



TUTORIAL ON HIGH DYNAMIC RANGE VIDEO



Institut
Mines-Télécom



Erik Reinhard
Giuseppe Valenzise
Frederic Dufaux

About the presenters



- **Erik Reinhard: Distinguished Scientist at Technicolor R&I**
 - Academic positions at universities and research institutes in Europe and North America
 - Founder and editor-in-chief of ACM Transactions on Applied Perception
 - Author of a reference book on HDR
- **Giuseppe Valenzise: CNRS researcher at LTCI, Telecom ParisTech**
 - Ph.D. in Information Technology at Politecnico di Milano, Italy
 - Experience in video coding, quality assessment and perceptual studies
- **Frederic Dufaux: CNRS Research Director at LTCI, Telecom ParisTech**
 - Editor-in-Chief of Signal Processing: Image Communication
 - Participated in MPEG and JPEG committees
 - Research positions at EPFL, Emitall Surveillance, Genimedia, Compaq, Digital Equipment, MIT



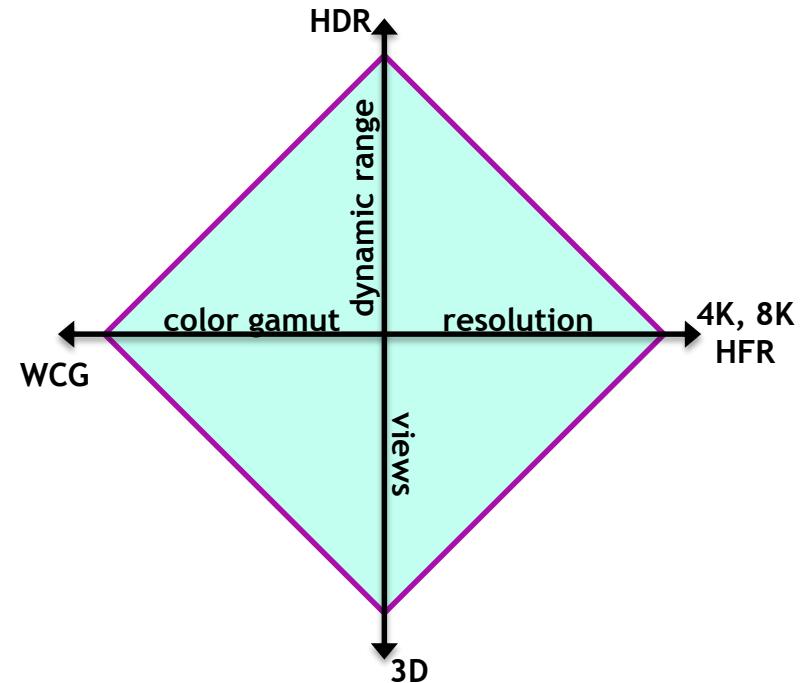
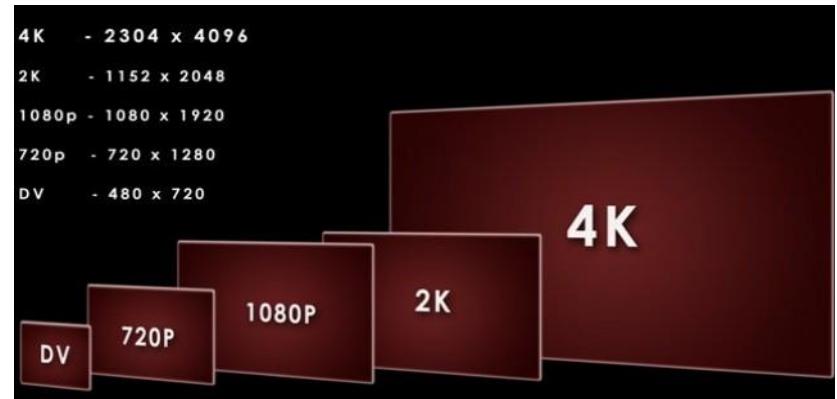
Outline

- **Introduction**
 - Background and fundamental concepts related to HDR.
- **Perception**
 - Properties of human visual system
- **Capture/Acquisition**
 - Camera technologies, multi-exposure techniques, ghost removal
- **Tone Reproduction**
 - How to display HDR video on a standard display, curve-based solution, spatial processing, video processing, inverse tone reproduction
- **Color Management**
 - Gamut boundary management techniques, luminance - chroma interactions
- **Video Coding**
 - Compression techniques for HDR video, pre- and post-processing, on-going standardization activities in MPEG related to HDR and Wide Color Gamut
- **Display**
 - Display hardware, display characterization, dual modulation
- **Quality of Experience**
 - The concept of QoE in the context of HDR, objective measures to predict HDR image and video quality
- **Applications & Wrap up**

INTRODUCTION

Context and Trends

- **Higher spatial and temporal resolutions**
 - Ultra High Definition (UHD), 4K, 8K
 - High Frame Rate (HFR)
- **Higher pixel depth**
 - up to 14 bits per component
 - High Dynamic Range (HDR)
- **More colors**
 - 4:4:4 color sampling
 - Wide Color Gamut (WCG)
- **More views**
 - 3D, multi-view, free viewpoint



Context and Trends

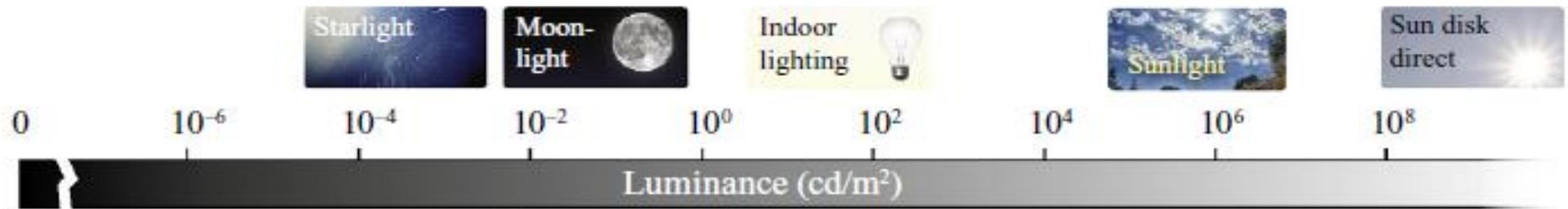
- **Driven by**
- **Improved user experience**
 - More realistic scene rendering
 - More details
 - Immersive
 - Better perceived depth
- **New video technologies**
 - New devices
 - New multimedia services



Some definitions

- **Luminance**

- A photometric measure of the luminous intensity per unit area
- Candela per square meter, cd/m^2 (also referred to as *nits*)



Some definitions

- **Dynamic range or contrast ratio**
 - The ratio between the brightest and the darkest objects in a scene
- **f-stops**
 - Ratios of light or exposure
 - Defined in power-of-2 steps
- **Orders of magnitude**

$$\frac{L_{\max}}{L_{\min}}$$

$$\log_2 L_{\max} - \log_2 L_{\min}$$

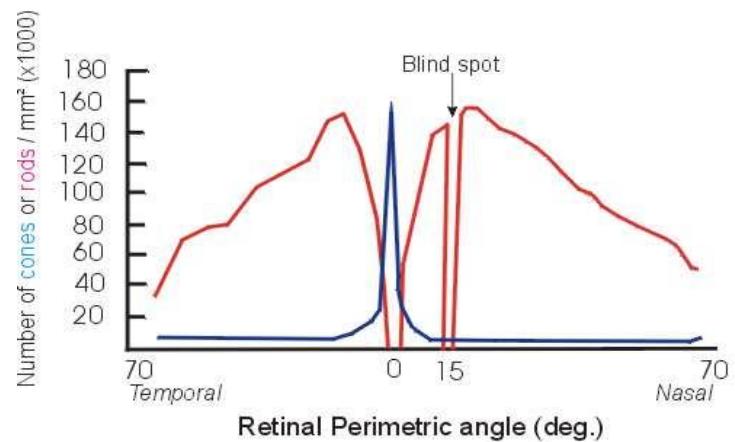
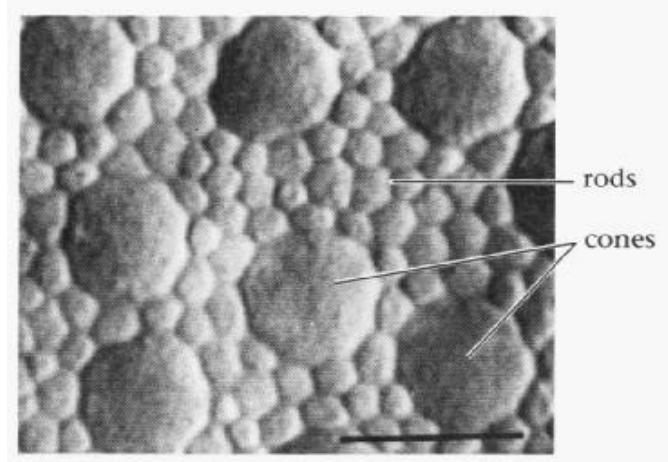
$$\log_{10} L_{\max} - \log_{10} L_{\min}$$

Some definitions

- **Low (Standard) Dynamic Range**
 - ≤ 10 f-stops
 - Three channels, 8 bit/channel, integer
 - Gamma correction
- **Enhanced (Extended, Wide) Dynamic Range**
 - 10 to 16 f-stops
 - More than 8 bit/channel, integer
- **High Dynamic Range**
 - ≥ 16 f-stops
 - Floating points
 - Linear encoding

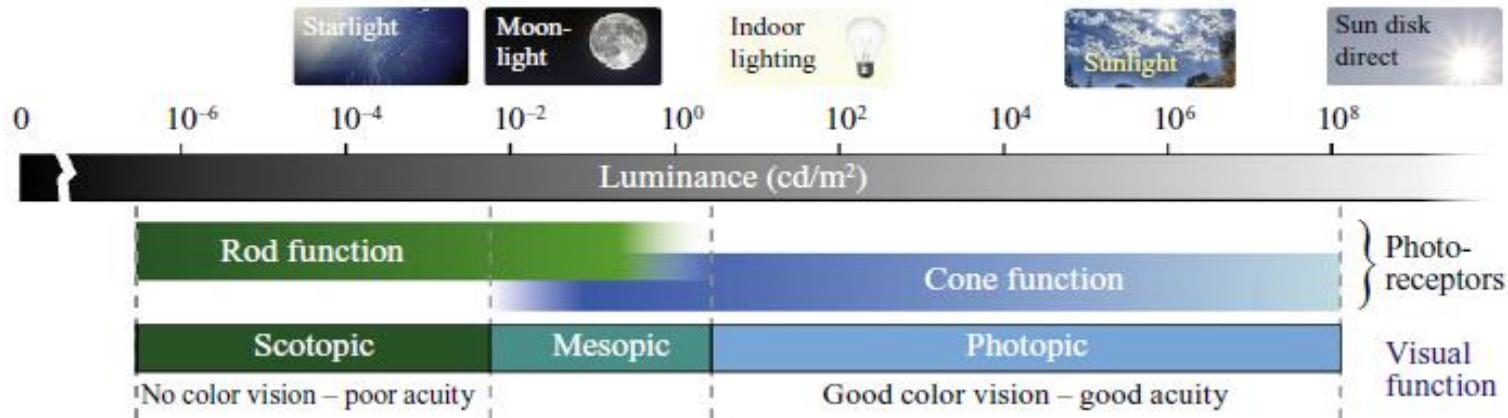
Human Visual System - Retina

- **Rods**
 - 100+ millions photoreceptor cells
 - Peripheral retina
 - Scotopic monochrome vision: 10^{-6} to 10 cd/m^2
- **Cones**
 - 6 millions photoreceptor cells
 - Near the fovea
 - Photopic color vision: 0.03 to 10^8 cd/m^2
 - Long- (L, red), Medium- (M, green), and Short-wavelength (S, blue)
 - High resolution vision



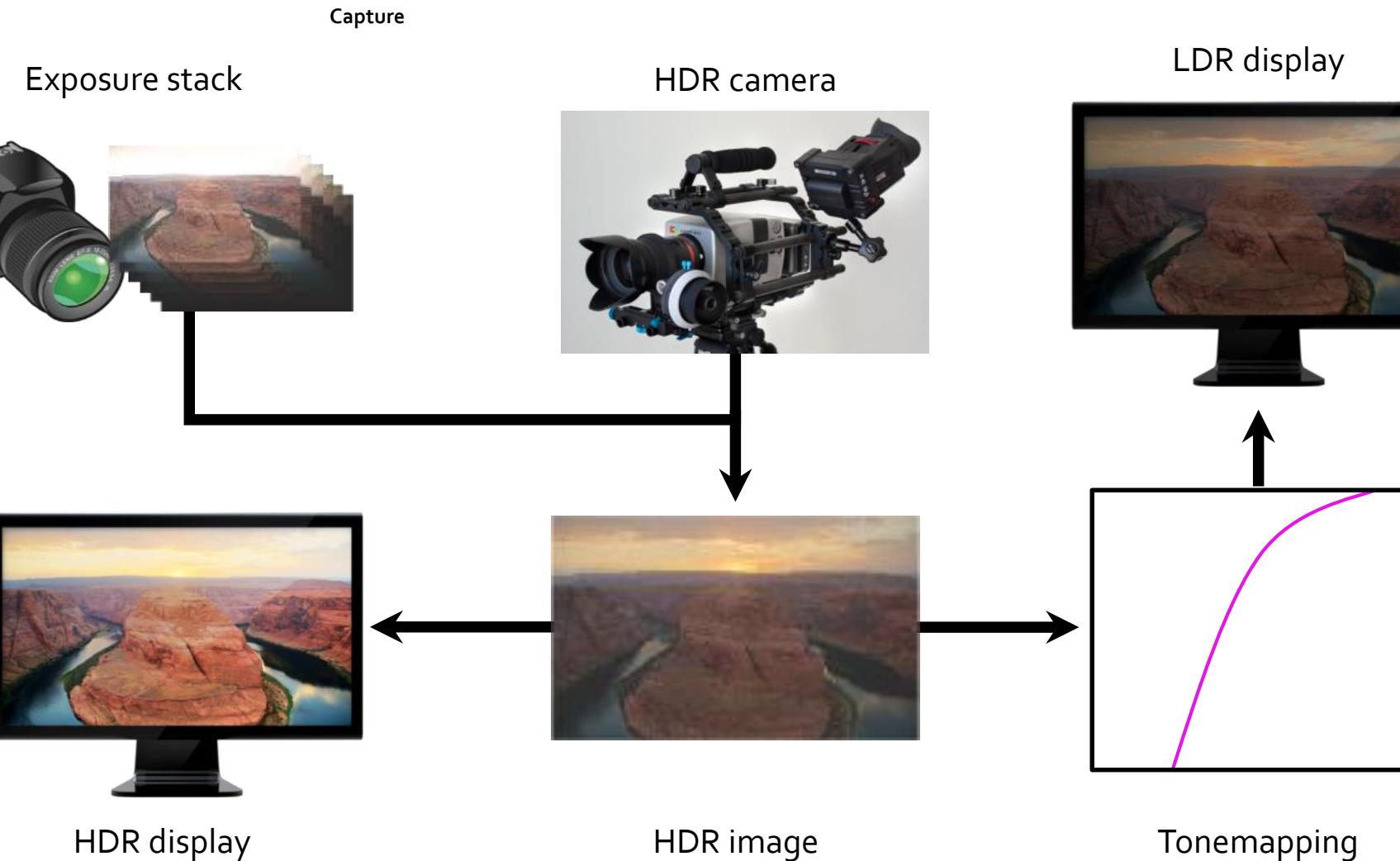
Adapted after Østerberg, 1935

Human Visual System



- **Human Visual System can adapt to a very large range of light intensities**
 - At a given time: 4-5 orders of magnitude
 - With adaptation: 14 orders of magnitude
 - *Mechanical, photochemical and neuronal adaptive processes*

HDR Pipeline



HDR Pipeline

Capture

Bracketing



HDR camera



CG content

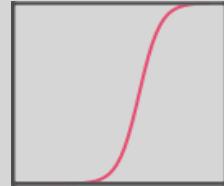


Processing

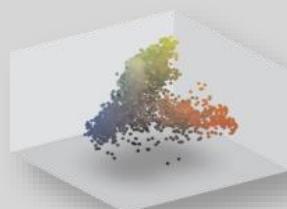
Merging/Fusion



Tonemapping



Color correction



Distribution

Format



Encoding

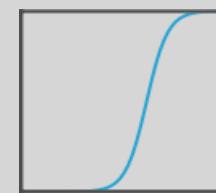


Rendering

Decoding



Display side
TMO/iTMO



Display

LDR display



HDR display

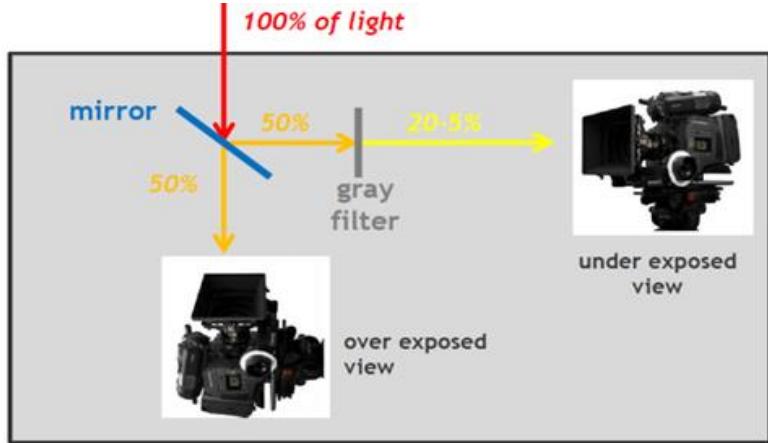


New Challenges at each stage

- **Content creation**
 - True HDR cameras (when?)
 - Upgrading legacy content to HDR
- **Distribution**
 - Efficient video coding solutions
 - New standards for interoperability
 - Backward compatibility
- **Processing / rendering**
 - Tone mapping and inverse tone mapping
 - Color management
- **Display**
 - Professional displays up to 4000 nits
 - Consumer displays up to 1000 nits
- **Quality of experience**
 - Taking into account HVS properties



Capturing HDR video



F3 camera, 1080p 25 fps, 21 f-stops

When does HDR help most?



LDR



- **Scenes with difficult lighting conditions**
- **Better opportunity to convey director's intent**



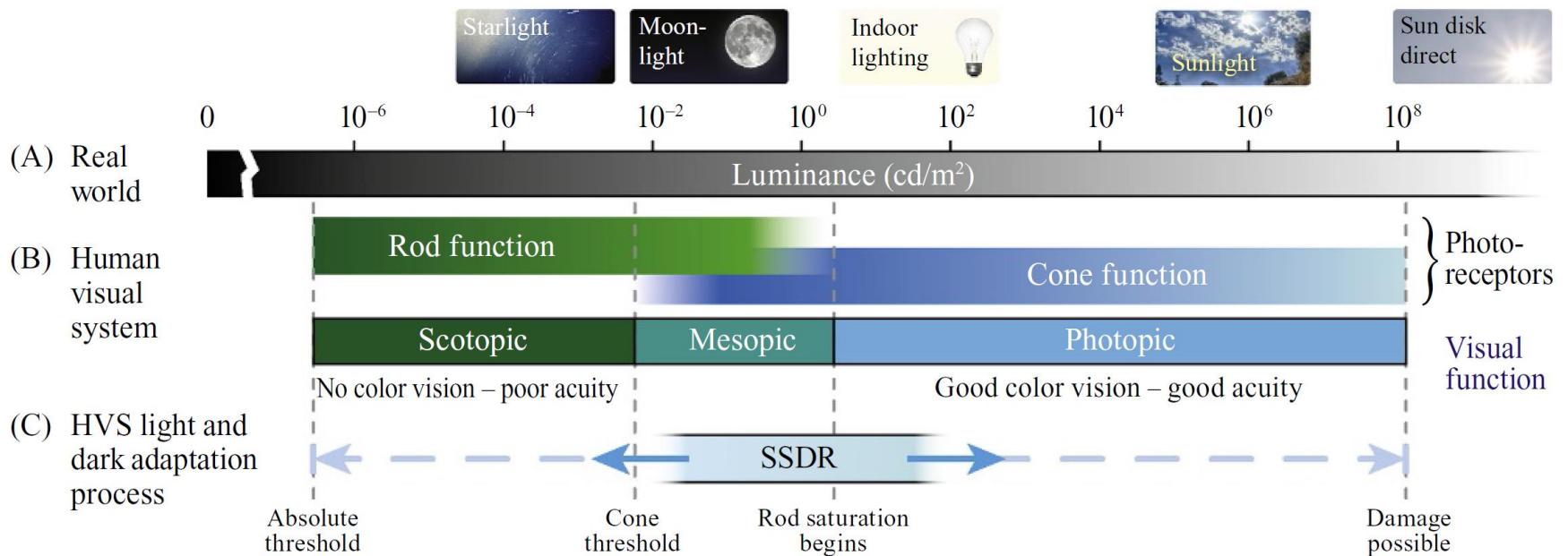
HDR

NEVEX

PERCEPTUAL PHENOMENA IN HDR

HDR and visual adaptation

- Human eye can perceive a range of approximately $14 \log_{10}$ units (46 f-stops)
- But only about $4 \log_{10}$ units at the same time
- High Dynamic Range perception through *adaptation*:
 - Steady-state dynamic range (SSDR) compression
 - Light/dark adaptation (rods and cones activation)
 - Chromatic adaptation (color constancy)



[Kunkel et al. 2016]

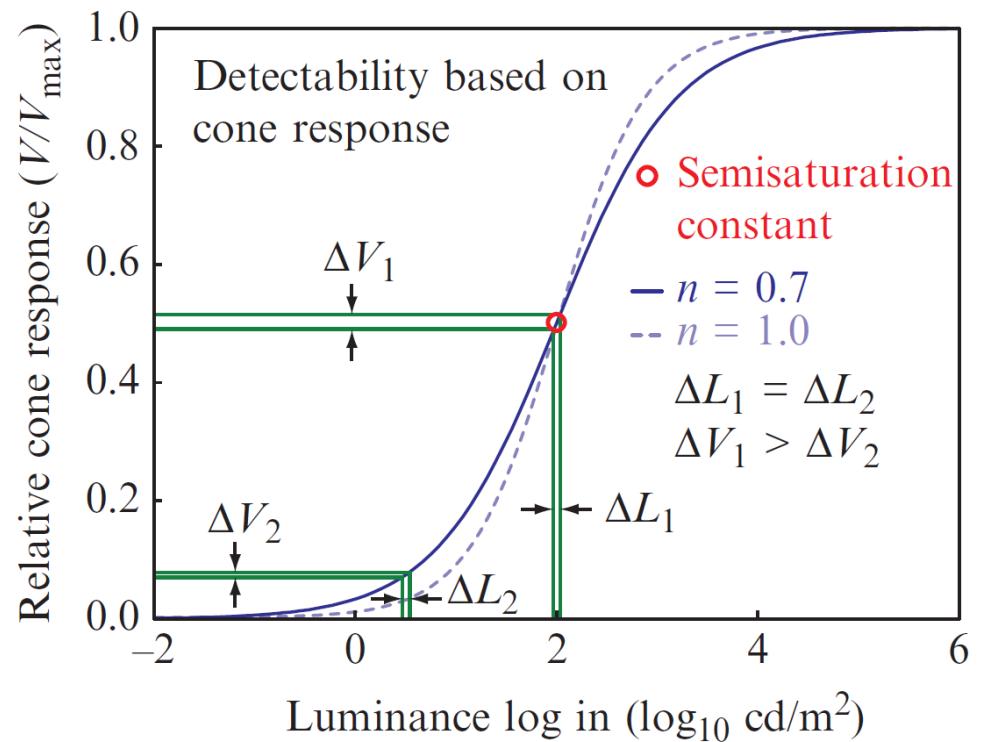
Steady-state Dynamic Range

- Between 3 and 4 \log_{10} units
- SSDR adaptation takes less than 500 ms
- Nonlinear response of photoreceptors (Naka and Rushton, 1966; Michaelis and Menten, 1913):

$$\frac{V}{V_{max}} = \frac{L^n}{L^n + \sigma^n}$$

where:

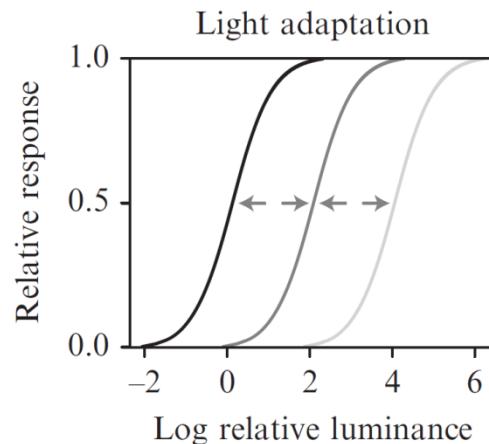
- V = signal response
- L = input luminance
- σ = semisaturation constant
- $n = 0.7 \div 1$



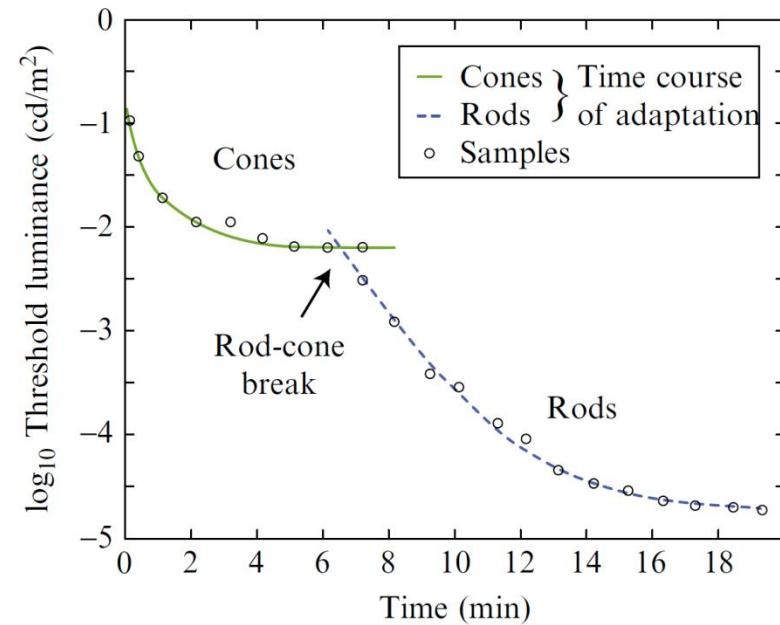
[Kunkel et al. 2016]

Light/Dark adaptation

- The gain of *all* photoreceptors is adjusted to the background luminance
 - Similar to automatic exposure control in digital cameras
- The semisaturation constant is equal to the adaptation luminance
 - This process is *local* in the retina



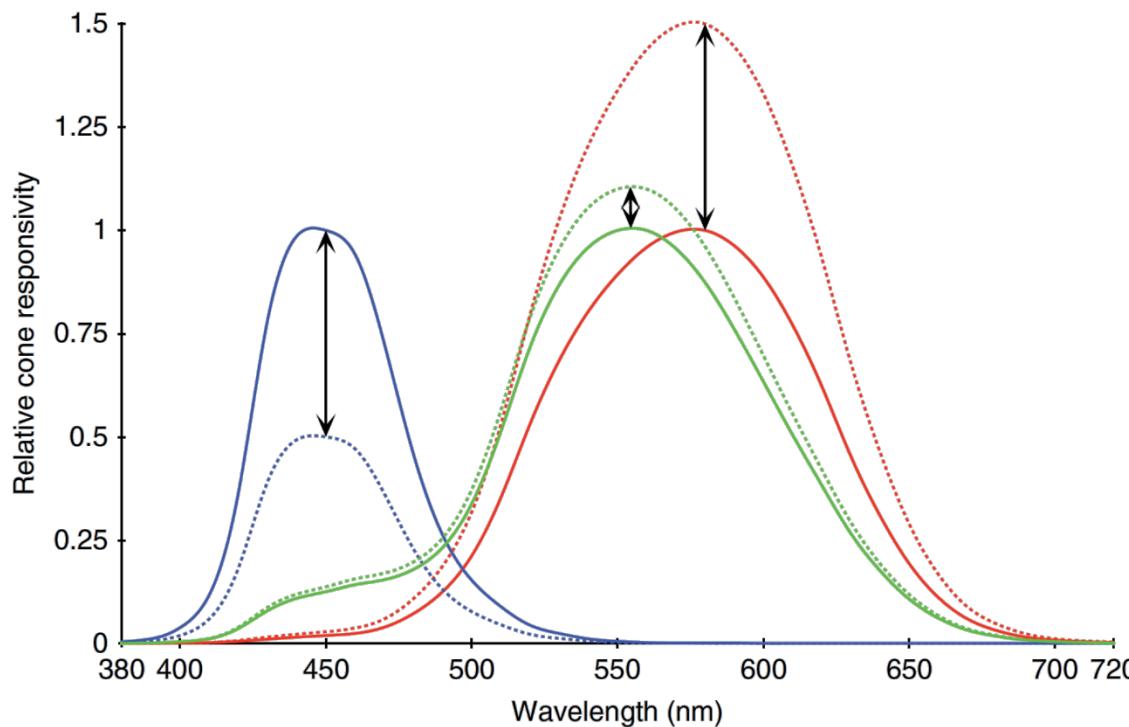
- Function of time:
 - Full light adaptation takes about 5 minutes
 - Full dark adaptation is much slower, and takes up to 30 minutes
 - Time course of dark adaptation:



[Kunkel et al. 2016]

Chromatic adaptation

- The sensitivity of each cone photoreceptor (L, M, S) is adjusted *individually*
- Basic mechanism of color constancy
 - Similar to automatic white balance in digital cameras



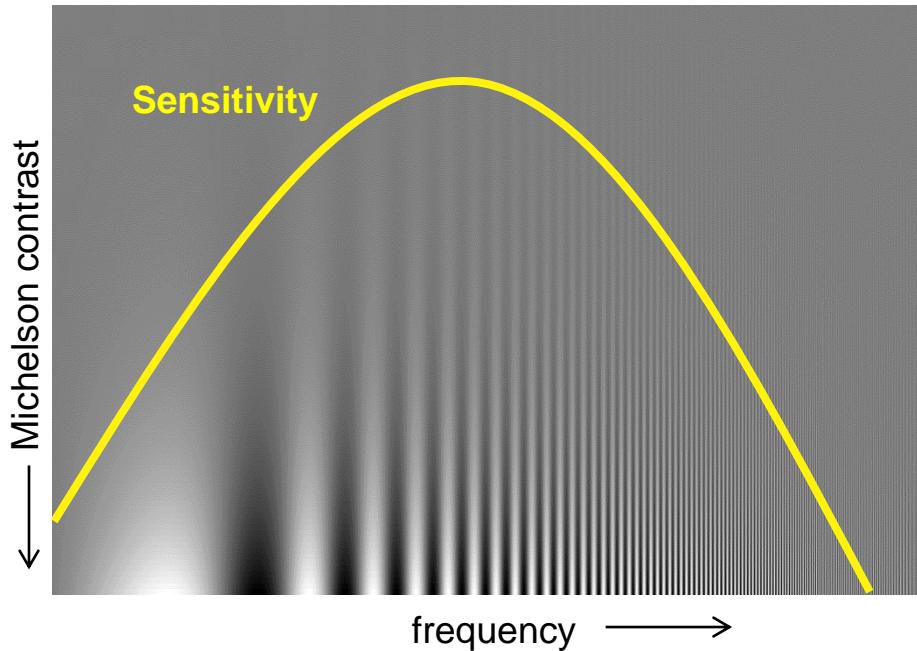
[Fairchild, 2013]

Perception of luminance

- **Just-noticeable difference (JND):**
 - the minimum amount that must be changed in order for a difference to be detectable at least 50% of the times
 - also called *contrast detection threshold*
 - Contrast sensitivity = 1/threshold
- **Weber's law (1834): the JND between two stimuli is proportional to the magnitude of the stimuli, i.e.,**
$$\Delta R \sim \frac{\Delta L}{L}$$
 - $\Delta L/L$ is called Weber ratio, and is assumed constant (about 1%)
 - when $\Delta \rightarrow 0$, by integration, $R \sim \log L$ (Fechner's law, 1860)
 - valid only on a limited range of luminance
- **Stevens' power law (1961): $R \sim L^\alpha$**
 - E.g., $\alpha = 1/3$ in CIELAB brightness predictor

