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Static Analysis of Dynamic Languages

Harm Delva

1 Introduction

The university of Ghent has developed the Dodona platform which students can use to submit solutions to and receive immediate feedback. This feedback is in large part done through unit testing. This lets the students know whether or not their solution is correct but doesn't really help them forward if it's not. To remedy this, there is a visual debugger included which students can use to step through their program. This comes with a couple of caveats unfortunately, for example it's unable to process file IO. More importantly, it can only let the user scroll through execution states. If an error occurred after a couple of thousand executed statements, this becomes a very tedious process.

That's just the nature of debugging. Fortunately, there are ways to avoid this pain altogether. Some programming languages have a strict compiler to catch obvious mistakes. There are linter tools such as JSLint and Pylint which emit warnings on error prone patterns. The Dodona platform uses these tools as well, and relays the warnings to the students.

The Pylint tool for Python has noticeably helped students avoid mistakes. Which in turn allowed them to focus more on the actual assignment and less on learning how to program. The goal of this thesis is to build on top of that, giving the students even more and even better feedback. An extensive data-flow analysis can untangle even the worst spaghetti code, which makes it a prime starting point for further analysis and feedback.

2 Literature

2.1 Static Analysis

NASA's source code of the Apollo 11 Guidance Computer was recently digitized and put on Github. All of it was written in an Assembly language and that worked just fine. The C programming language was made for the Unix operating system so it could run on various CPU architectures. In essence it's a pretty light abstraction over Assembly languages, it doesn't take much pressure off of the programmers. Unix did just fine as well. One could argue that programmers don't need tools to aid them – they seem to know what they're doing.

As the field of research grew, and with it the projects, it started becoming apparent that programmers can't always rely on themselves. Even veteran developers occasionaly discover a major vulnerability in their code – like the Heartbleed vulnerability in OpenSSL. Everyone makes mistakes but not all mistakes go unnoticed for years in critical code. A first line of defence against these costly mistakes is a proof of correctness. NASA's code was reliable because they had formal proofs that the most critical parts were correct [13] [4] [10]. Doing this is not only a massive amount of work, a proof can still be wrong. An implementation oversight can easily carry over into a proof oversight, so you'd need an extra pair of eyes to check all proofs as well.

A lot of functional programming languages are closely related to this method of provable correctness, while also automizing some of checks. Notable examples of such languages are

Haskell and ML. Both have a strong theoretical foundation and provide the programmer with a strong type system to make code easier to reason about. This stands in stark contrast with languages like C. While Haskell was made to facilitate writing correct code [20], C was made to be *close to the metal* and efficient [36]. The C compiler doesn't help the programmer nearly as much as the Haskell compiler. Correctness is obviously paramount to any computer program, so C's priorities don't always align with a programmer's.

That's where static analyzers come into play. They analyze a program, either in its source code form or its compiled form, and try to find as many possible mistakes as possible. These mistakes are often very and rare but encountering one can ruin someone's week. Code sample 2.1 comes from Google's Error Prone Github page and is a great example of how subtle serious bugs can be.

```
public class ShortSet {
  public static void main (String[] args) {
    Set<Short> s = new HashSet<>();
    for (short i = 0; i < 100; i++) {
        s.add(i);
        s.remove(i - 1);
    }
    System.out.println(s.size());
}</pre>
```

Code sample 2.1: Short Set

Although trivial, this code seems to be just fine at first glance. Sample 2.2 contains of the static analysis of the code.

```
error: [CollectionIncompatibleType] Argument 'i - 1' should not be
passed to this method; its type int is not compatible with its
collection's type argument Short
    s.remove(i - 1);
```

Code sample 2.2: Analysis of code sample 2.1

Subtracting an int from a short resulted in an int. In this case it probably won't cause an actual bug because both types use the same hashing function. The JVM originally didn't support generics, so their implementation is a bit rough. The remove method of a List instance doesn't do any type checks, its argument can be any Object instance. This can result in calls that never actually remove anything. If that call happens to only occur in a corner case in the 1000th iteration of a loop, this can lead to some very confusing bugs.

2.1.1 Powerful Languages

Every commonly used programming language is Turing complete, so in theory they should all be equal. This is a misconception that's been called the Turing tar-pit [31]. Everything is possible in a Turing tar-pit, but nothing of interest is easy. Programming languages where things of interest are perceived to be easy can be considered powerful. These languages are often the ones with lenient compilers or runtime environments such as C, Python, Javascript, ... In other words, languages were the language doesn't get in the way of the programmer too often.

As illustrated in the previous section this may not always be a good idea as humans tend to glance over subtle details. This makes the need for additional tools very important

for any project that aims to achieve high reliability. The alternative is long and painful debugging sessions. At some point these languages no longer make it easy to do things of interest in.

\mathbf{C}

The C programming language has been one of the most popular programming languages for a couple of decades now. Depending on who you ask, the best thing about C is either its efficiency or its simplicity. Both come at a cost. Its simplicity is what gives developers the power they desire. This comes at a cost however, as the old addendum says "with great power comes great responsibility".

Let's focus on the other main attraction of C, the efficiency. This comes at a cost as well and it's a one many people forget about. C's $raison\ d'\hat{e}tre$ isn't making developers feel good about themselves, it's generating efficient code. It was created to be a thin abstraction over various assembly languages that were limiting software development at the time [36].

