# Developments of a Simple Model to Elucidate the Shape of Enveloped Viruses: Motivated by Monkeypox and SARS-CoV-2

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# Objective

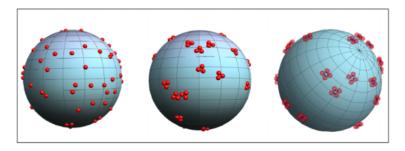
First, to develop new models and simulations to study how the viral genome architecture (its shape, length and flexibility) influences the membrane. By combining polymer physics and liquid-state physics, such as crowding effects, we hope to gain a deeper understanding of viral assembly. By simulating how viral genomes behave in confined environments, we can uncover key principles behind virus formation and stability. It could contribute to more effective strategies for prevention and treatment of viral infections, especially for viruses like Monkeypox and SARS-CoV-2.

Second, studying the pressure inside viruses helps us better understand how viral genomes infect host cells and spread disease. When a virus packages its genetic material into its capsid/membrane, it builds up a lot of internal pressure. This pressure is key to how viruses inject their DNA or RNA into host cells quickly and efficiently. By studying this process, we can uncover new ways to block viruses from replicating, such as targeting the proteins responsible for genome packaging, which could reduce internal pressure and prevent successful infection. It can inspire new drug delivery systems that work like viruses, help design better and more stable vaccines, and teach us more about the physical limits of DNA/RNA in extreme conditions.

## Motivation

In previous study, we developed a simple yet insightful model to investigate how monomers can self-organize into dimers, trimers, and tetramers on spherical surfaces, inspired by the trimeric spike proteins found in viruses like COVID-19. Using Monte Carlo simulations with attractive

Yukawa potentials that include both radial and angular dependencies, we showed that trimers form more easily and are generally more stable than dimers. Tetramers, in contrast, require stronger attractive forces to form and are prone to aggregation when those forces become too strong. Analyses of energy and entropy contributions revealed that trimers are often more stable than dimers and, under certain conditions, as stable as tetramers. These findings are consistent with structural observations from cryo-electron microscopy studies of SARS-CoV-2 spike proteins, which show that trimers dominate the virion surface architecture[1].



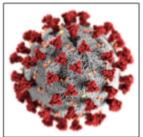
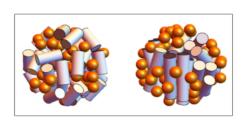


Figure 1: Left image: Simulation of the SARS-CoV-2 spike protein on a spherical surface, illustrating the progression from randomly distributed monomers (left) to trimer (center) and tetramer (right) formations. Right image: SARS-CoV-2 for Covid-19 schematic image (CDC Public Health Image Library) [2]

Beyond virus-related modeling, the researchers also explored how rod-like molecules behave inside confined spaces, such as droplets or cavities, under molecular crowding. Our simulations showed that shorter rods tend to accumulate near the boundary, while longer rods align toward the center, consistent with experimental observations. These results emphasize



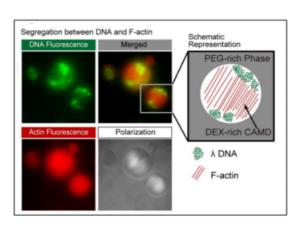


Figure 2: **Left image:** Short DNA rods distribute near wall under molecular crowding. Long F-actin rods distribute in cavity interior and show high orientation ordering. Long F-actin rods distribute in cavity interior and show high orientation ordering. Specific localization of long DNA ( $\lambda$  DNA) and F-actin in DEX-rich CAMDs. **Right image:** Fluorescence microscopic images of DNA (GelGreen), actin (Alexa Fluor 546), and merged views are shown, along with polarization microscopy observations (four panels on the left). The images were captured under the conditions of 120  $\mu$ M  $\lambda$  DNA, 10  $\mu$ M actin, and 4.0 mM KCl. F-actins were observed to be in a nematic liquid-crystal state at the center of DEX-rich CAMDs, while DNA molecules appeared segregated from the center. In other words, long DNA strands are compressed by the aligned F-actin region, as schematically illustrated in the right panel. Scale bar: 100  $\mu$ m.[3]

the important role of both energetic and entropic factors in determining molecular organization in confined systems.

Building on this foundation, we have successfully simulated the membrane along with the spike protein on its outer surface. We are now shifting our focus from the exterior to the interior of the membrane, concentrating on the interactions between the membrane and the enclosed genome. This approach aims to provide deeper insights into how viruses are organized, how the membrane and genome influence each other's fluctuations, and how genetic material is ultimately released—knowledge that could inform the development of new antiviral strategies.

### Introduction

Viral infections have a critical impact on global health, emphasizing their role in pandemics and outbreaks. These infections pose significant risks to public health and encompass a wide range of diseases, from seasonal influenza to more severe infectious diseases such as Monkeypox and COVID-19. Both Monkeypox and COVID-19 viruses are classified as enveloped viruses, which are distinguished by their lipid membranes that surround and protect their genetic material (genomes). These membranes serve several crucial functions: they provide protection by shielding the viral genome from environmental factors and potential damage, and they facilitate transmission by enabling the virus to enter host cells. The membrane plays a key role in this process by interacting with specific receptors on host cells, thereby promoting viral infection and the delivery of the genome into the host. We need to further understand these mechanisms to develop effective prevention and treatment strategies.

Virions are acellular, meaning they are not made up of cells and therefore lack cellular components like organelles, ribosomes, or a plasma membrane. To elucidate the shape of enveloped viruses, one essential factor is on their genomes. The genome of a Monkeypox virus constitutes of a double stranded DNA of about 190 kb (kilo-bases) or 95 kbp (kilo-base pairs), that is 3000 nm in contour length, compared to the dimension of a virus particle at around 250 nm long[4][5]. In Figure 3, the virus particles show spherical and oval shape, corresponding to immature and mature viruses, respectively.

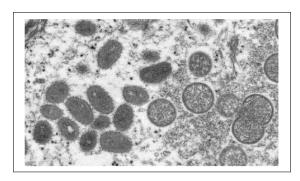
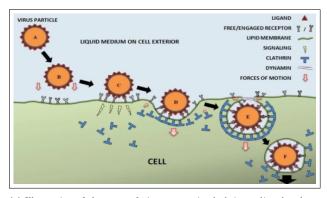


Figure 3: Electron microscopic (EM) image for Monkeypox virus particles. Oval-shaped virus particles are mature, and spherical particles are immature virions [6]

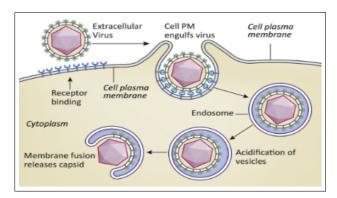
We aim to investigate the relationship between genome shape and membrane morphology in virus particles, focusing on the transition from spherical to oval geometries. Spherical shapes are typically associated with immature viruses, while mature viruses tend to exhibit more elongated, oval forms. By using a coarse-grained model and Monte Carlo simulations, we will explore how changes in the genome configuration—such as compaction, fluctuation, or spatial arrangement—affect the deformation and final shape of the surrounding lipid membrane. This study will help elucidate how the shape of the genome affects membrane curvature during virus maturation.