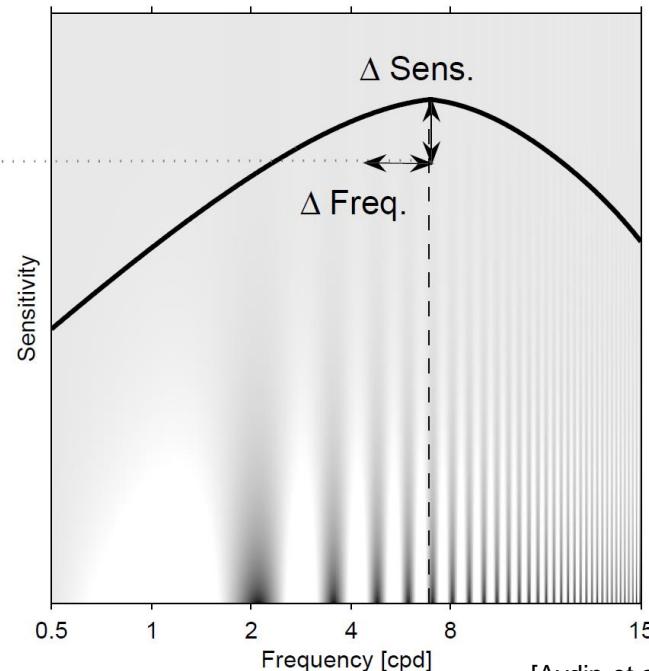
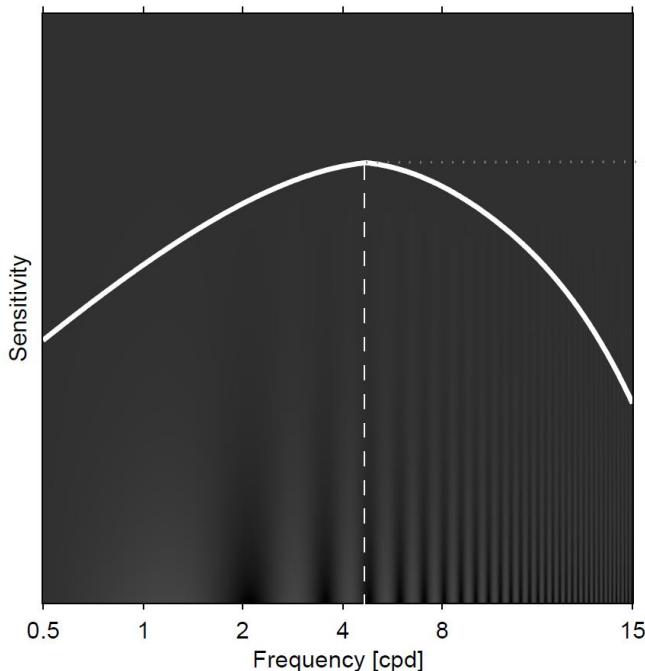
Spatial properties of the HVS

- The contrast detection threshold depends on the spatial frequency of a stimulus
- **Campbell-Robson chart**
 - Sinusoidal grating with exponentially increasing frequency and contrast
 - Michelson contrast measure: $\frac{L_{max}-L_{min}}{L_{max}+L_{min}}$
 - The *contrast sensitivity function* (CSF) is *band-pass* (low-pass for color)



CSF as a function of average luminance

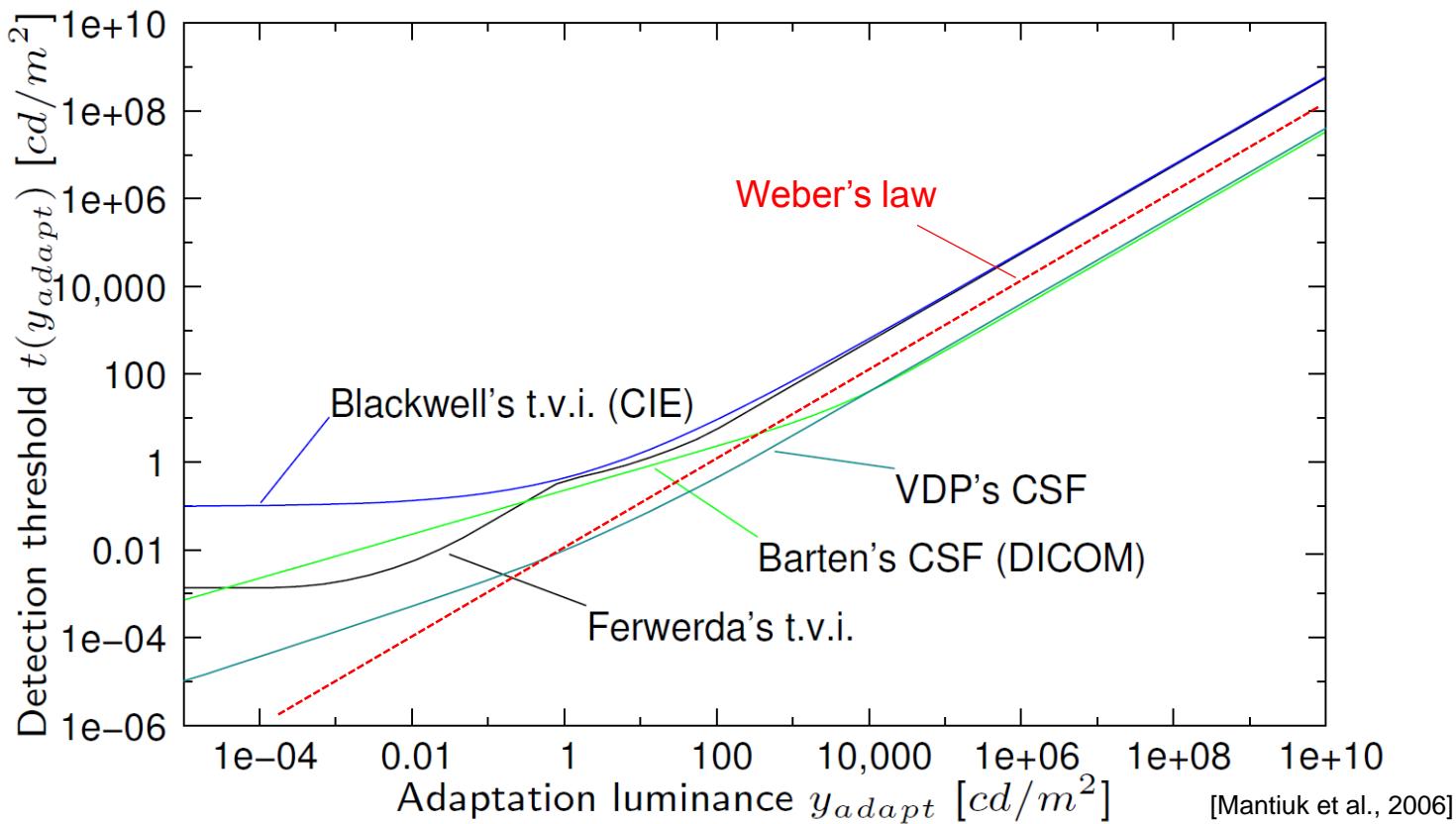
- **The CSF changes with the adaptation luminance**
 - The contrast sensitivity increases with adaption luminance, and drops in dimmer conditions where rods predominate and visual acuity is lower
- **The peak of the CSF at a given luminance level gives the lowest detection threshold at that luminance**
 - Conservative estimation of JND



[Aydin et al., 2008]

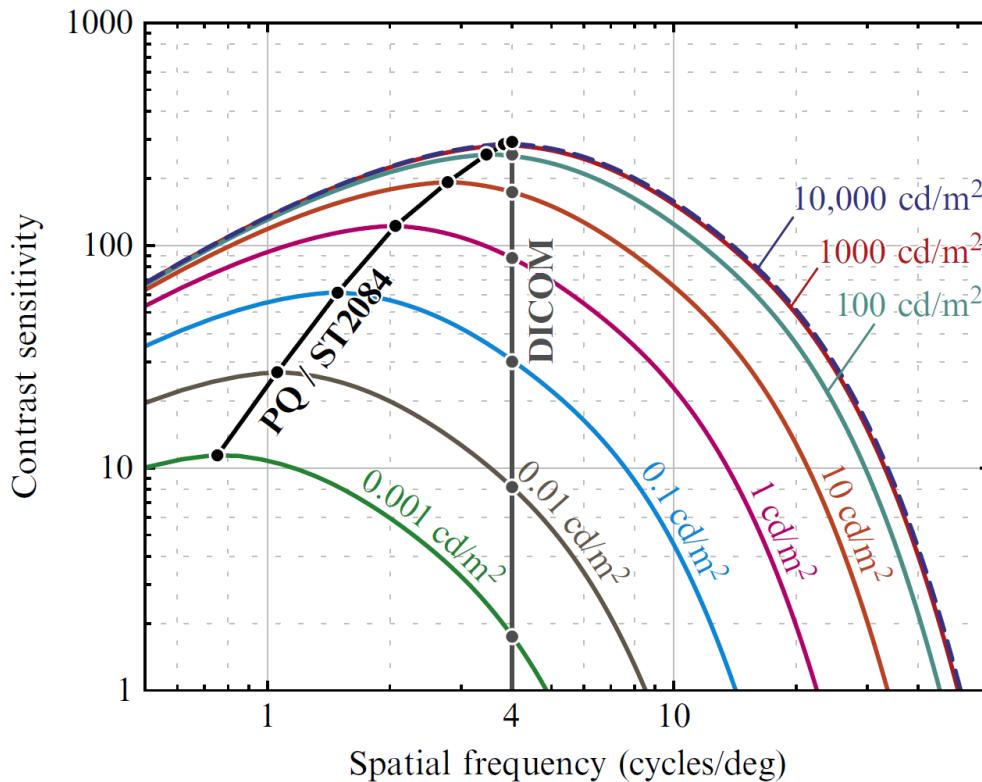
Contrast-versus-intensity (c.v.i.) function

- Describes how the detection threshold changes with adaptation luminance
 - Threshold-versus-intensity (t.v.i.) are computed on a single frequency
 - CSF-based models track the peaks of CSF's (more conservative)



Barten's CSF model

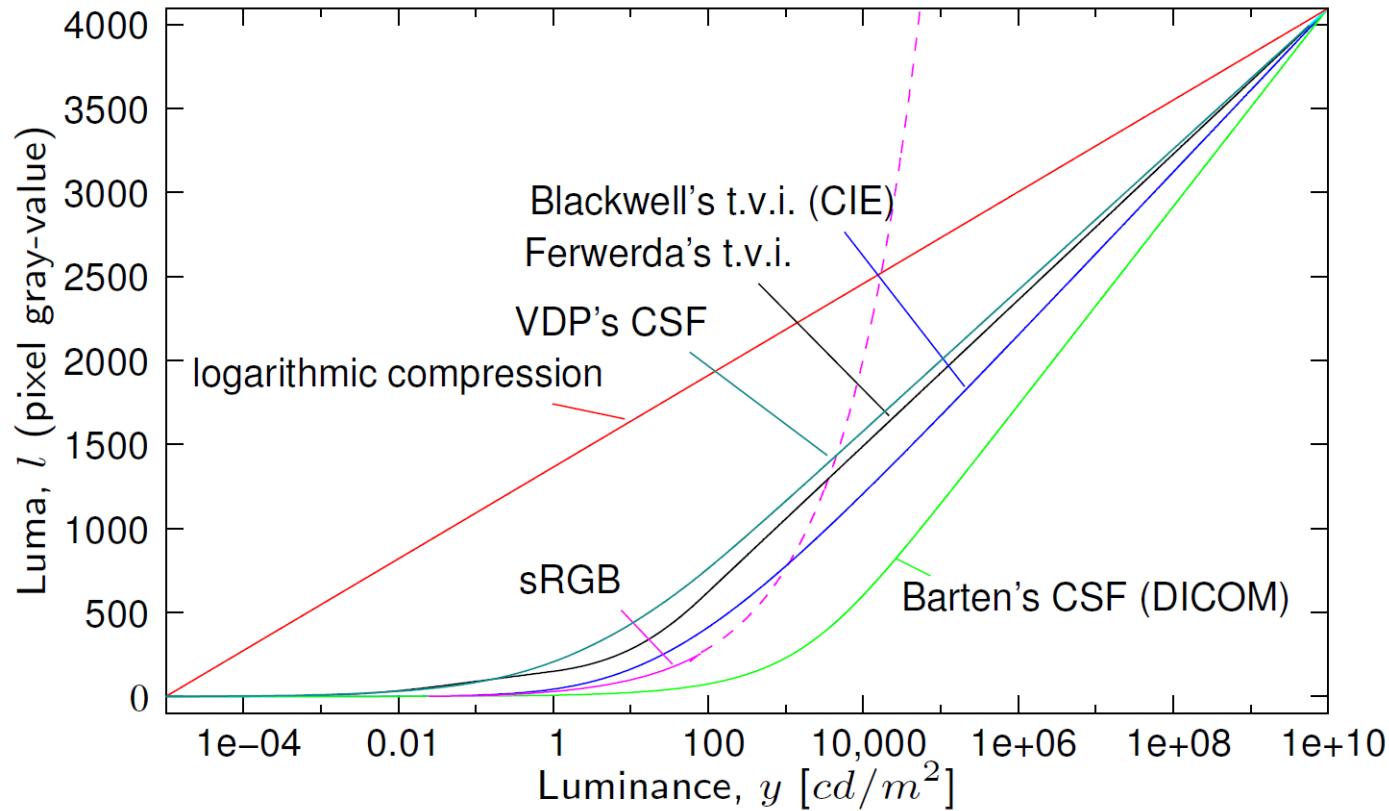
- Accurate closed-form model describing CSF for different adaptation luminances (Barten, 1996)
 - Considers neural noise, lateral inhibition, photon noise, external noise, optical modulation transfer function, temporal filtering, etc.
- Used in DICOM biomedical standard and for PQ / ST2084 EOTF



- Detection thresholds obtained at a fixed frequency (4 cpd) for DICOM
- Detection thresholds obtained by tracking CSF peaks for PQ EOTF

Luminance to Luma mapping

- A luminance-to-brightness transfer function can be obtained as the cumulative sum of threshold values
 - Quantized with 2^n levels to obtain a *luma* signal
- Conventional 1/2.2 (sRGB) gamma is quite accurate for dark luminance regions, while at high luminance the logarithmic behavior prevails



HIGH DYNAMIC RANGE CAPTURE / ACQUISITION

HDR Video Capture / Acquisition

- **Single Sensor**
 - Ideal solution but expensive
 - 14 – 16.5 f-stops at 4K capture
 - Sensors may suffer from noise in low light
- **Temporal Bracketing**
 - Alternating frames 2-6 f-stops apart
 - Introduces ghosting artefacts in moving scenes
 - Typically requires high frame rate for video
- **Spatial Bracketing**
 - Beam splitters or mirrors redirect some of the light to additional sensors
 - Need to correct the geometric disparity between images
 - No temporal mismatches = no ghosting
- **Synthesis from Conventional Content**

Single Sensor

- **Every pixel captures a higher dynamic range**
 - Technically challenging
 - 14 – 16.5 f-stops of dynamic range claimed
 - Difficult to manage noise
- **Trade-off:**
 - Resolution
 - Noise
 - Dynamic Range



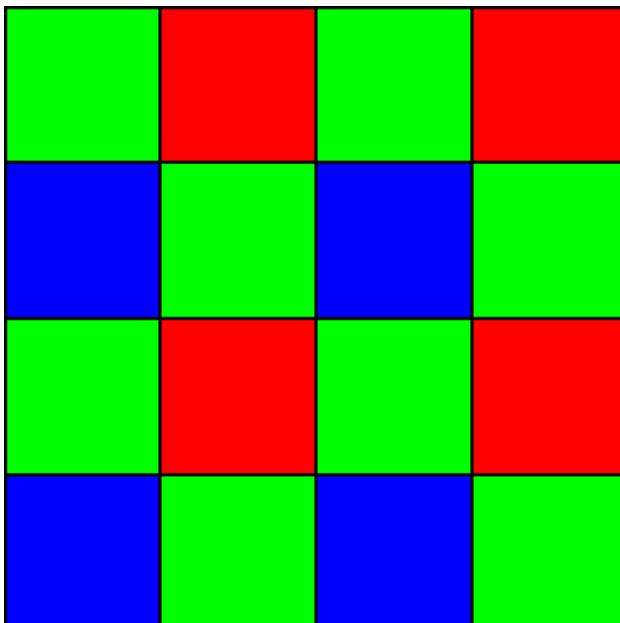
Arri Alexa



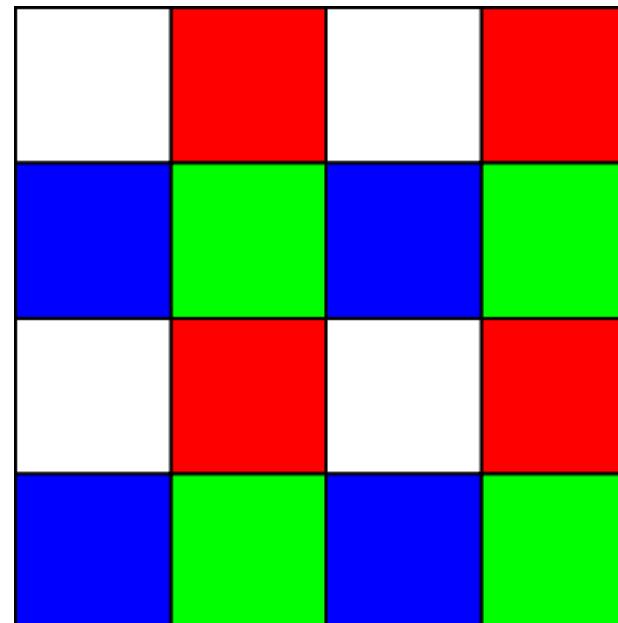
Sony F65

Single Sensor

- Light sensitivity of sensors can be increased by adding a white pixel



Standard Bayer pattern

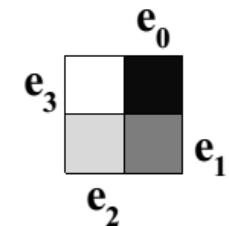
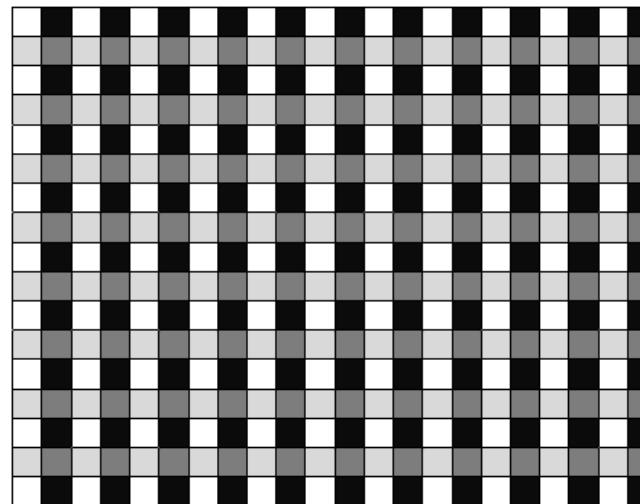
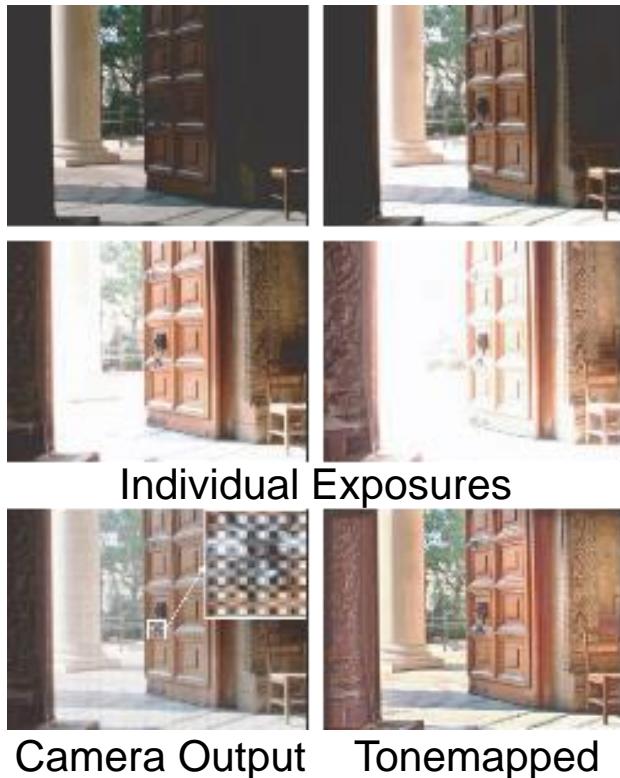


RGBW pattern

Sugiyama, T., 'Image-capturing apparatus', U.S. Patent Application
11/094,653, 2005

Single Sensor

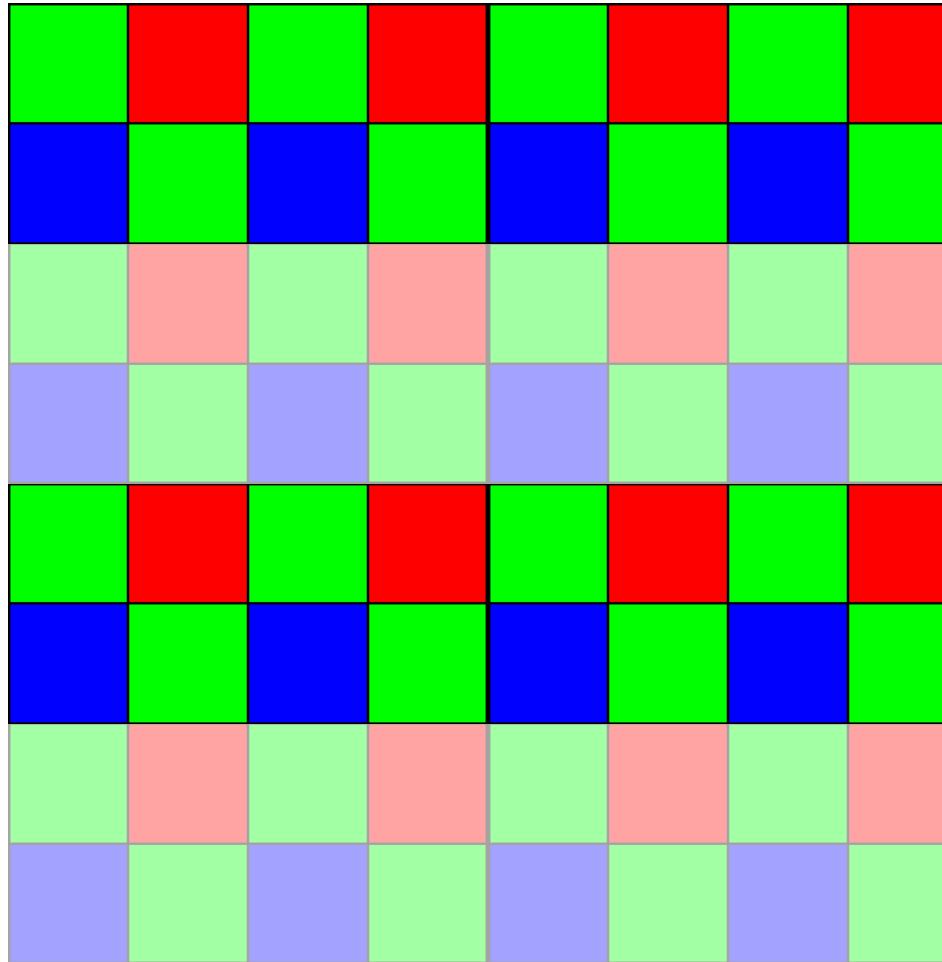
- **Each pixel captures different exposure**
- **Filters placed on the sensor elements**



Nayar, S. & Mitsunaga, T., 'High dynamic range imaging: Spatially varying pixel exposures', IEEE CVPR 2000

Single Sensor

- **Bayer Strips (proposed for mobile sensors)**

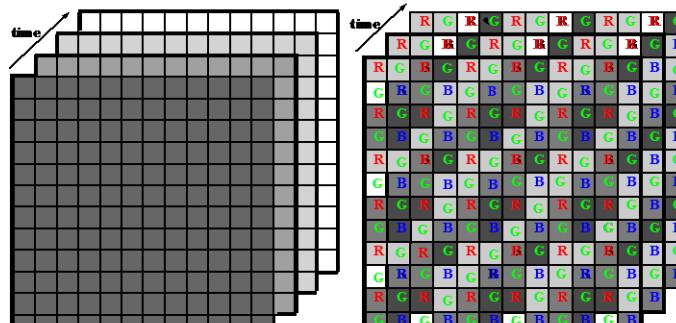
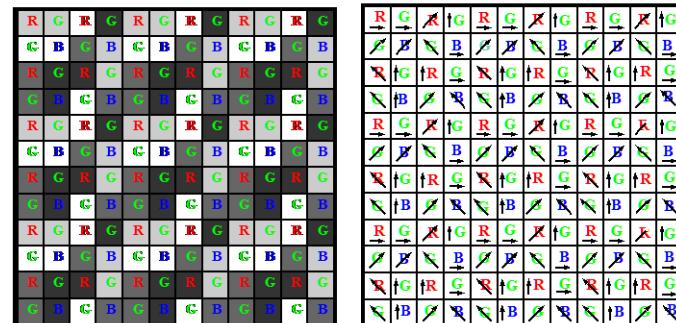
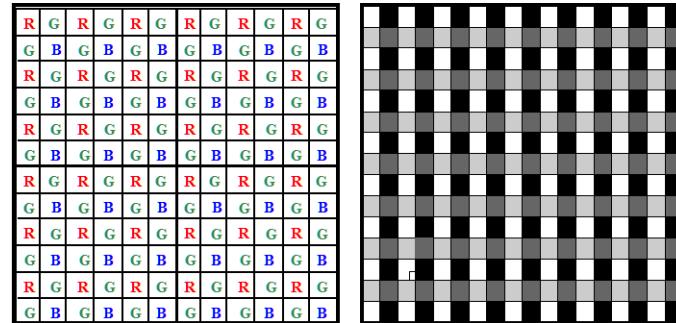


Single Sensor

'Assorted pixels'

The arrangement of pixels can be varied to achieve different effects:

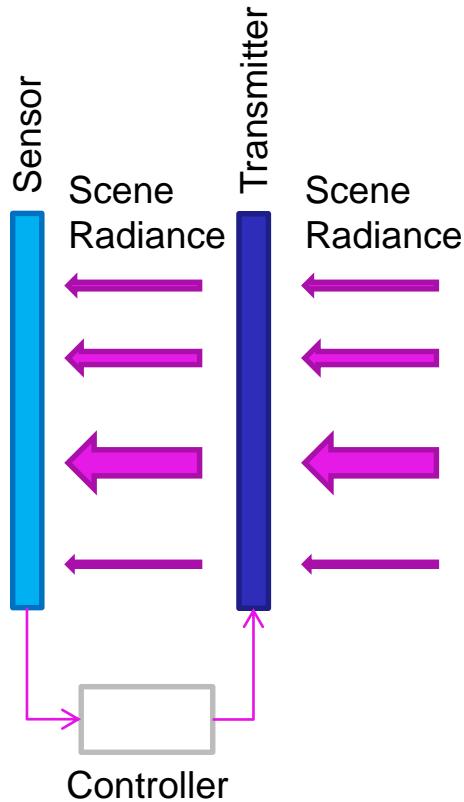
- **Dynamic range**
- Wider gamut
- Polarization
- Etc...



Nayar, Shree K., and Srinivasa G. Narasimhan.
"Assorted Pixels: Multi-Sampled Imaging with
Structural Models." *ECCV*, pp 636-652, 2002.

Single Sensor

- Adaptive Dynamic Range Imaging



Nayar, S. & Branzoi, V., 'Adaptive Dynamic Range Imaging: Optical Control of Pixel Exposures over Space and Time, ICCV 2003

Single Sensor

- Control CMOS readout timing and exposure per row
 - Use rolling shutter to our advantage
 - Well suited for images where exposure varies horizontally

Normal image



Coded rolling shutter



Gu, Jinwei, et al. "Coded Rolling Shutter Photography: Flexible Space-Time Sampling." *IEEE International Conference on Computational Photography (ICCP)*, 2010.

Temporal Exposure Bracketing

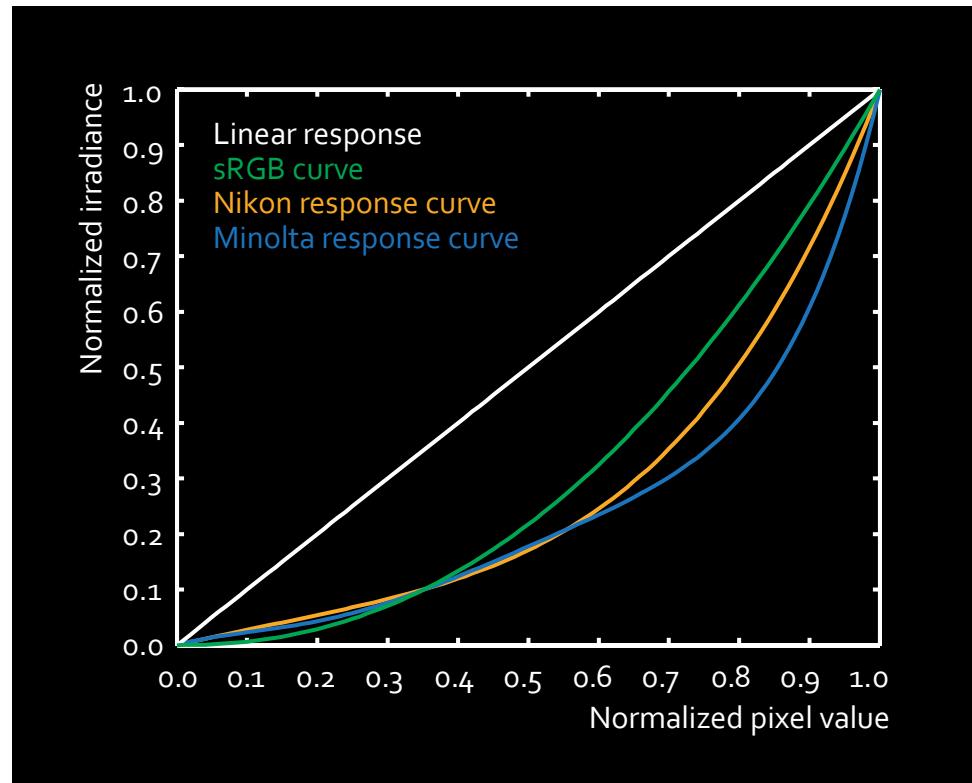
- Each image has some well-exposed pixels
- Merge into HDR:
 - Apply inverse camera response function $f()$ to pixel value Z
 - Divide by exposure time t
 - Mask under- and over-exposed pixels with weight function w
 - Sum exposures

$$L(x, y) = \frac{\sum_{i=1}^n w(Z_i(x, y)) \left(\frac{f^{-1}(Z_i(x, y))}{t_i} \right)}{\sum_{i=1}^n w(Z_i(x, y))}$$

- Method is effective if:
 - Camera is motionless
 - Nothing moves in the scene
- Hence: much research devoted to removing these limitations!