Undefined Behavior

There are a lot of things the language specification doesn't specify a behavior for, which leads to undefined behavior. Some are well-known, such as using freed memory. Others catch people by surprise, dividing by zero in C for example is undefined behavior. The GNU libc website still claims that 1/0 yields inf [32], even though the C99 clearly contradicts them [11]. Entire papers have been written on the subject of undefined behavior [38] [24] [27]. One striking thing is how recent a lot of these papers are. Even though the language is over 40 years old, this is still an active field of research. Compilers are getting more advanced and with it the optimizations they perform.

Wang et al. [24] give a great example in their paper. Code sample 2.3 was part of PostreSQL.

```
if (arg2 == 0)
  ereport(ERROR,
    errcode(ERRCODE_DIVISION_BY_ZERO),
    errmsg("division by zero"));

/* No overflow is possible */
PG_RETURN_INT32((int32) arg1 / arg2);
```

Code sample 2.3: Undefined Behavior

The ereport function never returns, it does some logging before calling exit. In the mind of the developer this prevents the division by zero on the next line. Looking at the code on Github, the function this sample came from indicates that calling it will return a Datum. The body of the null check does not return anything, so the compiler concludes that the rest of the function will also be executed and division by arg2 will always get occur.

Division by zero is undefined in C, so the compiler concludes that arg2 won't ever be zero – it wouldn't get used in a division otherwise. As a result, the null check gets flagged as dead code, and is removed entirely.

Code sample 2.4 contains the fixed code. By adding an explicit return (in the form a macro), the compiler leaves the null check intact.

Notice how the comment blames a "gcc bug". This illustrates how even experienced developers seem to misunderstand their language of choice.

Code sample 2.4: Fixed Undefined Behavior

Tools

Not a single other programming language comes close to having as many external tools as C (and by extension C++). Many developers heavily depend on these tools in their usual workflow. One of the most established ones are the ones in Valgrind.

Valgrind is a suite of dynamic analysis tools, the most famous of which is Memcheck. Memory related bugs are some of the hardest to track down because most of them fall under undefined behavior. For example, using a memory location after freeing might not always crash the program. There's an informal term for bugs like these: heisenbugs. Something might go wrong but when you try to isolate the cause everything seems to be just fine. Especially since Address Space Layout Randomization (ASLR) tends to be disabled during debugging but not during normal execution.

This is where Memcheck comes into play. It analyses the program during execution and keeps track of what happens to the memory. This way it can notice memory related bugs such as use-after-free and report them back to the developer. Unfortunately it's not a perfect solution. There can be false positives as well as false negatives. It is quite incompatible with some libraries such as OpenMPI [33].

A lot of companies rely on analysis tools to manage their large C projects. And when there's demand in a market, the supply will follow. There's an impressive amount of commercial analysis tools. Coverity is one of the most established ones.

Dawson Engler is one of Coverity's co-founders and has become one of the leading researchers in the field of static analysis. He also co-authored a great paper in which he describes how difficult static analysis is in the real world [2]. One particularly interesting part of the paper mentions how there's a fundamental misunderstanding of what programming languages and compilers are. A programming language can exist as an abstract idea or a piece of paper. While the language a program is written in is whatever the compiler accepts. In other words, compilation is not certification. A good first step for a static analysis tool is to make sure that the input adheres to the specification. They go to pose the hypothetical question: "Guess how receptive they are to fixing code the "official" compiler accepted but the tool rejected with a parse error?"

Even with a plethora of tools available, C remains an untamed beast. Some tools like Valgrind are great at what they do but are still limited. Other tools like Coverity seem to fight stubborn developers as often as they fight bugs.

Dynamic Languages

Moving on to the topic of this thesis, dynamic languages. According to Guido Van Rossum, he made Python because he wanted to make a descendant of ABC that would appeal to Unix/C hackers [15]. After reading the previous section some spidey senses should start tingling.

Javascript's situation isn't great either. There are no namespaces, no modularization system, no classes, no interfaces, no encapsulation, ... Eric Lippert, who was on the ECMA committee during the early days has a Stackoverflow post where he discusses why Javascript is so ill-fit for static analysis and programming in the large in general [30]. Even though Stackoverflow is a dubious source for any academic work, the author's experience should make up for it.

Both languages are known as productive languages. Developers don't spend a lot of time writing boiler plate code or declaring types, they can get right to the good part. The dynamic nature of the languages even makes it extraordinarely easy to write generic functions, which makes code reuse easier and should make the code easier to maintain.

The following examples are more anecdotal than those in the previous section. As most people who use dynamic languages should be able to confirm, they can misbehave in the most spectacular fashion. The examples are supposed to be relatable and bring back memories of frustrating debugging sessions.

Classes

Python and Ruby are object-oriented languages, Javascript is prototype-oriented language but in essence comes very close to how the other two languages do classes. Lots of developers are familiar with class hierarchies and like using them. There is one glaring difference between how static languages and dynamic languages handle classes however. In most static languages, the class definition declares which methods are defined for objects of that class. This isn't the case with dynamic languages, adding a method to an object is as simple as assigning to a callable object to an attribute.

This is bad news for a static analysis tool that tries to do type inferencing on dynamic languages. Consider the following problem that occured while working on the Dodona platform.

