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**Topic:** Simulation and Comparison of Various Attacks on the RSA Cryptosystem

**Attacks** (From Research\*):

- **Message space search**
  - The encryption algorithm must be communicated to each party, hidden within the message space.
  - Encrypt the message blocks with each other until plaintext is the result.
  - Takes a long time, very inefficient
- **Guessing  $d$  (the private exponent)**
  - Requires the attacker knows both a corresponding plaintext and ciphertext pair.
    - Attackers can “guess”  $d$  over and over until encrypting the plaintext results in the ciphertext.
  - Once  $d$  is found, the attacker has full access to all future communications.
- **Cycle attack, aka iteration attack**
  - If the attacker repeats the encryption process enough times on the ciphertext, the result will eventually be the decrypted text (plaintext message)
  - Not an ideal attack due to variations in the amount of encryption iterations needed to decrypt the text. If the message space is large, this can take a long time.
  - Number of iterations should be saved so the attacker knows how many cycles to encrypt for future messages.
- **Common modulus**
  - A common modulus is sometimes used for employees/people within a business/organization. This makes things more convenient for administrators, however, it has security implementations. Attackers are able to mock employees' private keys from their public keys by factoring the modulus  $N$ .
- **Low private exponent**
  - **Private:** a small private exponent can cut back on performance time tremendously, but the system can be broken using Wiener's law.
    - Weiners law decreases the amount of exponents possible for the cryptosystem. Therefore, the attacker can search through the exponents faster, and break the system easier.
- **Factoring the public key**
  - **\*\*Very effective attack on RSA**
  - RSA relies on integer factorization for generation of public keys
  - If the attacker can find the prime factors used in the RSA process, they can compute the exponent  $d$  from any party's public key
  - With the public key and exponent, they can decrypt the ciphertext.

- **Blinding**
  - Uses a party's digital signature from one message to sign another message that the party did not consent to.
- **Partial Key Exposure attack**
  - The attacker has part of the private key available to them
  - Since the attacker has part of  $d$ , they are able to determine the full value of  $d$  faster using bit operations
    - Better to have the part of  $d$  containing the least significant bits.
- **Timing Attacks**
  - Ex: RSA smartcard that stores private key
  - By measuring the time the card takes to perform the decryption/encryption, an attacker is able to determine the exponent  $d$ .
- **Random Faults**
  - Some RSA Algorithms use the Chinese Remainder theorem
  - If an error occurs during the encryption/decryption process, the chinese remainder theorem can result in false signatures.

#### Goals:

- Narrow down to two or three of the above attacks and implement them.
  - **Currently focusing on:** Factoring the public key, blinding, partial key exposure attack
- Compare the difficulty of the implementation, reality of execution, etc
- Discuss the ethical implementations of using RSA and attacking RSA.

#### Research:

- Possible attacks on RSA: [http://www.members.tripod.com/irish\\_ronan/rsa/attacks.html](http://www.members.tripod.com/irish_ronan/rsa/attacks.html)
- [https://math.boisestate.edu/~liljanab/ISAS/course\\_materials/AttacksRSA.pdf](https://math.boisestate.edu/~liljanab/ISAS/course_materials/AttacksRSA.pdf)
- 20 Years of Attacks on RSA: <https://crypto.stanford.edu/~dabo/papers/RSA-survey.pdf>
- Active vs Passive Attacks: <https://www.geeksforgeeks.org/active-and-passive-attacks-in-information-security/>
- Cryptographic attacks: [https://en.wikipedia.org/wiki/Category:Cryptographic\\_attacks](https://en.wikipedia.org/wiki/Category:Cryptographic_attacks)
- [https://en.wikipedia.org/wiki/RSA\\_\(cryptosystem\)#Integer\\_factorization\\_and\\_RSA\\_problem](https://en.wikipedia.org/wiki/RSA_(cryptosystem)#Integer_factorization_and_RSA_problem)

#### Back up plan:

- OTP: Attacks on Stream Ciphers and the One time pad: <https://www.coursera.org/lecture/crypto/attacks-on-stream-ciphers-and-the-one-time-pad-euFJx>