Camera Response Recovery

- Cameras have non linear response
- To merge exposures, they need to be linearized first
- Requires recovery of the camera response curve $f()$
- Several approaches:
 - Mann & Picard (1995)
 - Debevec & Malik (1997)
 - Mitsunaga & Nayar (1999)
 - Robertson et al. (2003)



Temporal Exposure Bracketing

- **Two or more exposures taken one after the other**
 - Exposure times varied by a fixed number of f-stops (exponential)
 - More optimal spacing: using Fibonacci sequence – facilitates image registration (Gupta, Iso and Nayar, ICCV 2013)
 - Metering-based spacing
- **Possible even on smartphones**
- **Not well suited to dynamic content**
- **Trade off:**
 - Ghosting vs dynamic range
- **E.g. RED Epic Cameras (HDRx)**
 - 18.5 f-stops claimed for RED Epic Mysterium



Temporal Exposure Bracketing

- Multiple shots taken of the same scene
- Exponential sequence:
 - Exposure time multiplies by a factor between each image
 - For example: factor of 2 (i.e. 1 f-stop)
- Most modern cameras offer automated settings (AEB - Auto-exposure bracketing)



Temporal Exposure Bracketing

- Each exposure captures part of the scene
- Exposure stack can be merged into HDR image

Visualisation:

- Bit-pattern for each channel:
 - 1: well exposed
 - 0: under or over exposed



Temporal Exposure Bracketing

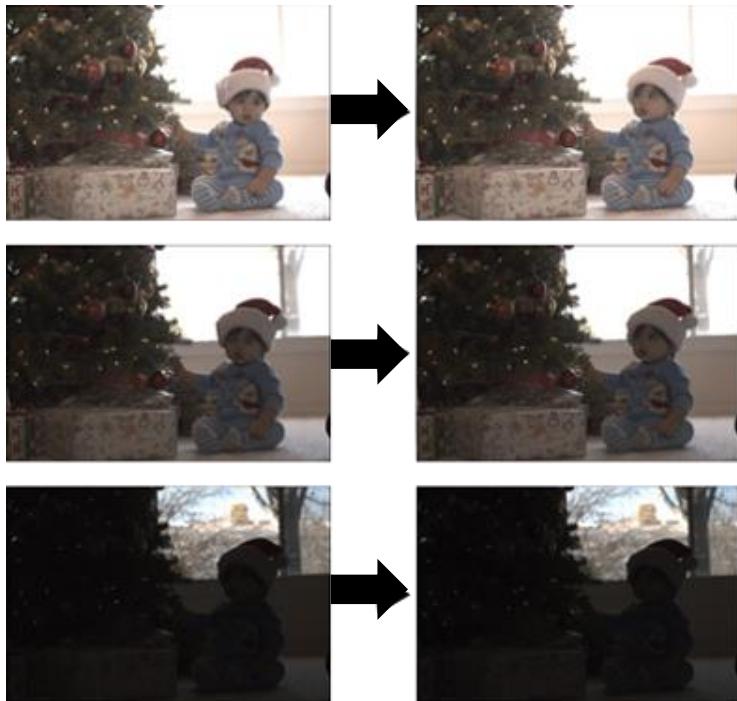
- **Merge exposure sequences into HDR imagery using Patch Match**
 - Finds and merges patches from different exposures
 - Extends to video by combining optical flow techniques with patch-based reconstruction
- **Advantages**
 - Implicit exposure alignment
 - Implicit ghost removal

Sen, P., Kalantari, N.K., Yaesoubi, M., Darabi, S., Goldman, D.B. and Shechtman, E., ‘Robust Patch-Based HDR Reconstruction of Dynamic Scenes’, *ACM Trans. Graph.*, 31(6), 2012

Kalantari, N.K., Shechtman, E., Barnes, C., Darabi, S., Goldman, D.B. and Sen, P., ‘Patch-Based High Dynamic Range Video’, *ACM Trans. Graph.*, 32(6), 2013

Joint Deghosting and Reconstruction

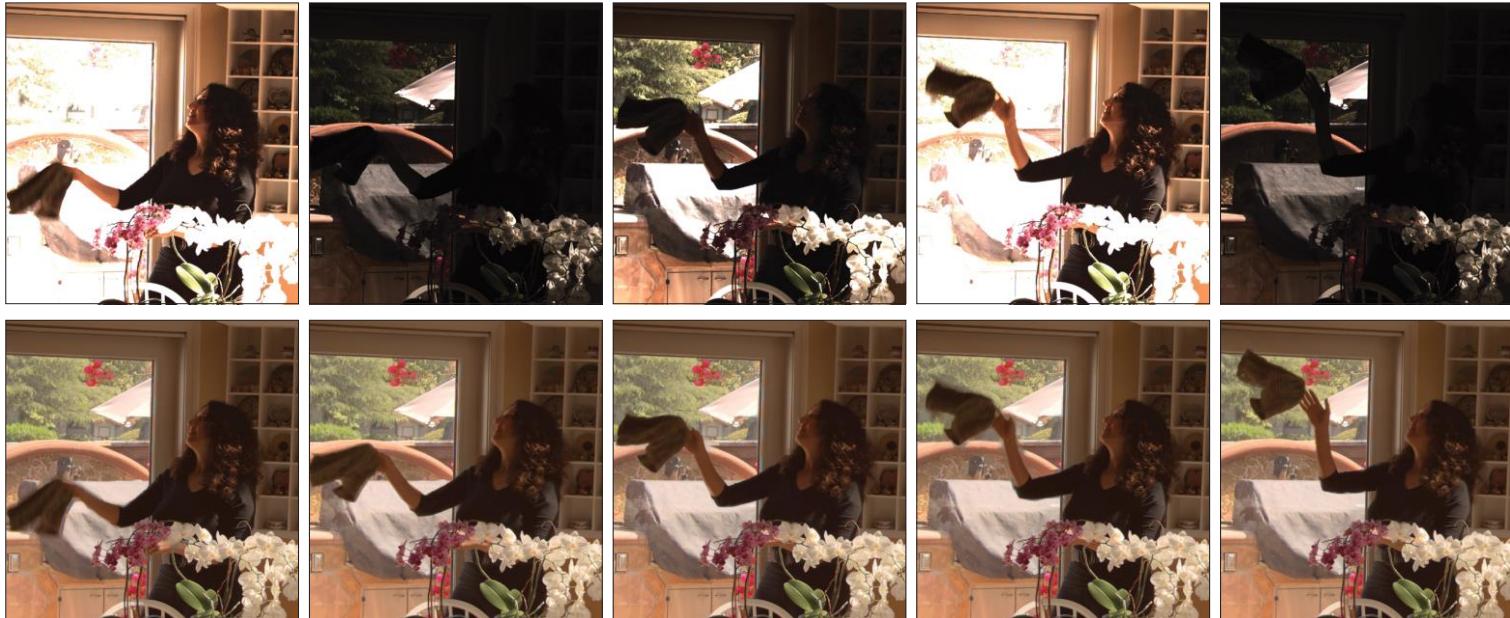
- Alternatively we can try reconstruct new exposures where features are aligned
 - Patch-wise alignment to reference image



Sen, P., Kalantari, N. K., Yaesoubi, M., Darabi, S., Goldman, D. B., & Shechtman, E., 'Robust Patch-Based HDR Reconstruction of Dynamic Scenes, ACM Transactions on Graphics, 31(6), 2012

Joint Deghosting and Reconstruction

- This can be extended to video
 - Each exposure captured leads to one HDR frame
 - No loss of framerate



Nima Khademi Kalantari, Eli Shechtman, Connelly Barnes, Soheil Darabi, Dan B. Goldman and Pradeep Sen, 'Patch-Based High Dynamic Range Video', SIGGRAPH Asia, 2013

Metering Strategies

- Typically exposures are evenly spaced
 - For example: -2, 0, 2 f-stops



Metering Strategies

- **Metering allows scene-adaptive exposure selection**
 - Uses histogram analysis
 - For noise reduction
 - For capturing a higher dynamic range with fewer exposures



Gelfand, N., Adams, A., Park, S.H. and Pulli, K., 'Multi-exposure imaging on mobile devices', *ACM Int. Conf. on Multimedia*, 2010

Metering Strategies

- First capture many exposures fast at a lower resolution
 - Then reconstruct a histogram over the full dynamic range of the scene
 - Finally, determine exposures that minimize noise, maximize dynamic range etc.
-
- Shown to reduce the number of exposures for an equivalent dynamic range
 - However, histogram construction takes time
 - Not suitable for video

Gallo, O., Tico, M., Manduchi, R., Gelfand, N. and Pulli, K., 2012, May. 'Metering for Exposure Stacks', In *Computer Graphics Forum* (Vol. 31, No. 2, pp. 479-488).

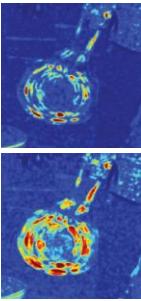
Metering Combined with Patch-Based Reconstruction

- **Solution for HDR video capture on mobile devices**
- **Uses previously captured frames for (partial) metering**
 - Steps up and down through exposure times based on histogram and motion analysis
- **Algorithm outline:**
 - Consider 2 previous frames
 - Estimate motion
 - Define threshold of ‘allowed’ under/over exposed pixels
 - Use motion and under/over exposure information to determine how to expose the next frame
- **Off-line processing: adapted form of patch-math**
- **Result: HDR video with frame rate identical to capture rate**

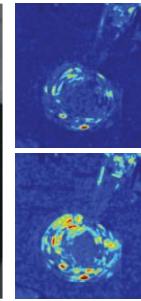
Gryaditskaya, Y., Pouli, T., Reinhard, E., Myszkowski, K. and Seidel, H.P., 2015, July. Motion Aware Exposure Bracketing for HDR video. In *Computer Graphics Forum* (Vol. 34, No. 4, pp. 119-130).

Example results

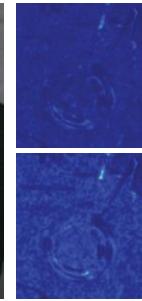
[-3, 0]



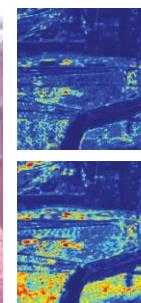
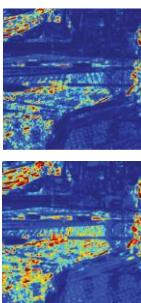
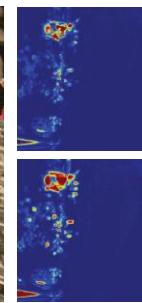
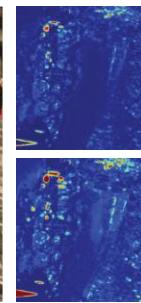
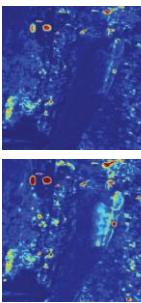
[-2,0,2]



With metering



Ground truth



Potential Problems with Temporal Bracketing

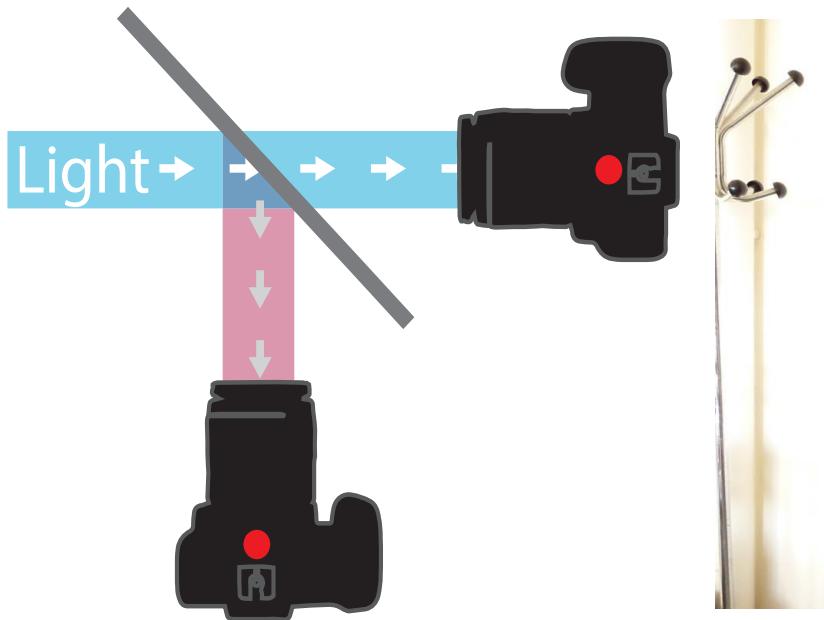
- **Noise**
 - Division by exposure time may amplify noise
- **Image alignment**
 - Hand-held exposures may be misaligned
- **Ghosting**
 - Objects may move between exposures
 - When reconstructing the HDR image, some information will be missing between exposures
 - Leads to ghosting artefacts

Spatial Bracketing

- Light can be split and redirected to different sensors
- Split may be done in front of the lens or behind the lens
 - Use multiple cameras, placed in front of a beam splitter
 - Split light after the main lens in a single camera containing a beam splitter
- Exposures are captured simultaneously
 - Optical filters control the amount of light reaching each sensor
- Advantages
 - No temporal mismatches
 - No ghosting

Example: NEVEX HDR Capture

- Based on modified stereo capture rig
- Beam splitter redirects light to second camera
- Cameras must be synchronized and aligned
- Disadvantage: cumbersome post-processing



Example: Contrast HDR Camera

- **Capture multiple LDR images**
 - Beam splitter redirects light to various sensors
 - Beam splitter attenuates light by different amounts dependent on direction
- **Structurally identical images**
- **In theory any sensor could be used**
- **Large dynamic range**
- **Single camera lens**
- **Light-efficient**



Tocci, M.D., Kiser, C., Tocci, N. and Sen, P., 'A Versatile HDR Video Production System', ACM *Transactions on Graphics (TOG)*, 30(4), 2011

Summary

- **Multi-camera approaches impractical**
 - Multiple cameras with lenses means high material costs
 - Alignment / registration means significant (possibly manual) postprocessing
- **Multi-exposure approaches artifact-prone**
 - Ghost removal will be necessary in practical situations
- **Spatial bracketing provides good trade-off**
 - Multiple sensors are factory-aligned
 - All technology hidden from the user: operation should be no more straightforward
- **Synthesis from SDR content**
 - Most likely professionally employed solution for the foreseeable future (episodic content, movies, live broadcast)
 - In essence, this is the inverse of tone reproduction
 - Discussed later in this tutorial

TONE REPRODUCTION

Tone Reproduction

- Consider an HDR image that has a range of values that is much larger than a given display can display
 - Some range reduction will need to be applied
 - On some sense this means loss of information must occur
- The main research question is which information must be maintained, and which information is visually less pertinent and could be removed
 - Preserve details?
 - Preserve contrast?
 - Preserve visual appearance?

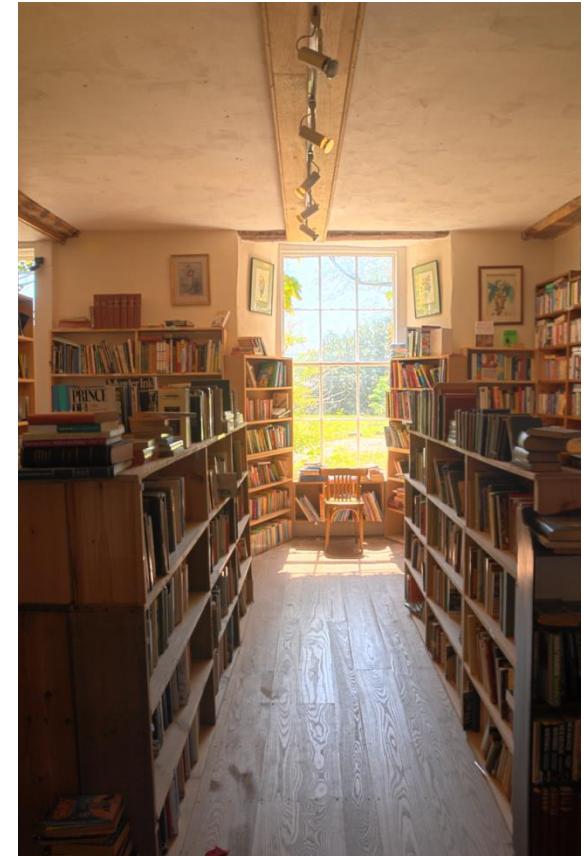
Why do we need tonemapping?



Linear compression

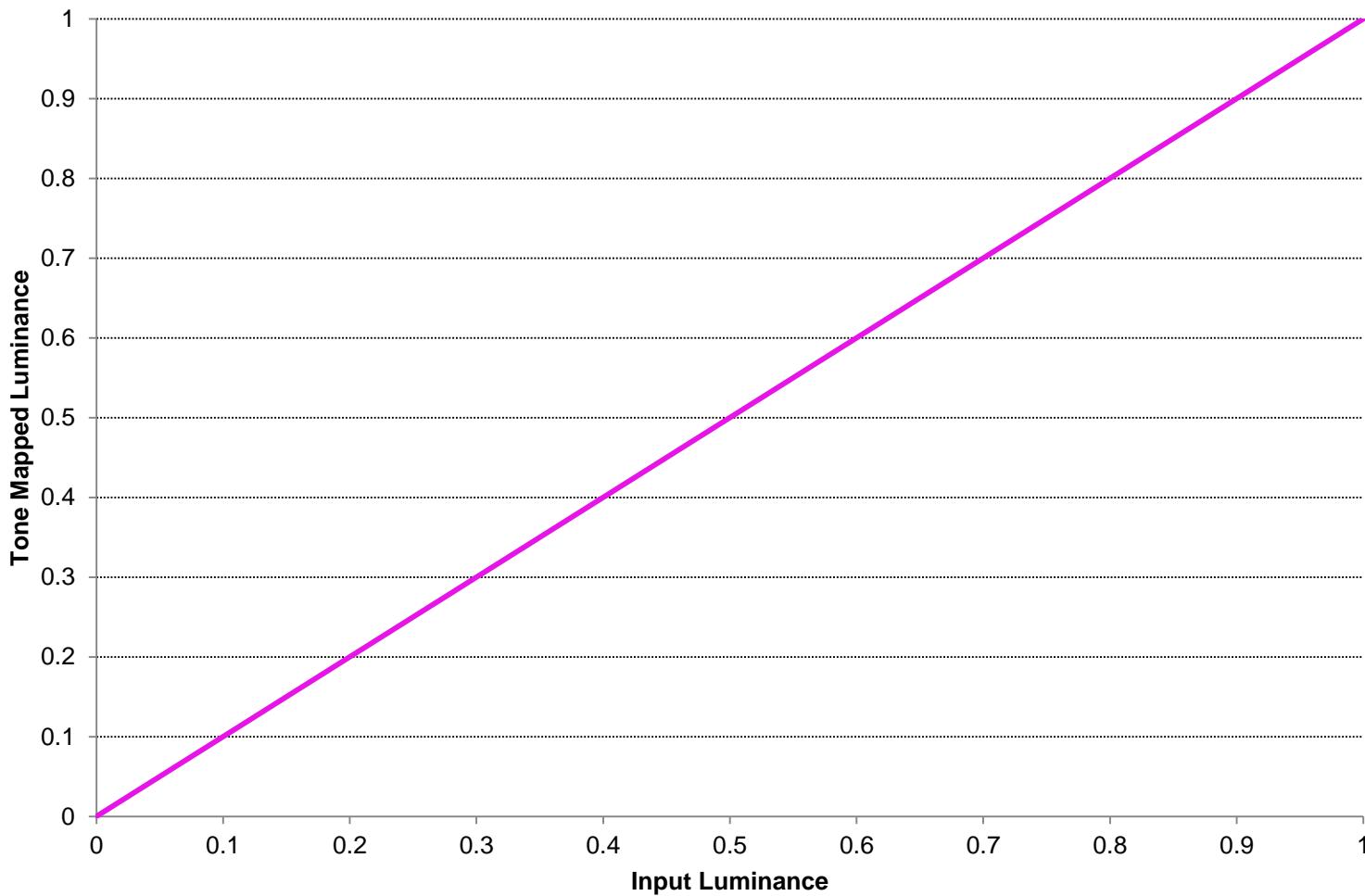


HDR luminance color map
(4 orders of magnitude - 13 f-stops)



Tonemapped

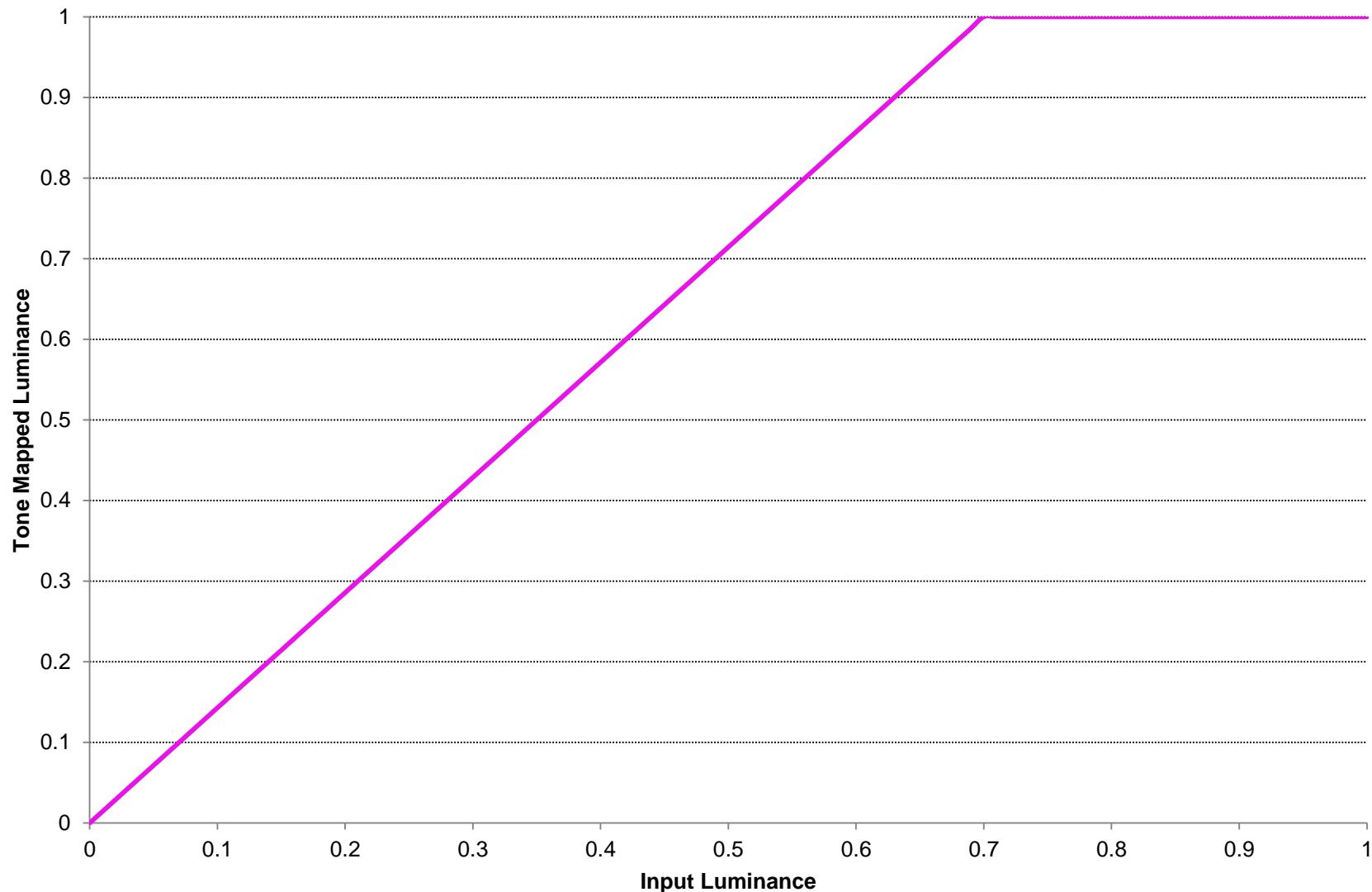
Linear Scaling



Linear scaling



Linear + Clamping

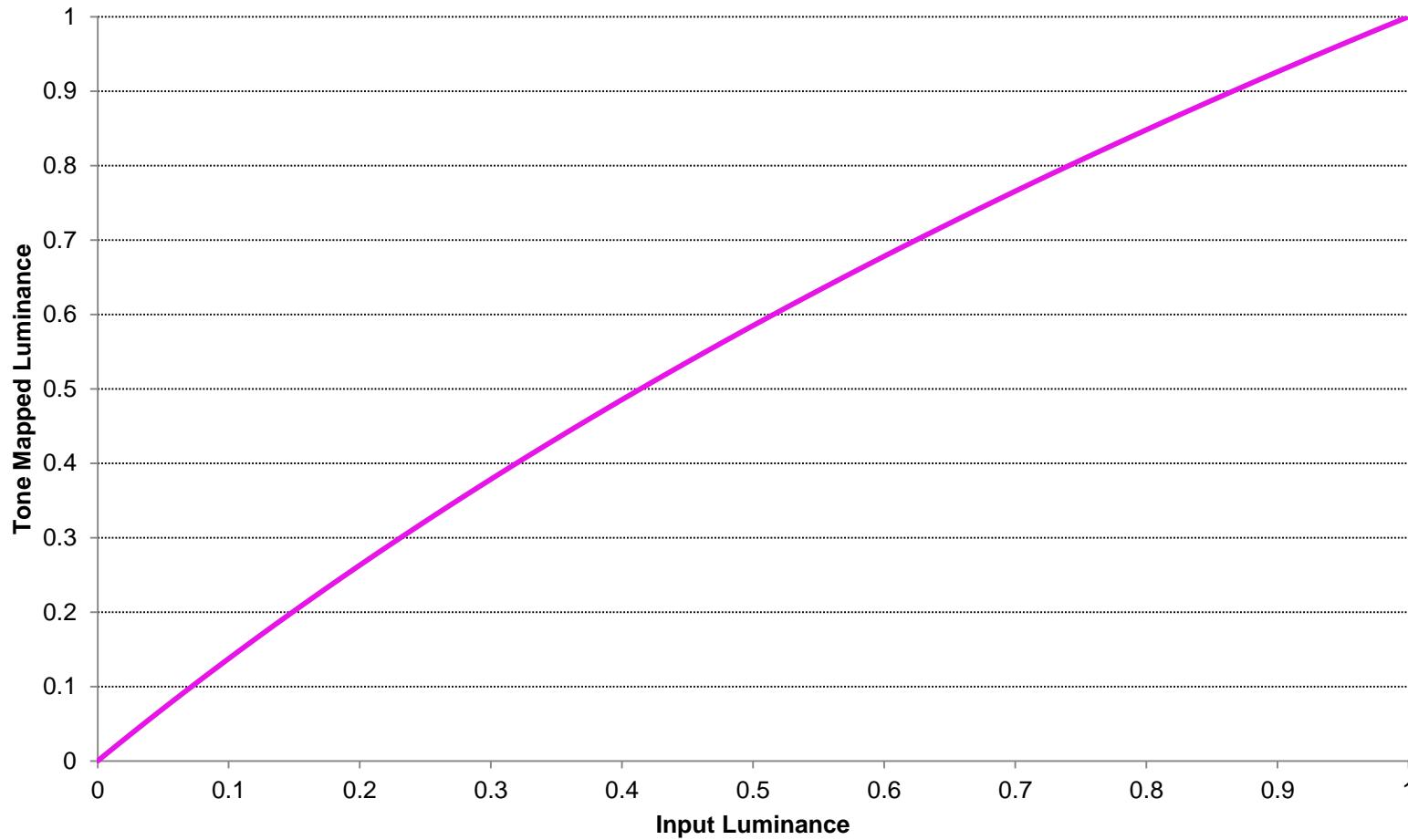


Linear + Clamping



Logarithm

$$L_d = \log(L + 1)$$



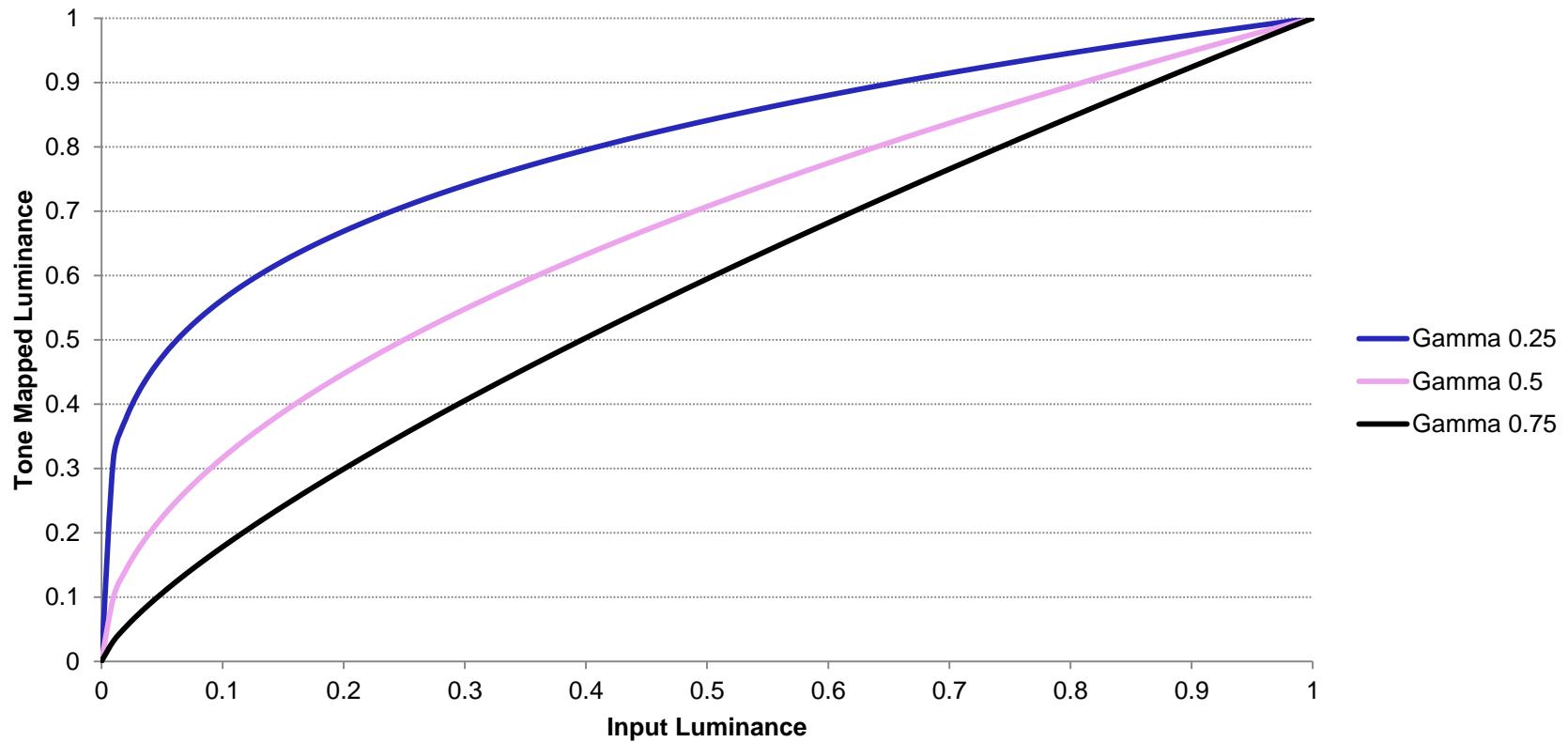
Logarithm



Power Function (gamma)

- Smaller power gives more compression

$$L_d = L^\gamma$$



Power Function – gamma = 0.75



Power Function – gamma = 0.50

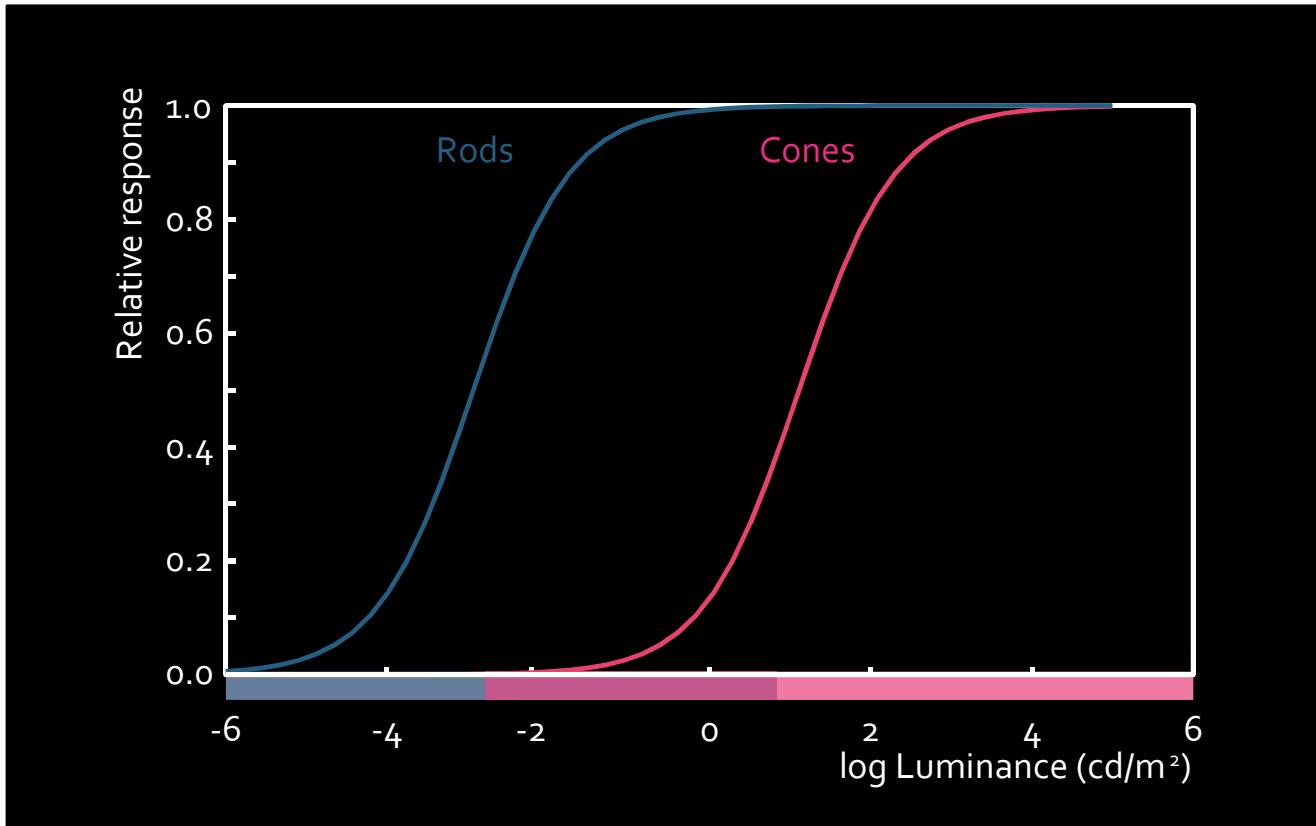


Power Function – gamma = 0.25



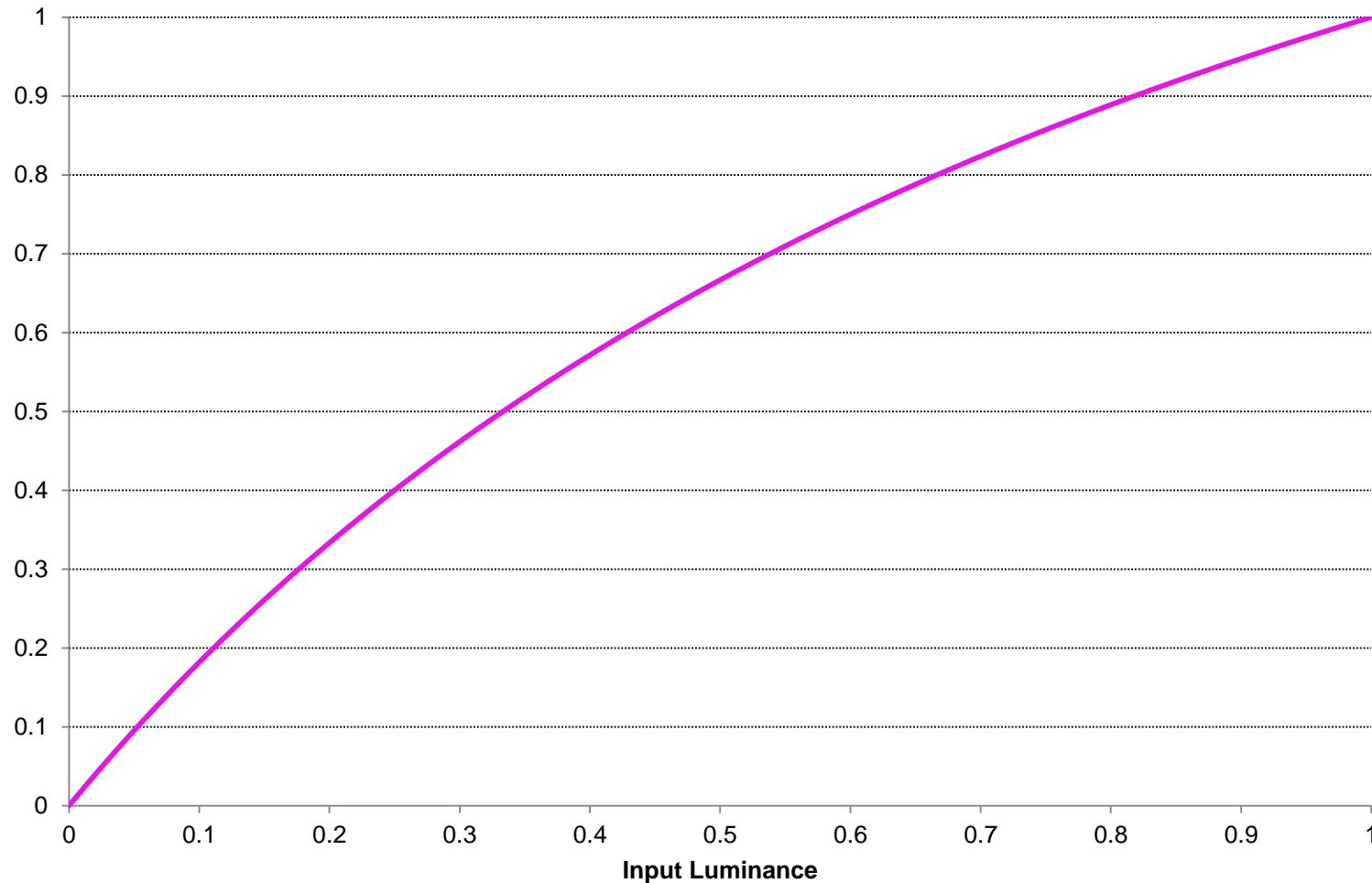
Perception-based TMOs

- Human visual system faces similar problem
- Photoreceptors compress light non-linearly