The Ruby builtin String class provides a split that does the same thing as in most other languages: its argument is some separator which it uses to cut the String object into an array of smaller String objects. Calling the split method on some object returns the sameobject. Using puts on the object just shows the same exact String, weird. The documentation says that it should work. Testing the method in a REPL environment confirms that the split method should split the String. A few confused hours later, it turns out the object wasn't a String but an Array. The Ruby documentation doesn't mention that Array defines a split method. Googling "ruby array split" refers to the Ruby on Rails documentation. A library silently declared a method on a builtin type. puts prints every element of an Array on a separate line, so it just prints a single String.

This sort of reckless approach to classes has some serious implications. Not only does it confuse newcomers to a supposedly simple language, it confuses static analysers as well. Due to the lack of type declarations, a logical alternative would be type inference. But consider the following case, split is being called on something that's either an Array or a String at the current stage of inferencing. A regular Ruby analysis tool might wrongly conclude that the object must be a String. Analysing Ruby on Rails code would either require the tool to analyse the entire framework's code as well to learn that it adds a split method to Array, or it might even require a custom analyser for Rails altogether.

This is why static analysis of dynamic languages is typically done using an extensive data-flow analysis [16]. You don't have to infer the type of an object if you know where it came from.

Refactoring

Python's lack of structure makes it hard to work incrementally. At some point during implementation of the interpreter, line and column information had to be added to the AST structure. Python's ast module contains everything one could need to work on Python's AST, including lineno and col_offset for seemingly all classes. With the

exception of a few classes, such as **generator**. Implementing generators didn't come until much later, long after the analyser depended on the existance of lineno and col_offset for every node.

Refactoring dynamic languages is a challenge. What if we want to change the name of a method called add to insert. Can we replace all occurences of .add to .insert? That might change other classes their method names as well. As discussed in the previous section, type inferencing is non-trivial. Even IDEs that are renowned for their ability to refactor code, such as the JetBrains IDEs, rely on manual feedback to filter out the false positives. Reporting false positives is not always an option however. As stated by Bessey et al. [2], that's what causes people to question your tool.

2.1.2 NaN

As an aside, the existance of NaN should be considered error prone as well. Some languages like Python and Java do a good job at preventing NaN from entering your program through raising exceptions, but once they do find their way in you're left at the mercy of the IEEE 754 standard. The most recent version of the standard is IEEE 754-2008 was heavily influenced by the ISO C99 standard, which introduced NaN and inf to the C standard.

Since this standard, if one of the function's argument is NaN but the other arguments already determine the function's value, the result is no longer NaN. For example, this means that pow(1, NaN) is equal to 1. Mathematically this is at least a bit dubious, $1^{0/0}$ shouldn't be defined if 0/0 isn't either. The C99 standard introduced various other oddities [11]. $pow(-1, \pm \inf)$ is 1 because all large positive floating-point values are even integers. And having a NaN in the imaginary part of a complex number does not matter when the value is being casted to a real number, it's apparently possible for a value to be only slightly undefined.

It has become normal for NaN values to somehow disappear as if nothing was wrong, leading to some very confusing bugs. A friend ran into the consequences while implementing his own thesis [21]. The Theano framework has a function to compute the gradient of some expression. A NaN found its way into the input of this function but the result somehow didn't contain a single NaN, instead it became seemingly random noise. When implementing something algorithm intensive, any person's first instinct would be that the algorithm is wrong.

Static analysis should be able to help alleviate this problem. If the floating-point value that's being used came from a sqrt function, there should be an isNaN check first. Alternatively, the Rust programming language tries not to hide the fact that floating-pointing values can be NaN. Without providing your own implementation of the Ord trait for the f64 type, it's impossible to order a vector of f64 values because comparing two f64 might be meaningless. It does however provide an implementation of the PartialOrd trait, which returns an Option<Ordering>, which makes it clear that the result can be None.

2.1.3 Safe Languages

Now that it's firmly established that some languages gladly let their users shoot themselves in the foot, let's look at languages that protect their users. Most of these languages are functional languages but there are notable exceptions such as Ada.

Haskell

Having strong ties to the lambda calculus [20], Haskell is the archetype of safe languages. Its type system is unforgiving. Being a pure functional language, all state in a Haskell program is implicit and by extension there are no side-effects. One of core concepts of the

language is that Haskell code should be easy to reason about. That's why this language deserves a section in a thesis about static analysis and data-flow analysis; Haskell's design makes these things pleasantly simple.

```
def reset(arg):
    arg.attr = None

x = A()
x.attr = 4
y = x

reset(y)
x.attr += 1
```

Code sample 2.5: Aliasing

Consider the Python code in Code sample 2.5. Knowing that x and y are the same is integral to realizing that x.attr += 1 will result in a type error, as x.attr is None since the call to reset. Haskell has no side-effects – function calls like reset(y) won't change anything. Additionally, it has no explicit state and thus no assignments and no aliasing to begin with. This trait can be mimiced in other languages using the Static Single Assignment (SSA) form where every variable is immutable. A later section will discuss this form and how it relates to code analysis.

Rust

A newer language that favors safety over accessibility is Rust. While it does have explicit state, Rust also makes the aliasing problem trivially easy for static analysers. With some exceptions like the reference counting types, every piece of memory has a single owner in Rust – which means that by default there's a single way to access any data. This prevents the aliasing problem in sample 2.5 because after executing y = x, x is no longer a valid identifier – its data has been moved to y. On top of that, Rust has explicit mutability. This concept came from C/C++ where it's good practice to label all immutable things with const, except that Rust does it the other way around. This means that unless y was declared to be mutable, the assignment to y attr wouldn't compile either.