In contrast to Monkeypox viruses, SARS-CoV-2, the virus responsible for COVID-19, are spherical and their diameter is around 80-120 nm, much smaller than the size of a Monkeypox virion. In terms of their genomes, Covid-19 viruses belong to the family of RNA viruses as common corona flu viruses. Unlike seasonal flu viruses, the Covid-19 virus has the longest RNA among known corona viruses, consisting of a single 30 kb strand of RNA with a contour length at about 1,400 nm. [7][8]

SARS-CoV-2 enters a host cell by first using its spike (S) protein to bind to a specific receptor on the surface of human cells called ACE2 (angiotensin-converting enzyme 2). This spike protein acts like a key, allowing the virus to attach tightly to the host cell. After attachment, the virus enters the cell either through direct fusion with the cell membrane or via endocytosis.[9][10] When a virus infects a host, it deliberately breaks this symmetry. Doing so creates weaker areas on the surface of the capsid, which then open up to allow the virus to inject its genetic material (RNA or DNA) into the host cell. In this way, breaking symmetry is an essential part of the infection mechanism.



(a) Illustration of the steps of virus entry via clathrin-mediated endocytosis. (A) Virus approaches the cell surface. (B) Biochemical interactions between ligands and receptors attract virus to the cell surface. (C) Virus attaches to the cell surface and signals the cell. (D) A clathrin-coated pit is formed around the bound virus. (E) A clathrin-coated vesicle is formed, and the dynamin at the neck region facilitates vesicle scission. (F) The vesicle travels to the cell interior [9].



(b) Membrane fusion. Many viruses, both enveloped and unenveloped, are brought into cells by endocytosis. The low pH environment in the endosome triggers molecular rearrangements of capsid or envelope proteins. In this example, an enveloped virus is fusing with an endosomal membrane to release the capsid into the cytosol [10].

Figure 4: Comparison of virus entry mechanisms: (a) Clathrin-mediated endocytosis, and (b) Membrane fusion.

Once inside, the viral envelope is removed (a process called uncoating), releasing its positive-sense single-stranded RNA genome into the host cell's cytoplasm. This viral positive-sense single-stranded RNA acts directly as messenger RNA (mRNA) and is translated by the host's ribosomes to produce viral proteins, including more spike proteins, structural proteins, and enzymes necessary for viral replication. The viral genome is also copied to make more RNA strands. These components are then assembled into new viral particles. Finally, the new viruses are released from the cell by budding, often taking a piece of the host's membrane with embedded spike proteins, allowing them to infect new cells. The spike protein is essential for both the entry of the virus and for determining which cells it can infect.

Viruses pack their genetic material DNA or RNA into capsids/membrane under extremely high pressure, often reaching tens of atmospheres, far greater than the pressure inside a champagne bottle. During the assembly of a virus, a specialized motor protein powered by ATP works to push the viral genome into the small, enclosed space of the capsid. This step requires a significant amount of energy because the DNA or RNA has to be crammed into a space much smaller than its relaxed form. As a result, the genetic material becomes tightly packed, creating considerable internal pressure. This pressure mainly arises from two factors: the repulsion between the negatively charged parts of the nucleic acid strands and the physical strain of bending a rigid, long molecule into such a confined area.[11]

This pressurization plays a crucial role in the infection process. When a virus encounters a

host cell, the built-up pressure inside the capsid acts/membrane like a compressed spring, forcefully ejecting the genome into the host cell. This mechanism ensures that the viral genetic material enters the cell rapidly and efficiently, allowing the virus to take over the host's cellular machinery almost immediately. This strategy is not limited to a single type of virus; it is conserved across many viral families, including those that infect humans, bacteria, and archaea. For instance, studies have shown that herpes simplex virus type 1 (HSV-1) can exert internal pressures of up to 20 atmospheres, which is essential for successfully delivering its DNA into the host[11].

We plan to study how internal pressure builds up and is released in viruses by focusing on the physical and structural mechanisms that generate and regulate this pressure. Specifically, we aim to investigate how the arrangement of the genome and the properties of the surrounding membrane or capsid contribute to pressurization. Using coarse-grained modeling and Monte Carlo simulations, we will explore how genome packing and membrane deformation interact to generate internal forces. By understanding these mechanisms, our research could help identify potential targets—such as structural components or genome configurations—that can be disrupted to prevent the pressure-driven ejection of the viral genome, offering insights for future antiviral strategies.

### From Early Polymer Theories to Modern Coarse-Grained Models

Back in the 1960s and '70s, long before computational biology became mainstream, polymer scientists were already developing clever ways to simplify and understand how long-chain molecules behave. They built theoretical models like the freely-jointed chain, worm-like chain, and Gaussian chain—each designed to capture how flexible or stiff a polymer might be, and how it moves in space. These early ideas laid the foundation for what we now call coarse-grained simulations.

Building on these foundational models, researchers have developed a wide range of coarse-grained techniques that better balance physical realism with computational efficiency. Polymers are often described as long, flexible chains whose properties scale with their size. Coarse-grained models capture key features such as bonding and excluded volume, allowing

large-scale behavior to be studied with reduced complexity. However, to accurately predict the behavior of specific polymers, one must also consider their chemical composition.

While molecular dynamics simulations can offer a high degree of realism, they are computationally demanding and often impractical for simulating the slow dynamics of large systems over long timescales. To address this limitation, more efficient coarse-grained (CG) models have been developed, offering a practical compromise between resolution and performance.

A notable example of such a model is the bead-spring representation, which emerged during the same era as the early theoretical chain models. It represents a polymer as a series of connected beads linked by springs—a simple yet powerful approach. The bead-spring model has proven highly effective for studying how polymers move, tangle, and interact in bulk materials, and remarkably, this basic idea is still widely used today in modern polymer simulations [12].

# Polymer-Like Behavior of Biomolecules

The genomic material, protein shell, and membrane of viruses like SARS-CoV-2 (which contains single-stranded RNA) and Monkeypox (which contains double-stranded DNA) all exhibit polymer-like behavior.

# A. Polymer

The polymer is a large molecule composed of identical monomers or different types of monomers linked by covalent bonds[13].

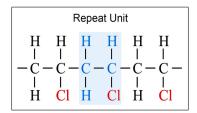


Figure 5: Polymer

# B. Protein/Amino Acid chain

Coarse-grained modeling started making an impact in protein science back in the 1970s, when researchers like Michael Levitt, Ariel Warshel, and Martin Karplus began simplifying protein structures to make them easier to study. Biochemists began adopting a more abstract

modeling approach, often representing entire amino acids as single "beads." This simplification enabled the simulation of complex processes such as protein folding and molecular motion.

Proteins are natural polymers made up of amino acids, which are like the individual links in a chain. Each amino acid has the same basic structure: a central carbon atom (called the alpha carbon) bonded to a hydrogen, an amino group (-NH<sub>2</sub>), a carboxyl group (-COOH), and a unique side chain, known as the R group. These amino acids connect through peptide bonds, forming a

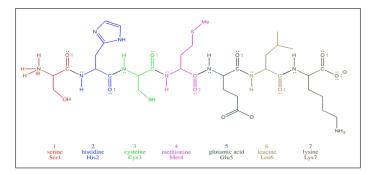


Figure 6: Amino acid chain

A protein is fundamentally a polymer—a long chain of amino acids linked together. In its unfolded state, this chain behaves like a typical polymer: flexible, disordered, and dynamic. As it folds, however, it transforms into a highly organized and functional structure. The folding process begins with the formation of local secondary structures, such as alpha helices and beta sheets, followed by the overall folding of the chain into a specific three-dimensional shape (tertiary structure). In some cases, multiple folded chains assemble into a larger complex, forming a quaternary structure. Despite this transformation, the polymer backbone remains; it's simply arranged in a compact and functional form.

