Module04HW

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# Assignment: Stat 6021: Homework Set 4

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## Question 1: Use the dataset swiss which is part of the datasets package.

Load the data. For more information about the data set, type ?swiss.

The goal of the data set was to assess how fertility rates in the Swiss (French-speaking) provinces relate to a number of demographic variables.

# load the data  
?swiss

## starting httpd help server ... done

attach(swiss)

**About Swiss**

Standardized fertility measure and socio-economic indicators for each of 47 French-speaking provinces of Switzerland at about 1888.

A data frame with 47 observations on 6 variables, each of which is in percent, i.e., in [0, 100].

[,1] Fertility Ig, ‘common standardized fertility measure’

[,2] Agriculture % of males involved in agriculture as occupation

[,3] Examination % draftees receiving highest mark on army examination

[,4] Education % education beyond primary school for draftees.

[,5] Catholic % ‘catholic’ (as opposed to ‘protestant’).

[,6] Infant.Mortality live births who live less than 1 year.

head(swiss)

## Fertility Agriculture Examination Education Catholic  
## Courtelary 80.2 17.0 15 12 9.96  
## Delemont 83.1 45.1 6 9 84.84  
## Franches-Mnt 92.5 39.7 5 5 93.40  
## Moutier 85.8 36.5 12 7 33.77  
## Neuveville 76.9 43.5 17 15 5.16  
## Porrentruy 76.1 35.3 9 7 90.57  
## Infant.Mortality  
## Courtelary 22.2  
## Delemont 22.2  
## Franches-Mnt 20.2  
## Moutier 20.3  
## Neuveville 20.6  
## Porrentruy 26.6

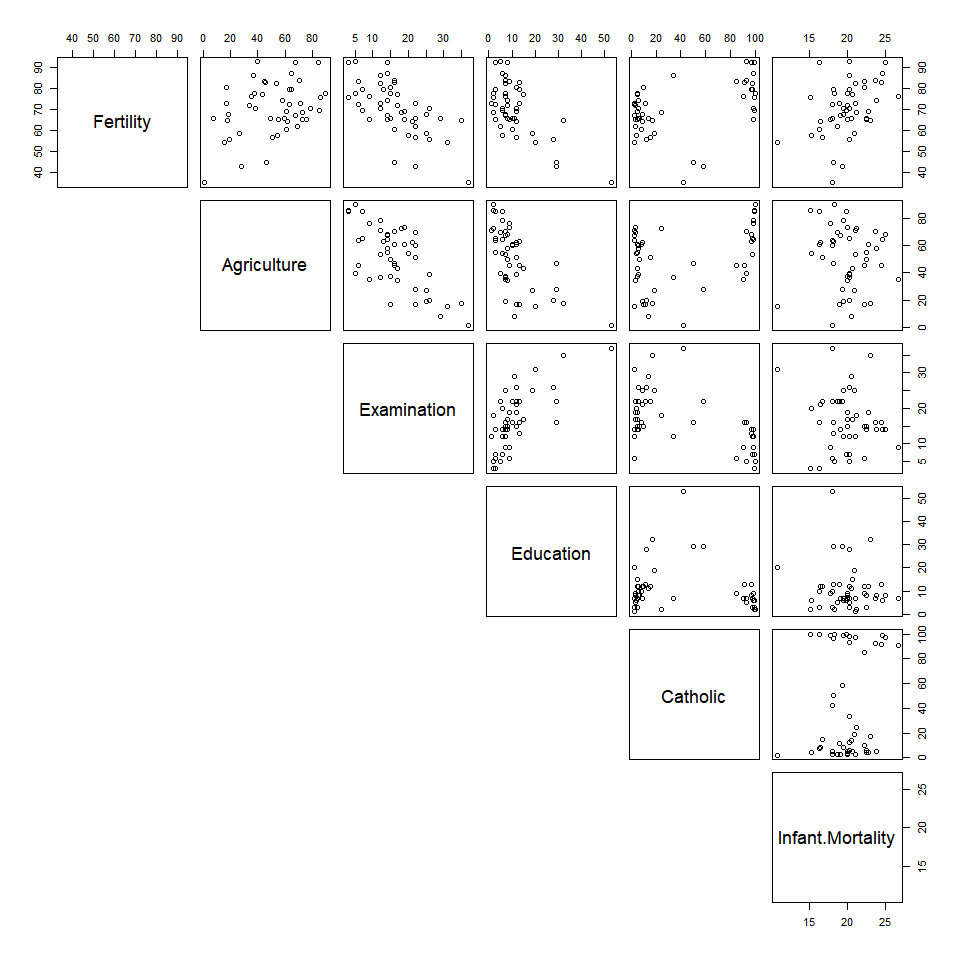
summary(swiss)