In languages like Java which heavily advocate encapsulation it's not uncommon to write something like a List<Element> getElements() method, so that other modules can see which data is present. Returning the original list would mean anybody can change its contents. That's why it's considered good practice to return a deep copy of the list instead. Deep copies carry a significant overhead with them, so developers end up choosing between a safe architecture or an efficient implementation. Rust lets data be borrowed, so that other modules can see its contents. The result is a reference which is very similar to a pointer in C, with the exception that borrowed references carry a lot more type information with them. For starters, it's possible to borrow something mutably or immutably. If there is a single mutable borrow to an object, there can't be other borrows at the same time. This is a mechanism that's supposed to avoid unexpected side-effects. Another thing that's part of a borrow's type is its lifetime. If object A wants to something from object B, B has to exist at least as long as A. This mechanism directly prevents all sorts of memory related bugs that occur in C.

Rust is an interesting example of the relationship between languages (more specifically the compilers) and static analysers. The Rust compiler enforces a lot of things that the C compiler doesn't but that the C community has written their own tools for. One might wonder why C is even still around if Rust seems to be a more complete package. Part of the answer seems to be that Rust is a very restrictive language which leads to frustrated

developers. Keeping in mind Coverity's paper [2], it's a lot easier to ignore a analyser than it is to fix a compile error.

In fact, this had received the informal label of being an XY problem. If a person knows to do something using method X, he's less likely to learn method Y – even if method Y is clearly the better choice. Rust has received a lot of criticism from renowned developers for ridiculous reasons, such as being unable to have two mutable references to the same object. That's how they'd do it in C, so it must be the right way. This problem is relevant in this paper for two reasons. For starters, static analysis tools run into the same mentality issues [2]. More importantly, it shows that it's important to never pick up bad habits in the first place. The field of application of this thesis is ultimately helping students learn how to program, before they even have any bad habits.

2.1.4 Middle Ground

It's unrealistic to expect that all programs be rewritten in safe languages. That doesn't mean that we should abandon all hope of having reliable programs though. This is why analysis tools have emerged alongside the language; to fill the gap.

There is a class of static analysers that's particularly interesting, the linters. What sets them apart from other tools is that they report error prone patterns rather than actual errors. Preventing bugs is better than fixing them. One of the most renowned linting tools is JSLint, its Github page contains the following wisdom [34]:

"The place to express yourself in programming is in the quality of your ideas and the efficiency of their execution. The role of style in programming is the same as in literature: It makes for better reading. A great writer doesn't express herself by putting the spaces before her commas instead of after, or by putting extra spaces inside her parentheses. A great writer will slavishly conform to some rules of style, and that in no way constrains her power to express herself creatively."

Few developers should find anything anything wrong in that reasoning. The main point of contention is which rules to follow. Crockford is a proponent of using certain language features sparsely [6]. In his book titled Javascript: The Good Parts he describes which features of Javascript he deems good (or great and even beautiful) and which parts should be avoided. The bad parts are everything that lead to error prone code. The most obvious examples would be the switch statement. He has given a good presentation at Yahoo where he gives more examples of why JSLint discourages the patterns that it does [29].

2.2 Inspirations

Analysis tools all serve a common purpose but are still very diverse. Static and dynamic analysis tools do things very differently and even within static analysis tools there's a lot of variation. Linters work mostly syntactical, focusing on speed and immediate feedback. Other tools like Coverity do a much deeper analysis and usually run nightly. Another major difference among static analysers is soundness. Generally speaking, sound analysis tools are based on formal logic, slower, more comprehensive but more prone to false positives. Unsound methods seem to coming out on top as most practical languages are unsound themselves [14]. Others simply say that it doesn't matter how you do it, as long as the results are good [2].

2.2.1 Code Smells

More important than how to do the analysis is perhaps what to look for. Code smells are a taxonomy of indicators that something may not be right about the code. The term was coined in a book by Kent Beck in a book on refactoring [8]. In that book code smells are indicators that some refactoring might be necessary. Aimed at software architects, they're informal descriptions of things that may induce technical debt. They're

```
x += 1
y += 1
z += 1

x = sqrt(x)
y = sqrt(y)
z = sqrt(z)

u = x - 1
v = y - 1
w = z - 1
```

Code sample 2.6: Duplication

not actual bugs yet but error prone patterns, the sort of things Linters aim to detect. One of the code smells ins *cyclomatic complexity*, having too many branches or loops. This is something Pylint also recognizes. What Pylint lacks however is the refactoring aspect of the code smell. Code smells were meant to be refactored manually by professional software architects, but in an educational setting you have to take into account that the students may not be able to refactor it themselves.

```
def foo(x):
    x += 1
    x = sqrt(x)
    return x - 1

u = foo(x)
v = foo(y)
w = foo(z)
```

Code sample 2.7: Refactored version of sample 2.6

There are also code smells that linters currently do not pick up because they'd require some very deep analysis. The most notable of which would be the *Code Duplication* smell. JetBrains has developed some of the best refactoring IDEs such as IntelliJ and PyCharm but started off by developing code refactoring tools such as IntelliJ renamer for Java and Resharper for C#. Made for commercial code bases, these tools are ultimately advanced heuristics that still miss obvious duplication. PyCharm 2016 was unable to find the duplication in code sample 2.6. Even it should probably be refactored to something like code sample 2.7.

```
x += 1
x = sqrt(x)
u = x - 1

y += 1
y = sqrt(y)
v = y - 1

z += 1
z = sqrt(z)
w = z - 1
```