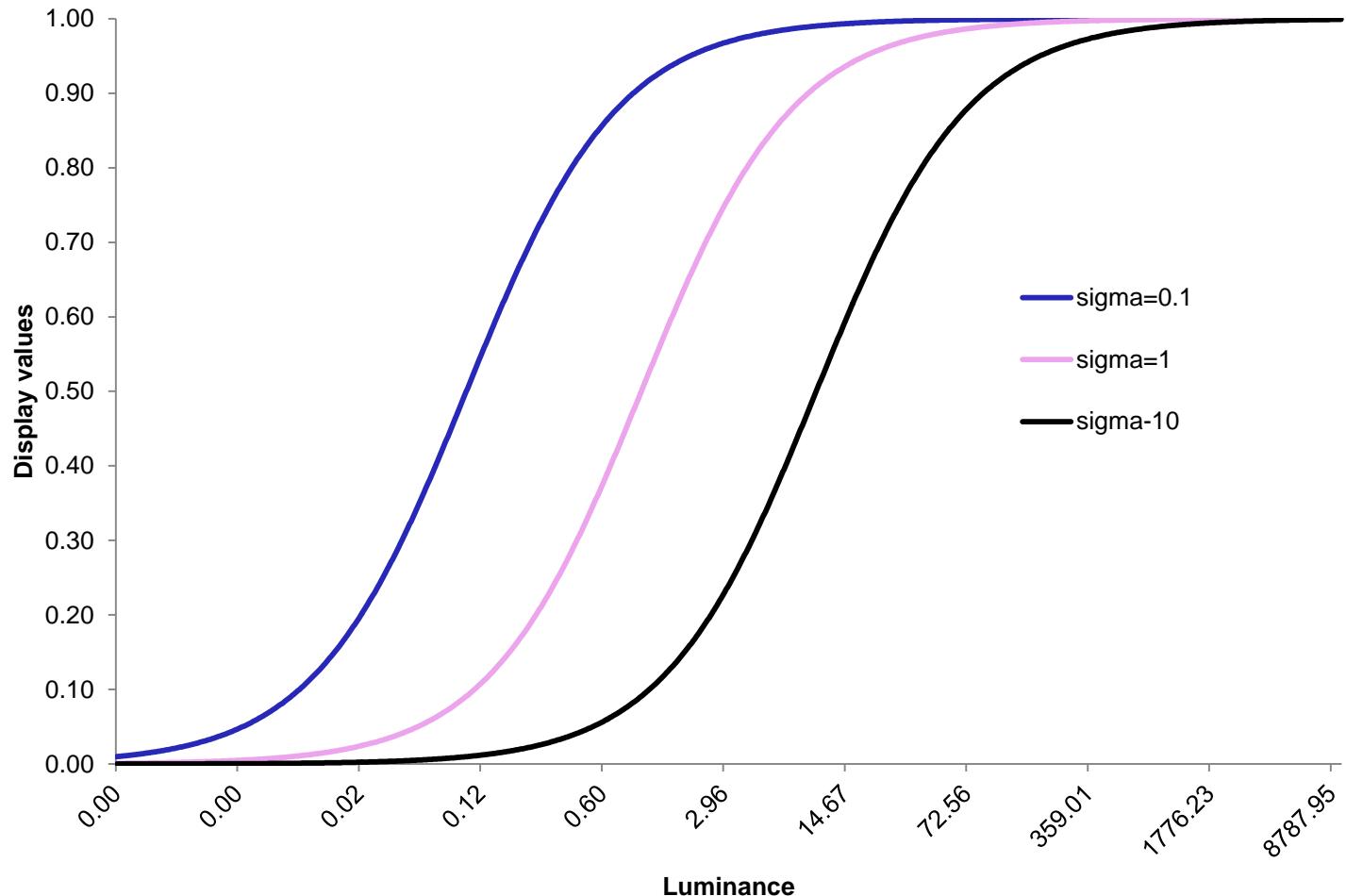
Sigmoid

$$L_d = \frac{L}{L + \sigma}$$



Sigmoid

$$L_d = \frac{L}{L + \sigma}$$



Sigmoid - $\sigma = 10$



Sigmoid - $\sigma = 1$



Sigmoid - $\sigma = 0.1$



Perception-based TMOs



Sigmoidal
(Reinhard 2002, 2005)



Display-adaptive
(Mantiuk 2008)



Full photoreceptor model
(Pattanaik 2000)

Global operators

- **Recap:**

- Easy to implement!
- Real time implementations possible
- Some provide very reasonable amounts of compression and lead to plausible results
- Useful for medium to high dynamic range images
- No local compression means flat appearance

Global to local

- Global



Global to local

- Local



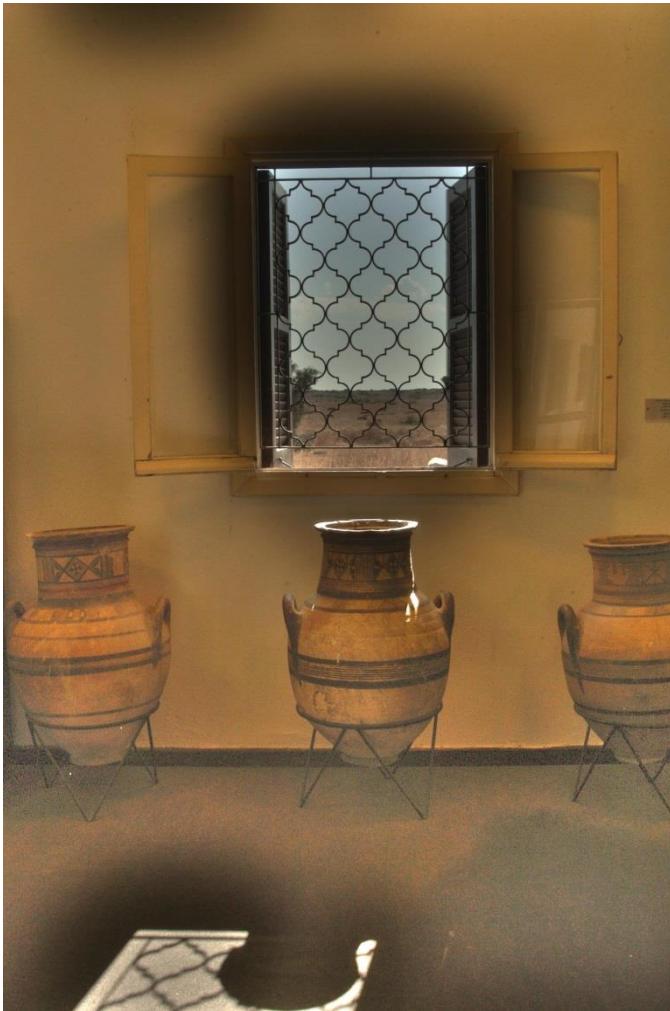
Global to local

- Simple solution:
- Replace global parameter (e.g. σ) with local average
- For sigmoid: σ based on local neighborhood determined through low pass filtering:
 - $L_d(x, y) = \frac{L(x, y)}{L_{LPF(x, y)} + L(x, y)}$
- How do we decide the size of local region?

Local Tone Mapping through Low Pass Filter

- For each pixel the size of the LPF kernel should be such that it does not overlap with sharp discontinuities
- But we still want to average over the largest spatial area for which the above is true (which may be different for each pixel)
 - Flat areas = large possible kernel
 - High contrast areas = smaller kernel
- Too large a kernel can cause halos!
- Too small a kernel reduces local contrast

Halos



How to compute?

- Multi-scale analysis using difference of Gaussians to compute local kernel size (Reinhard 2002, Ashikhmin 2002)
- Multi-scale decomposition (bilateral filter, mean shift algorithm, weighted least squares filtering etc)
- Distance to light sources (Reinhard et al 2012)

Multi-layer Decompositions

- Instead of preserving local detail directly, it can be removed first and then added back after compression
- Two or more layer decompositions
 - Coarse levels encode global contrast
 - Finer levels encode local contrast and detail
- Different creative effects can be achieved by compressing each level differently

Base/Detail Decomposition

- Split image into base and detail layers
- Base layer: image luminance filtered using edge stopping filter
- Detail layer: residual



Base



Detail

Base/Detail Decomposition



Gradient Domain Compression

- **Compute image gradients in log space**
- **Large gradients = large contrasts**
 - By attenuating only large gradients, high contrasts are compressed but local contrast is preserved
- **Reconstruct image by integrating gradients**
 - By numerically solving a Poisson equation



Fattal, Raanan, Dani Lischinski, and Michael Werman, 'Gradient Domain High Dynamic Range Compression', *ACM Transactions on Graphics*, 21 (3), 2002.

Gradient Domain Compression



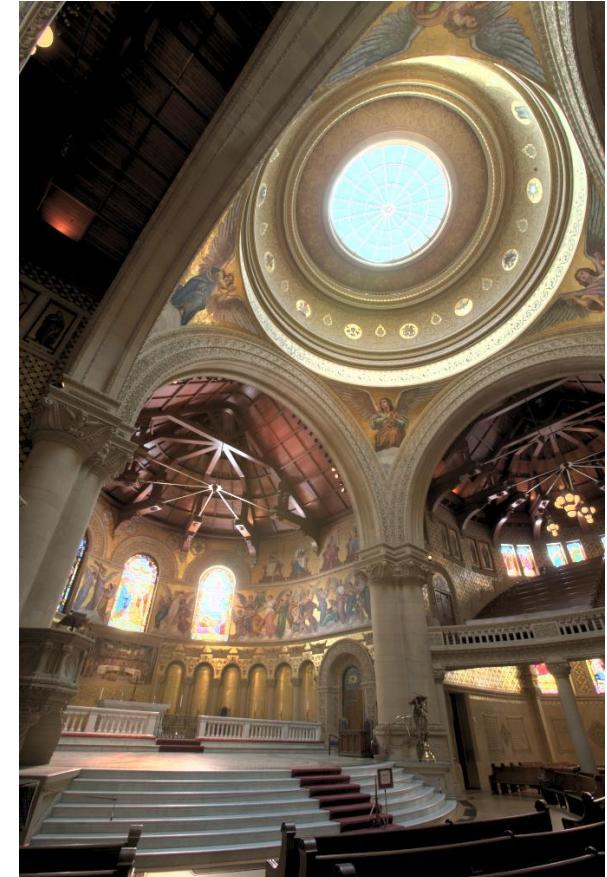
Informal Comparison



Linear scaling

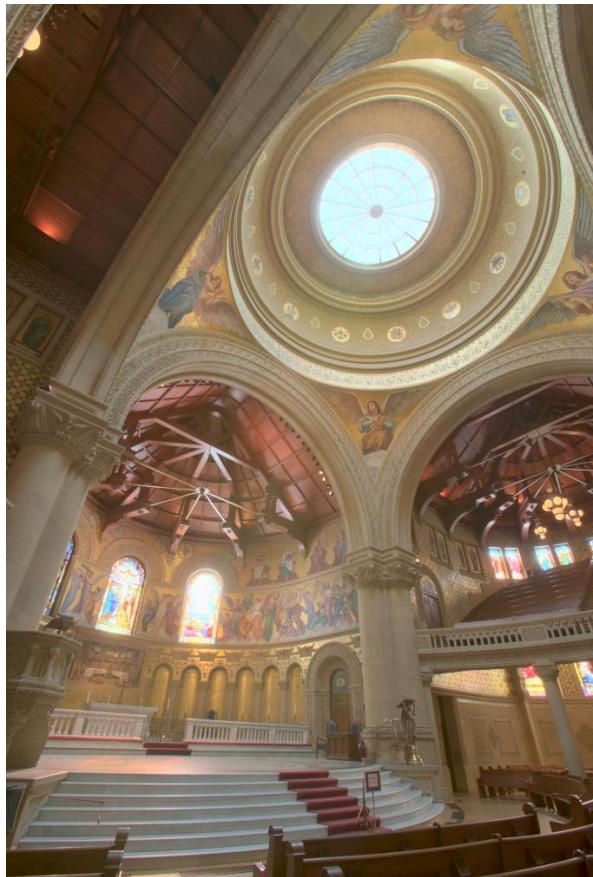


Linear with clamping

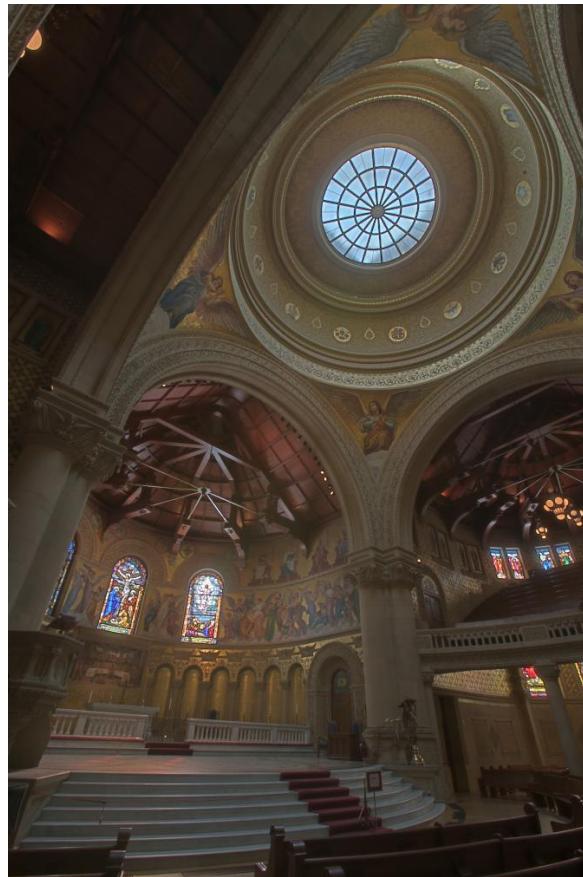


Linear with clamping (pct)

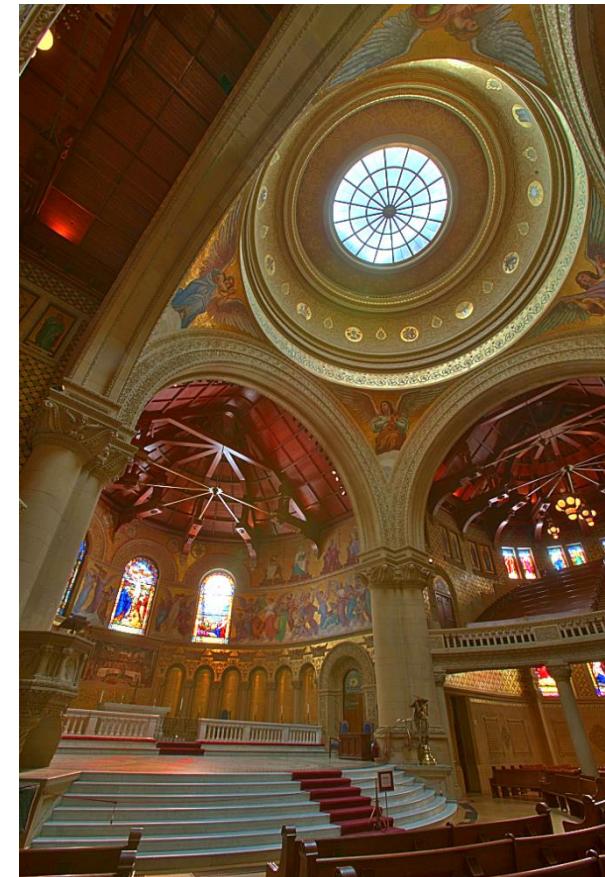
Informal Comparison



Reinhard 2002

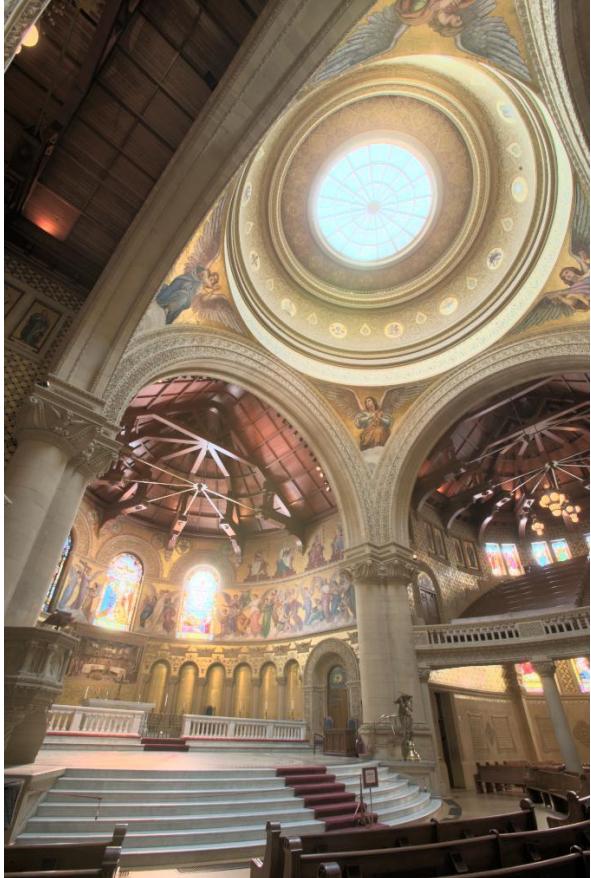


Ashikhmin 2002

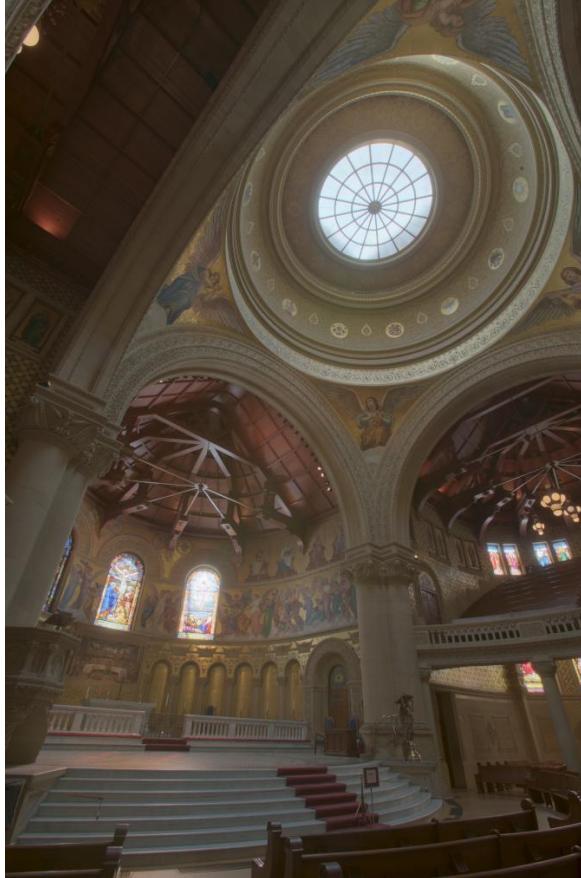


Li 2005

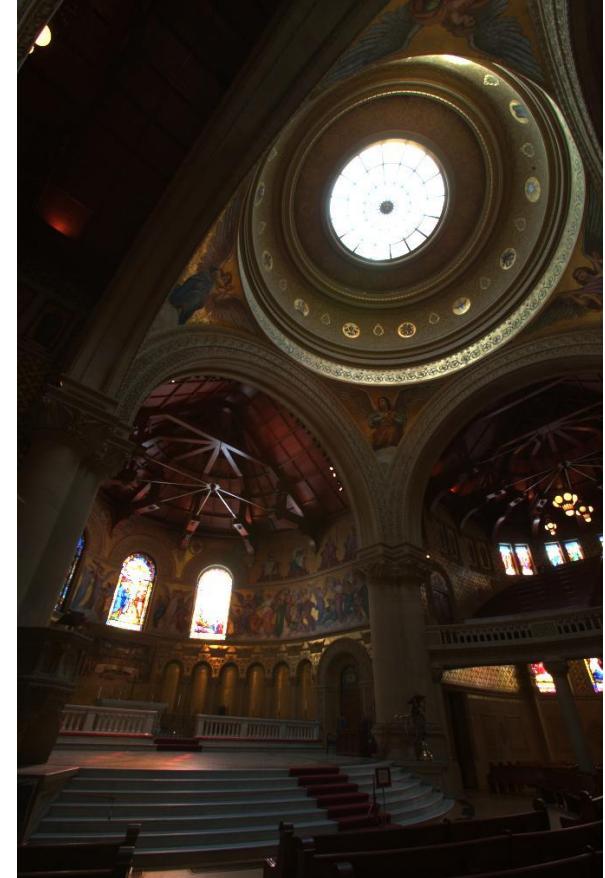
Informal Comparison



Histogram adjustment



Photoreceptor-based

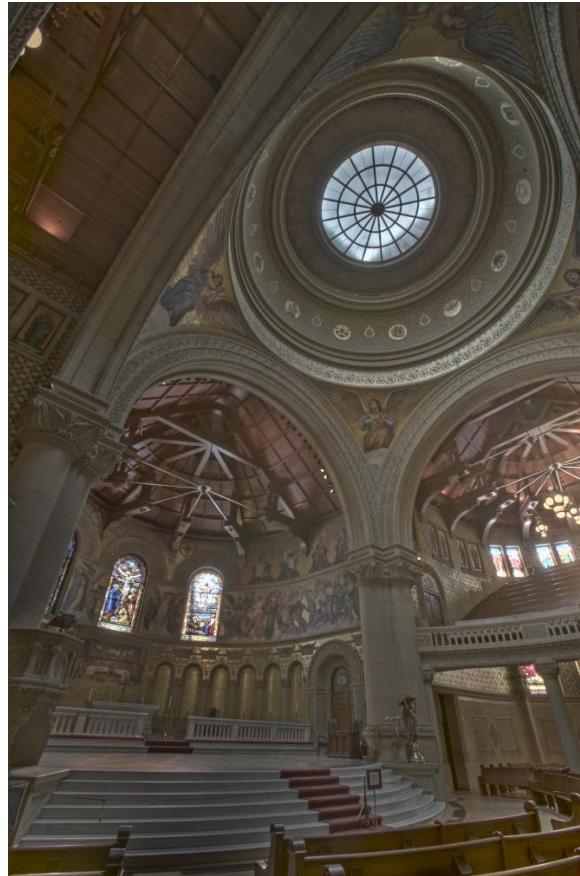


Tumblin-Rushmeier

Informal Comparison

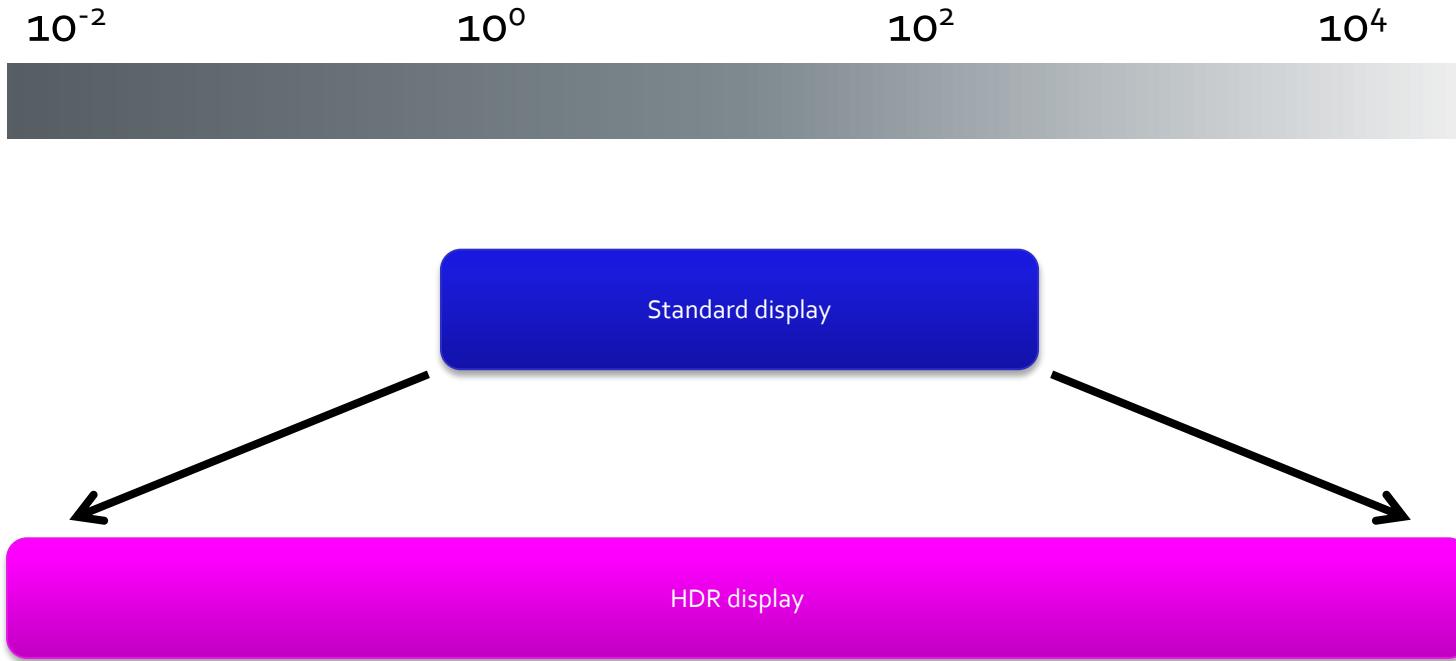


Bilateral filter



Gradient compression

Inverse Tone Mapping



Goal:

Increase the dynamic range of content to match that of an HDR display, to improve visual the experience while preserving artistic intent

Inverse Tone Mapping

- **Conceptually the reverse problem of tone mapping:**
 - Begin with a standard dynamic range (SDR) image
 - Recreate a high dynamic range image from it
- **Possible approach**
 - Many tone mappers use monotonically increasing curves
 - Take any such tone mapping operator, and invert it
- **Things to look out for**
 - Management of director's intent
 - Blacks should not be pulled apart
 - Mid-tones should not be raised too much
 - Artefacts should not be amplified, esp. noise

Inverse Tone Mapping

- What is the best way to expand the range?
- Several psychophysical studies conducted
 - Banterle et al.: Inverse sigmoid
 - Masia et al.: Image dependent gamma
 - Akyuz et al.: Linear
 - Global vs Local debate, like for tone mapping
- Technicolor:
 - <http://www.technicolor.com/en/solutions-services/technology/technology-licensing/hdr-technologies/hdr-intelligent-tone-management-solution>
- Opto-Electrical Transfer Functions (OETF)
 - SMPTE 2084
 - ITU-R BT.2100

Global Inverse Tonemapping

- **Single curve to expand luminance**

$$L_d(x, y) = f(L(x, y))$$

- **All pixels treated the same**
- **Examples:**

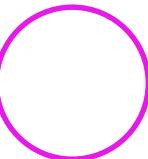
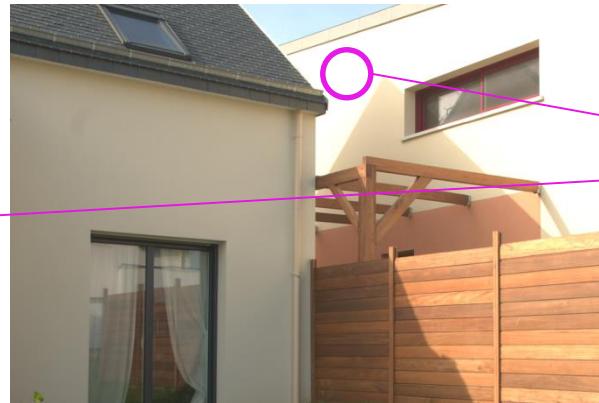
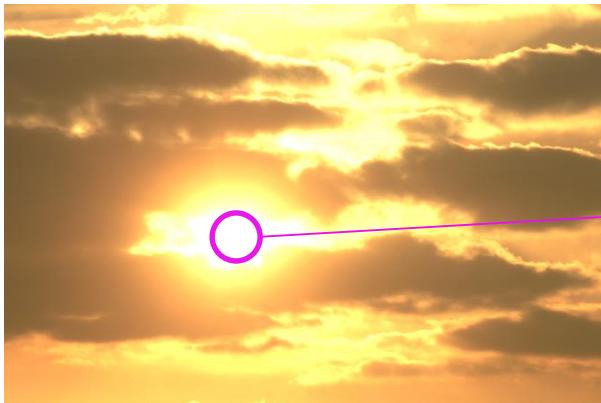
- Solve: $\left(\frac{\alpha}{\bar{L}_W} (1 - L_d(x, y)) \right)^2 + \frac{4\alpha^2}{\beta \bar{L}_W} L_d(x, y) \geq 0$

- Compute: $L_d(x, y) = L(x, y)^{g(L(x, y))}$

- **Computationally efficient, but perhaps not enough control in practice**

Local Inverse Tonemapping

- Detect highlight regions
 - Global expansion to all pixels
 - Extra expansion for highlights
-
- Challenge:
 - Distinguish specularities, light sources and diffuse white areas



Highlight Expansion

- Most methods dedicate most of the range to highlights
- Compute brightness map to determine location of highlights
 - Median cut (Banterle 2006)
 - Multi-scale analysis (Rempel 2007)
- Modulate expansion depending on brightness map

Inverse Tonemapping – Additional Considerations

- **How to deal with noise?**
 - Expanding content may also expand noise
 - Artefacts that were below visible threshold, may become visible
- **How to deal with compression artefacts?**
 - Compression algorithms are very efficient at keeping artefacts just below visible threshold
 - Even slight expansion may render such artefacts visible
- **How to deal with over-exposed areas?**
 - Over-exposed areas are by definition featureless
 - Expanding such areas will make them very conspicuous and distracting
 - ‘Declipping’ may be applied with some success

Summary

- **Tonemapping**
 - Much research has led to good, practical solutions
- **Inverse Tonemapping**
 - Research in this area remains sparse
 - Basic expansion functions are relatively straightforward to design
 - Dealing with amplification of artefacts remains a challenge

COLOR MANAGEMENT

Color Management for HDR

- Color appearance changes if we only modify luminance!