## Fertility Agriculture Examination Education   
## Min. :35.00 Min. : 1.20 Min. : 3.00 Min. : 1.00   
## 1st Qu.:64.70 1st Qu.:35.90 1st Qu.:12.00 1st Qu.: 6.00   
## Median :70.40 Median :54.10 Median :16.00 Median : 8.00   
## Mean :70.14 Mean :50.66 Mean :16.49 Mean :10.98   
## 3rd Qu.:78.45 3rd Qu.:67.65 3rd Qu.:22.00 3rd Qu.:12.00   
## Max. :92.50 Max. :89.70 Max. :37.00 Max. :53.00   
## Catholic Infant.Mortality  
## Min. : 2.150 Min. :10.80   
## 1st Qu.: 5.195 1st Qu.:18.15   
## Median : 15.140 Median :20.00   
## Mean : 41.144 Mean :19.94   
## 3rd Qu.: 93.125 3rd Qu.:21.70   
## Max. :100.000 Max. :26.60

### (a) Create a scatterplot matrix

and find the correlation between all pairs of variables for this data set.

pairs(swiss,lower.panel = NULL)

 **Answer the following questions based on the output:**

**i. Which predictors appear to be linearly related to the fertility measure?**

Answer: Fertility appears to be linearly related to: Agriculture (+), Examination (-), Education (-), but with an outlier/influencer at the extreme+ end of Education.

Catholic has two or three distinct clusters and a constant variance issue.

Infant.Mortality appears linearly correlated but with a constant variance issue, the plot is cone shaped with decreasing variance.

**ii. Do you notice if any of the predictors are highly correlated with one another?** If so, which ones?

Answer:

* agriculture appears corrleated with examination(-) and education(-)
* examination appears correlated with education (+)

### (b) Fit a multiple linear regression

with the fertiliy measure as the response variable and all the other variables as predictors.

swissModel <-lm(Fertility ~ Agriculture + Examination + Education + Catholic + Infant.Mortality)  
  
swissModel

##   
## Call:  
## lm(formula = Fertility ~ Agriculture + Examination + Education +   
## Catholic + Infant.Mortality)  
##   
## Coefficients:  
## (Intercept) Agriculture Examination Education   
## 66.9152 -0.1721 -0.2580 -0.8709   
## Catholic Infant.Mortality   
## 0.1041 1.0770

Use the summary() function to obtain the estimated coefficients and results from the various hypothesis tests for this model.

summary(swissModel)

##   
## Call:  
## lm(formula = Fertility ~ Agriculture + Examination + Education +   
## Catholic + Infant.Mortality)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -15.2743 -5.2617 0.5032 4.1198 15.3213   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) 66.91518 10.70604 6.250 1.91e-07 \*\*\*  
## Agriculture -0.17211 0.07030 -2.448 0.01873 \*   
## Examination -0.25801 0.25388 -1.016 0.31546   
## Education -0.87094 0.18303 -4.758 2.43e-05 \*\*\*  
## Catholic 0.10412 0.03526 2.953 0.00519 \*\*   
## Infant.Mortality 1.07705 0.38172 2.822 0.00734 \*\*   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 7.165 on 41 degrees of freedom  
## Multiple R-squared: 0.7067, Adjusted R-squared: 0.671   
## F-statistic: 19.76 on 5 and 41 DF, p-value: 5.594e-10

**i. What is being tested by the ANOVA F statistic?**

Answer: ANOVA F statistic is calculated by (MS-explained by model) / (MS-residual errors in model). Fewer unexplained errors, compared to fewer explained errors result in a larger F0.