Code sample 2.8: Alternative order of sample 2.6

JetBrain's tools are closed source so it's unclear if 2.6 was deemed too simple to refactor. Assuming they work in a similar fashion as competing tools however, it's the order of statements that causes it to fail. Tools like Simian, Sonar, PMD, and Dup Loc all work on a token stream in the same order as it appears in the file. Code sample 2.8 illustrates how sample 2.6 could be reordered so that tools can detect the duplication just fine.

```
x = []

s = int(input()) + 1
x.append(s)
```

Code sample 2.9: Duplication

When analysing student code, this can be a serious limitation. Consider code sample 2.9, which just reads 4 numbers from stdin, increments them, and stores them in x. Even if this duplication gets detected, most tools are targeted at professional developers who would never write code like this. The critical difference here is that the refactoring shouldn't introduce a new function but a loop such as in 2.10.

```
x = []

for _ in range(4):
    s = int(input()) + 1
    x.append(s)
```

Code sample 2.10: Refactored version of sample 2.9

Compilers face the same problem; their refactorings are optimizations. We'll revisit this problem in a later section about the Static Single Assignment (SSA) form.

There are some other code smells besides code duplication that could be interesting for new programmers. The following list contains some that at first glance look like the most interesting.

- Large class: A class that's grown too large and probably has too many responsibilities.
- Long method: Much like the previous one, this method probably has too many responsibilities.
- Inappropiate intimacy: When a class heavily depends on implementation details of another class.
- Excessive use of literals: Also known as magic numbers, these should probably become descriptive constants.
- Cyclomatic complexity: Too many branches, also informally referred to as spaghetti code. Linters do a fair job at pointing them out but offer little help in fixing them.

2.2.2 Compilers

Static analysers aren't the only tools that aim to make code better – compilers do so as well. Refactoring from a software architect's point of view is aimed at making the code

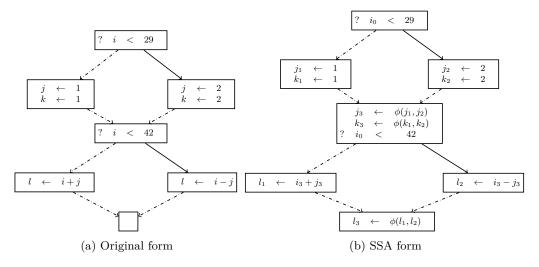


Figure 1: SSA transformation

easier to read and more maintainable. Optimizations are aimed at making code more efficient. These two things sometimes do completely opposite things, unfolding the loop in 2.10 results in sample 2.9. Both operations transform code in a conservative manner though, i.e. without changing the semantics (of valid code). Optimization is a very active area of research, with companies like Google and Apple powering LLVM, Oracle for the JVM, Red Hat for the GCC, ... More importantly, even the most esoteric features in compilers have proven their worth as they're part of a real product, which gives confidence that a static analysis that uses the same principles will work as well.

SSA

Static Single Assignment (SSA) form is a program representation that's well suited to a large number of compiler optimization such as constant propagation [25], global value numbering [1], and code equivalence detection [26]. The term was first used in a paper by IBM [1] in the 80s but had little practical success initially. It wasn't until several optimizations were found [7] [5] that it started becoming popular. Since then it's found its way into most popular compilers. LLVM has used it for its virtual instruction set since its inception in 2002 [38], it's what powered Java 6's JIT [12], and it's what's behind recent GCC optimizations [17] [18].

The idea is very simple, every variable can be assigned to once. This can be done by adding incremental numbers to each variable. For example, $\mathbf{x} = \mathbf{x} + 1$ becomes $\mathbf{x}_1 = \mathbf{x}_0 + 1$. This is a trivial transformation for straight-path code but becomes a bit harder when dealing with branches. Figure 1 illustrates how to handle such code. Every branch introduces new variables as before and a *phi-node* gets inserted at the of the branch. This node mimics a function call which can return either of its two arguments. This doesn't correspond to an actual function call, it's just a token that gets inserted to help with the analysis.

Memory SSA

The SSA form has a lot of benefits, as cited in the beginning of this section, but is limited to scalar values and not well suited for structures and arrays. One of the solutions to this problem is Memory SSA as implemented by GCC [17]. This is a transformation that runs on a sufficiently low-level representation of the source code. It has to be low-level so that there's a notion of LOAD and STORE instructions.

Because the actual memory locations are not known during compilation some abstractions are needed. GCC uses compiler symbols which they called tags to represent regions of

memory along with two virtual operators VDEF and VUSE. For every LOAD a VUSE of some tag gets inserted, and likewise for STORE and VDEF.

There are three types of tags:

- Symbol Memory Tag (SMT): These are the result of a flow-insensitive alias analysis and is almost purely type-based. For example, all dereferences of an int * receive the same tag.
- Name Memory Tag (NMT): These are the result of a points-to analysis applied after the program is in SSA form and inherits its flow-sensitive properties [17]. In other words, multiple SSA forms get used.
- Structure Field Tags (SFT): These are symbolic names for the elements of structures and arrays.

Tags get used in a similar way to variables in the regular SSA algorithm. Assigning to a tag is like assigning to all symbols that have received that tag. In the original implementation, call clobbering i.e. a function call overwrites some memory of an argument, such as in code sample 2.5 is handled the same way as global variables [17]. Quoting the authors: "All call clobbered objects are grouped in a single set". The current implementation has rewritten all call-clobber related code to use an aliasing-oracle [28].