Original



Tonemapped
(no color correction)



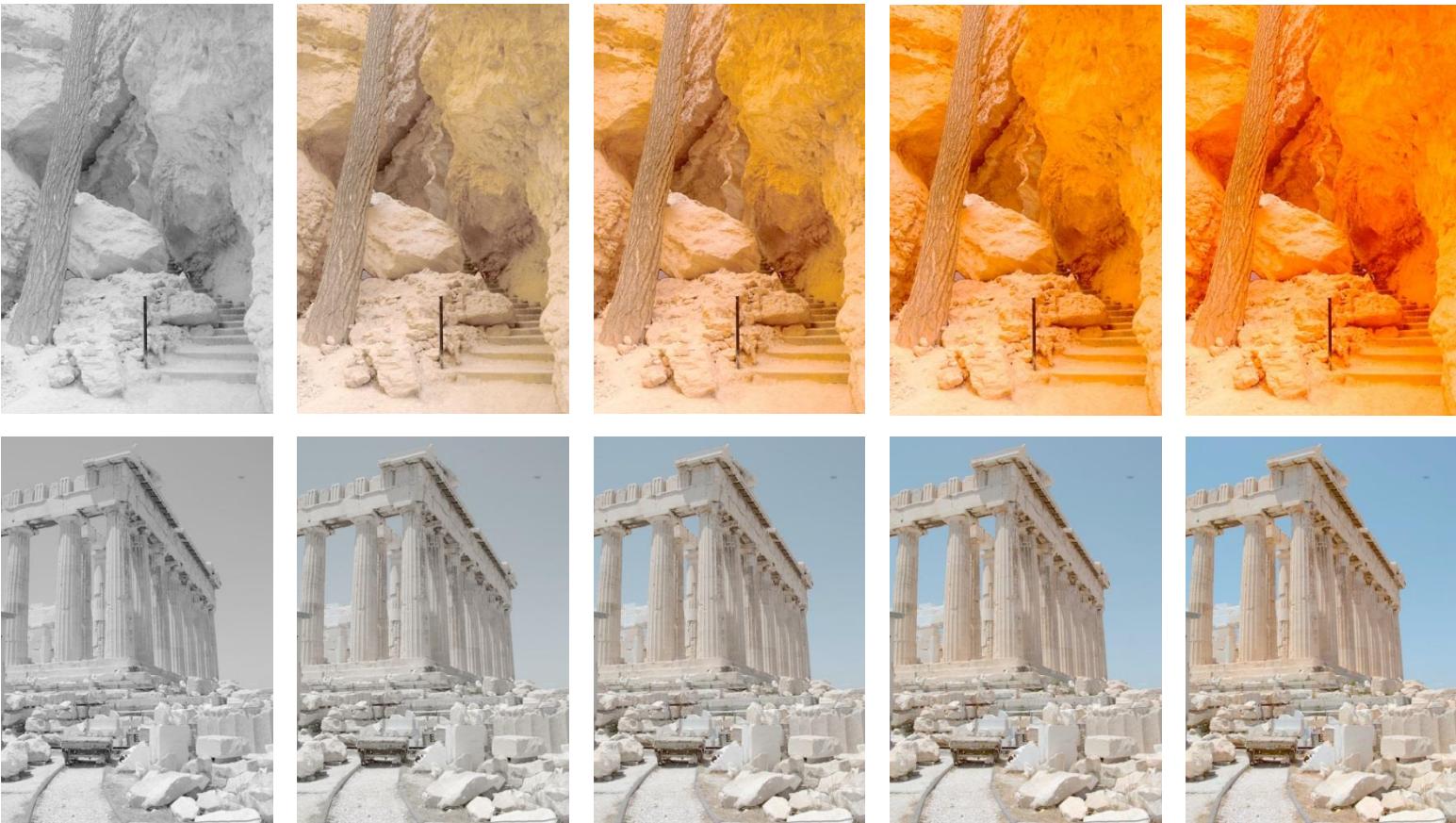
Tonemapped
(color correction)

Schlick Correction

- Exponent s controls saturation
 - Can cause luminance & hue shifts
-
- $C_{out} = \left(\frac{C_{in}}{L_{in}}\right)^s L_{out}$

C. Schlick, ‘Quantization Techniques for the Visualization of High Dynamic Range Pictures’, Eurographics Rendering Workshop, 1994

Schlick's Method



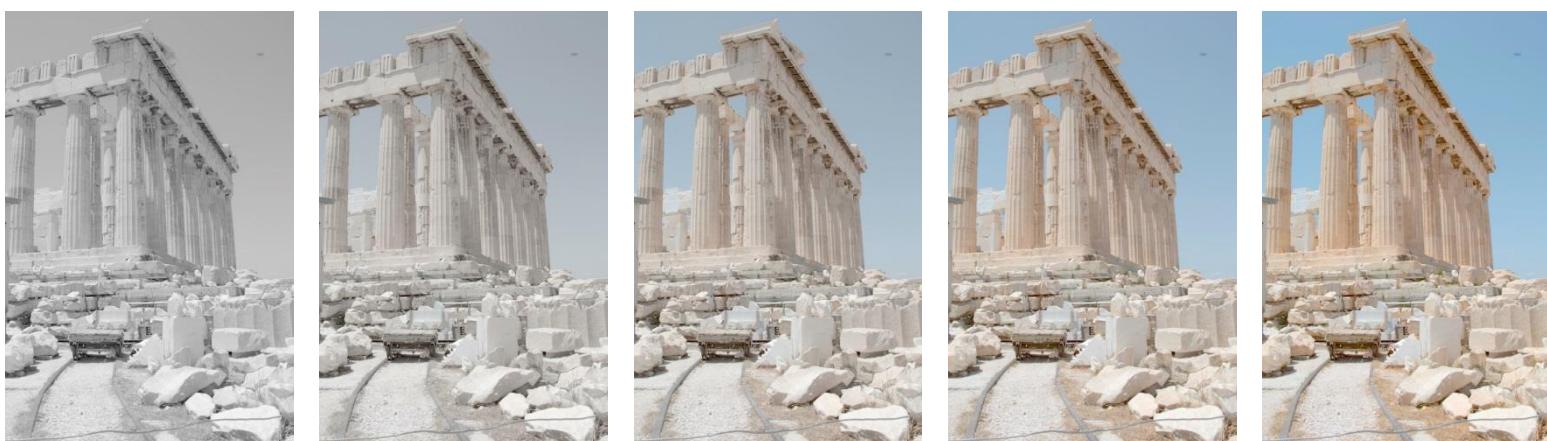
← Saturation parameter **s** →
lower higher

Mantiuk Correction

- Reduces luminance shifts
 - May cause hue shifts
 - Parameter s can be determined based on the slope of the tone mapping curve
-
- $C_{out} = \left(\left(\frac{C_{in}}{L_{in}} - 1.0 \right) s + 1.0 \right) L_{out}$

R. Mantiuk, R. Mantiuk, A. Tomaszewska and W. Heidrich,
'Color Correction for Tone Mapping', Eurographics 2009

Mantiuk's Method

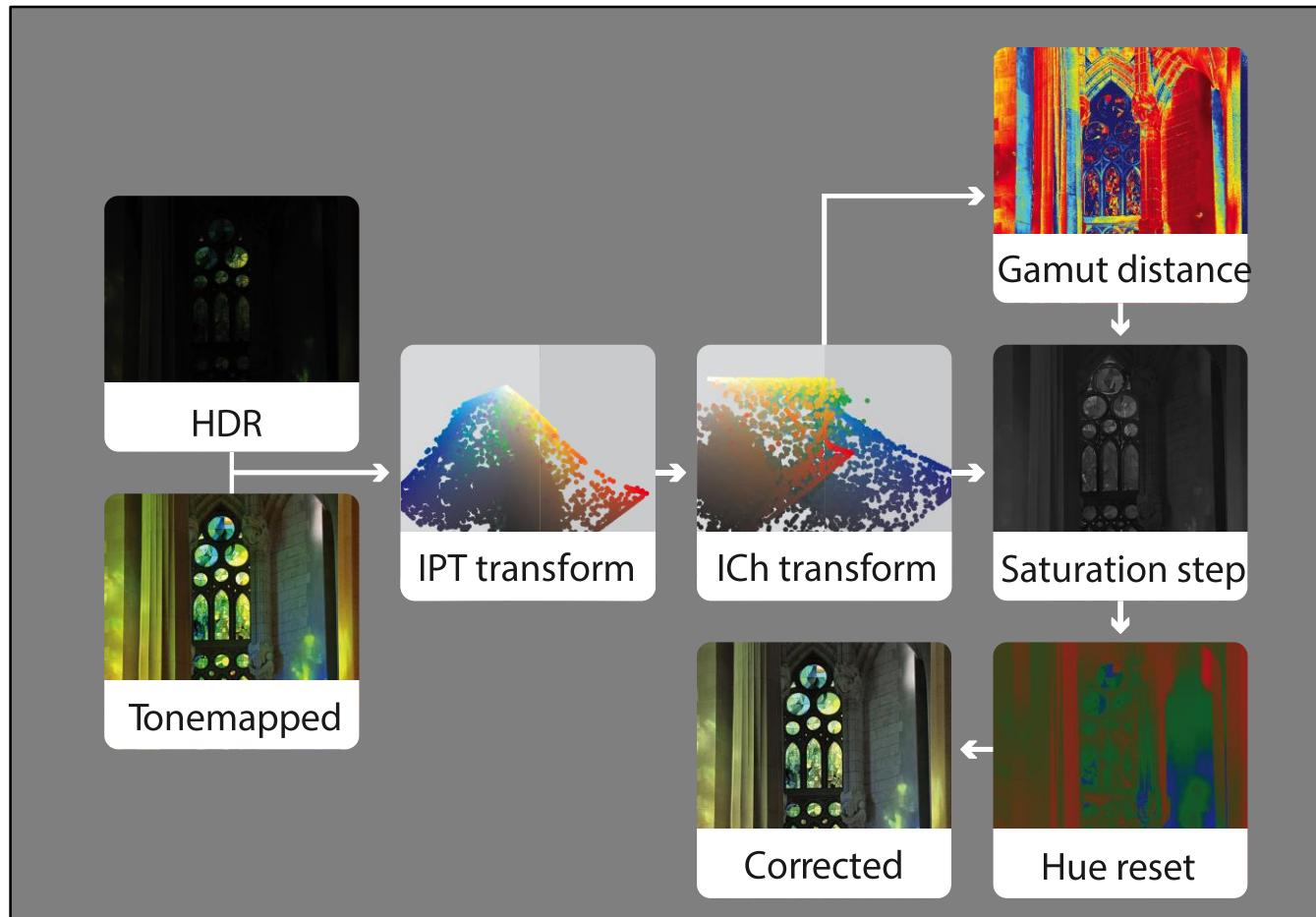


← lower Saturation parameter s higher →

Color Correction

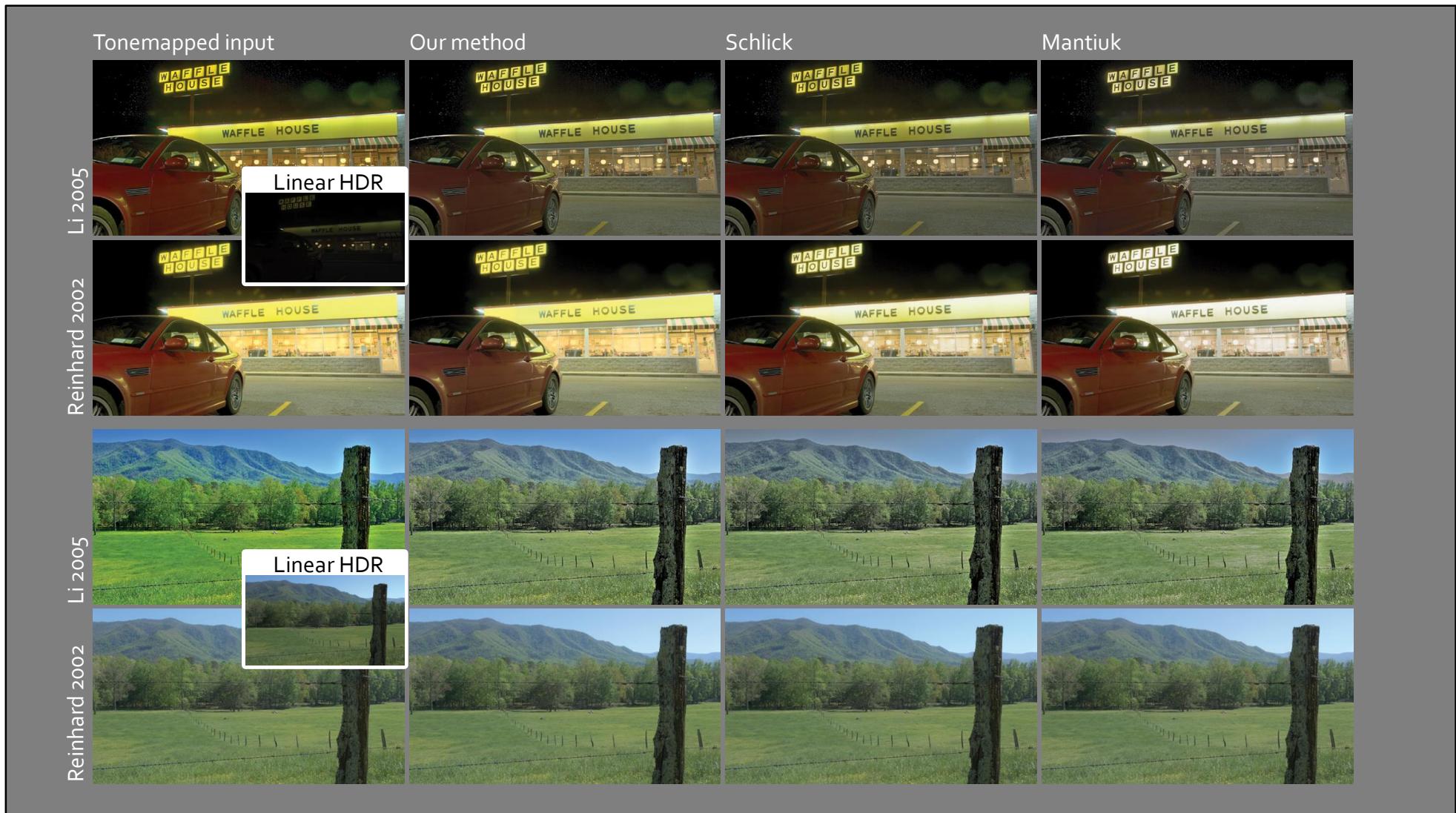
- Both Schlick and Mantiuk corrections require manual parameter adjustment
- Restricted to global tonemapping operators
- Alternatively, given input and tone mapped image we can analyze saturation and try to preserve it:
- $Saturation = \frac{Chroma}{Lightness}$

Color Correction using Input/Tone mapped Pair



Pouli T., Artusi A., Banterle F., Akyüz, Seidel H-P. and Reinhard E., 'Color Correction for Tone Reproduction', *Color and Imaging Conference*, 2013.

Comparisons



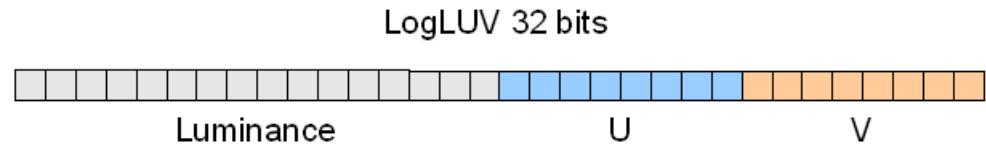
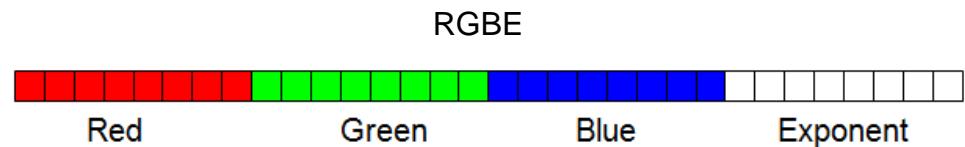
HDR VIDEO CODING

HDR formats

- **HDR images**

- Physical values of luminance
- Represented using floating point
- Cover full color gamut
- Significantly higher raw data rate
- Not appropriate for storage or transmission

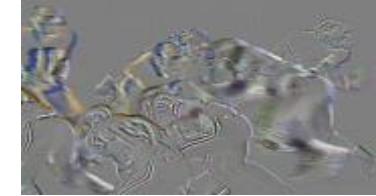
HDR Formats	bpp
OpenEXR (.exr)	48 (half-float), 96 (float)
RGBE, XYZE (.hdr)	32 (float)
LogLuv TIFF (.tiff)	24, 32 (integer)



Compression: general concepts

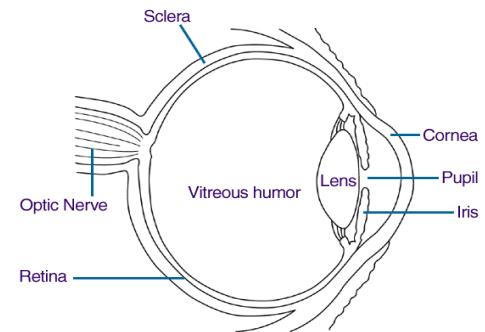
- Exploit the correlation in the data

- Reduce redundancies
 - Lossless



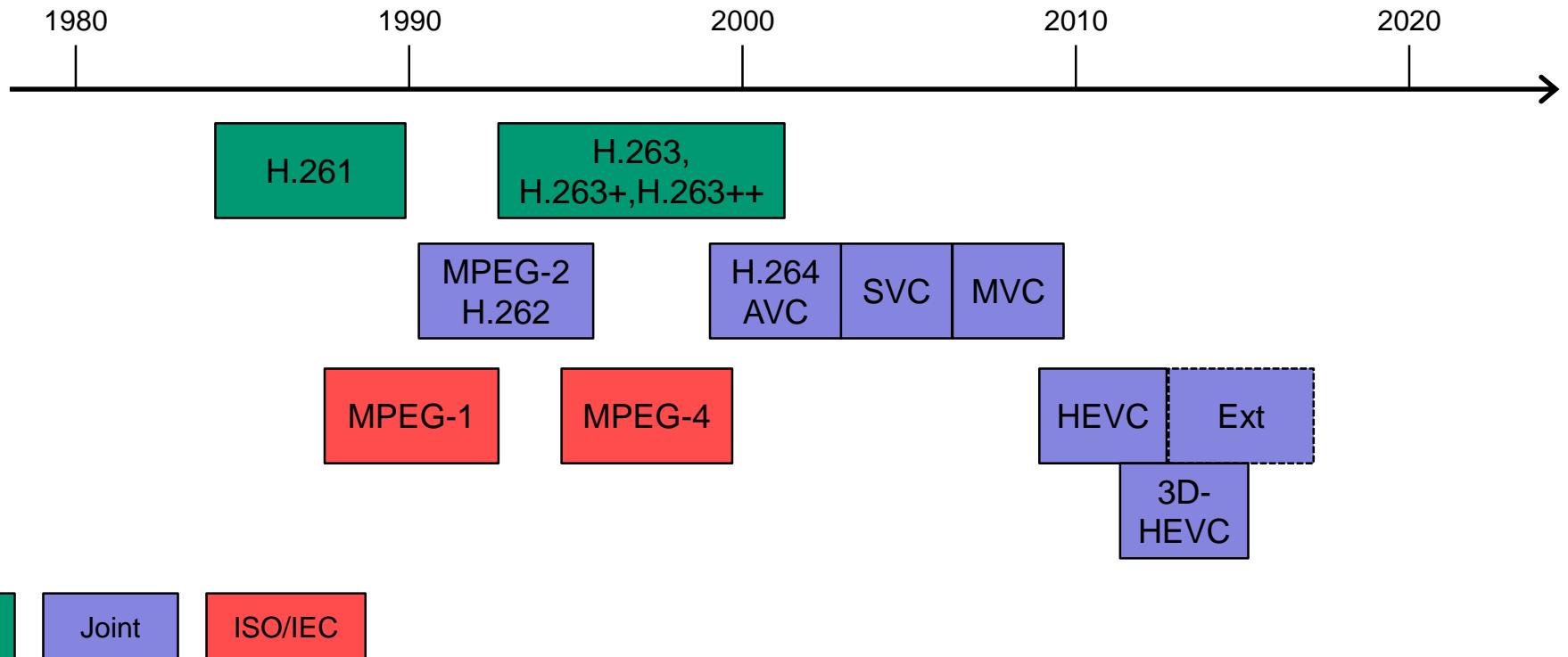
- Exploit the human visual system

- Remove imperceptible data
 - Introduce (hardly) noticeable distortions
 - **HDR: adapt human visual system models**



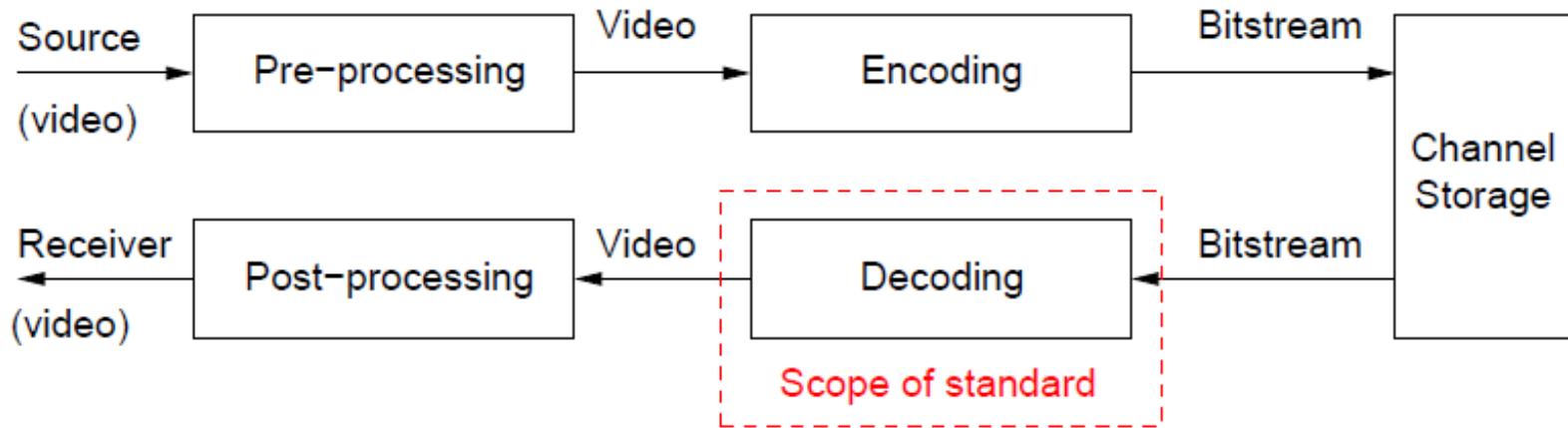
- Performance measured in terms of *rate-distortion*

Timeline of video coding standards



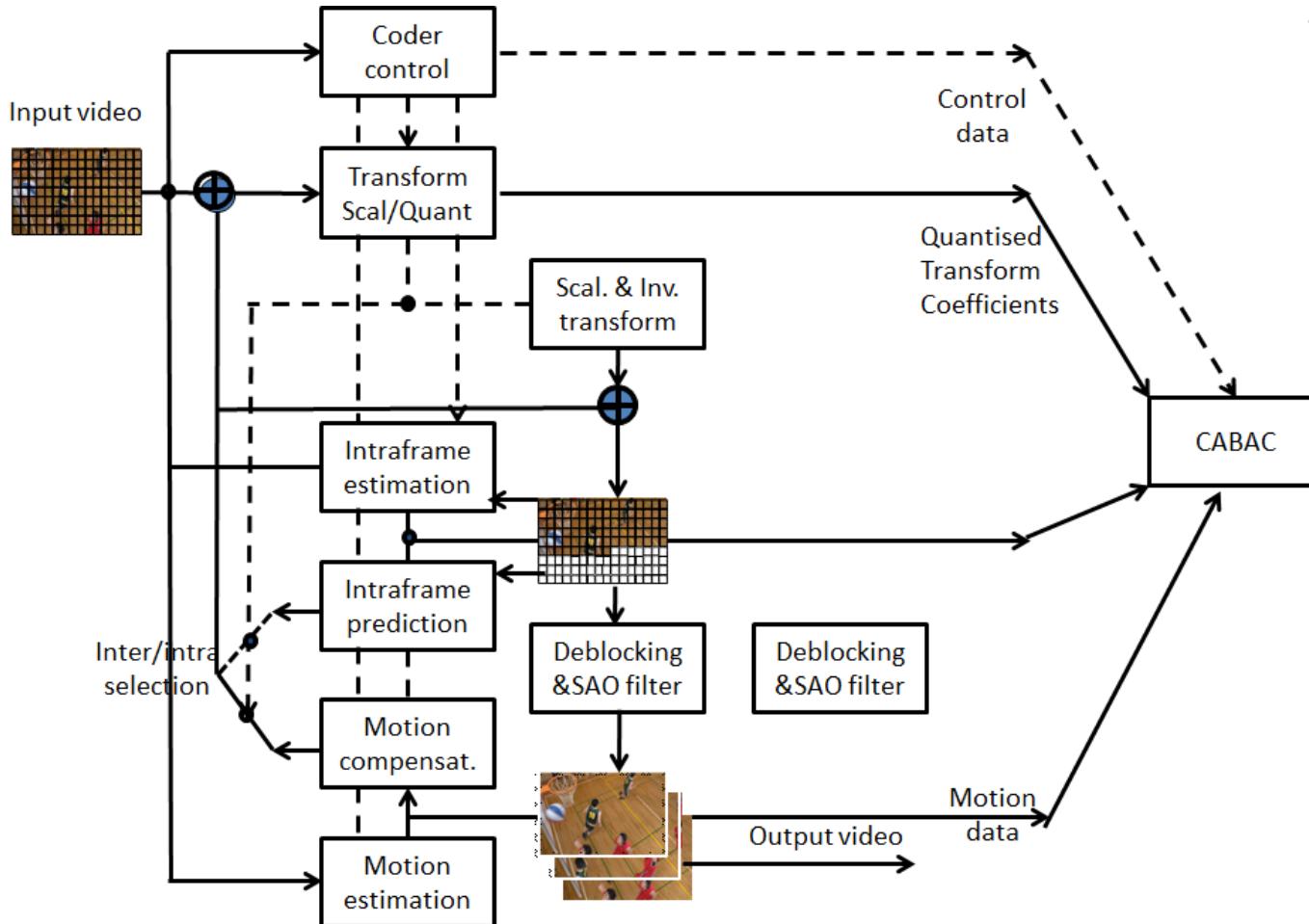
- **MPEG: Moving Picture Expert Group**
 - ISO: International Standardization Organization
 - IEC: International Electrotechnical Commission
- **VCEG: Video Coding Expert Group**
 - ITU: International Telecommunication Union

Scope of video coding standards



- **Minimum for interoperability**
 - Syntax and semantic of the compressed bitstream
 - Decoding process
 - Leaves room for competition in the market place and future improvements

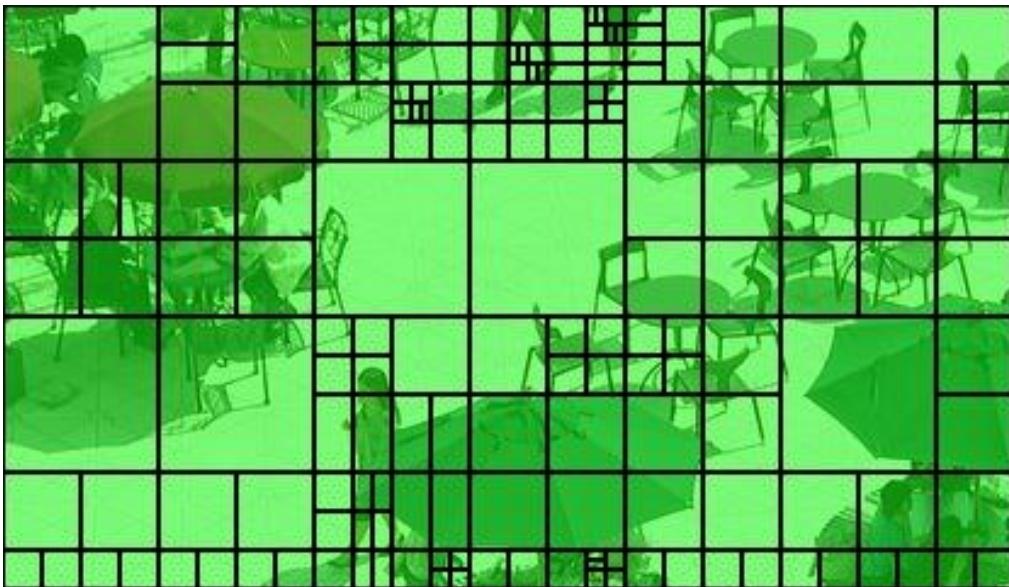
HEVC (MPEG-H – H.265)



- **Hybrid video coding**

- Transform coding:
DCT-like transform to compact the energy of the signal
- Predictive coding:
Intra or Inter (motion compensated) prediction
- Entropy coding:
context-adaptive binary arithmetic coding (CABAC)

HEVC

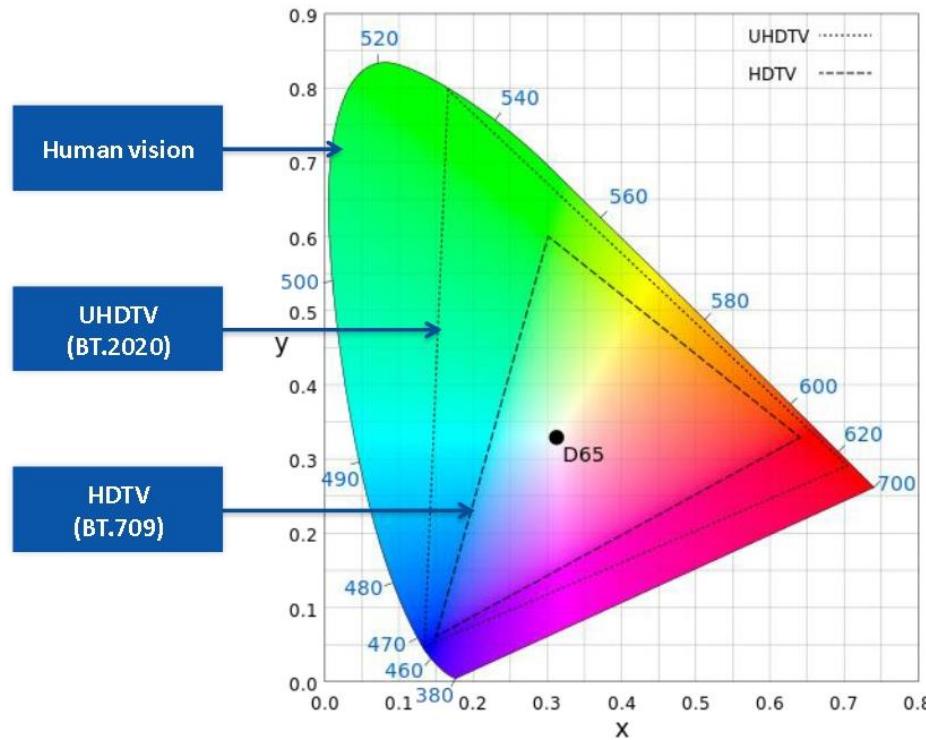


- **Quad-tree decomposition**
 - Coding Tree Units (CTU)
 - Coding Units (CU)
 - Prediction Units (PU)
 - Transform Units (TU)

- **First version completed in 2013**
 - Approx. 50% bit rate savings compared to its predecessor H.264/AVC at the same quality
 - Main profile: 8 bit depth, 4:2:0 chroma sampling
 - Main 10 profile: 10 bit depth, 4:2:0 chroma sampling -> UHDTV
- **Second version in 2014**
- **Range extensions (RExt)**
 - More than 10 bits per sample
 - 4:0:0, 4:2:2 and 4:4:4 chroma sampling
- **Scalability extensions of HEVC (SHVC)**
 - Encode once, decode at different resolution/quality levels
 - Backward-compatible base layer, enhancement layers
 - Interlayer prediction mechanisms
 - Bit depth and color gamut scalability, also handles different transfer function

Wide Color Gamut - BT.2020 vs BT.709

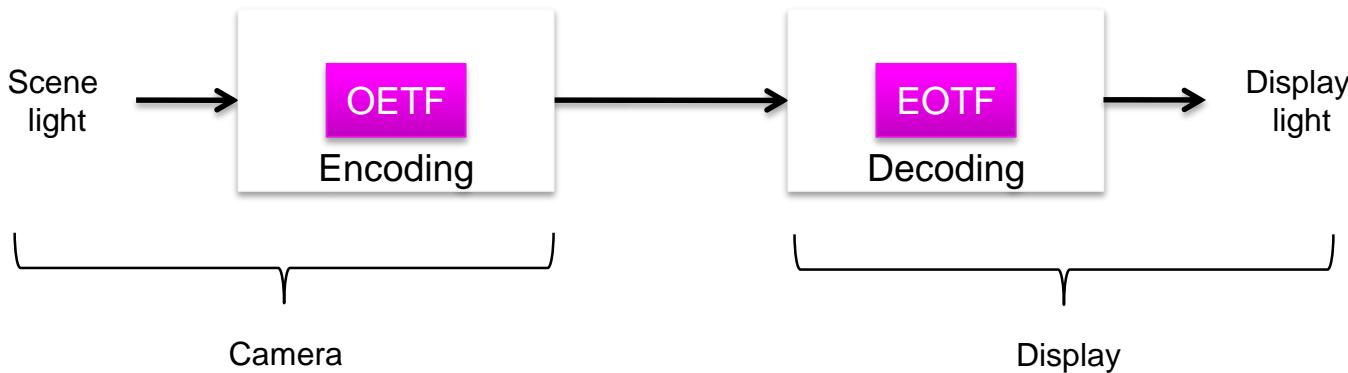
- **BT.709 specifies formats for HDTV**
- **BT.2020 specifies formats for UHDTV**
 - Resolution, frame rate, chroma subsampling, bit depth, and color space
 - BT.2020 covers a wider color gamut