F0 explains the adequacy of our model in comparison to a normal distribution of errors when B1 … Bj are all == 0.

**What is the relevant conclusion in context?**

**ii. Look at the numerical values of the estimated slopes as well as their p-values.** **Do they seem to agree with or contradict with what you had written in your answer to part 1a?** Briefly explain what do you think is going on here.

When Agriculture, Examination, Education, Catholic, and Infant.Mortality are all used as predictor variables for Swiss fertility in 1888, Education, Catholic, and Infant.Mortality are have the most predictive power based on their B p-values.

Some aspects of this finding agree and some disagree:

**Agree** with my initial reading of the plots:

Because Education was correlated with both Agriculture and Examination these B p-values indicate that when all three are included in the model, Education has the most predictive value.

**Disagree** with my initial reading of the 4 plots:

I had seen too much variance in the Infant.Mortality plot to consider it a good linear relationship.

I had not considered Catholic a good linearly relationship because of the two clusters. It appeared more of a piece-wise linear relationship.

With MLR all the predictor variable not only influence the response variable, but influence the influence of each other. Catholic appears to have predictive value in the center of the residual plot, and Infant.Mortality appears to have predictive power at the + and - extremes of the residual plot. I believe that the combination of the two variables together creates the higher predictive power when they are used together in the model.

## 2. (No R required) Data from n = 113 hospitals are used …

to evaluate factors related to the risk that patients get an infection while in the hospital. The response variable is **InfctRsk**, the percentage of patients who get an infection while hospitalized.

The predictors are

* **Stay**, the average length of stay,
* **Age**, the average patient age,
* **Xrays**, a measure of how many Xrays are done in the hospital, and
* **Services**, a measure ofhow many different services the hospital orders.

We consider the following multiple regression equation:

E(InfctRsk) = B0 +B1Stay+B2Age+B3Xrays+B4Services.

Some R output is shown below. You may assume the regression assumptions are met.

#### Knowns from chart

B0: 0.170874

B1 (Stay): 0.237209

B2 (Age): -0.014071

B3 (Xrays): 0.020383

B4 (Services): 0.022718

Est. Standard Error, t value, p-value of t B1 (Stay): 0.0609571 3.891 0.00173\*\*\*

Est. Standard Error, t value, p-value of t B2 (Age): 0.022708 \_\_\_\_\_ \_\_\_\_\_\_\_

Est. Standard Error, t value, p-value of t B3 (Xrays): 0.005524 3.690 0.000354\*\*\*

Est. Standard Error, t value, p-value of t B4 (Services): 0.006970 3.260 0.001493\*\*

Residual Standard Error: 1.04 on 108 degrees freedom

Multiple R squared: \_\_\_\_

Adjusted R squared: \_\_\_\_

F-stat: 19.56 on 4 and 108 degrees freedom

p-value of F0 = 3.96e-12

### (a) What is the value of the estimated coeffcient of the variable Stay?\*\*

**Write a sentence that interprets this value.**

**Answer** The estimated coefficient of Stay, B1, is 0.237209

An interpretation of this coefficient is: In the presence of all of the model’s predictor variables, each unit increase in Stay produces a 0.237209 increase in the percentage of patients who get a HAI (healtcare acquired infection) in the hospital.

My model predicts an increase of 0.237 percent infections for each unit increase in the average length of hospital stay when controlling for the effect of other predictors.