LLVM's usage of Memory SSA is not quite as documented. Their documentation refers to GGC's paper [17, 35] and mention that "Like GCCs, LLVMs MemorySSA is intraprocedural.". As referenced in the previous section, this isn't entirely true for GCC anymore. It doesn't seem to be true for LLVM either, a recent publication describes *Static Value-flow* analysis which produces an interprocedural SSA form [23]. It has been part of LLVM since 2016 and like GCC's implementation it uses the results of an external points-to analysis.

2.2.3 Symbolic Execution

Rather than using concrete values, symbolic execution uses symbolic values. Those values represent possible values through a set of constraints. This technique is commonly used to find interesting corner cases to use in unit testing [3, 19, 22] and the original SSA paper used similar principles as well to make their analysis more precise [1].

At each branch point a path constraint gets introduced, which is a symbolic expression that must be true for the current branch to be taken. If there are no values that satisfy all the constraints, the branch gets flagged as a dead branch. In the case of a static analysis tool this will most likely result in a warning, a compiler will just remove the conditional and the dead branch. For example, consider code sample 2.11. y>0 becomes a constraint during the execution of the positive branch, as well as x>-1. The former constraint is pretty simple to add, the latter requires some serious bookkeeping. Thorough symbolic execution relies on some form of data-flow analysis.

```
x = int(input())
y = x + 1

if y > 0:
    z = sqrt(y)
else:
    z = 0
```

Code sample 2.11: Symbolic Execution

Symbolic execution is a very powerful tool but comes with a few limitations. One is the *state explosion problem*, the number of paths can increase *very* fast. The Java Pathfinder

manages this problem using state matching and backtracking [19]. State matching will check if a similar state has already been processed, if it has it will backtrack to the next state that still has unexplored choices.

Another limitation is that symbolic executors typically work on scalar values, with most of them working on a low-level representation such as JVM bytecode or LLVM IR. Things get a lot harder when dealing with structures and collections. Consider code sample 2.12 for example which defines a function foo that prints homogeneous if and only if its argument is a collection and all elements in that collection are of the same type. Not only does the positive branch introduce a constraint on the length of \mathbf{x} , all elements have to be of the same unspecified type as well. The most advanced symbolic executor for Python seems to be PyExZ3 but even that one doesn't handle heterogeneous collections. The relation between uniqueness and the length of a set is also non-trivial, even though it's a very pythonic pattern.

```
def foo(x):
   if len(set(map(type, x))) == 1:
     print('homogeneous')
   else:
     print('heterogeneous')
```

Code sample 2.12: Symbolic Execution Challenge

3 Fosite

Named after the Frisian god Fosite and foresight, Fosite is the name of the abstract interpreter developed for this thesis. A relatively unknown god, Fosite is the god of reconcilitation, justice, and mediation. These are also qualities that a static analyser should aim to have to gain a user's trust [2].

3.1 Area of Application

Unlike most existing tools, Fosite's focus is analysing small student submissions. This has both advantages and disadvantages. The biggest advantage is that we're free to explore precise but inefficient methods. Not entirely free however, feedback should be fast (<1s) because a lot of students will send a lot of submissions at the same time. Imagine being a stressed out student, working on your final exam and every submission takes a minute to run because submissions come in faster than they get processed. It would also be nice if the tool has little runtime dependencies, since by the Dodona design it'll have to run in Docker containers. These two requirements make the Rust programming language a good fit, since it generates fast native code without the unexpected problems C and C++ might induce.

Perhaps the most requirement of all, any warnings have to be as detailed as possible. More details should make the errors more convincing and will be met with less resistance from the user [2]. This is important when dealing with new programmers; simply pointing out bad style is not enough if that person does not know how to fix it themselves. Fosite uses a data-flow analysis to pinpoint the source of problems and uses that information to inform the user.

The analysis should work as close as possible to the submitted code and at the very least maintain a one-to-one relationship to it. This is important because the end goal is automated refactoring, which becomes hard when the input becomes mangled beyong recognition.

3.2 Approach

As a first step towards automated refactoring, Fosite is an abstract interpreter with the intention of doing data-flow analysis. This by itself isn't entirely new; PyPy uses a similar principe to power their optimizations [37]. PyPy's solution is intraprocedural though which unfortunately isn't ideal for analysing call clobbering. Others have successfully used abstract interpreters to perform a may-alias analysis on Python with the goal of optimization [9]. Fosite is based on their conclusions and results but is ultimately made for a different cause i.e. detailed static analysis.

The result isn't exactly an SSA form. The Memory SSA approach by the GCC and LLVM isn't an option since that relies on a low-level representation. That's a luxury only optimizations have, when working towards refactoring we need to stay close to the original source code. Regular SSA is of course an option since PyPy does it [37], but is limited to intraprocedural analysis.

Fosite generates use-def information instead. A use refers to any data depedency, such as resolving a variable name or retrieving an element from a collection. A def is the inverse such as assigning something to a variable name or inserting an element into a collection. Within Fosite, a use and a def are respectively called a dependency and a change. As with SSA, incremental numbering can be applied to subsequent changes. The main difference with regular SSA is that this requires a separate data structure. This allows a single expression or statement to have multiple changes. For example, a conditional's dependencies and changes are the sum of its branches's. A conditional statement is exactly that – a statement, and it can be useful during refactoring to treat it as a single atomic thing. Another useful consequence of this is that a function call can induce multiple changes, for each of its call clobbered arguments.

