

DISCRETE MATHEMATICS IN COMPUTER SCIENCE

HSIEN-CHIH CHANG MARCH 7, 2022

ADMINISTRIVIA

- Final exam
 - Mar 13 (Sun) 8—11AM
 - LSC 100 (this room)
- SAS/Conflict/COVID
 - Come talk to me

- Homework 9 is optional

- Closed-book written exam
- Scope: Module C on counting
- One-page two-sided cheatsheet
 - Must be hand-written





HOW MANY DIFFERENT POKÉMON DO WE HAVE AFTER BUYING N CARDS, GIVEN THERE ARE N POKÉMON IN TOTAL?

GOTTA CATCH 'EM ALL



HOW CARDS WE EXPECTED TO BUY TO COLLECT ALL THE POKÉMON?

GOTTA CATCH 'EM ALL



HOW CARDS WE EXPECTED TO BUY TO COLLECT ALL THE DIFFERENT POKÉMON?

GOTTA CATCH 'EM ALL



```
\frac{\text{DRAwLots}(L):}{n \leftarrow |L|}
\text{for } i \leftarrow 1 \text{ to } n
\text{remove a random lot } x \text{ from } L
R[i] \leftarrow x
\text{return } R[1..n]
```

GENERATE RANDOM PERMUTATIONS



```
FISHERYATES(L[1..n]):
  for i \leftarrow 1 down to n
         Chosen[i] \leftarrow False
  for i \leftarrow n down to 1
         repeat
               r \leftarrow \text{Random}(n)
         until \neg Chosen[r]
         R[i] \leftarrow L[r]
         Chosen[r] \leftarrow True
   return R[1..n]
```

FISHER-YATES ALGORITHM

SELECTIONSHUFFLE(A[1..n]): for $i \leftarrow n$ down to 1 swap $A[i] \leftrightarrow A[RANDOM(i)]$

DURSTENFELD SHUFFLE

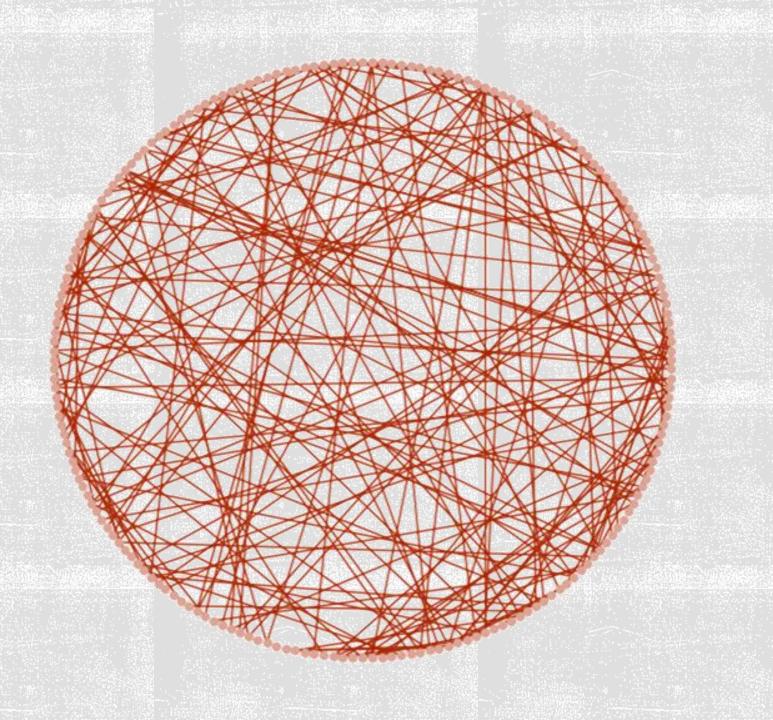


INSERTIONSHUFFLE(A[1..n]): for $i \leftarrow 1$ to nswap $A[i] \leftrightarrow A[RANDOM(i)]$

DURSTENFELD SHUFFLE



PROBABILISTIC METHODS



RANDOM GRAPH G(n,p)

HOW MANY VERTICES DO WE NEED IN ORDER TO GET A TRIANGLE OR AN ANTI-TRIANGLE?

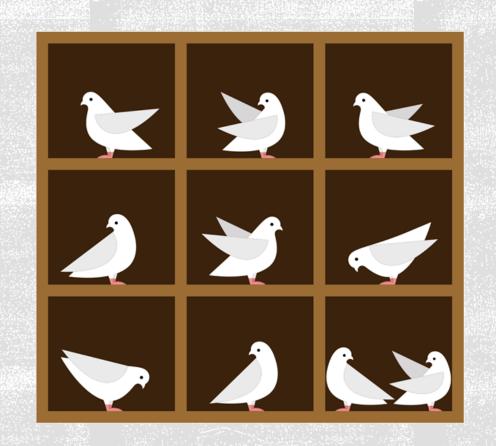
RANDOM GRAPH How many



OPTIMISM PRINCIPLE

-If Pr[good event] > 0,
then good event will happen.

-If Pr[bad things] < 1,
then good things will happen.</pre>





HOW MANY VERTICES DO WE NEED IN ORDER TO GET A COMPLETE K-SUBGRAPH OR AN ANTI-COMPLETE K-SUBGRAPH?

RANDOM GRAPH How many





