0.1310751

```

## #IRS

```

hv_irs = dea(inputs, outputs, RTS = "irs") #solve lp problem
e_irs = eff(hv_irs)
e_irs

```

```
## [1] 1.0000000 1.0000000 1.0000000 1.0000000 1.0000000 0.8963283
```

```
peers(hv_irs)
```

```

##      peer1 peer2 peer3
## [1,]      1    NA    NA
## [2,]      2    NA    NA
## [3,]      3    NA    NA
## [4,]      4    NA    NA
## [5,]      5    NA    NA
## [6,]      1     2     5

```

```
lambda(hv_irs)
```

```
##           L1           L2 L3 L4           L5
## [1,] 1.0000000 0.0000000 0 0 0.0000000
## [2,] 0.0000000 1.0000000 0 0 0.0000000
## [3,] 0.0000000 0.0000000 1 0 0.0000000
## [4,] 0.0000000 0.0000000 0 1 0.0000000
## [5,] 0.0000000 0.0000000 0 0 1.0000000
## [6,] 0.4014399 0.3422606 0 0 0.2562995
```

## #DRS

```
hv_drs = dea(inputs, outputs, RTS = "drs") #solve lp problem
e_drs = eff(hv_drs)
e_drs
```

```
## [1] 1.0000000 1.0000000 1.0000000 1.0000000 0.9774987 0.8674521
```

```
peers(hv_drs)
```

```
##      peer1 peer2 peer3
## [1,]     1    NA    NA
## [2,]     2    NA    NA
## [3,]     3    NA    NA
## [4,]     4    NA    NA
## [5,]     1     2     4
## [6,]     1     2     4
```

```
lambda(hv_drs)
```

```
##           L1           L2 L3           L4
## [1,] 1.0000000 0.00000000 0 0.0000000
## [2,] 0.0000000 1.00000000 0 0.0000000
## [3,] 0.0000000 0.00000000 1 0.0000000
## [4,] 0.0000000 0.00000000 0 1.0000000
## [5,] 0.2000000 0.08048142 0 0.5383307
## [6,] 0.3428571 0.39499264 0 0.1310751
```

## #FRH

```
hv_frh = dea(inputs, outputs, RTS = "add") #solve lp problem
e_frh = eff(hv_frh)
e_frh
```

```
## [1] 1 1 1 1 1 1
```

```
peers(hv_frh)
```

```
##      peer1
## [1,]      1
## [2,]      2
## [3,]      3
## [4,]      4
## [5,]      5
## [6,]      6
```

```
lambda(hv_frh)
```

```
##      L1 L2 L3 L4 L5 L6
## [1,]  1  0  0  0  0  0
## [2,]  0  1  0  0  0  0
## [3,]  0  0  1  0  0  0
## [4,]  0  0  0  1  0  0
## [5,]  0  0  0  0  1  0
## [6,]  0  0  0  0  0  1
```

```
table = cbind(inputs, outputs, e_vrs, e_fdh, e_crs, e_irs, e_drs, e_frh)
table
```

```
##      staff hours/day supplies/day reimbursed privately paid      e_vrs e_fdh
## [1,]              150           0.2       14000           3500 1.0000000      1
## [2,]              400           0.7       14000          21000 1.0000000      1
## [3,]              320           1.2       42000          10500 1.0000000      1
## [4,]              520           2.0       28000          42000 1.0000000      1
## [5,]              350           1.2       19000          25000 1.0000000      1
## [6,]              320           0.7       14000          15000 0.8963283      1
##      e_crs      e_irs      e_drs e_frh
## [1,] 1.0000000 1.0000000 1.0000000      1
## [2,] 1.0000000 1.0000000 1.0000000      1
## [3,] 1.0000000 1.0000000 1.0000000      1
## [4,] 1.0000000 1.0000000 1.0000000      1
## [5,] 0.9774987 1.0000000 0.9774987      1
## [6,] 0.8674521 0.8963283 0.8674521      1
```

**Under VRS, all facilities but 6 are efficient, which operates at 89.63% efficiency. DMU(6) is peers with 1,2,5 with weights of .40, .34, and .26.**

**Under FDH, all DMUs are efficient. There are no peers.**

**Under CRS, DMU(1-4) are efficient, and DMUs(5,6) is 97.8% and 86.74% efficient respectively. DMU(5,6) have peer units with DMU(1,2,4) with weights of .2, .08, and .54 (DMU(5)) and .34, .39, and .13 (DMU(6)).**

**Under IRS, all DMUs except DMU(6) are efficient, with DMU(6) having an efficiency of 89.63%. DMU(6) has peer units with DMU(1,2,5) with weights of .4, .34, .26.**

**Under DRS, DMU(1-4) are efficient, and DMUs(5,6) is 97.8% and 86.74% efficient respectively. DMU(5,6) have peer units with DMU(1,2,4) with weights of .2, .08, and .54 (DMU(5)) and .34, .39, and .13 (DMU(6)).**

**Under FRH, all DMUs are efficient. There are no peers.**

#FRH or FDH are the most suitable models for Hope Valley.