To achieve the same level of precision as Memory SSA, Fosite uses two kinds of changes and dependencies. For starters, there's the usual identifier dependency, which is useful for to model reachability of data. Consider code sample 3.1 in which x gets defined twice. In between assignments the first value of x gets used to call in a call to print. This gets modeled using an identifier dependency. Another sort of dependency is the object dependency, which is useful to model an internal state dependency. The second assignment to x assigns a list to it, which gets printed as well. Before printing however an element gets appended to it. Appending an element to a list doesn't change anything about the identifier and thus can't be modeled in the same way. In other words, the final call to print has a dependency to both the x identifier and to whichever object x points to at the same time – and both dependencies serve their own purpose.

```
x = int(input())
y = int(input())
print(x - y)

x = []
x.append(1)
print(x)
```

Code sample 3.1: Dependency Example

There are hidden dependencies in this program as well. The first two lines of code will read two lines from stdin and parse them to integers. The order in which this happens is important since the two values get subtracted from each other. This can be modeled by adding implicit state. The call to input both depends on the implicit state and changes it, which will ensure that the relative order between the two calls remains the same. Other IO functionality such as the print call will do the same.

3.3 Modules

Since languages tend to share a lot of features, it's not unthinkable to have an abstract interpreter that can process multiple languages. The first thing this would need is a common input format. Fosite defines a *General Abstract Syntax Tree* (GAST), which is similar to any other AST with a few exceptions. First of all, it has to be able to capture all *syntactic* features of the languages it supports; the semantics aren't important yet. There's a good chance that adding support for an additional language will require some new nodes or some extra information in existing nodes. Since only things will have to get added interpreting the existing languages can just ignore the additional node types. Another thing that's special about the GAST is that every node has its unique identifier, and the identifiers are totally ordered. If one node's identifier is less than another's, that must mean it came before that other node in the original source file. This is important to accurately report warning but also because some optimizations rely on it.

GAST only provides a common syntactical framework to work on, the interpreter has to be able to add semantics to this. A different Executor instance may be assigned for every supported node for every supported language. Languages that share the same features can reuse existing Executor implementations. Common and fundamental features such as function scoping are even available inside the interpreter's implementation itself.

3.4 Power of Interpretation

While linters recognize error prone patterns, interpreters can recognize error prone logic as well as some outright errors. An additional benefit of an interpreter-based approach is that it approaches feedback the same a person would: starting at the beginning, step by step. This section gives a few interesting examples of what an interpreter can do that linters (or at least PyLint) can not.

Code sample 3.2: Function Returns

Code sample 3.2 contains an error prone pattern of Python-like code. A student actually had written something like this which resulted in one out of 200 unit tests failing. Written like this, it's possible that the none of the intended return statements gets executed. If this happens the return value is going to be None, which makes the unit test fail in an unexpected way – nowhere did they specify a None value should be returned. Fosite gives an accurate description of the cause – a return statement was missing – instead of just the result.

```
x = []
...
while tuple([0] * i) not in x:
    ...
    x += tuple([0] * i)
```

Code sample 3.3: Heterogeneous Collections

One the assignments required that a sequence of tuples should be generated, stopping whenever a tuple of zeroes has been added. Code sample 3.3 is based on one of the submissions. Up until the adding of the tuple of zeroes, the type of x was List[Tuple[int]] (in the notation used in Python 3.5 type hints). Instead of appending the tuple however, += will concatenate the tuple's elements to x. This changes the type to List[Union[int, Tuple[int]]]. This transition to a heterogeneous type is valid Python code but ultimately very error prone. In fact, this causes an infinite loop in this case, as the expected element never gets added.

```
def change(x, d = None):
    list1 = ''
    list2 = []
    for i in range(0, len(x)):
        while x[i] != ' ':
        list2 += x[i]
        list1 += translate(list2[0], d)
        list2 = []
    return list1
```

Code sample 3.4: Endless Loop

Although the deciding that a given piece of will never stop is impossible, it is possible in some trivial cases. Those trivial cases also happen to be quite common. Code sample 3.4 is an excerpt for a submission. The student intended to tokenize the string x, building the token in list2. Every token should then get translated and the translated tokens get stored in list1. There are a number of mistakes but the most important one is arguably the endless while loop. The student wanted index i to be a starting position of the token, with the while loop building the token from that point. That's of course not what the code does, the same character will get added over and over since none of the values in the loop condition ever change. Data-flow analysis remembers when and where variables get their values, so it can be used to recognize that the variables are still the same. This approach will also flag any while True loop as error prone, which is arguably a good thing.

3.5 Implementation

3.5.1 Core Objects

- No values at the time, so limited symbolic execution
- Collections do get modelled, but is very hard

Pointers and Objects

Paths and Mappings

Ordered by node ID, very important

Scope

Find example of why this is a non-trivial component.