Once folded, a protein may not resemble a simple polymer visually or functionally. Though still composed of repeating amino acid units, these units are now intricately arranged—spiraling into helices, flattening into sheets, and looping into turns that define the protein's function. It no longer appears as a linear chain, but it retains key polymer-like properties: flexibility, responsiveness, and dynamic movement in response to its environment.

This underlying polymer nature is why coarse-grained (CG) modeling remains effective, even for folded proteins. Rather than representing every atom, CG models group atoms into larger units or "beads," allowing us to study large-scale behaviors—such as folding,

conformational changes, or molecular interactions—without the computational cost of atomic detail. Because proteins are still polymers at their core, coarse-graining offers a powerful way to explore their structure and function at a broader scale.

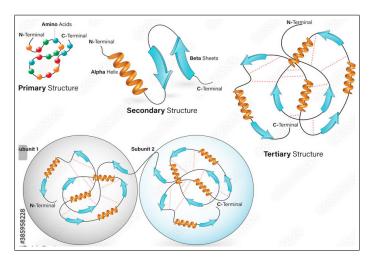


Figure 7: Protein

### C. Membrane/Phospholipids

In the 2000s, coarse-grained models found a natural fit in the study of lipid membranes, as researchers began adapting these techniques to simulate the complex behavior of biological membranes.

Phospholipids are the main ingredients of cell and viral membranes, and their structure is actually a lot like a simple polymer. The head is connected to the tails through a small backbone, so the whole molecule looks kind of like a matchstick or a two-tailed kite. Because one part of the molecule wants to be near water and the other part wants to avoid it, phospholipids naturally arrange themselves into layers when they're in water. These layers form flexible membranes that act a lot like soft polymer sheets—they can bend, move, and even stretch a little. In fact, scientists often use ideas from polymer physics to study how these membranes behave, especially when trying to understand things like how viruses wrap themselves up or how they enter cells.

Membranes share several important similarities with polymers that make them comparable in some ways. Both are soft, flexible materials capable of bending, stretching, and fluctuating, which reflects their shared physical nature as entropic, deformable systems. Like polymers, membranes are composed of repeating units—in this case, lipid molecules arranged in a bilayer

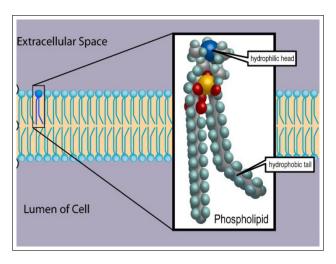


Figure 8: membrane subunit

rather than monomers linked in a chain—giving rise to a collective, cohesive structure.

Additionally, membranes exhibit entropic elasticity, meaning they resist stretching and bending because such deformations reduce the number of accessible configurations, similar to how polymers respond to mechanical forces.

Despite their similarities, membranes and polymers also exhibit significant differences. A key distinction lies in their dimensionality: a polymer is typically a long, 1-D chain of monomers, while a membrane is a 2-D sheet of molecules organized in a bilayer structure. This bilayer arrangement features a hydrophobic core formed by lipid tails, sandwiched between hydrophilic surfaces of lipid head groups, giving membranes a unique amphiphilic character essential for their stability and biological function. Moreover, membranes serve a fundamentally different purpose than polymers; while polymers can form single chains that fold into complex three-dimensional structures (such as proteins), membranes create continuous, self-sealing barriers that separate and compartmentalize cellular contents, supporting life's essential processes.

Given these differences, especially the two-dimensional fluid nature of membranes and their role in large-scale processes, a continuum model becomes especially valuable for studying membranes. A continuum model is not exactly an extension of a coarse-grained model, but rather a higher-level, more abstract description of the same system (See Figure 10). While coarse-grained models can still capture important molecular details, they often become computationally intensive or overly complex when studying large-scale, collective phenomena. In contrast, continuum models are particularly useful for exploring the large-scale, collective mechanical properties of

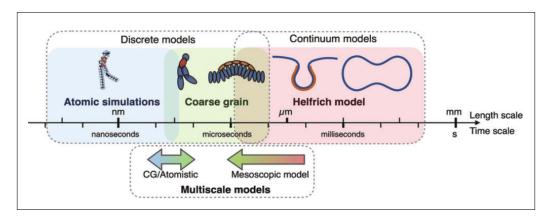


Figure 9: Different computational methods developed to study cellular membranes are valid in different length and time scales.[14]

membranes, including bending rigidity, surface tension, area compressibility, spontaneous curvature, Gaussian modulus, and, in some cases, shear elasticity. These properties describe how membranes deform, flow, and undergo shape transitions — all of which are critical for understanding their biological functions and large-scale dynamics.

### D. Genome/DNA/RNA

Since the mid-2000s, coarse-grained modeling has become a vital tool for understanding how our genomes are organized and function at a large scale. Instead of simulating every atom in a DNA molecule—a task impossible for chromosomes with millions or billions of base pairs—researchers began simplifying the problem in smart and effective ways.

DNA and RNA are long chains made up of smaller units called nucleotides. Each nucleotide is like a puzzle piece, made of a sugar, a phosphate group, and a nitrogen base. In DNA, the sugar is called deoxyribose, and in RNA, it's ribose. The bases are the parts that carry genetic information—A, T, G, and C in DNA, and A, U, G, and C in RNA (with U replacing T in RNA). These nucleotides link together through bonds between the phosphate of one and the sugar of the next, forming a backbone, kind of like beads on a string.

DNA and RNA are made of repeating nucleotides, similar to how polymers are made from repeating monomers. These long chains of nucleotides form biopolymers that can bend, twist, coil, and stretch like synthetic polymers such as plastic or rubber. This flexibility allows them to fold into diverse shapes and form complex secondary structures.

Even in their three-dimensional conformations, DNA and RNA retain key polymer-like

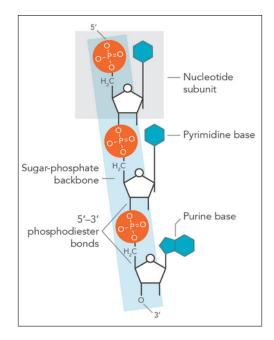


Figure 10: Nucletide subunits

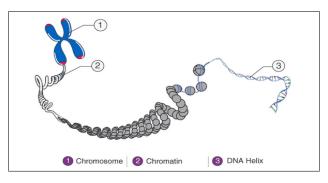


Figure 11: DNA, Chromatin and Chromosome[15]

behaviors. Like synthetic polymer chains, they adopt a wide range of configurations driven by thermal fluctuations, chain connectivity, and molecular flexibility. Their ability to bend, coil, loop, and supercoil in 3D can be effectively described using physical models such as the worm-like chain or bead-spring representations.

A widely used example is the "bead-on-a-string" model, where each bead represents a segment of DNA or a nucleosome. These coarse-grained models, grounded in polymer physics, allow researchers to simulate how DNA folds, forms loops, and compacts into the crowded space of the nucleus. Over the past decade, such models have significantly advanced our understanding of genome organization inside interphase nuclei [16].

Despite their biological complexity and sequence-specific interactions, DNA and RNA behave in ways consistent with polymer theory. Their structure and dynamics are influenced by

nucleotide sequence, chemical interactions, environmental conditions, and protein binding—factors that are essential for processes like gene regulation, genome packaging, and viral assembly. Because of these polymer-like properties, coarse-grained polymer models provide a powerful framework for studying and simulating the behavior of DNA and RNA.