CIE 1931 chromaticity diagram

OETF & EOTF

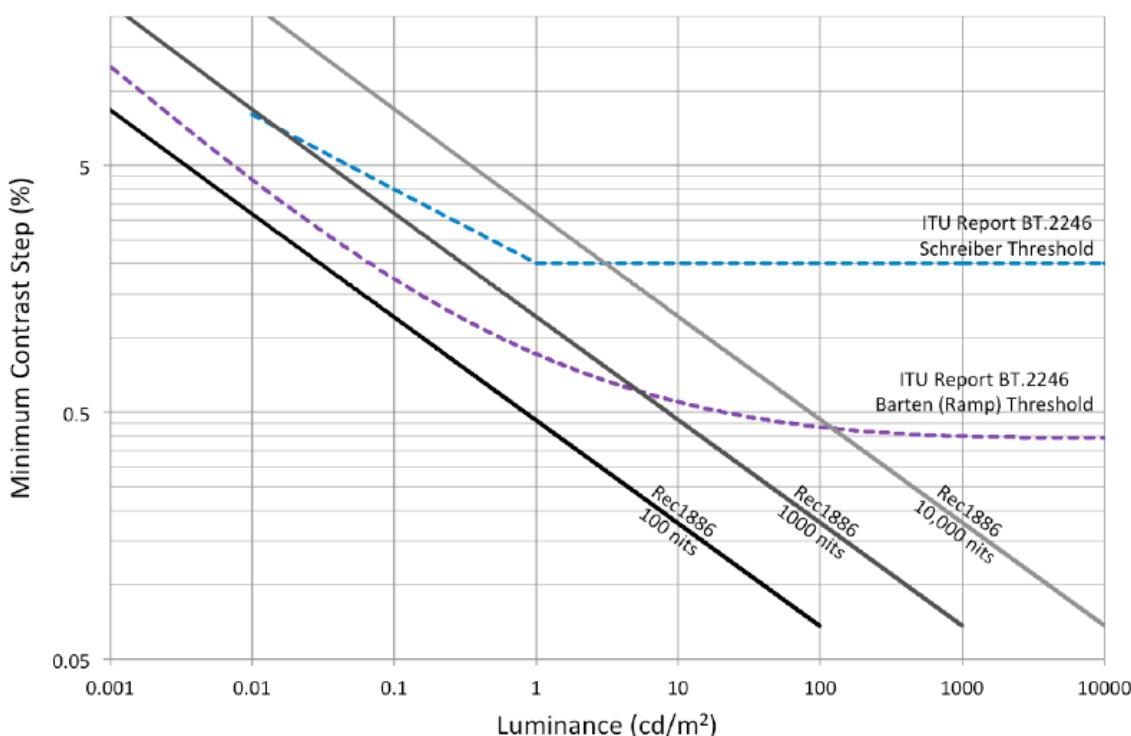
- **Opto-Electronic Transfer Function (OETF)**
 - Non-linear transfer function implemented within the camera
- **Electro-Optical Transfer Function (EOTF)**
 - Non-linear transfer function implemented within the display



BT.1886 – Gamma encoding

- **EOTF for television**

- Well suited for a peak level of 100 nits, i.e. below visual detection thresholds
- 12 bit gamma curve is above Schreiber and Barten thresholds for higher peak luminance levels



Schreiber threshold: Weber's law above $1 \text{ cd}/\text{m}^2$ and gamma nonlinearity below

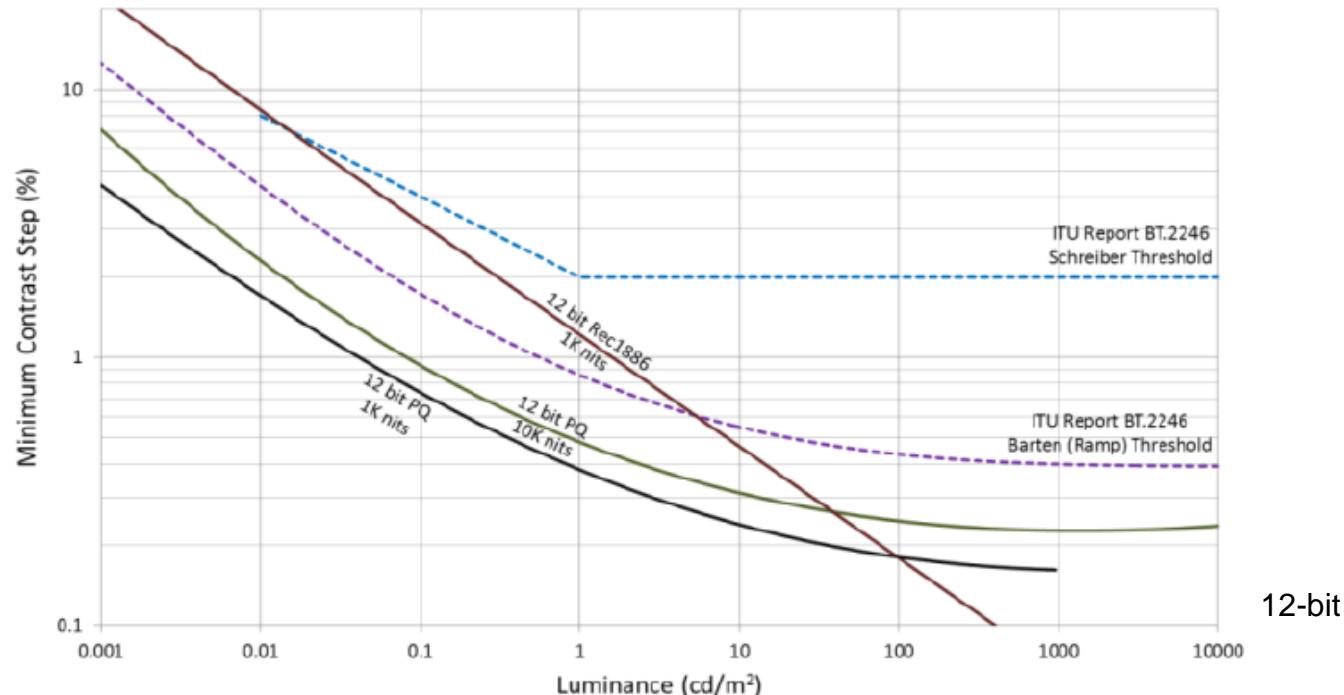
Barten threshold: based on model of Contrast Sensitivity Function

12-bit @
100 nits
1000 nits
10000 nits

Perceptual Quantizer (PQ) - SMPTE ST 2084

- Derive an EOTF based on perception

- Maximize the dynamic range of the signal by setting each quantization step to be proportional to the Just Noticeable Difference (JND)
- Iterative EOTF computation, exploiting the Barten CSF model
- In the range 0 to 10000 nits

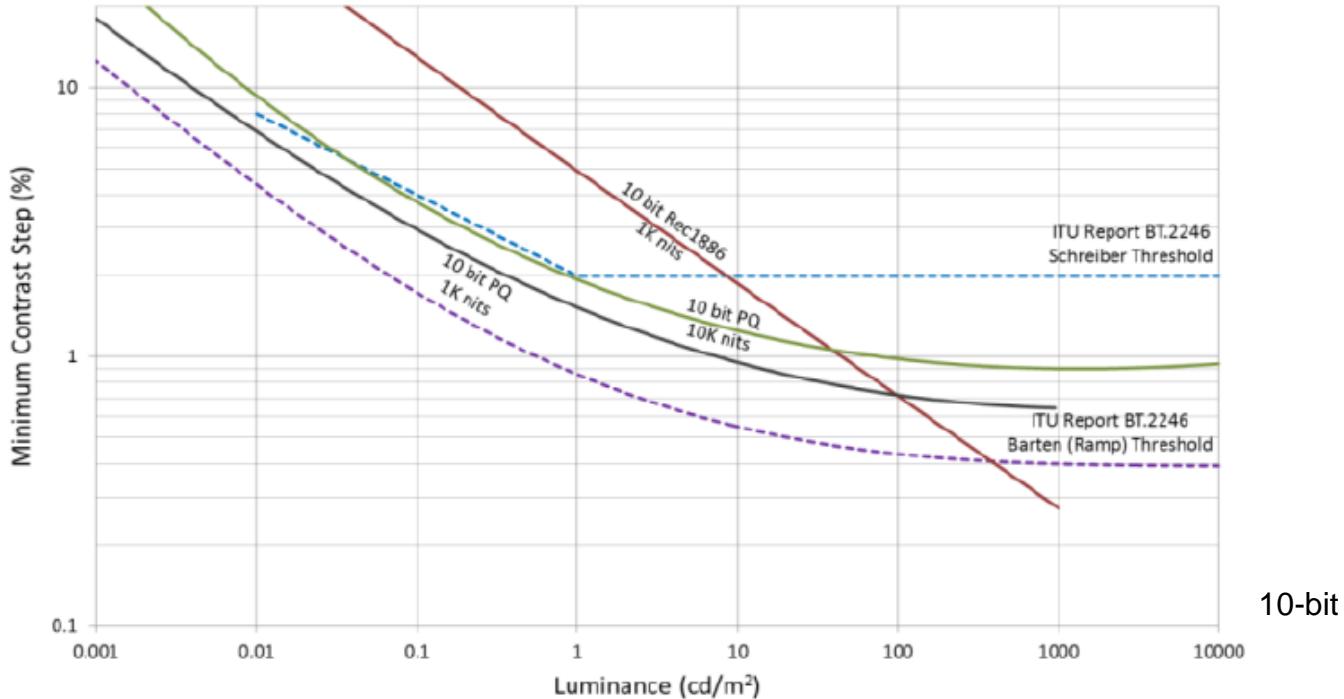


Can be approximated by the model, known as PQ (SMPTE ST 2084):

$$Y = L \left(\frac{V^{1/m} - c_1}{c_2 - c_3 V^{1/m}} \right)^{1/n}$$

12-bit PQ remains below perceptual thresholds

Perceptual Quantizer (PQ) - SMPTE ST 2084



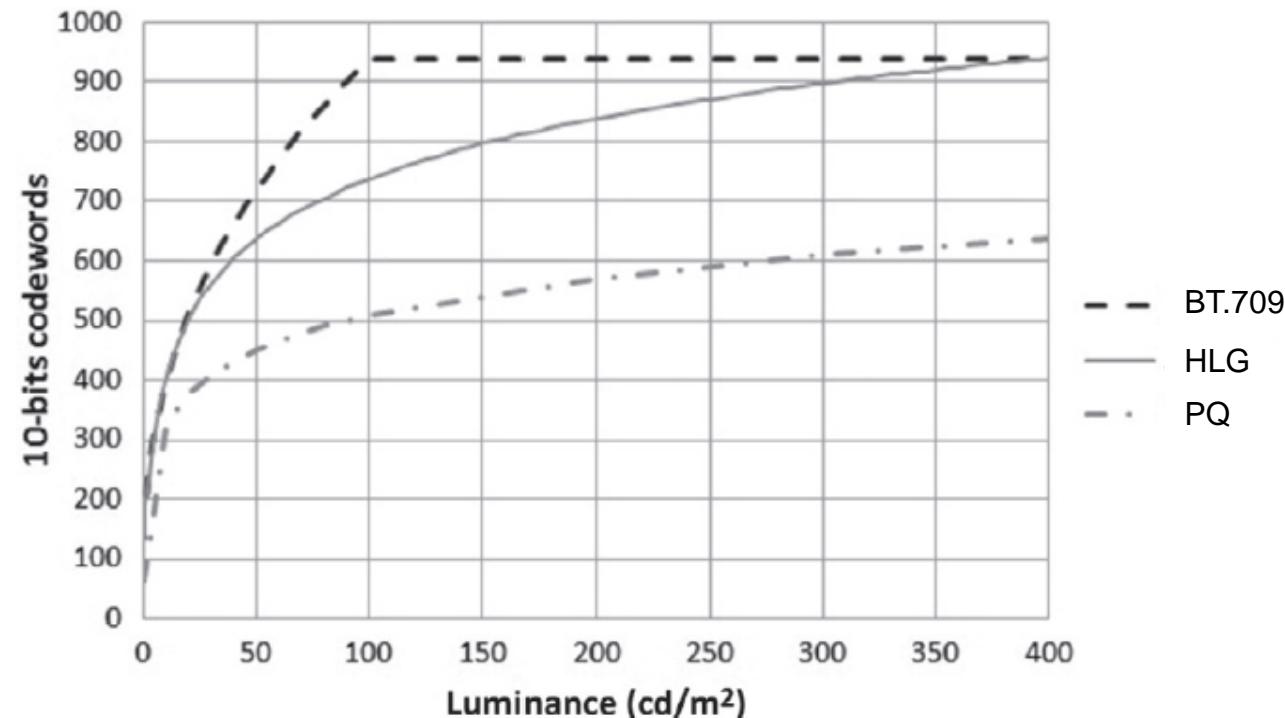
10 bit video is still the norm;
HEVC Main 10 profile is
foreseen for distribution

**10-bit PQ still near or below
perceptual thresholds**

S. Miller, M. Nezamabadi, S. Daly, Perceptual Signal Coding for More Efficient Usage of Bit Codes
2012 SMPTE Annual Technical Conference & Exhibition

Hybrid Log-Gamma (HLG) - ARIB STD-B67

- Designed for backward compatibility with the BT.709 OETF and the corresponding BT.1886 EOTF with gamma encoding
 - The same content can be displayed on both LDR and HDR displays (at least in principle)
 - Working well for peak luminance up to approx. 1000 cd/m^2

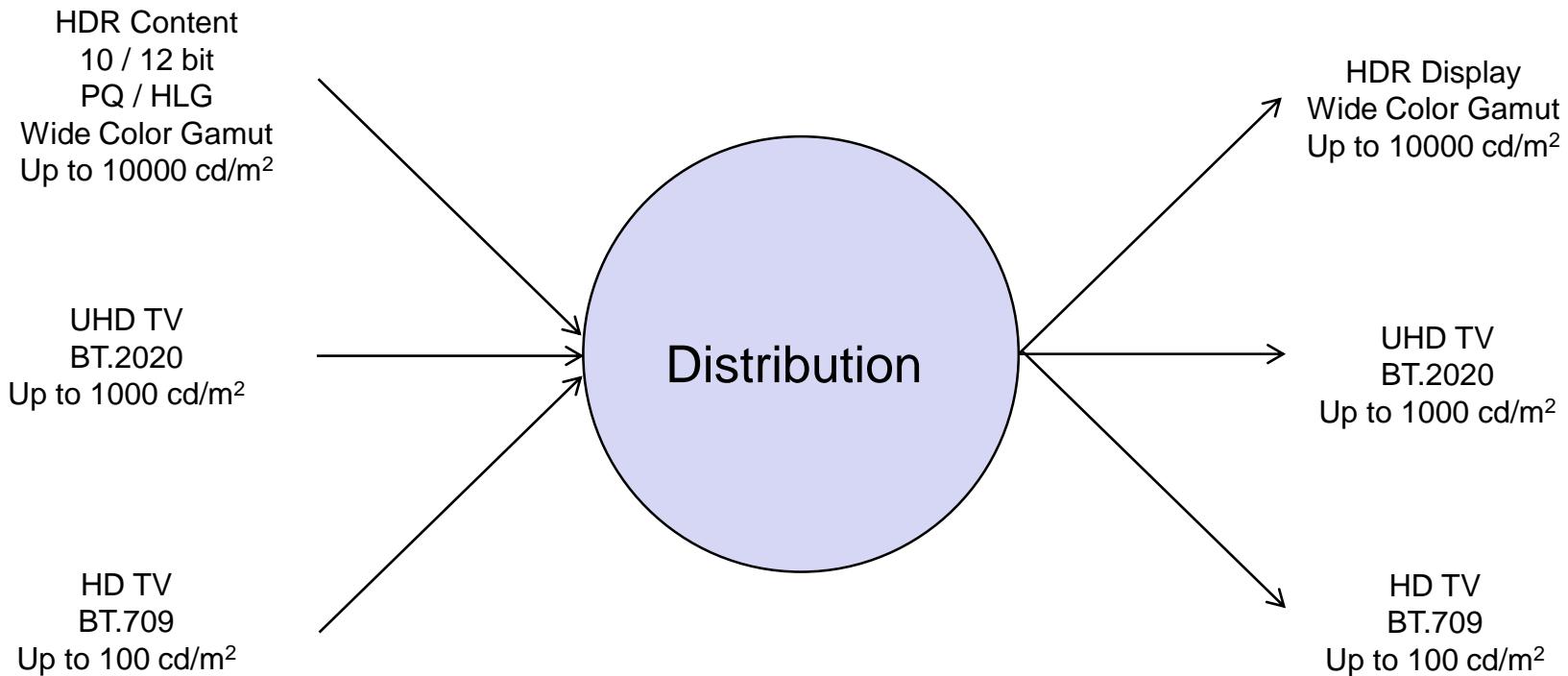


Inflexion point at relative luminance value μ

- Below μ , the curve is similar to the BT.709 transfer function
- Above μ , the curve is stretched

Both PQ and HLG are currently standardized in ITU-R BT.2100

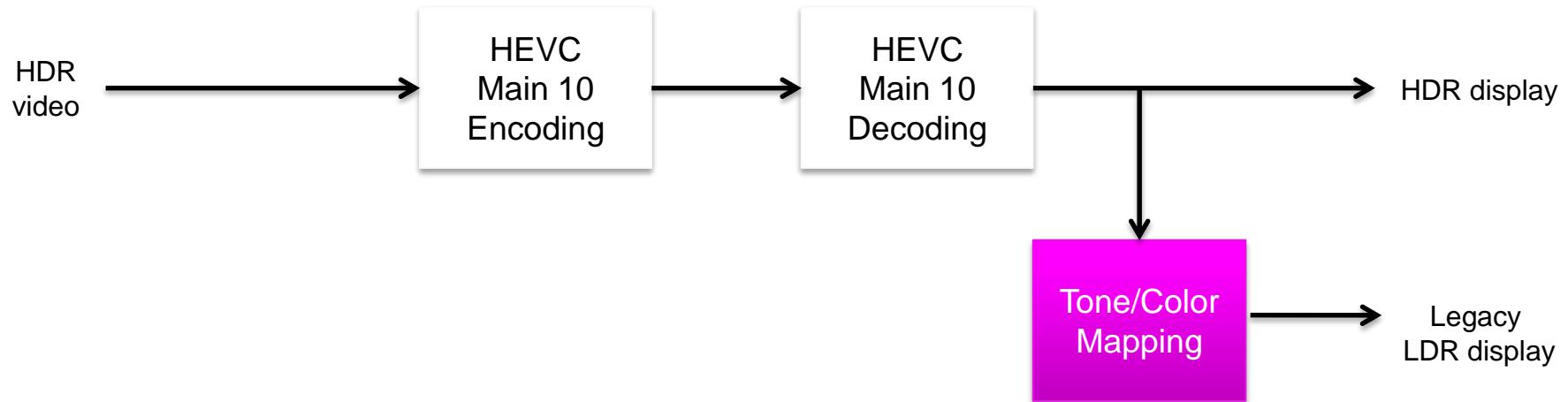
Heterogeneous Environment



Different distribution scenarios

- **Single-layer**

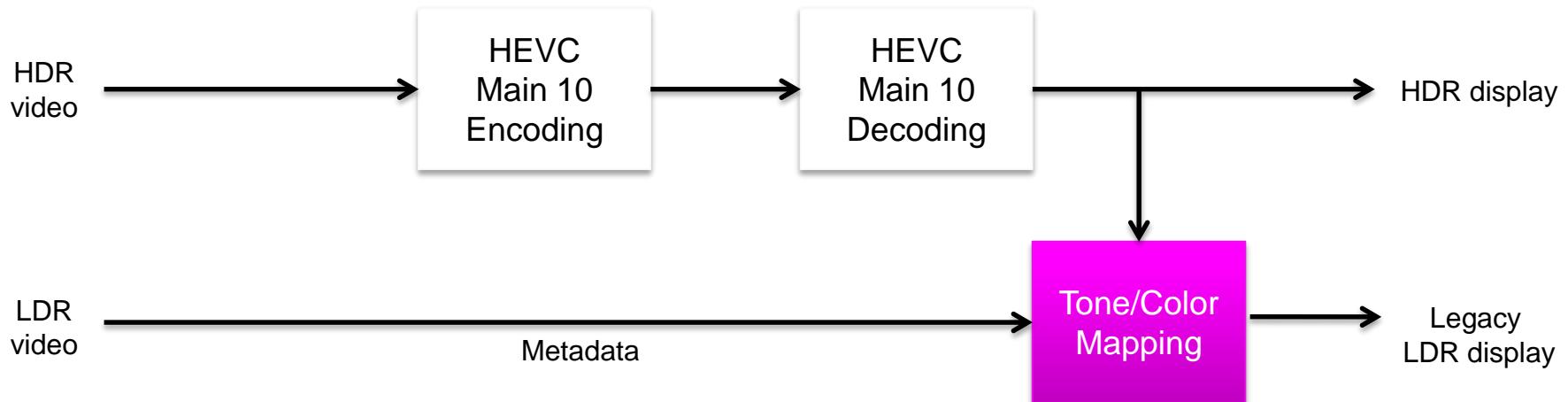
- HDR video coding using HEVC Main 10
- HDR-to-LDR mapping at the receiver side (real-time)



Different distribution scenarios

- **Single-layer**

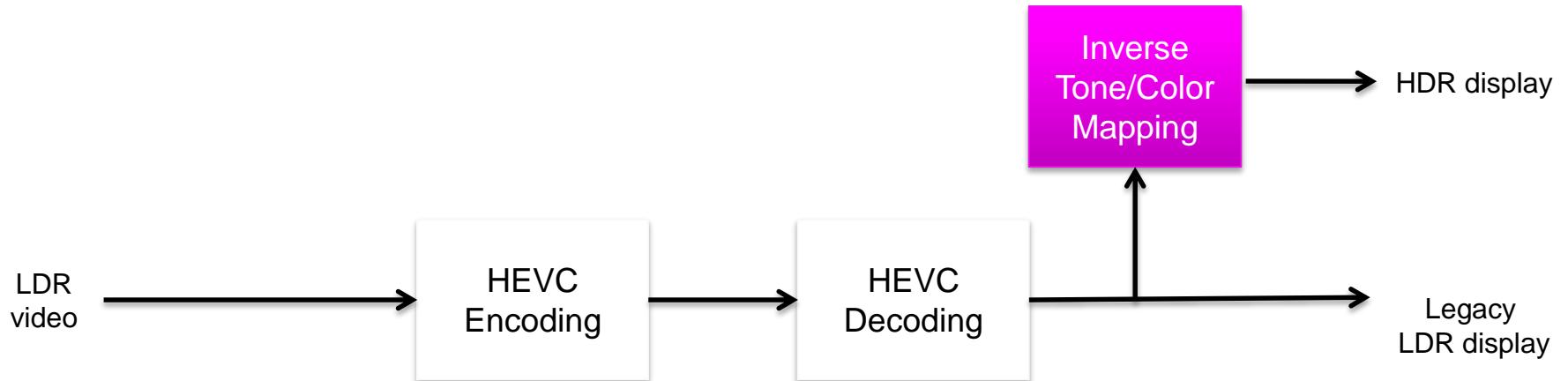
- HDR video coding using HEVC Main 10
- HDR-to-LDR mapping at the receiver side (real-time)
- Metadata from LDR master video to improve tone/color mapping and preserve artistic intent



Different distribution scenarios

- **Single-layer**

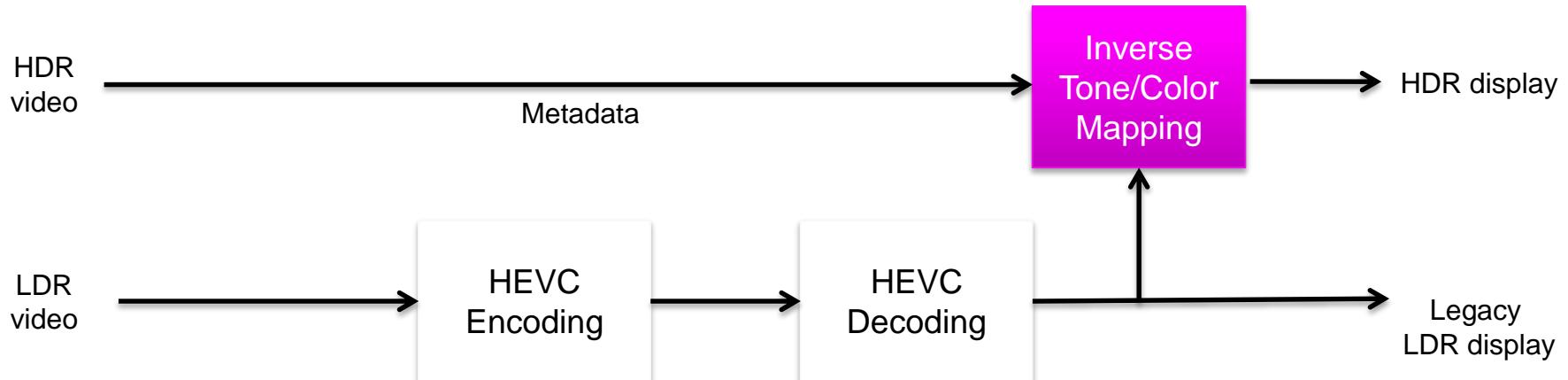
- LDR video coding using HEVC
- LDR-to-HDR mapping at the receiver side (real-time)



Different distribution scenarios

- **Single-layer**

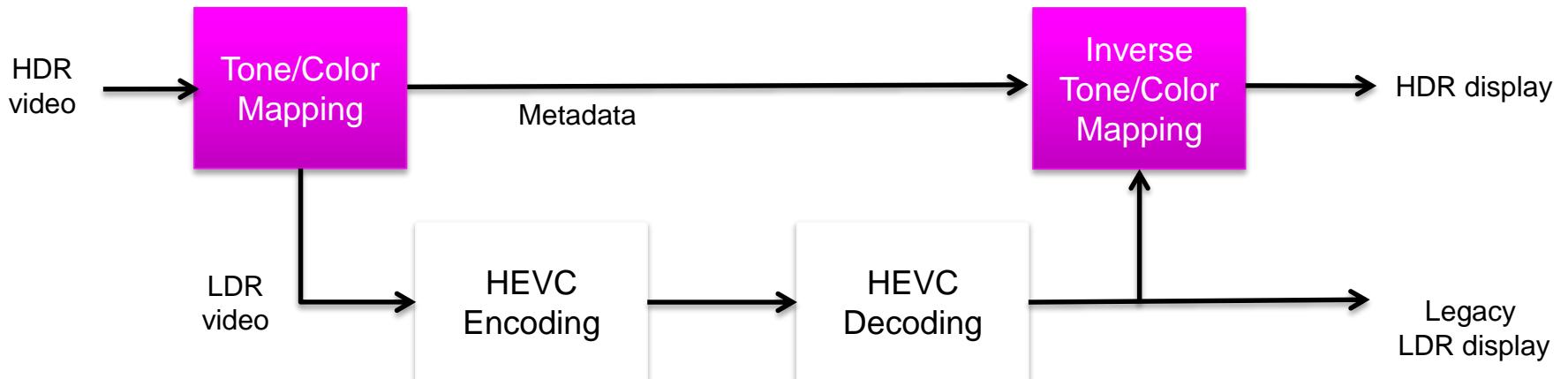
- LDR video coding using HEVC
- LDR-to-HDR mapping at the receiver side (real-time)
- Metadata from HDR master video to improve inverse tone/color mapping and preserve artistic intent



Different distribution scenarios

- **Single-layer**

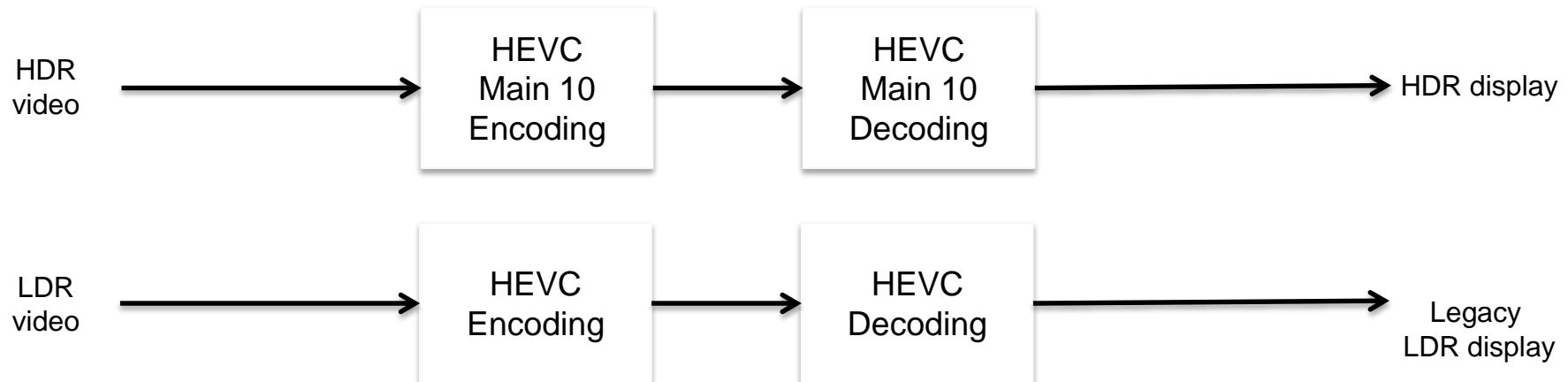
- LDR video coding using HEVC
- LDR-to-HDR mapping at the receiver side (real-time)
- LDR video obtained by HDR-to-LDR tone/color mapping



Different distribution scenarios

- **Dual-layer, simulcast**

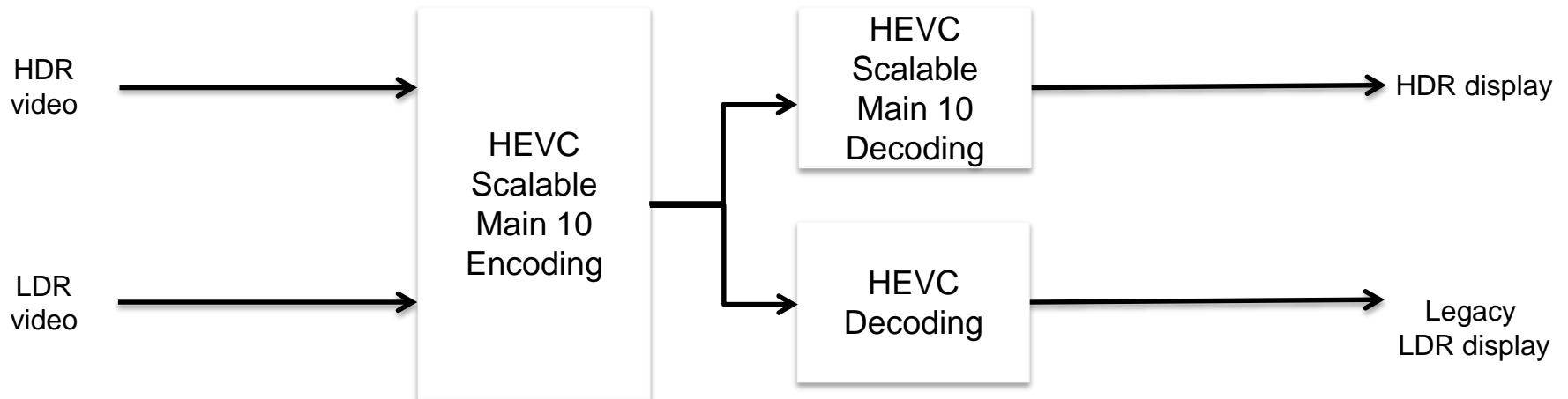
- Simulcast (independent coding) of LDR and HDR video sequences
- Not optimal in terms of bandwidth



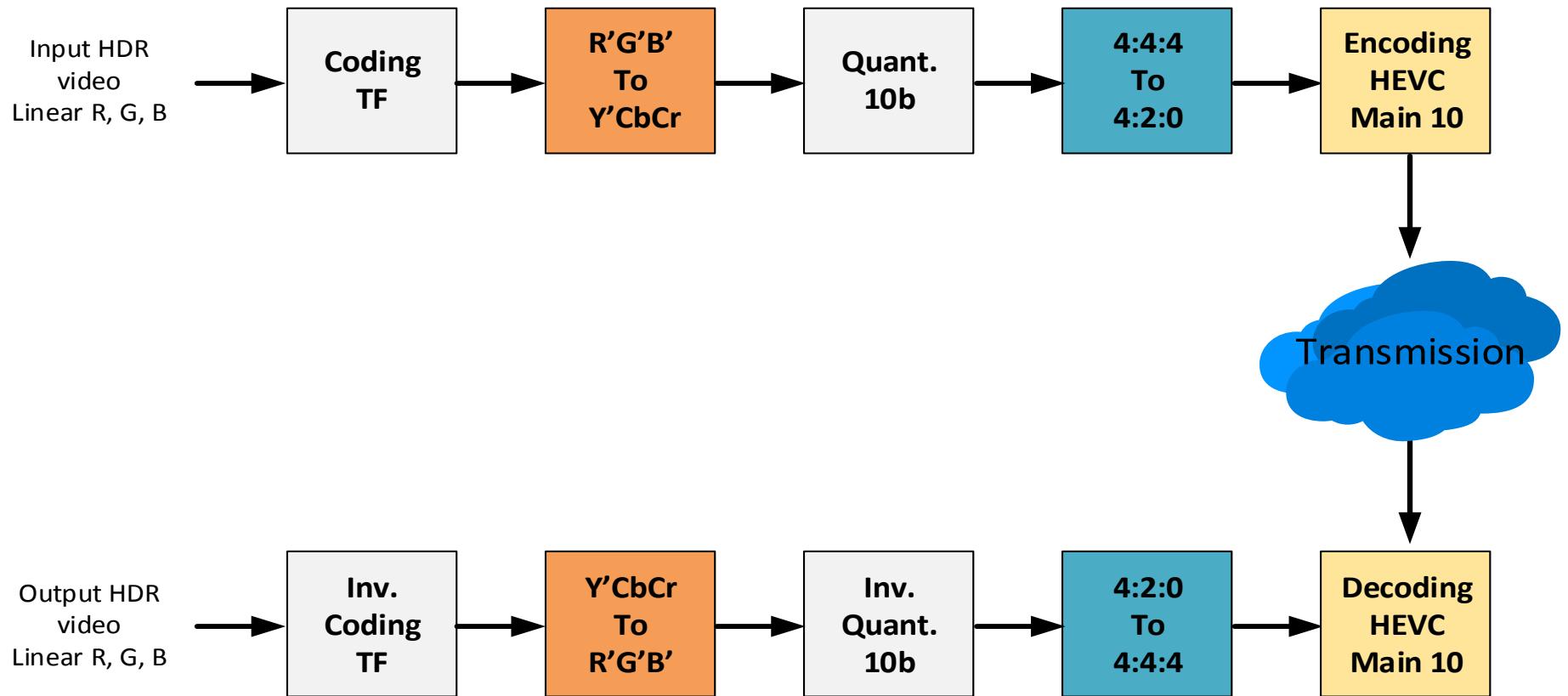
Different distribution scenarios

- **Dual-layer, scalable coding**

- Joint coding of LDR and HDR video sequences using SHVC
- HDR enhancement layer can be predicted from LDR base layer
- Exploit better data redundancies