- Introduce Frames
- Every frame corresponds to a branching node in the execution path

- A frame contains its own set of mappings, of all changes that happened in this execution path
- Changing an identifier starts at the root
- Iterate over the nodes in the change's path
- If the scope doesn't have enough frames, push new frames corresponding to the current node in the iteration
- Only have to check the number of frames, not the actual branches the frame corresponds to
 - Assuming that the scope's contents are consistent with the current execution state two things can happen during assignment
 - The last change to the scope was done in the same execution path. In this case, there are enough frames as it is.
 - The scope's execution path is a strict subset of the current execution path. In this case, we only have to append the missing frames. Ordering of the AST nodes ensures that we know exactly where the subset ends.
 - This system depends on the correct merging of frames, see later
- Resolving an identifier starts at the right, the most recent change in this scope
- Absolutely no need to introduce branches corresponding to the current execution path
- Resolving an identifier does not include the information of the frame's path node or its parents's path nodes.

Code sample 3.5 illustrates why name resolution is done this way.

```
x = 42
if cond:
    y = 'string'
    x + y
```

Code sample 3.5: Name Resolution

This example will always fail if line 4 is reached, because in that case x will always have type int, while y will always have type string. So naturally, we want to report it in the same way.

- Merging frames is a necessary step to ensure consistency the the interpreter's execution state.
- Two ways of merging
 - Actually merging the last two frames into the parent frame (used for function scoping)
 - Discarding the last two frames (used for block scoping)
 - Latter is easy, former requires some special attention

As illustrated in code sample 3.6, merging requires some special attention.

If the negative branch of the condition at line 4 is not taken, the above code will fail at line 7. In that case, x still has the value it received at line 1, but is that all that should be reported? x only has that value if the negative was taken. So if we want to accurately describe why it has that value, that information should be there as well.

This can be achieved by simply resolving the identifiers for both possible branches, and adding the frame's path node to every result; as described in algorithm 1.

```
x = 42
y = 'string'

if cond:
    x = '42'
x + y
```

Code sample 3.6: Merging

Algorithm 1 Merge

```
1: function MERGE
       negative \leftarrow frames.peek()
       positive \leftarrow frames.peek()
 3:
       parent \leftarrow frames.peek()
 4:
       identifiers \leftarrow positive.identifiers \cup negative.identifiers
 5:
       mappings \leftarrow []
 6:
       for all identifiers do
 7:
           nmap \leftarrow resolve(identifier)
 8:
 9:
           nmap.augment(negative.node)
10:
           mappings += nmap
       switch_ranches()
11:
       for all identifiers do
12:
13:
           \texttt{pmap} \leftarrow \texttt{resolve}(\texttt{identifier})
           pmap.augment(positive.node)
14:
15:
           mappings += pmap
16:
       parent.add_mappings(mappings)
```

3.5.2 Conditionals

Observation

Every execution branch is either taken, or it isn't. Figuring out which is the case is well-known to be uncomputable, for the simple reason that the branch condition can be arbitrarily hard to evaluate. This implies that in some cases, we can't decide whether or not a given branch gets taken. The best we can do in these conditions is conclude that the branch *might* get taken. In the following section, we'll denote this possibility with Maybe, in line with Python's True and False.

Observation

In some cases, we do need a definitive answer. Consider the following examples

The above examples gives a pretty good indication that in some cases, we really need an exact example. This is particularly important for any sort of input validation. The first example is a common pattern for filling in optional arguments, while the second one is just good practice in general. Other examples include checking the length of a certain collections and type-checks.

Boolean Expressions with Certainty

There aren't a lot of boolean expressions which we can evaluate with certainty. Luckily enough, the ones that we can do are mostly the ones of interest. The is operator for example should compare the addresses of two objects and return True if and only if they're equal. So internally, we can mimic this behavior – and answer with certainty and under which conditions, the objects have the same address in our own analysis. The other possibilities are harder to do, and the best we can realistically return is Maybe.

The == operator is a special case. If the __eq__ method was implemented correctly, this should at the very least return True if the two objects being compared are the same – as with is. The analyzer in its current state does not properly support analysis of operator overloading, so it will assume that __eq__ does indeed have a sane implementation. The analysis of the == operator in this case becomes the same as the analysis of the is operator. Likewise for the <= and >= operators.

The and and or operators are quite obvious. and will return True if both sides are true with certainty, False if either side is false with certainty, and Maybe in any other case. The or operator is analogous.

Definition: containment

A path A is contained in another path B if every node of path A occurs in the same way as it does in path B

3.5.3 Path exclusion

When executing an execution branch, we should have information about why that specific branch is being executed. If that information includes for example that we are sure that ${\tt x}$ is not None, we should disregard any mapping that says the opposite. And even better, we can exclude any mapping that would occur under the same contradictory conditions – even if those mappings don't have an explicit connection to ${\tt x}$. For example in the following trivial example:

```
if cond1:
    y = None
    z = None

if y is not None:
    print(z.attribute)
```

In the positive branch of the first condition, there's a point where both y and z become None. After evaluating the second branching condition, we can be absolutely sure that the positive branch of the second branch will not be taken if the positive branch of the taken has been taken. In effect, this means that the mapping for z where it receives the value Nonein the first branch is of no use while evaluating z.attribute.

The exclusion of certain mappings is what we'll conveniently call *path exclusion*. We can give this term a more formal representation as well.

Assume that resolving an identifier x resulted in a set of mappings M. Every mapping $m \in M$ is of the form (p, a), where a is the address to which x can point, and p is the execution path that's required to get this mapping from x to a.

Call R the set of restrictions; the set of every execution pth that is of no concern while evaluating. If there exists a path r in R for a given mapping (p, a), for which it holds that p is contained within r, we can exclude the mapping from the current evaluation.

4 Results

5 Discussion

6 Future Work

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