In studies that explore how genome and membrane shapes influence each other, using different modeling approaches for each component is effective. A continuum model fits well for the membrane because it captures large-scale deformations, curvature, and bending behavior without needing to simulate individual lipid molecules. This is important for understanding how the membrane flexes or reshapes in response to internal forces. On the other hand, a coarse-grained model is well-suited for the genome, as it treats the long DNA or RNA strand as a chain of simplified units, preserving essential polymer behavior like folding, looping, and confinement. This balance—continuum for the membrane and coarse-grained for the genome—allows us to efficiently simulate the mechanical interaction between the flexible genome and the deformable membrane, revealing how their shapes affect each other in confined environments.

## Method

### 1.1 Coase-grain models

# Adveantage of Coase-grain model

Using a coarse-grain model in polymer science is really helpful because it makes things simpler and more efficient, especially when dealing with large and complex systems. One of the biggest reasons to use coarse-graining is that it saves a lot of computational power. Polymers are often made up of thousands or even millions of atoms, so simulating each individual atom takes a huge amount of time and resources. Instead of modeling each atom, a coarse-grain model groups several atoms or monomers into a "bead," which reduces the number of particles in the simulation. This allows researchers to study bigger systems and longer timescales without overwhelming their computers.

Another advantage is that coarse-graining allows us to focus on the big picture of polymer behavior. At the atomic level, polymers have tons of detailed interactions, but often what we care about are the overall properties, like how the polymer stretches, bends, or reacts to forces. Coarse-graining simplifies this by letting researchers study these larger-scale behaviors without getting caught up in the tiny atomic details, which are often less important for understanding real-world polymer behavior.

Coarse-grain models also make it easier to model interactions between polymers. Instead of focusing on each individual monomer, coarse-graining represents groups of monomers as beads.

This makes the interactions between polymer chains less complex and easier to study. This is really useful for studying complicated systems like polymer networks, gels, or blends, which would be too difficult to model atom by atom.

Another reason coarse-grain models are so valuable is that they help rus simulate larger systems over longer periods of time. By reducing the number of particles in the model, simulations can run much faster and allow for studies over longer timescales. Instead of simulating each tiny atom's movement, which can take a long time, coarse-graining lets researchers study the overall behavior of the polymer chain over much longer periods. This is really useful for looking at things like polymerization processes or phase transitions that occur over time.

Coarse-grain models also focuses on the important polymer properties that matter most, like flexibility, shape changes, and how polymers self-assemble. These properties are often determined by the overall structure of the polymer, not by the exact positions of every single atom. So by simplifying the model, researchers can study how polymers fold, how they form membranes, or how they interact with other molecules, without having to get into the atomic-level details.

Finally, coarse-grain models are essential for designing new materials. When researchers are developing new types of polymers—whether for drug delivery, biodegradable plastics, or high-performance materials, these models help predict how the polymer will behave in different environments. This helps researchers optimize the materials for real-world uses without needing to simulate every tiny detail. In the end, coarse-grain models are incredibly useful in polymer science because they simplify complex systems, making it easier to study their behavior. They save time and computational power while still allowing scientists to focus on the big picture—like how polymers stretch, bend, and interact—helping to design better materials and understand how polymers work in the real world.

#### 1.2 Monto Carlo simulation

Monte Carlo (MC) simulation is a technique used to explore different configurations of a system by randomly sampling possible states based on probability rules related to energy. Unlike molecular dynamics, which tracks every small movement over time, MC simulation decides whether to accept each move based on energy criteria.

This approach becomes especially powerful when combined with coarse-grained (CG) models, which simplify complex systems by grouping atoms or monomers into larger units. By reducing the number of particles and interactions, CG models significantly speed up computations, allowing MC techniques to efficiently explore a broader range of configurations. This combined method is particularly useful for studying large-scale behaviors such as polymer folding, self-assembly, phase transitions, and interactions with other structures. In coarse-grained polymer simulations, for example, MC methods can rotate or shift chain segments and evaluate how these changes affect the system's overall energy or structure.

Together, MC simulation and CG modeling provide an efficient and effective framework for investigating complex polymer systems—yielding insights that would be difficult to obtain using fully atomistic methods.

In applying Monte Carlo simulations to biological systems, it is essential to incorporate realistic physical constraints to ensure meaningful results. One of the most important constraints is excluded volume, which prevents particles from overlapping in space. This is especially critical in coarse-grained models where simplified representations of molecules must still obey fundamental physical principles. Without enforcing excluded volume, the configurations sampled during Monte Carlo steps could include unphysical overlaps, leading to inaccurate predictions of structural and thermodynamic properties. Therefore, integrating appropriate repulsive interactions into the simulation framework is key to capturing the true behavior of the system.

### Excluded volume

Excluded volume is an essential aspect of Coarse rained (CG) modeling, ensuring that two particles do not occupy the same space. Without it, particles in a simulation may overlap or penetrate each other, leading to unphysical results. To account for excluded volume, repulsive

interaction potentials—such as the Lennard-Jones potential or its softer variants used in models like MARTINI or DPD—are applied. These potentials create a repulsive force that prevents particles from getting too close. Key parameters like bead size  $(\sigma)$  and interaction strength  $(\varepsilon)$  must be carefully tuned to reflect the physical size and behavior of the particles.

Before running a simulation, energy minimization and equilibration steps are typically used to eliminate any initial overlaps and ensure a stable starting configuration. Properly enforcing excluded volume is particularly important in biomolecular and polymer systems, where structural integrity and thermodynamic behavior depend on particles keeping natural distances and not overlapping unrealistically. Ignoring or mishandling excluded volume can compromise the accuracy and reliability of the simulation.

In our study of the genome—membrane system, we use a coarse-grained model and continuum model to simplify the complex biological structures and apply Monte Carlo simulation to explore their behavior. This combination allows us to efficiently capture key physical properties while significantly reducing computational cost. Monte Carlo methods also aid in fitting the parameters of the coarse-grained model, making the approach well-suited for simulating large, complex systems such as polymers and membranes with reasonable accuracy.

### Procedure

#### A. Kremer-Grest Model for DNA chain

The Kremer-Grest (KG) model is a bead-spring type of coarse-grained model. KG model is specifically for polymers, including those relevant to chromosome structure and genome organization, and a popular way to simulate polymers in computer-based molecular dynamics. It is a specific, well-defined bead-spring model that includes Lennard-Jones (LJ) potential for excluded volume (non-bonded interactions) and FENE (Finitely Extensible Nonlinear Elastic) potential for the bonds between adjacent beads.

Instead of tracking every atom, it simplifies the system by representing each polymer chain as a string of connected beads. These beads interact with each other in two main ways: non-bonded beads repel each other using something called the Lennard-Jones (LJ) potential,

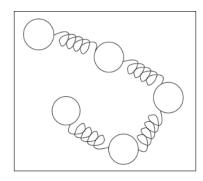


Figure 12: Bead-Spring Representation of a Polymer Chain (Kremer–Grest Model)

which helps prevent them from overlapping, and bonded beads (those directly connected in the chain) are held together by a FENE spring, which stretches like a real polymer bond but can't break or stretch too far. To keep the system at a steady temperature—like it would be in a real fluid—a Langevin thermostat is often used, adding both friction and random kicks to the beads. The model is simple, efficient, and captures the large-scale behavior of polymers really well, which is why it's used so widely in polymer research.