### (b) Derive the test statistic, p-value, and critical value for the variable Age.

t0 = Bj-hat / se(Bj-hat)

# calculate the B2 test statistics  
B2.teststatistic = -0.014071 / 0.022708  
print(paste("The B2 test statistic is: ", B2.teststatistic))

## [1] "The B2 test statistic is: -0.619649462744407"

# calculate the B2 p-value of the test statistic  
B2.pvalue = 2\*pt(-abs(B2.teststatistic), df=(113 - 4 - 1)) # calc p Value  
print(paste("The B2 p-value is: ", B2.pvalue))

## [1] "The B2 p-value is: 0.536793700887277"

# calculate the B2 critical value to compare the test statistic to  
criticalValue = qt(0.975, (113 - 4 - 1))  
print(paste("The critical value is: ", criticalValue))

## [1] "The critical value is: 1.98217348330773"

**Answer** The B2 test statistic is: **-0.619649462744407**

The B2 p-value is: **0.536793700887277**

The critical value is: **1.98217348330773**

#### What null and alternative hypotheses are being evaluated with this test statistic? \*\*

???QUESTION????

H0: B2 = 0 Ha: B2 != 0 in the presence of other Bi where i != 2.

????IS THIS RIGHT????

#### What conclusion should we make about the variable Age?\*\*

When my model includes Stay, Age, Xray, and Services, the predictor Age does not statistically affect the performance of the linear model.

### (c) A classmate states: “The variable Age is not linearly related to the predicted infection risk.”

Do you agree with your classmate’s statement? Briefly explain.

**Answer**

No, I do not agree. The classmate’s statement is not complete because it does not include the phrase “when controlling for the effect of other predictors.”

### (d) Using the Bonferroni method, construct 95% joint confidence intervals for B1, B2,and B3.

\*\* 2d Work\*\*

delta multiplier = t((alpha/2)/g,n-k-1)

where,

g = 3 = number of intervals we are constructing

n = number of observations

k = number of regressors

alpha/2p

CI for Bj-hat = Bj-hat +- (delta \* se(Bj-hat))

B1 <- 0.237209  
se.B1 <- 0.060957  
  
B2 <- -0.014071  
se.B2 <- 0.022708  
  
B3 <- 0.020383  
se.B3 <- 0.005524  
  
delta <- qt((1 - (.05/6)), (113 - 4 - 1))  
  
B1.CI.low <- B1 - (delta \* se.B1)  
B1.CI.high <- B1 + (delta \* se.B1)  
print(paste("The simultaneous 95% CI for B1 is: ", B1.CI.low, " - ", B1.CI.high))

## [1] "The simultaneous 95% CI for B1 is: 0.0889712597151198 - 0.38544674028488"

B2.CI.low <- B2 - (delta \* se.B2)  
B2.CI.high <- B2 + (delta \* se.B2)  
print(paste("The simultaneous 95% CI for B2 is: ", B2.CI.low, " - ", B2.CI.high))

## [1] "The simultaneous 95% CI for B2 is: -0.0692932485750457 - 0.0411512485750457"

B3.CI.low <- B3 - (delta \* se.B3)  
B3.CI.high <- B3 + (delta \* se.B3)  
print(paste("The simultaneous 95% CI for B3 is: ", B3.CI.low, " - ", B3.CI.high))

## [1] "The simultaneous 95% CI for B3 is: 0.00694950955044247 - 0.0338164904495575"

**Answer** The simultaneous 95% CI for B1 is: 0.0889712597151198 - 0.38544674028488

The simultaneous 95% CI for B2 is: -0.0692932485750457 - 0.0411512485750457

The simultaneous 95% CI for B3 is: 0.00694950955044247 - 0.0338164904495575

### (e) Fill in the values for the ANOVA table for this regression model.

**2e Work**

n = 113

MS-E == sigma^2 == 1.04^2 == 1.0816

F0 = 19.56

MS-E == SS-E / n-4-1

F0 = MSR / MSE

SS-R = MS-R \* df

R2 = SSR / SST

R2-adj = (SSE / (n-p)) / (SST / n-1))

|  |  |  |  |
| --- | --- | --- | --- |
| Source of Variation | DF | SS | MS |
| Regression | 4 | 2284.8584 \* 4=**9139.4336** | 19.56 \* 116.8128=**2284.8584** |
| Error | 113-4-1 = **108** | 1.0816 \* 108=**116.8128** | **1.0816** |
| Total | 113-1 = **112** | **9256.2464** | \*\*\* |