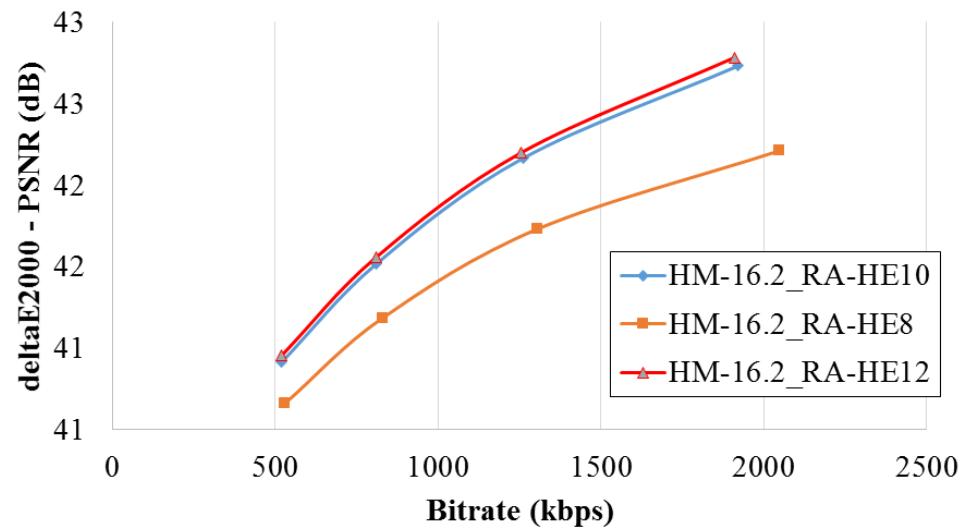
MPEG approach



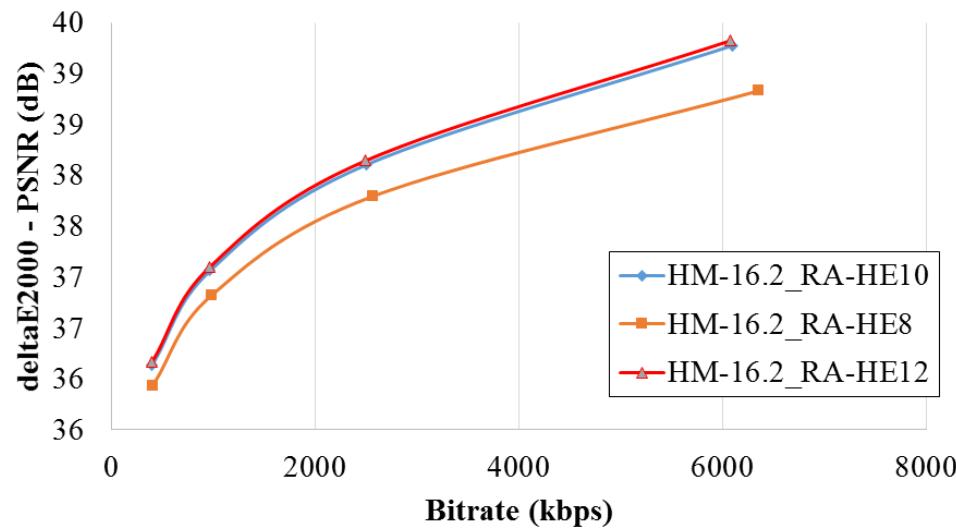
MPEG approach

- **SMTPE 2084/PQ**
 - Comparison of 8-, 10- and 12-bit HEVC coding

FireEaterClip4000r1



Tibul2Clip4000r1



Dual-modulation scheme

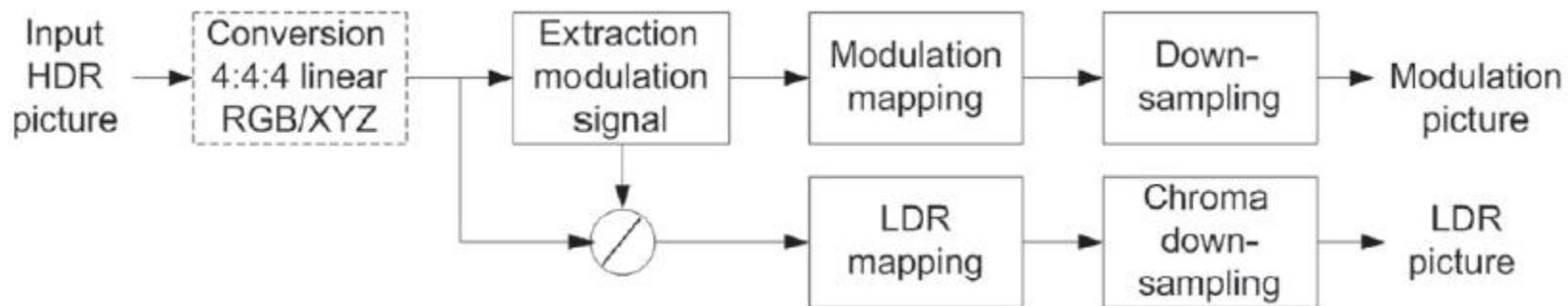
- **Dual-modulation scheme**

- Two multiplicative layers
- Assume that the dynamic of the HDR image is limited within a small spatial area
- The modulation signal is smooth and can be downsampled
- Mimic the process of HDR displays

$$P_{\text{HDR}} = P_{\text{mod}} \times f^{-1}(P_{\text{LDR}})$$

P_{mod} : low-frequency monochromatic version of the input signal

P_{LDR} : remaining part of the signal

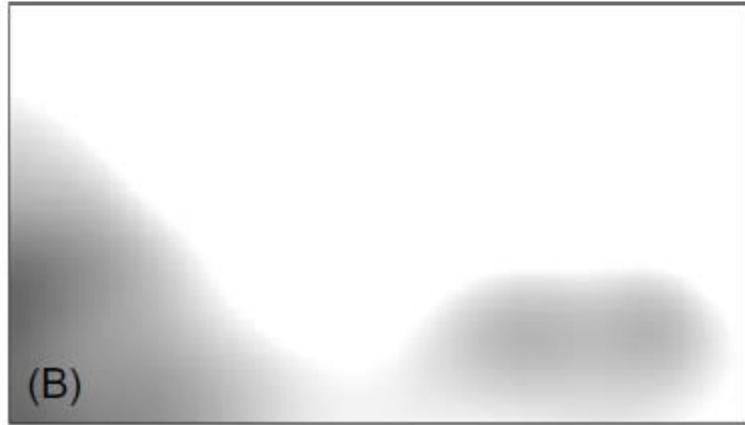


Dual-modulation scheme

$$P_{\text{HDR}} = P_{\text{mod}} \times f^{-1}(P_{\text{LDR}})$$



modulation frame

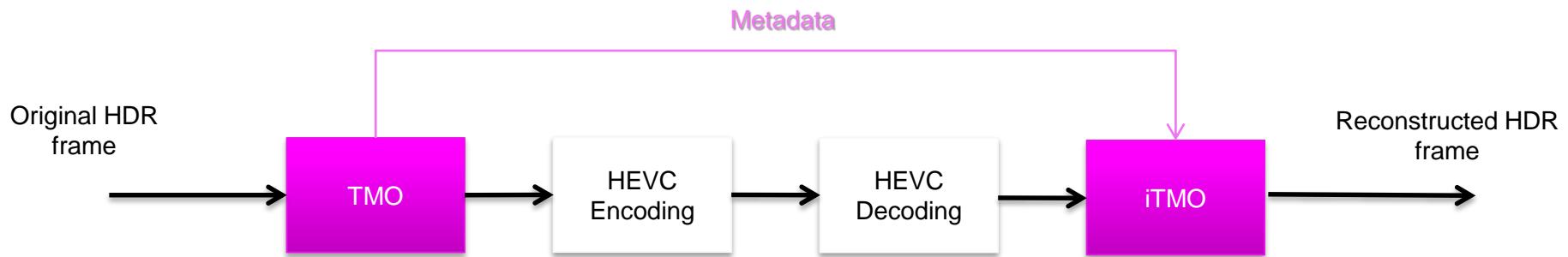


E. François, P. Bordes, F. Le Léannec, S. Lasserre, P. Andrivon
High Dynamic Range and Wide Color Gamut Video Standardization — Status and Perspectives

Schemes based on content-adaptive TMO

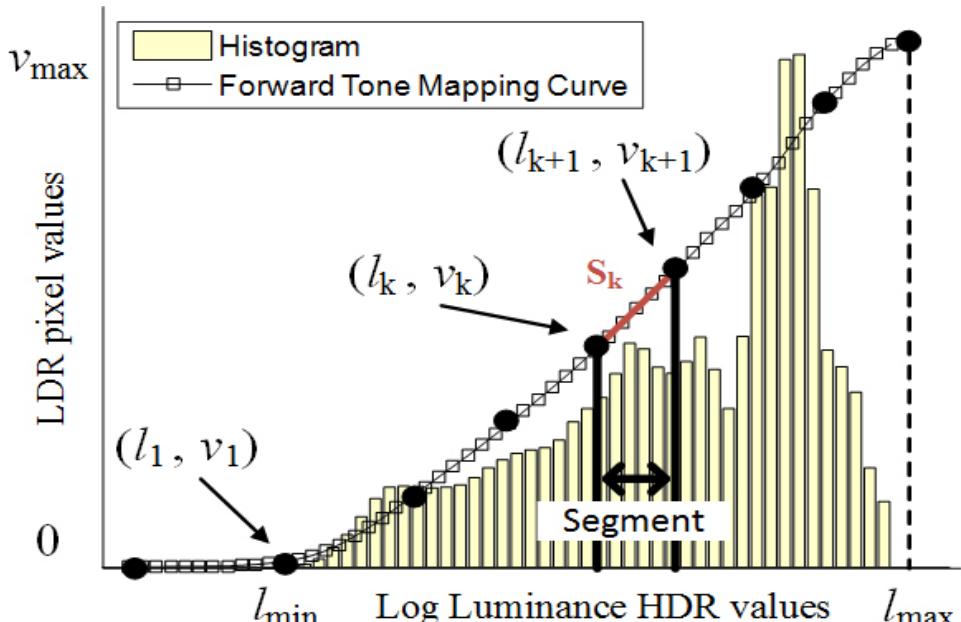
- **Content-adaptive TMO**

- Take into account the statistical characteristics of the input HDR frame
- Metadata need to be transmitted, but with a negligible overhead cost



MSE optimal TMO

- Piecewise linear TMO



$$s_k = \frac{d_k}{\delta}, \quad d_k = v_{k+1} - v_k$$

- TMO minimizing the MSE between original and reconstructed log values

$$\min_s \sum_{k=1}^N p_k s_k^{-2} \quad \text{s.t.} \quad \sum_{k=1}^N s_k = \frac{v_{\max}}{\delta}$$

- Closed form solution

$$s_k = \frac{v_{\max} \cdot p_k^{1/3}}{\delta \cdot \sum_{k=1}^N p_k^{1/3}}$$

p_k : k'th bin of the normalized luminance histogram

Z. Mai, H. Mansour, R. Mantiuk, P. Nasiopoulos, W. Ward and R. Heidrich,
Optimizing a tone curve for backward-compatible high dynamic range image
and video compression, IEEE TIP 2011

Spatial regularization

- **Optimization problem**

$$\min_s \left(\sum_{k=1}^N p_k s_k^{-2} + \lambda \operatorname{TV}(I(s)) \right) \quad \text{s.t.} \quad \sum_{k=1}^N s_k = \frac{v_{\max}}{\delta}$$

- **Spatial regularization term**

- Total variation

$$\operatorname{TV}(I(s)) = \sum_i \|(\nabla I)_i\|$$

- **Non-smooth convex function**

- No closed-form solution
 - Primal-dual M+LFBF algorithm [Combettes and Pesquet, 2012]

P. Lauga, G. Valenzise, G. Chierchia, and F. Dufaux, Improved Tone Mapping Operator for HDR Coding Optimizing the Distortion/Spatial Complexity Trade-Off, in *Proc. European Signal Processing Conference (EUSIPCO 2014)*, Lisbon, Portugal, Sept. 2014.

Temporal regularization

- Optimization problem

$$\min_s \left(\sum_{k=1}^N p_k s_k^{-2} + \lambda C(I_t) \right) \quad \text{s.t.} \quad \sum_{k=1}^N s_k = \frac{v_{\max}}{\delta}$$

- Temporal regularization term

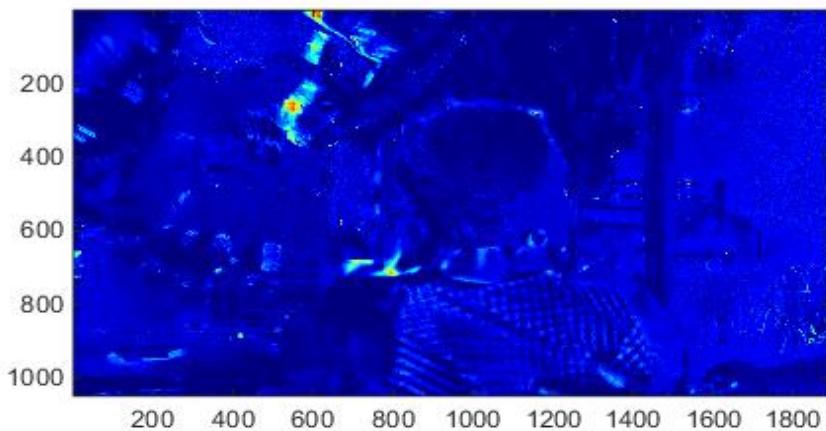
$$C(I_t) = \sum_{i,j} (I_t(i,j) - M(I_{t-1}(i,j)))^2$$

- $M(I_{t-1}(i,j))$ is the motion compensated frame
 - Optical flow computed on the HDR frames at time t and $t-1$

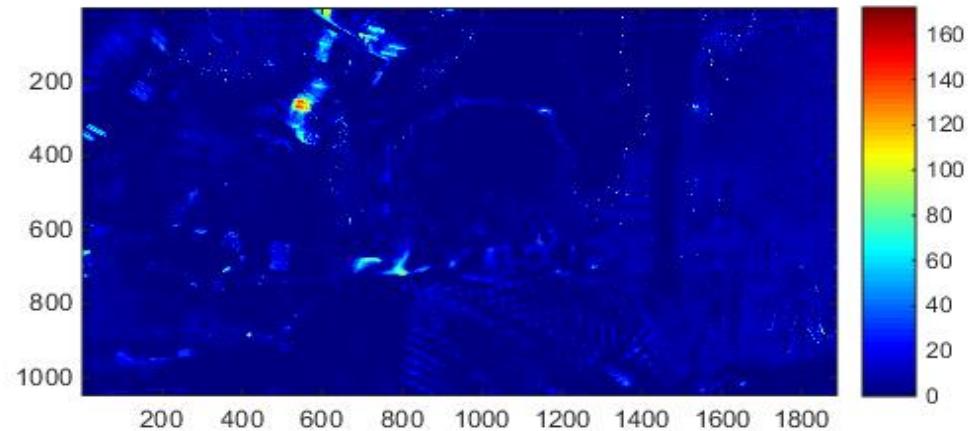
C. Ozcinar, P. Lauga, G. Valenzise, F. Dufaux, HDR Video Coding based on a Temporally Constrained Tone Mapping Operator, in *Proc. IEEE Digital Media Industry and Academic Forum*, July 2016.

Frame difference

Carousel_Fireworks_03

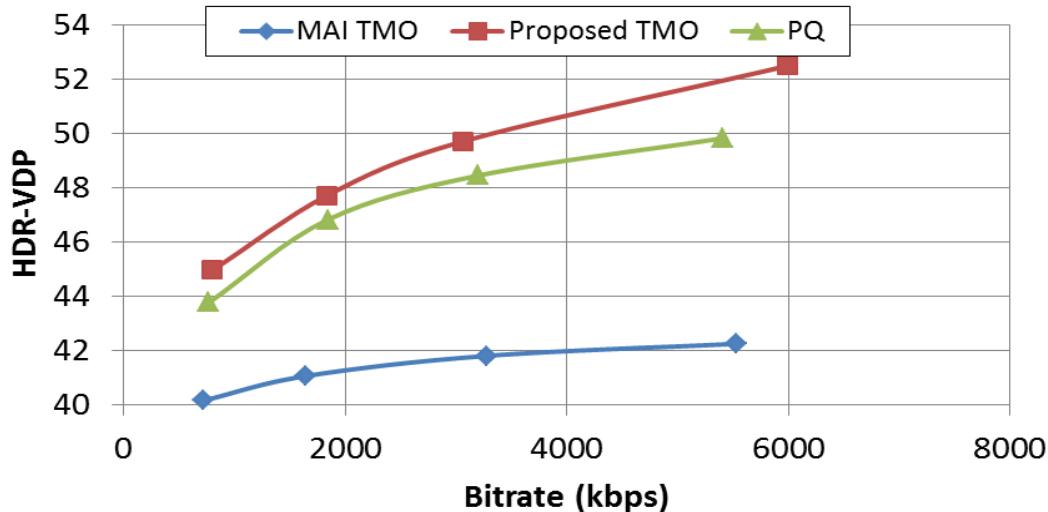


MSE optimization only

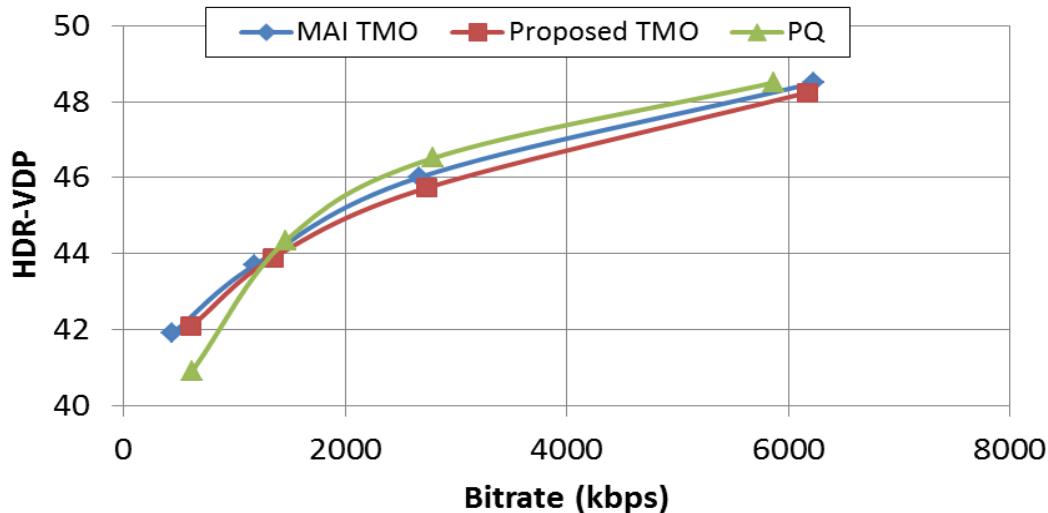


With temporal regularization

Rate-distortion results using HDR-VDP 2.2.1



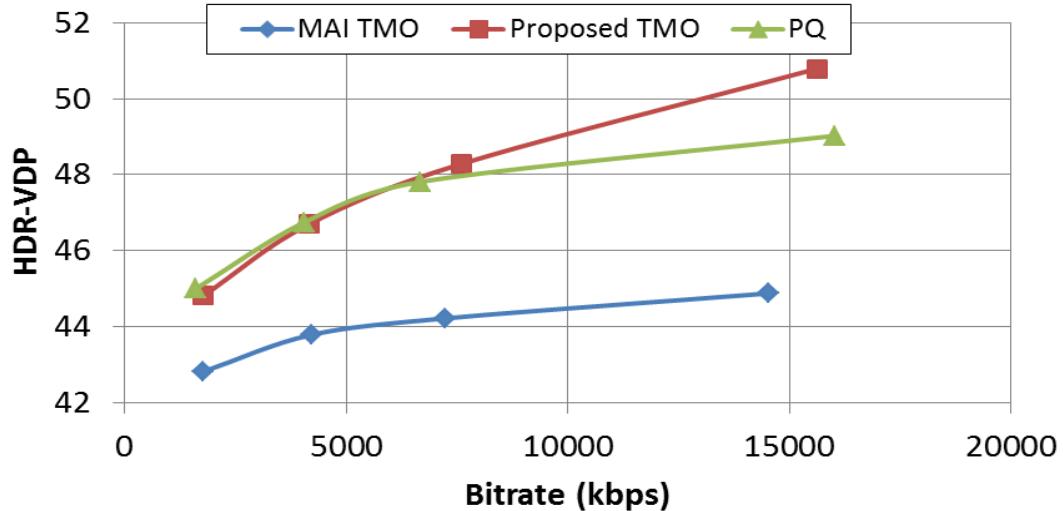
Tibul2



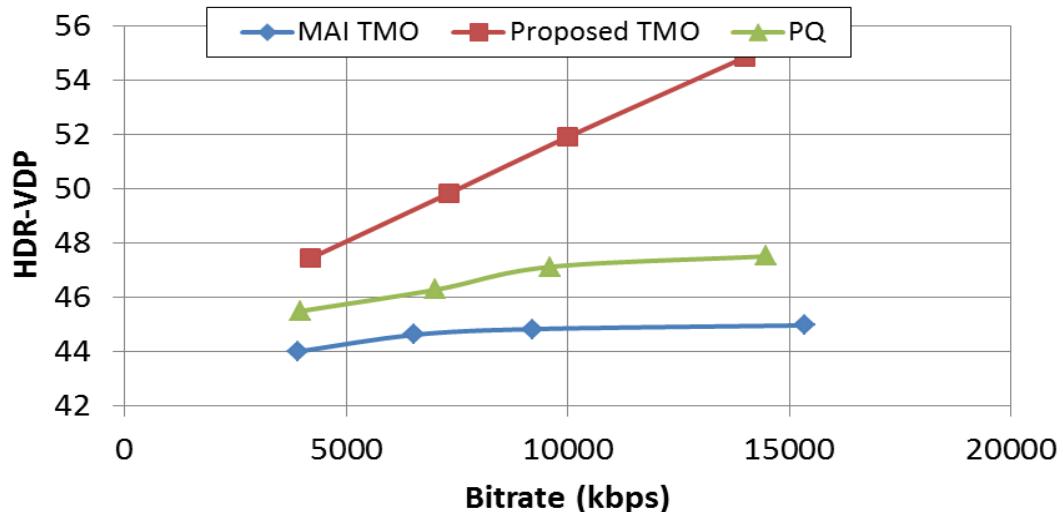
FireEater2



Rate-distortion results using HDR-VDP 2.2.1



Carousel_Fireworks_03



Carousel_Fireworks_04



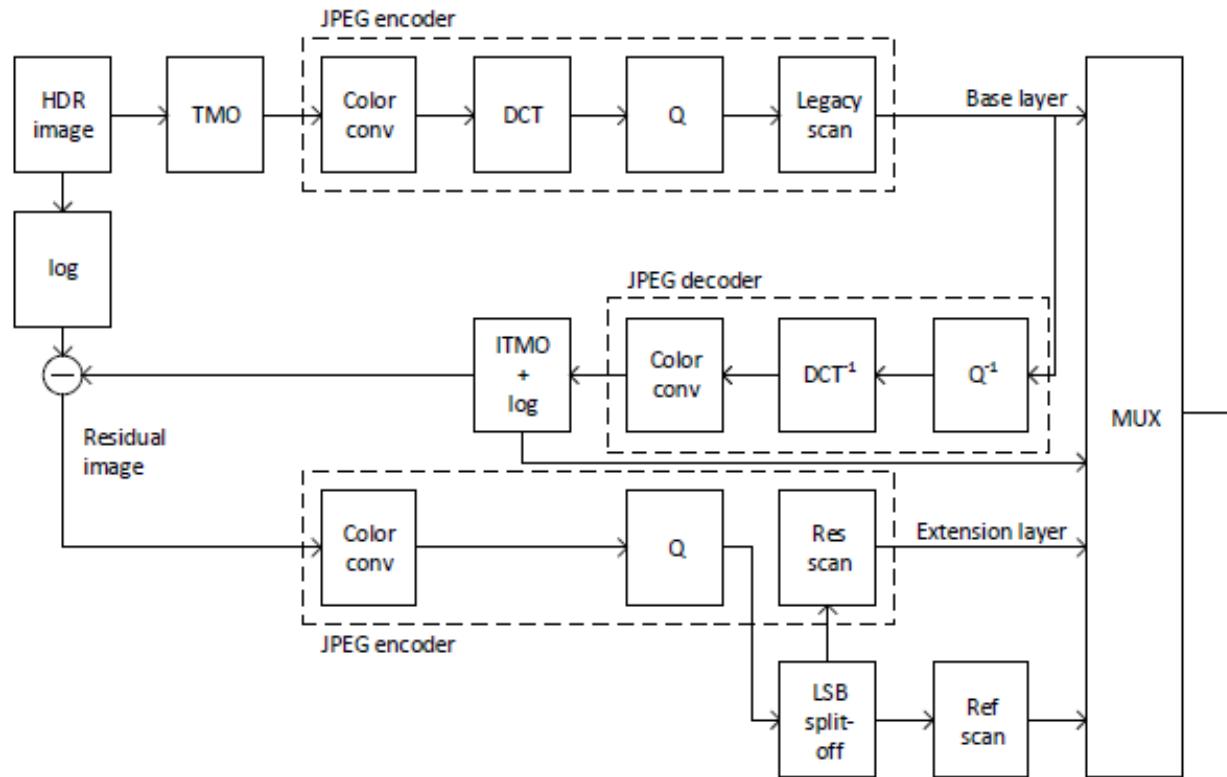
JPEG family of standards

- **JPEG 2000**
 - State-of-the-art still image coding scheme, based on a discrete wavelet transform (DWT)
 - Bit-depth in the range of 1 to 38 bits per component
- **JPEG XR**
 - Cost-effective compression, based on block-transform design
 - Different image representation pixel formats: 8- and 16-bit unsigned integer, 16- and 32-bit fixed point, 16- and 32-bit floating-point
- **JPEG XT**
 - Backward compatible extensions to the legacy JPEG standard for HDR image compression
 - Two layers design
 - Base layer: tone-mapped and encoded using JPEG
 - Extension layer: residual information by subtraction and/or division

JPEG family of standards

- **JPEG XT Profile C**

- Residual = the ratio of the HDR image and the inverse tone-mapped image, implemented as a difference of logarithms



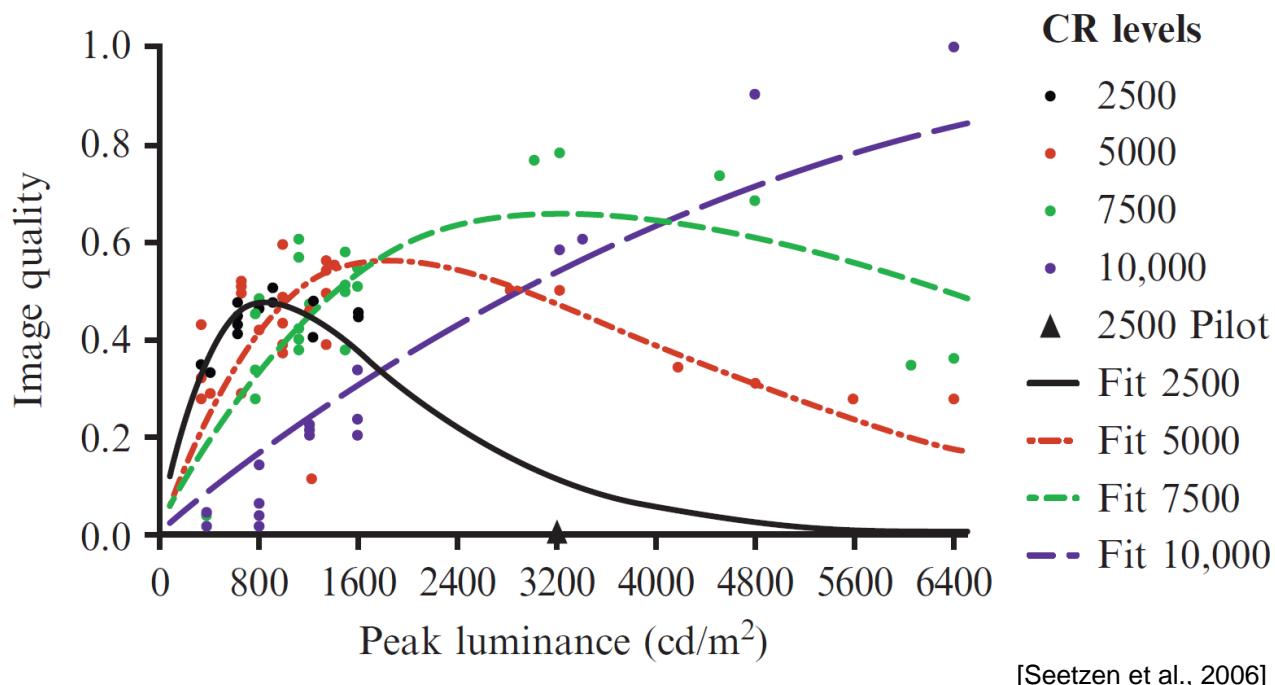
HDR DISPLAY TECHNOLOGY

Motivation

- **Displaying HDR images and videos directly, without tone mapping**
- **Conventional Liquid Crystals Displays (LCD) technology**
 - Max luminance ~ 300-400 cd/m²
 - Max dynamic range ~ 500:1
 - *Human eye can perceive a much higher range of luminance, even at a single state of adaptation*
- **Questions:**
 - What is the needed peak luminance?
 - What is the needed dynamic range?
 - How to build hardware solutions to achieve them?

Peak brightness alone is not sufficient

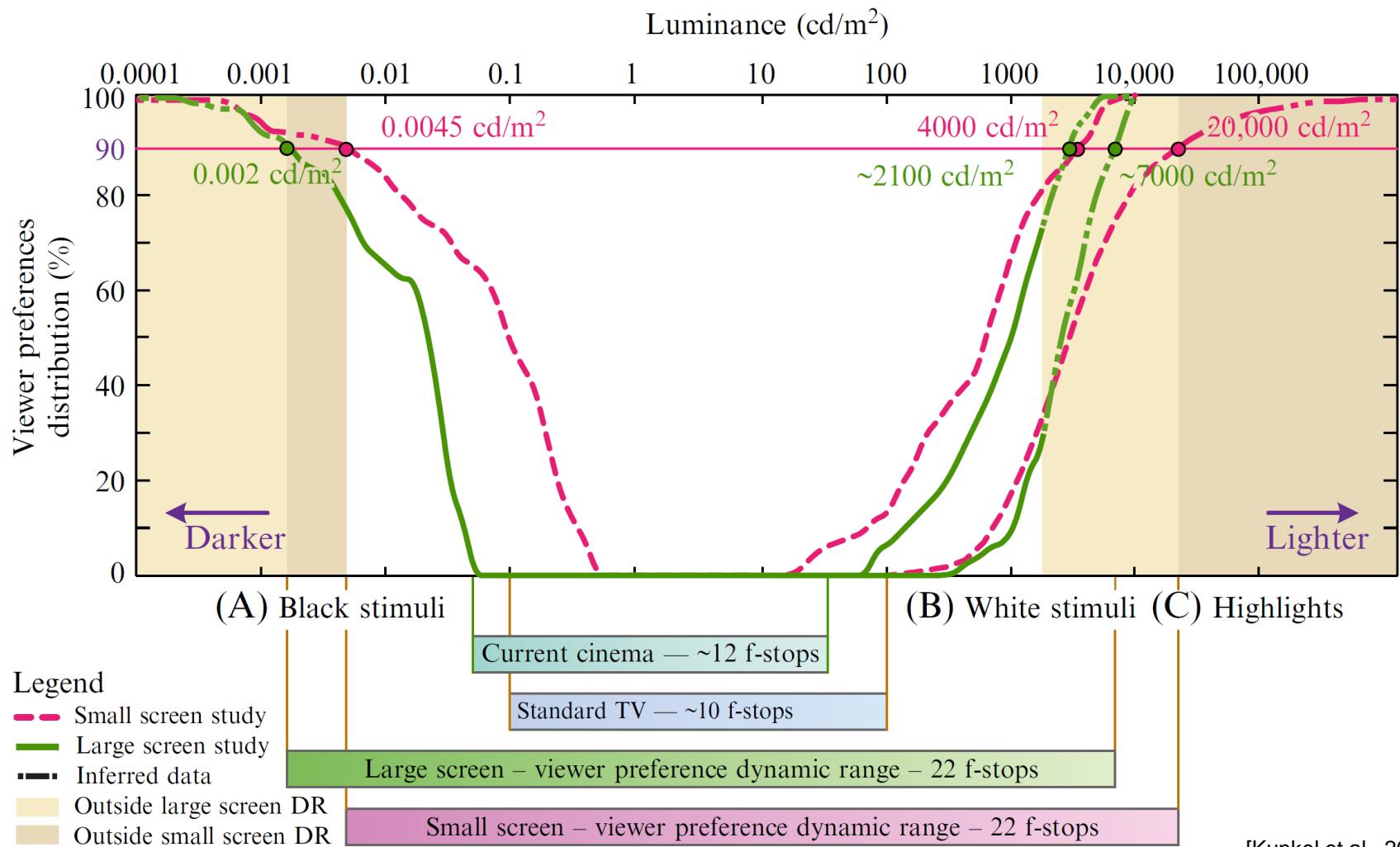
- Viewers prefer higher peak brightness *provided that* dynamic range increases concurrently (Akyuz, 2006; Seetzen, 2006)
- Problem of the *black level*
 - If the display dynamic range (also called contrast ratio) is fixed, increasing peak brightness rises the black level



What is the required dynamic range?