The Kremer-Grest model incorporates built-in excluded volume through the WCA potential, a modified form of the Lennard-Jones (LJ) potential that retains only the repulsive portion and removes the attractive part. This potential strongly repels beads when they come too close, preventing them from overlapping. This ensures that genome strands cannot pass through each other, similar to real physical strands that can bend and twist but cannot pass through themselves in crowded environments.

The FENE (Finitely Extensible Nonlinear Elastic) spring keeps beads connected but prevents them from stretching too far or breaking — making simulations stable even under tension or confinement.

Kresmer—grest Model is more physically realistic for polymers than a basic harmonic model and bead—spring model. It prevents bond crossing by FENE and WCA and it has been extensively validated and used in thousands of studies.

### Simulation setup of Monte Carlo Simulation for a Bead-Spring Genome

#### 1. System Initialization:

(1) Represent the genome as a chain of NN beads.

- (2) Each bead has a position  $\vec{r_i} = (x_i, y_i, z_i)$ .
- (3) Initialize positions with a non-overlapping random walk or a stretched chain.
- 2. Interaction Potential Two energy terms used in the Coarse grain simulation:
  - (1)Non-Bonded Interaction-WCA potential:

For all non-bonded pairs (i, j), with |i - j| > 1:

$$U_{\text{WCA}}(r) = \begin{cases} 4\varepsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^{6} \right] + \varepsilon, & \text{if } r \leq 2^{1/6}\sigma \\ 0, & \text{if } r > 2^{1/6}\sigma \end{cases}$$
 (1)

#### (2)Bonded Interaction-FENE:

For each bonded pair (i,i+1)(i,i+1):

$$U_{\text{FENE}}(r) = -\frac{1}{2}kR_0^2 \ln\left[1 - \left(\frac{r}{R_0}\right)^2\right] \tag{2}$$

| Parameter  | Meaning              | Typical Value (KG model) |
|------------|----------------------|--------------------------|
| k          | FENE spring constant | 30                       |
| $R_0$      | Max bond length      | 1.5                      |
| $\epsilon$ | WCA strength         | 1.0                      |
| σ          | Bead diameter        | 1.0                      |
| δ          | Move size            | ~0.1                     |

Table 1: Parameters for the KG model.

$$\Delta E = \Delta U_{\text{FENE}} + \Delta U_{\text{WCA}} \tag{3}$$

 $\Delta E$ : This is the change in energy of the system due to the proposed move, calculated as  $E_{\text{new}} - E_{\text{old}}$ , where  $E_{\text{new}}$  is the energy of the system after the proposed change, and  $E_{\text{old}}$  is the energy before the change.

- 3. Monte Carlo Move Algorithm:
  - (1) Choose a bead at random.
  - (2)Propose a small displacement:

$$\vec{r}_i' = \vec{r}_i + \Delta \vec{r}, \quad \Delta \vec{r} \in [-\delta, \delta]$$
 (4)

- (3) Compute energy change  $\Delta E$ :
  - (i) Recalculate FENE bonds for affected neighbors.
  - (ii) Recalculate WCA interactions for all non-bonded beads within cutoff.
- (4) Accept or reject using the Metropolis criterion:

$$P_{\text{accept}} = \min\left(1, e^{-\beta \Delta E}\right) \tag{5}$$

where  $\beta = \frac{1}{k_B T}$ .  $k_B$  is the Boltzmann constant and T is the temperature of the system.  $\beta$  essentially measures how sensitive the system is to energy changes at a given temperature.

This is a key expression in the Metropolis-Hastings algorithm, often used in Monte Carlo simulations, particularly in statistical physics and computational chemistry, to determine the acceptance probability of a proposed move in a system.

If  $\Delta E \leq 0$  (i.e., the new state has lower or equal energy), then  $e^{-\beta \Delta E} \geq 1$ . The min function sets P=1, meaning the move is always accepted. This makes sense because a lower-energy state is more favorable according to the Boltzmann distribution.

If  $\Delta E > 0$  (i.e., the new state has higher energy), then  $e^{-\beta \Delta E} < 1$ , and  $P = e^{-\beta \Delta E}$ . The move is accepted with a probability that decreases exponentially as the energy difference  $\Delta E$  increases or as the temperature T decreases (since  $\beta$  is inversely proportional to T). At low temperatures, the system is less likely to accept moves that increase energy, favoring lower-energy states.

# B. Simple liquid Models for the organelles surrounding DNA

Simple liquid models that help understand the structure and behavior of polymer in crowded environments. Specifically, the simple liquid models referenced include Hard Sphere Model and Lennard-Jones Model.

Hard sphere model is used to understand the behavior of particles in crowded environments, where the excluded volume effect becomes important.

The Lennard-Jones model accounts for both attractive and repulsive forces between particles, which is important in understanding the interactions within fluids and condensed

matter. It helps model the behavior of molecules, especially in non-ideal conditions like those found in crowded environments.

### Simulation Setup of Monte Carlo for DNA and Crowders

1. Define DNA Model

Use bead-spring polymer (FENE bonds + WCA excluded volume).

2. Define Surrounding Particles (Crowders)

Add many free-floating particles around the DNA.

Interact using: WCA potential (for excluded volume) or or LJ potential

3. Interaction Potentials:

DNA-DNA: FENE (bonded) + WCA (nonbonded)

DNA-Crowder: WCA or LJ

Crowder-Crowder: WCA or LJ

- 4. Monte Carlo Simulation Steps:
  - (1)Initialize:
    - (i)Randomly place the DNA chain in the simulation box.
    - (ii)Random positions for crowding particles (no overlaps).
    - (2)Monte Carlo Loop:
      - (i)Propose random displacements for DNA beads and crowder particles.
      - (ii) For a large number of steps (e.g.,  $10^5\ {\rm or\ more}),$
      - (iii)Compute total energy:

Pick one particle (DNA bead or crowder).

Propose a small random displacement:

$$\mathbf{R}_{\text{new}} = \mathbf{R}_{\text{old}} + \delta \tag{6}$$

where  $\delta$  is random (small)

$$E = \sum_{\text{bonds}} U_{\text{FENE}} + \sum_{\text{nonbonded}} U_{\text{WCA}} + \sum_{\text{DNA-crowder}} U_{\text{WCA/LJ}} + \sum_{\text{crowder-crowder}} U_{\text{WCA/LJ}}$$
 (7)

| Parameter          | Suggested Value                    |
|--------------------|------------------------------------|
| $\sigma$           | Size of bead (DNA + crowder)       |
| $\varepsilon$      | LJ/WCA strength (e.g., 1.0)        |
| $k, R_0$           | FENE bond strength, limit          |
| Number of crowders | Depends on desired volume fraction |

Table 2: Simulation parameters for the DNA-crowder system.

(iv)Calculate energy difference:

$$\Delta E = E_{\text{new}} - E_{\text{old}} \tag{8}$$

(v)Accept or reject moves using Metropolis criterion:

$$P_{\text{accept}} = \min\left(1, e^{-\beta \Delta E}\right) \tag{9}$$

Repeat for many steps to allow the system to reach to a low-energy state with no overlaps or unphysical configurations.

#### 5. Sampling:

Collect statistics on DNA configurations, radius of gyration, looping, crowding effects.

#### C. Helfrich-Canham Model for the membrane

Membranes can be modeled at the coarse-grained level but we don't need to explicitly use a coarse-grained model. Instead, we directly use continuum models like the Helfrich-Canham model (See Figure 5). We can focus on big-scale behavior and treat the membrane as a smooth, continuous surface with properties like bending rigidity, spontaneous curvature, and surface tension. Coarse-grained models require tracking many particles, but continuum models replace them with smooth fields, making them more efficient for studying large-scale deformation

The Helfrich-Canham model, a specific type of continuum model, focuses on the membrane's curvature elasticity and bending energy[17].

Continuum models are a powerful framework used to describe and simulate the large-scale, smooth behavior of biological membranes (and other materials) without tracking individual atoms or molecules. Instead of focusing on discrete particles like in molecular dynamics, continuum

models treat the membrane as a continuous surface or material with defined physical properties.

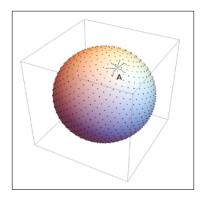


Figure 13: Sort all the vertices and make a network and identify the neighbors of A and link all the neighbors to A by Hookean spring. Introduce bending energy and curvature to vertice A. Choose spring constant and bending energy and (may be) curvature at point A so this point will maintain concave. Meanwhile it can induce shape changes for the membrane

Helfrich bending energy(The simplest form)

$$F_{\text{Helfrich}} = \int \frac{\kappa}{2} \left(2H - C_0(\vec{r})\right)^2 dA \tag{10}$$

This is the classical Helfrich–Canham model capturing bending energy. Good for studying large-scale shape changes without worrying about connectivity changes or constraints.

H is the mean curvature

 $C_0(\vec{r})$  is the spatially varying spontaneous curvature

dA is the surface element

The Helfrich–Canham model, a specific type of continuum models, focuses mainly on bending energy and curvature-driven deformations, It describes the total energy of a membrane by combining two main contributions: bending energy and surface tension energy. The bending energy reflects how much the membrane curves away from its preferred, or spontaneous, shape. Meanwhile, the surface tension energy accounts for the cost of stretching the membrane — it increases when the membrane's surface area grows. Together, these terms help explain how membranes bend, stretch, and maintain their shape in different environments.

The Helfrich–Canham model doesn't capture the details of lipid composition or molecular shape, local lipid phase transitions, specific molecular interactions, or fluctuations below the coarse-grained scale, such as nanometer-scale undulations, but it does capture large-scale bending deformations, the effects of spontaneous curvature, membrane elastic properties, shape transitions of vesicles and cells, and the response to pressure, tension, and curvature.

The total free energy of a closed lipid bilayer:

Continuum Form (Analytical Model):

$$F_{\text{full mem}} = \int_{S} \left[ \underbrace{\frac{\kappa}{2} (2H - C_{0}(\vec{r}))^{2}}_{\text{(1) spontaneous-curvature-modified bending}} + \underbrace{\kappa K}_{\text{(2) Gaussian-curvature term}} \right] dA$$

$$+ \underbrace{\lambda A}_{\text{(3) area constraint}} + \underbrace{pV}_{\text{(4) volume constraint}}. \tag{11}$$

This is a more complete energy functional for membranes. The membrane is treated as a smooth surface S.

 $\kappa$ : bending rigidity

 $\bar{\kappa}$ : Gaussian modulus

 $H: \text{ mean curvature} = \frac{1}{2}(c_1 + c_2)$ 

 $c_1, c_2$ : principal curvatures at a point on the surface

K: Gaussian curvature =  $c_1 * c_2$ 

 $C_0$ : spontaneous curvature

A: total surface area

 $\lambda$ : Lagrange multiplier for area constraint (surface tension)

P: Lagrange multiplier for volume constraint (pressure)

V: Enclosed volume

dA: Area element on the surface

 $(2H - C_0)^2$ : A spontaneous-curvature term for local bending preferences.

 $\bar{\kappa}K$ : A Gaussian-curvature term for energy changes.

Because analytical form includes these extra factors, the full (analyzed) form describes real membranes far more accurate you'd need to estimate the mean curvature H or Gaussian curvature K at many points across the entire mesh. Even a small change in one vertex forces you to recompute normals, gradients, and curvature over dozens—or hundreds—of triangles, and then

recalculate global area or volume constraints. In other words, a single vertex move would turn into a big, expensive calculation of geometry everywhere. That's why the angle-based form, which limits its work to just the edges touching the moved vertex, is far simpler and faster to use inside each Monte Carlo step.

It models the elastic energy of a smooth, flexible surface (like a lipid bilayer vesicle) as a function of curvature. This model alone does not specify how lipids or proteins are distributed on the surface — it just tells you what shapes minimize bending energy.

For a Monte Carlo study of a polymer confined inside a flexible membrane, the angle-based (discrete) form is the most practical choice. The Discrete Bending Energy (Angle-based Form):

$$E_{\text{bend}} = \kappa \sum_{\langle i,j \rangle} (1 - \cos \theta_{ij}) \tag{12}$$

is a widely used discrete approximation in simulations of triangulated membranes. While it is not directly derived from the Helfrich energy in a specific textbook, it appears in several foundational papers and review articles on triangulated surface models and coarse-grained simulations[18].

 $\kappa$  is the bending rigidity,

 $\theta_{ij}$  is the angle between adjacent triangles sharing edge  $\langle i, j \rangle$ .

We can distinguish between spherical and oval (ellipsoidal) shapes using the discrete form of the Helfrich energy Discrete model is widely used in simulations (including Monte Carlo and molecular dynamics) precisely because they can capture subtle shape changes, such as the transition from a sphere to an oval.

This is a discretized approximation of the bending energy, suitable for numerical simulations Monte Carlo or molecular dynamics. It captures curvature using local triangle normals instead of differential geometry.

$$E_{\text{area}} = \lambda (A - A_0)^2 \tag{13}$$

 $E_{\text{area}}$  is the area energy

 $\lambda$  is a parameter/coefficient

A is the current area

 $A_0$  is the reference/target area.

Volume constraint:

$$E_{\text{Volume}} = \lambda (V - V_0)^2 \tag{14}$$

 $E_{\text{Volume}}$  is the volume energy

 $\lambda$  is a parameter/coefficient that controls the strength of the volume constraint

V is the current volume

 $V_0$  is the reference/target volume

$$\Delta E = (E_{\text{membrane}}^{\text{new}} + E_{\text{polymer}}^{\text{new}}) - (E_{\text{membrane}}^{\text{old}} + E_{\text{polymer}}^{\text{old}})$$
(15)

Metropolis rule:

$$P = \min\left(1, e^{-\beta \Delta E}\right) \tag{16}$$

This is a key expression in the Metropolis-Hastings algorithm, often used in Monte Carlo simulations, particularly in statistical physics and computational chemistry, to determine the acceptance probability of a proposed move in a system.

P: The probability of accepting a proposed change in the system's configuration. In Monte Carlo simulations, we randomly propose changes to the system (e.g., moving a particle) and decide whether to accept or reject them based on this probability. If move is accepted then positions will be updated. If rejected then the move will be reverted.

 $e^{-\beta\Delta E}$ : It is derived from the Boltzmann distribution, which describes the probability of a system being in a particular state based on its energy.

 $\beta$ : This is defined as  $\beta = \frac{1}{k_B T}$ , where  $k_B$  is the Boltzmann constant and T is the temperature of the system.  $\beta$  essentially measures how sensitive the system is to energy changes at a given temperature.

 $\Delta E$ : This is the change in energy of the system due to the proposed move, calculated as  $E_{\text{new}} - E_{\text{old}}$ , where  $E_{\text{new}}$  is the energy of the system after the proposed change, and  $E_{\text{old}}$  is the

energy before the change.

If  $\Delta E \leq 0$  (i.e., the new state has lower or equal energy), then  $e^{-\beta \Delta E} \geq 1$ . The min function sets P = 1, meaning the move is always accepted. This makes sense because a lower-energy state is more favorable according to the Boltzmann distribution.

### Hypothesis

#### Hypothesis 1:

The shape of a virus forms after its genome architecture stabilizes. First, the genome reaches a steady state, and we then examine how it influences the viral membrane shape.

Goal:

- (1) If the genome is 1D rod-like, the viral membrane takes an 2D elliptical shape.
- (2) If the genome is circular, the viral membrane forms a 2D circular shape.

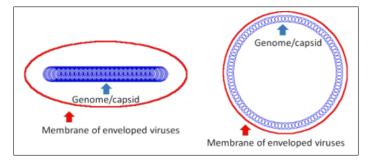


Figure 14: Preliminary 2D model studies to investigate the effect of the geometry of a genome on the shape of a virus. A rod-like genome induces an elliptic shape whereas a circular genome leads to a circular shape.

#### Hyperthesis 2:

The genome architecture may develop after the viral membrane shape stabilizes. In this case, the membrane reaches a steady state first, and we then observe how it affects the genome's geometry. By adjusting the length of 1D rod or the perimeter of the circle of the genome, we try to match the reference.[6]

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1\tag{17}$$

Goal:

(1) If the viral membrane takes an elliptical shape ( $a \neq b$ ), the genome geometry is

rod-like[19].

$$E_{\text{ellipse}} = \int_0^{2\pi} \frac{\kappa}{2} \left( C(\theta) - C_0 \right)^2 \cdot ds(\theta)$$
 (18)

(2) If the viral membrane forms a circular shape (a = b), the genome geometry is circular.

$$E_{\text{circle}} = \int_0^{2\pi R} \frac{\kappa}{2} \left(\frac{1}{R} - C_0\right)^2 ds = \kappa \pi R \left(\frac{1}{R} - C_0\right)^2$$
(19)

Comparing both shapes to a preferred curvature, such as the curvature of a circle of radius 4, we have  $C_0 = \frac{1}{4} = 0.25$ .

The shape of viral particles—such as those seen in the Monkeypox virus—can reveal important details about their developmental stage. Immature virions typically appear spherical, a form that facilitates the early assembly of genetic material and proteins in a flexible, efficient manner. As the virus matures, it undergoes structural rearrangements that reshape it into an oval form. This morphological transition enhances the particle's stability and improves its ability to interact with host cell receptors, thereby increasing infectivity and replication efficiency.

To investigate the mechanisms behind these shape transitions, we use computational simulations to model the coupled behavior of the viral genome and membrane. By systematically varying parameters such as membrane elasticity, area and volume constraints, and genome length or stiffness, we can explore how physical factors drive morphological changes during maturation. These simulations reveal how membrane shape influences genome configuration, highlighting the mechanical interplay between structural components. This approach not only deepens our understanding of viral assembly and stability but also informs experimental design and the development of targeted antiviral strategies.

#### Hypothesis 3:

The shape of a virus and its genome architecture form simultaneously. The model for this hypothesis allows both genome morphology and membrane shape to undergo simultaneous fluctuation until both arrive at a mutual steady state.

#### Hypothesis 4:

The internal pressure P generated during viral genome packaging is governed by the thermal

energy  $k_BT$ , the DNA persistence length  $\xi$ , and the radial distribution of DNA loops N(r). Modulating the structural or mechanical properties of the packaged genome—such as altering its stiffness  $(\xi)$  or spatial distribution (N(r))—can significantly influence the magnitude of this internal pressure. Therefore, by controlling these parameters, it is possible to reduce the pressure required for genome ejection and thereby affect the virus's ability to infect host cells.

The prior studies that define the packaging energy based on the DNA length inside the capsid, the capsid as a sphere and the genome as an extended semiflexible rod[20]. We depict the membrane as a sphere and RNA as an extended semiflexible rod. The pressure of the packaged RNA in confined membrane is then estimated as RNA bending energy devided by volume of membrane:

$$P = \frac{\sqrt{3k_B T \xi^2}}{R^3} \int_{R_{\rm in}}^{R_{\rm out}} \frac{N(r)}{r} dr$$
 (20)

Boltzmann's constant is denoted by  $k_B$ ; at 37 °C, the Boltzmann factor  $k_BT$  is approximately equal to  $4.28\,\mathrm{pN}\cdot\mathrm{nm}$ .

R is the radius of capsid/membrane

 $\xi$  is the persistence length of DNA

N(r) is the number of loops of DNA at a distance r from the spool axis

r is the radial distance from the central axis of the spool. The spool axis is the straight line going through the center.r measures how far a particular loop of DNA is from this central axis.

### Goal 1. Quantify the Relationship Between Genome Structure and Internal Pressure

To determine how variations in RNA persistence length  $\xi$  and the radial loop distribution N(r) affect the internal pressure P generated during genome packaging, as described by the pressure equation.

$$P = \frac{\sqrt{3}k_B T \, \xi^2}{R^3} \int_{R_{\rm in}}^{R_{\rm out}} \frac{N(r)}{r} \, dr$$

We begin by modeling RNA as a fine-grained polymer, such as a worm-like chain, which accurately represents the stiffness and bending behavior of RNA. This model is placed within a confined volume that mimics the  $60 \, \text{nm} \times 150 \, \text{nm}$  membrane[20].

Next, we insert small segments of RNA into the membrane step by step and calculate the

energy needed to overcome internal forces such as bending stress. This process allows us to track the buildup of internal pressure during packaging.

Once the genome is fully packaged, we simulate ejection dynamics by triggering a release mechanism, such as opening a virtual portal in the membrane. The RNA is then allowed to eject, and we record the ejection speed, force, and time as the internal pressure drives the genome out.

Simulating realistic physical conditions, since many experiments happen at constant pressure (example: 1 atm) and temperature (example: 298 K).

#### Goal 2. NPT Ensemble (Isothermal–Isobaric Ensemble)

NPT stands for:

N = Number of beads (constant)

P = Pressure (constant)

T = Temperature (constant)

Under NPT conditions, the system's pressure is controlled, allowing the volume to change naturally over time. In one approach, the membrane is initialized with a fixed oval or ellipsoidal shape, defined by the input parameters a, b, and c, which represent the lengths along its three principal axes. These parameters remain constant during the simulation, so the membrane maintains its overall shape while still allowing local fluctuations and interactions with the genome inside.

In another approach, the parameters a, b, and c are allowed to fluctuate during the simulation. This means the membrane can expand, shrink, or reshape dynamically in response to internal forces exerted by the genome. Such flexibility promotes more realistic interactions between the genome and the membrane — for example, the genome may push outward and deform the membrane, while changes in membrane tension or curvature can influence how the genome is organized. Using NPT conditions in this way provides a natural and dynamic view of the interplay between membranes and genomes in biological systems.

#### Goal 3. NVT Ensemble (Canonical Ensemble)

NVT stands for:

N = Number of beads (constant)

V = Volume (constant)

T = Temperature (constant)

Under NVT conditions, the volume of the system is fixed, meaning the membrane is constrained and cannot expand or contract. In one approach, the membrane is initialized with an oval or ellipsoidal shape, defined by input parameters a, b, and c, representing the lengths along its three principal axes. These parameters remain constant throughout the simulation, so the membrane keeps its shape even as the genome inside moves or grows. Because the membrane cannot adapt naturally to changes, any pressure exerted by the genome builds up inside, sometimes leading to artificial forces that would not normally appear in a flexible system.

In another approach, even though the overall volume remains fixed under NVT, small local fluctuations in the shape of the membrane are allowed while still keeping a, b, and c centered around their initial values. In this case, the membrane can slightly deform in response to internal forces from the genome without changing its total volume. While the confinement effect is still strong, allowing limited local fluctuations provides a somewhat more realistic interaction between the genome and the membrane. Studying the membrane—genome relationship in either method under NVT is useful for early-stage stabilization or when specifically exploring how genomes behave in confined, rigid environments.

#### **Timeline**

Months 0-3: Fine-tune the continuum membrane model.

Months 4-6: Investigate competition among different membrane shapes.

Months 7-9: Study chain model and crowding effect

Months 10-12:Expand the developed models from 2D to 3D.

### Extra

The prior studies that define the packaging energy based on the DNA length inside the capsid. We depict the membrane as a sphere and the genome as an extended semiflexible rod. The total energy of the packaged DNA is then estimated as the sum of interaxial repulsion energy and DNA bending energy. [20]:

$$E_{\text{Packaged DNA}} = E_{\text{interaction}} + E_{\text{bend}} = \sqrt{3}F_0L(c^2 + cd_s)\exp(-d_s/c) + \frac{2\pi k_B T \xi^2}{\sqrt{3} \cdot d_s} \int_{R_{\text{in}}}^{R_{\text{out}}} \frac{N(r)}{r} dr \quad (21)$$

We depict the membrane as a sphere and the genome RNA as an extended semiflexible rod. The total energy of the packaged RNA is RNA bending energy.

$$E_{\text{Packaged RNA}} = E_{\text{bend}} = \frac{2\pi k_B T \xi^2}{\sqrt{3} \cdot d_s} \int_{R_{\text{in}}}^{R_{\text{out}}} \frac{N(r)}{r} dr$$
 (22)

$$P = \frac{\sqrt{3k_B T \xi^2}}{r^3} \int_{R_{\rm in}}^{R_{\rm out}} \frac{N(r)}{r} dr \tag{23}$$

### References

- [1] Zhenhao Ke, Jose Oton, Kun Qu, Marcella Cortese, Vedran Zila, Liam McKeane, Takanori Nakane, Jasenko Zivanov, Christopher J Neufeldt, Bastian Cerikan, Jianmin M Lu, Julian Peukes, Xiaoli Xiong, Hans-Georg Kräusslich, Sjors H. W. Scheres, Ralf Bartenschlager, and John A. G. Briggs. Structures and distributions of sars-cov-2 spike proteins on intact virions. *Nature*, 588(7838):498–502, December 2020. Epub 2020 Aug 17.
- [2] Centers for Disease Control and Prevention (CDC). Sars-cov-2 illustration. https://www.cdc.gov/museum/timeline/covid19.html, n.d. Accessed April 18, 2025.
- [3] Naoki Nakatani, Hiroshi Sakuta, Makoto Hayashi, Shunsuke Tanaka, Kohei Takiguchi, Kouhei Tsumoto, and Kenichi Yoshikawa. Specific spatial localization of actin and dna in a water/water microdroplet: Self-emergence of a cell-like structure. *Chembiochem*, 19(13):1370–1374, 2018.
- [4] Nir Erez, Hagit Achdout, Einat Milrot, Yaron Schwartz, Yonit Wiener-Well, Nir Paran, Boaz Politi, Haim Tamir, Tomer Israely, Sharon Weiss, Adi Beth-Din, Orli Shifman, Ohad Israeli, Shmuel Yitzhaki, Shaul C Shapira, Shay Melamed, and Eli Schwartz. Diagnosis of imported monkeypox, israel, 2018. Emerging Infectious Diseases, 25(5):980–983, May 2019.
- [5] Shane Parker, Andrea Nuara, R Mark Buller, and David A Schultz. Human monkeypox: an emerging zoonotic disease. *Future Microbiology*, 2(1):17–34, Feb 2007.
- [6] Cynthia S Goldsmith and Russell Regnery. Monkeypox virus particle. Public Health Image Library, Centers for Disease Control and Prevention, 2003. Image ID: 22664.
- [7] Yinon M Bar-On, Avi Flamholz, Rob Phillips, and Ron Milo. Sars-cov-2 (covid-19) by the numbers. *Elife*, 9:e57309, Apr 2020.
- [8] Lei Wu, Wenhui Zhou, Lihua Lin, Anhong Chen, Jing Feng, Xiangmeng Qu, Hongbo Zhang, and Jun Yue. Delivery of therapeutic oligonucleotides in nanoscale. *Bioactive Materials*, 7:292– 323, 2022.

- [9] Emily Barrow, Anthony V. Nicola, and Jun Liu. Multiscale perspectives of virus entry via endocytosis. *Virology Journal*, 10:177, 2013.
- [10] Susan Payne. Viruses: From Understanding to Investigation. Elsevier, 2nd edition, 2022.
- [11] A. Brandariz-Nuñez, T. Liu, T. Du, and A. Evilevitch. Pressure-driven release of viral genome into a host nucleus is a mechanism leading to herpes infection. *eLife*, 8:e47212, 2019.
- [12] Kurt Kremer and Gary S. Grest. Dynamics of entangled linear polymer melts: A molecular-dynamics simulation. *The Journal of Chemical Physics*, 92(8):5057–5086, 1990.
- [13] Ralf Everaers, Ali Karimi, Frank Fleck, Nils Hojdis, and Carsten Svaneborg. Kremer–grest models for commodity polymer melts: Linking theory, experiment, and simulation at the kuhn scale. *Macromolecules*, 53, 2020.
- [14] Morgan Chabanon, Jeanne C. Stachowiak, and Padmini Rangamani. Systems biology of cellular membranes: a convergence with biophysics. Wiley Interdisciplinary Reviews: Systems Biology and Medicine, 9(5), sep 2017. Epub 2017 May 5.
- [15] BYJU'S. Chromatin. https://byjus.com/biology/chromatin/, n.d. Accessed: 2025-05-14.
- [16] Ludvig Lizana and Yuri B. Schwartz. The scales, mechanisms, and dynamics of the genome architecture. *Science Advances*, 10(15):eadm8167, April 2024. Epub 2024 Apr 10.
- [17] Patricia Bassereau, Benjamin Sorre, and Anne Lévy. Bending lipid membranes: Experiments after w. helfrich's model. Advances in Colloid and Interface Science, 208:47–57, June 2014. Epub 2014 Feb 11.
- [18] Gerhard Gompper and D M Kroll. Triangulated-surface models of fluctuating membranes.

  Journal of Physics: Condensed Matter, 9(42):8795–8834, 1997.
- [19] S. Harish, M. Murugan, M. Kannan, S. Parthasarathy, S.R. Prabhukarthikeyan, and K. Elango. Entomopathogenic viruses. In *Microbial Approaches for Insect Pest Management*, pages 1–57. Springer, 2021.

[20] Paul Grayson, Alex Evilevitch, Mandar M. Inamdar, Prashant K. Purohit, William M. Gelbart, Charles M. Knobler, and Rob Phillips. The effect of genome length on ejection forces in bacteriophage lambda. Virology, 348(2):430–436, 2006.