- **Lower bound: SSDR (steady-state dynamic range)**
 - About $4 \log_{10}$ units (~ 13 fstops)
 - Can be larger when looking at full images (changes with eye movements, viewing angle, etc.)
- **Upper bound: long-term adaptation**
 - Up to $14 \log_{10}$ units
 - Unrealistic to reproduce
- **The necessary dynamic range is somewhat in-between**

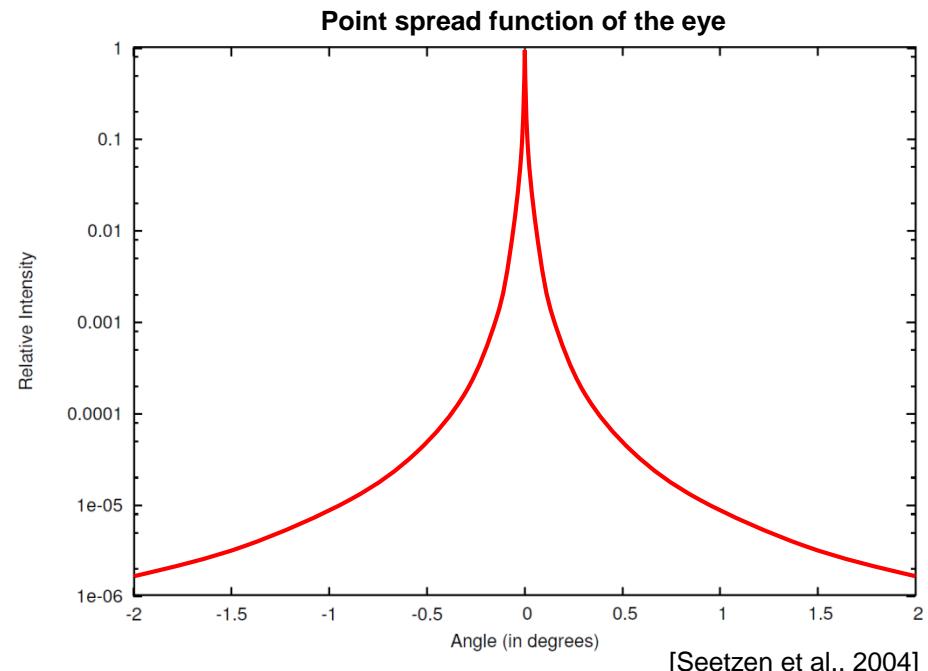
What is the required dynamic range? (contnd')



[Kunkel et al., 2016]

Local contrast perception

- How to reproduce 5 or more orders of magnitude of dynamic range simultaneously?
 - No conventional display technology is able to achieve this contrast
- Fortunately, it is not necessary!
 - The actually visible dynamic range in small regions (small visual angles) is much smaller
- Veiling glare effect:
 - The point spread function of the eye is not an impulse
 - A fraction of the light is scattered on neighboring receptors, lowering overall contrast
 - Maximum perceivable contrast $\sim 150:1$ (Seetzen et al., 2004)

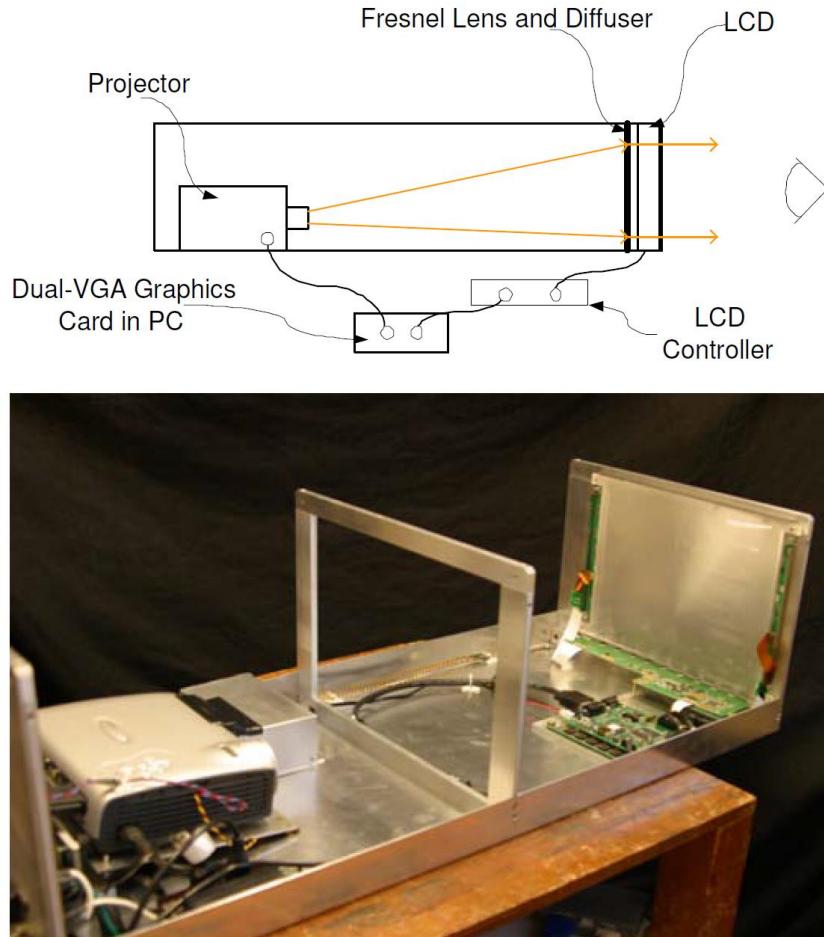


Hardware solutions to display HDR

- **Basic idea: two-layer solution (*dual modulation*)**
 - The first layer (*light modulator*) emits high-intensity, but low-resolution, light
 - The second layer (*optical filter*) filters the light with high-frequency details
- **If c_1 is the contrast ratio of the first layer, c_2 that of the second layer**
 - The theoretical maximum dynamic range achievable is $(c_1 \cdot c_2):1$
 - Limited by physical transmittance of the second layer
- **The optical filter is generally a LCD screen**
- **For the light modulator, two solutions** (Seetzen et al., 2004):
 - Digital Light Projector (DLP)
 - Array of ultra-bright LED's

Projector-based display

- Composed of a projector, an LCD display and a diffuser
 - The latter to avoid Moiré patterns
 - Achievable dynamic range > 50,000:1
- Very high image quality
 - Relative high-resolution of projector image
 - Adapt for research applications as a home-made solution
- Not practical for the consumer market
 - Form factor
 - High energy consumption
 - Projector cost
 - Higher bandwidth



[Seetzen et al., 2004]

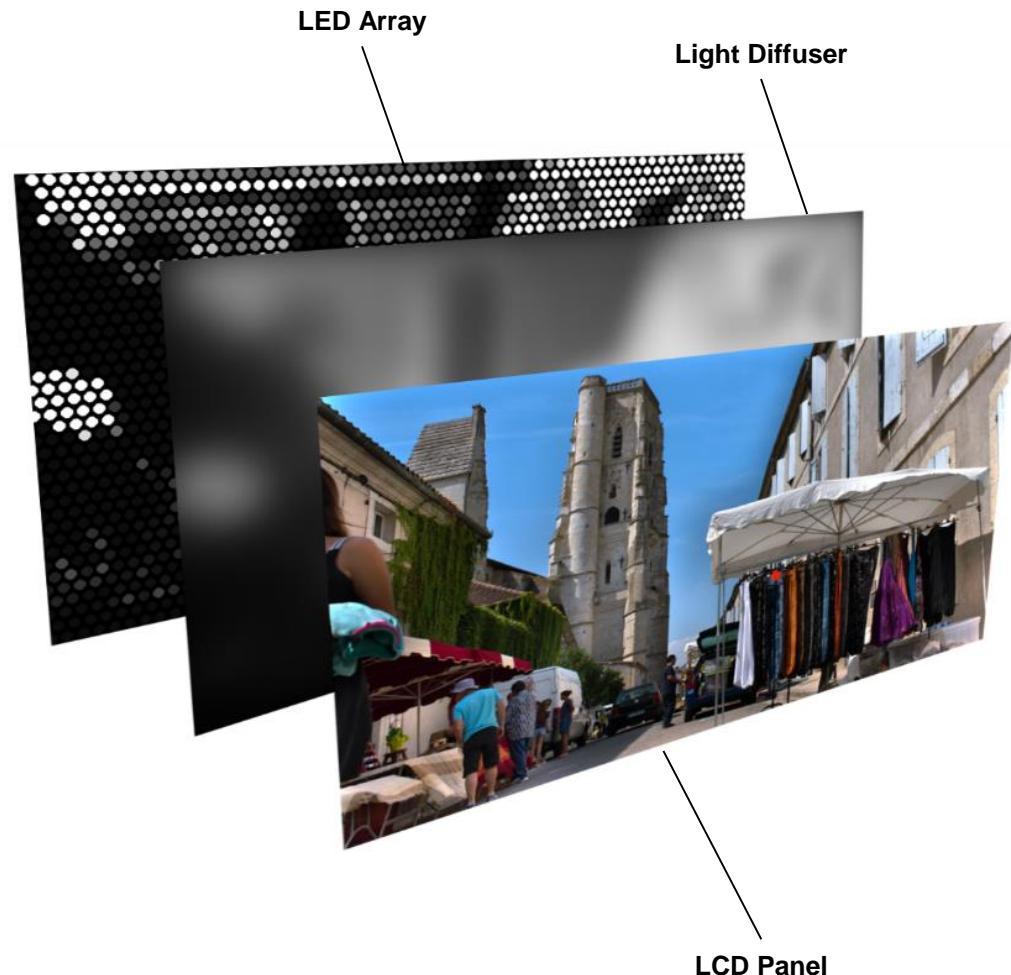
LED-based display

- Composed by the LED layer, diffuser and LCD panel

- LED's individually controllable, positioned in an hexagonal pattern
- Diffuser avoids discontinuities in LCD illumination

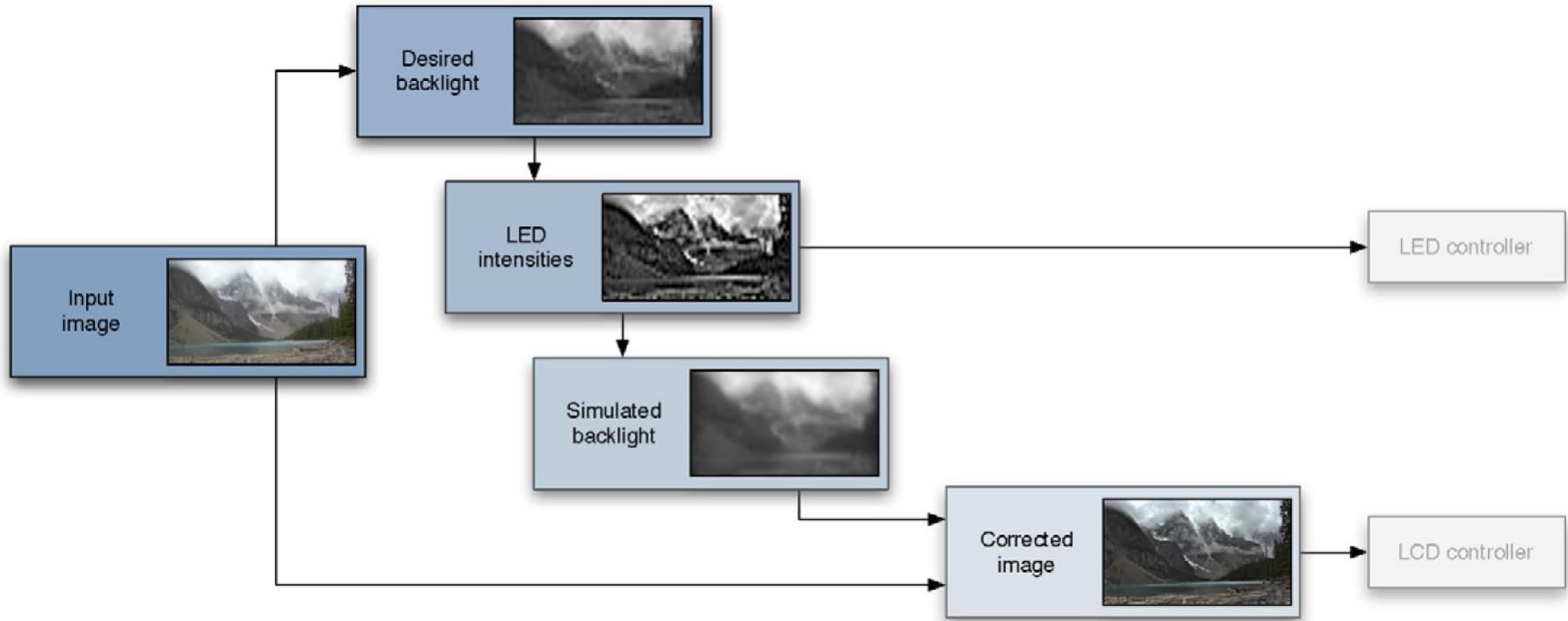
- W.r.t. projector-based:

- Reduced form factor
- Higher power efficiency
- Lower bandwidth (limited number of LED's, 2200 for SIM2 display)
- Higher computational complexity in the rendering due to the much larger support of the point spread function (PSF) of the diffuser



Dual modulation rendering

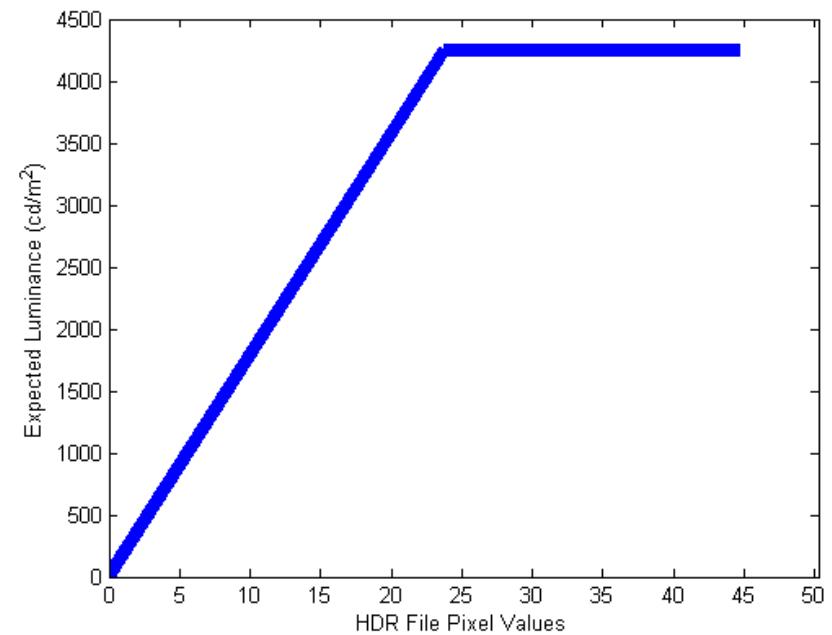
- The front and back panels have to be driven with separate signals, computed through a *dual modulation* algorithm
 - The LCD signal compensates for the low-resolution backlight
- E.g.: Brightside rendering for LED-based display



[Trentacoste et al., 2007]

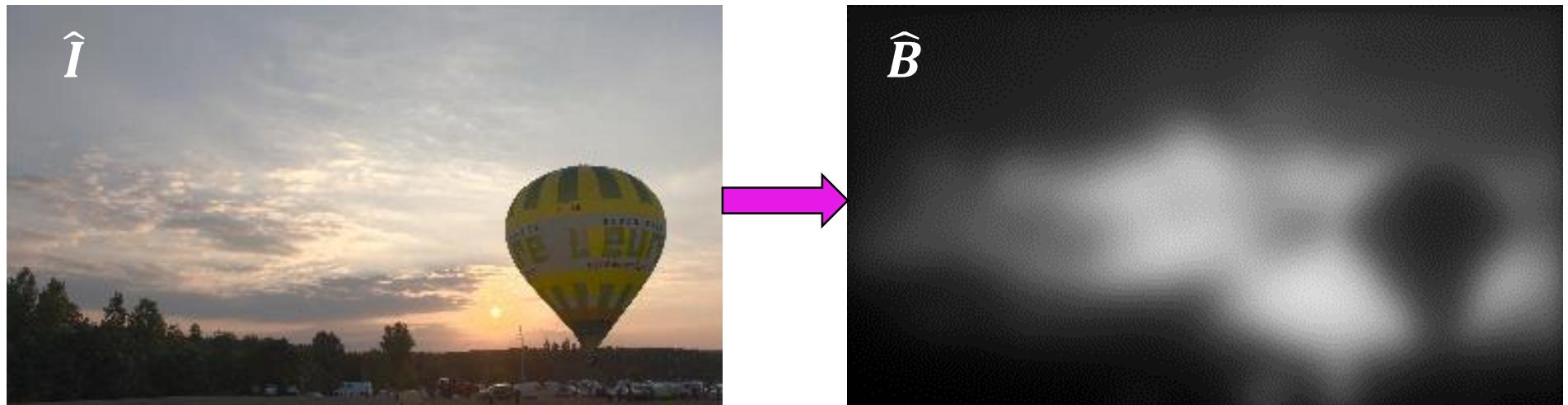
Target backlight computation

- Given the desired image \hat{I} , determine the target backlight distribution \hat{B}
 1. Compute image luminance as the maximum of the three color channels (to provide enough illumination for LCD)
 2. Clamp luminance values to be in the display luminance range



Target backlight computation

- Given the desired image \hat{I} , determine the target backlight distribution \hat{B}
 1. Compute image luminance as the maximum of the three color channels (to provide enough illumination for LCD)
 2. Clamp luminance values to be in the display luminance range
 3. Low-pass filter the luminance of the image and (possibly) down-sample it on the LED grid to reduce computational complexity



Derivation of LED values

- Find the LED activation values such that the resulting backlight is as close as possible to \hat{B}

- Essentially, a *deconvolution* problem
 - LED driving values $d \in [0,1]^N$, where, e.g., $N = 2202$ for SIM2 HDR47 display
 - Finding d corresponds to solving the following (over-constrained) least-square problem:

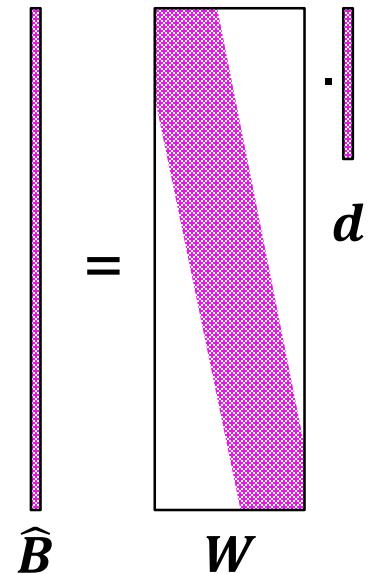
$$d^* = \arg \min_d \|Wd - \hat{B}\|$$

where W is a matrix containing the PSF of LED at each LED position

- *Most complex operation of the rendering pipeline*

- Several possible approximated solutions:

- Leverage the sparsity of W
 - Downsampling of \hat{B} and doing one step of Gauss-Seidel iteration (Trentacoste et al., 2007)
 - Iterative scaling (Zerman et al., 2015)



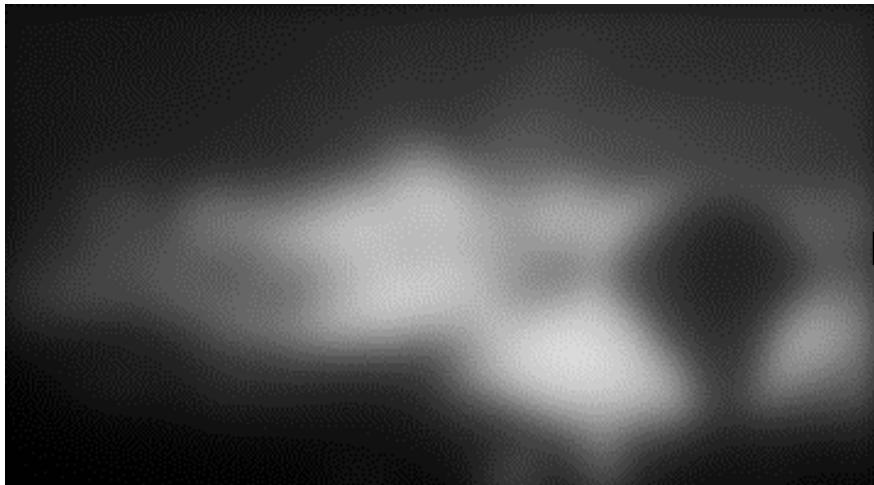
Derivation of LED values

- Estimated driving values
- Clipped in [0,1] and quantized on 8 bits
- Power absorption constraint:

$$\sum d_i P_{LED} \leq P_{MAX}$$

- The total absorbed power cannot exceed the maximum available power
- Re-scaling of LED values, or inclusion of the constraint in the optimization (Burini et al., 2013)

\hat{B}



d^*

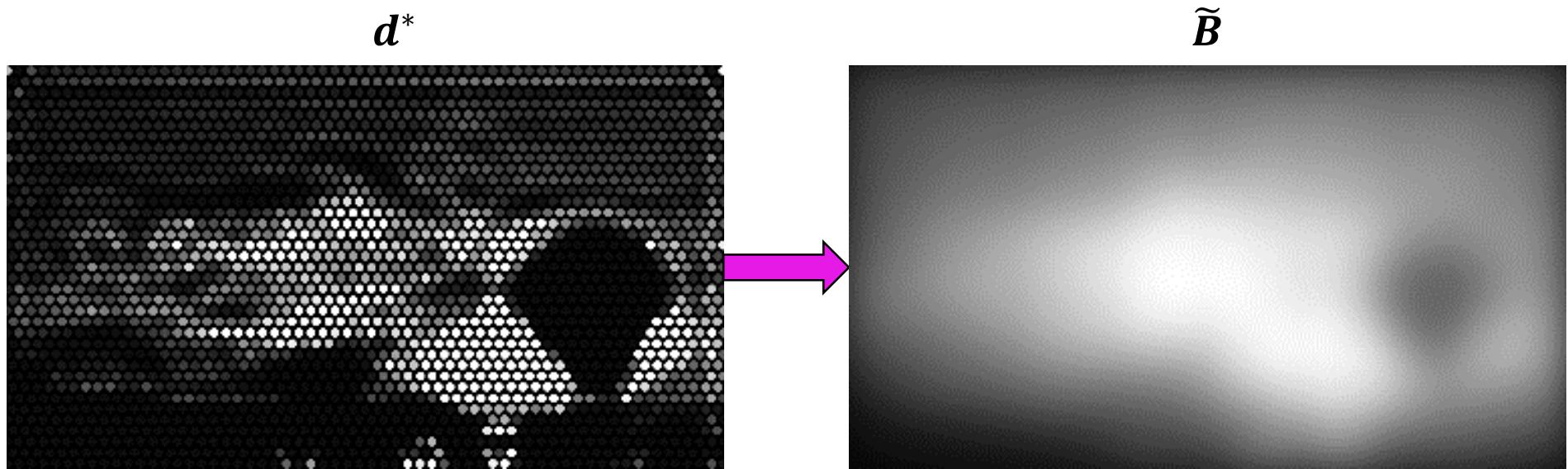


Forward backlight simulation

- Once the optimal LED driving values are known, the resulting backlight can be found by convolving the vector of Dirac's d^* with the PSF of LED's:

$$\tilde{B} = d^* * PSF$$

- Can be efficiently implemented in GPU through a splatting approach + alpha blending



Computation of LCD values

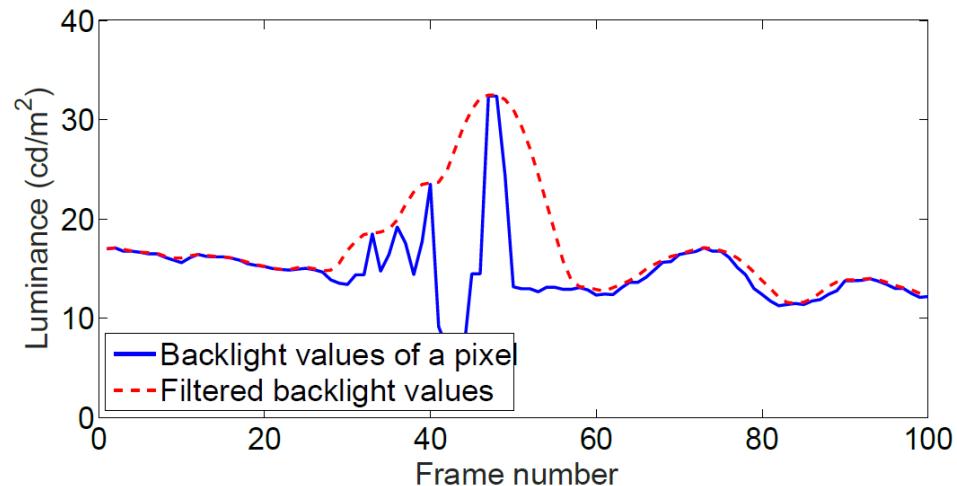
- Obtained by dividing the input target image by the computed backlight:

$$LCD = \frac{\hat{I}}{\tilde{B}}$$

- Performed per pixel and per color channel
 - The resulting LCD pixels are processed with the inverse response function of LCD panel (e.g., gamma), and clipped in [0, 255]
- Resulting LCD images have reversed contrast at edges (e.g., halo effects) to compensate for the backlight blur



- **Frame-by-frame rendering**
 - Changes in LED driving signals can produce flickering
 - The refresh time for LED and LCD panels are generally different, thus video rendering could be from unsynchronized frames
- **Spatial smoothing of backlight**
 - Fastest and most popular solution
 - Reduces the overall dynamic range
- **Temporal optimization algorithm**
 - Smooth backlight *temporally*
 - E.g., compute the envelope of luminance across backlight pixel trajectories (Zerman et al., 2016)



[Zerman et al., 2016]

Guidelines for HDR content rendering

- **HDR content adaptation**

- Although with a much wider dynamic range than LDR, HDR displays still have physical limitations
- HDR content should be adapted (e.g., tone-mapped) to meet the display capabilities!
- Clipping of specular highlights, manual grading, automatic display adaptive tone mapping (Mantiuk et al., 2008)

- **Modeling of the display**

- Accurate measurement of the LED PSF
- Characterization of power constraints, LCD gamma's, location of LED grid, alignment issues for projector-based models, etc.

- **Display limitations:**

- Trade-off between accuracy of reproduction, computational complexity, video flickering
- Current solutions are mainly heuristic
- Loss of contrast due to LCD leakage, lowered thresholds due to local adaptation, etc.

Laboratory HDR displays

- **SIM2 HDR47 series**

- Peak luminance 4,000 or 6,000 nits (LED-based)
- Dynamic range > 100,000 : 1
- Full HD resolution
- 60 Hz frame rate real-time rendering

- **High power consumption**

- 2202 LED's
- 1380 W @ 4,000 nits
- Full peak luminance available only on limited areas of the image to meet power constraints

- **Driving mode**

- HDR mode: LogLUV with 12 bits for luminance
- DVI+ mode: custom rendering



Consumer HDR displays

- **Professional displays**
 - E.g. Sony BVMX300
 - Used for professional HDR color grading
- **Consumer displays**
 - LED vs. OLED
- **UHD alliance “premium 4K experience” logo**
 - 1,000nits peak brightness and < 0.05nits black level (contrast ratio 20,000:1, 14.3 f-stops) for LED TVs which are brighter but with less black levels
 - > 540nits brightness and < 0.0005nits black level (contrast ratio 1,080,000:1, ≈20 f-stops) for OLED TVs which have deep blacks but much lower peak brightness.



HDR QUALITY OF EXPERIENCE

Quality of Experience (QoE)

- “The degree of delight or annoyance of the user of an application or service. It results from the fulfillment of his or her expectations with respect to the utility and/or enjoyment of the application or service in the light of the user’s personality and current state.” (Le Callet et al., Qualinet white paper, 2013)
- **Multidimensionality**
 - Immersiveness
 - Perceptual fidelity
 - Visual attention
 - Aesthetics and artistic intention
 - Naturalness, etc.
- **Measurement**
 - Subjective experiments
 - Computational models

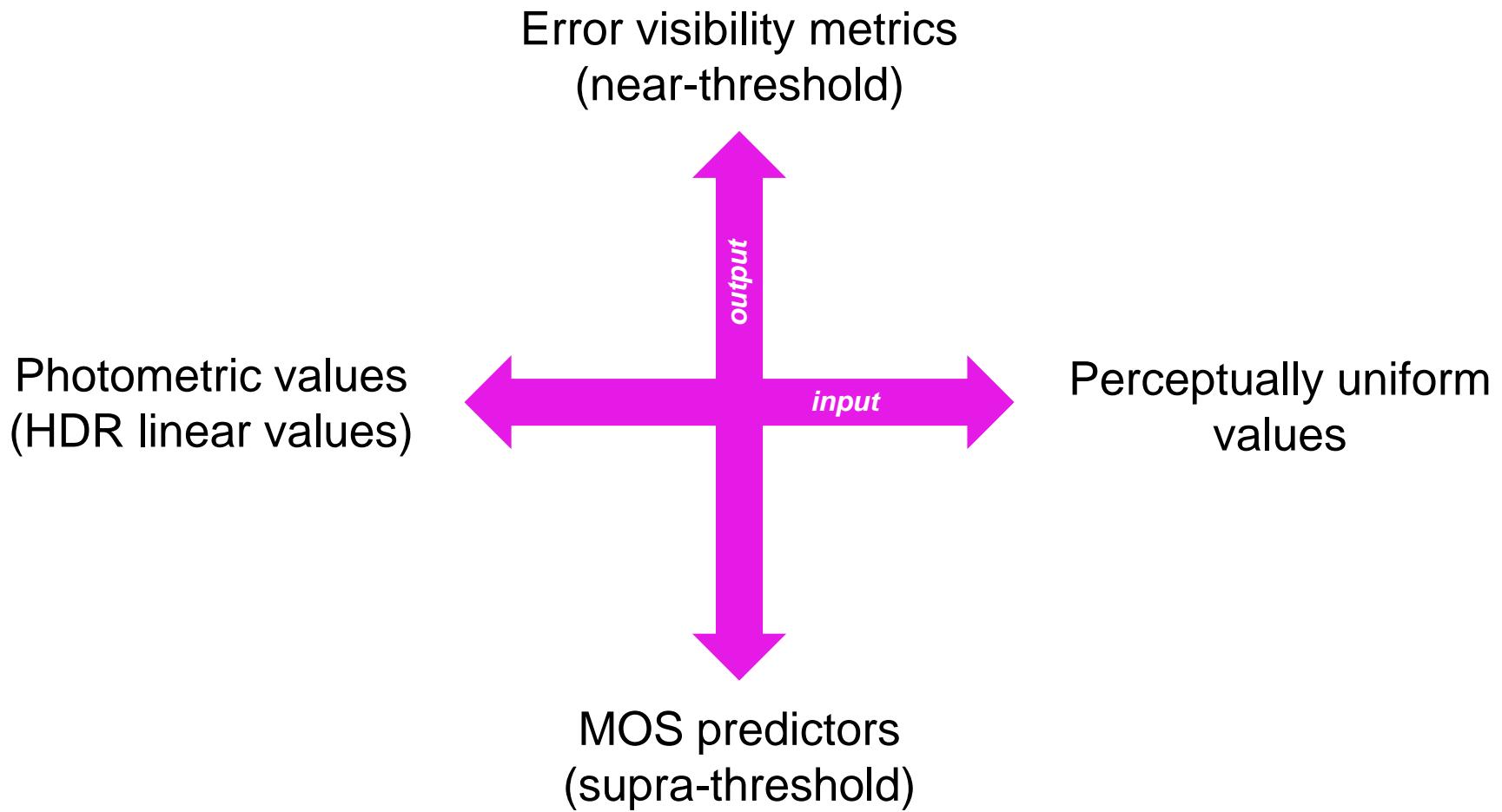
Measurement of HDR QoE through subjective tests

- **Some important differences w.r.t. LDR**
- **Effect of display**
 - Effects of high luminance and contrast
 - Higher visual fatigue and discomfort
 - Grading of the content: clipping of highlights, tone mapping for display
- **Ambient luminance**
 - Recommendation ITU-R BT.500-13 recommends the illumination should be approximately 15% of display peak luminance
 - About 600 cd/m² for a 4,000 nits display!
 - Too high ambient illumination increases perceived black level causing loss of details in the dark parts of the image (Mantiuk et al., 2010)
 - Too low ambient illumination induces discomfort and fatigue
 - Reflections on screen surface increase with luminance as well
- **Practical recommendations for ambient luminance:**
 - 150-200 cd/m² (Narwaria et al., 2014)
 - 10-20 cd/m² (Valenzise et al., 2014; De Simone et al., 2014; MPEG tests)

HDR image and video quality prediction

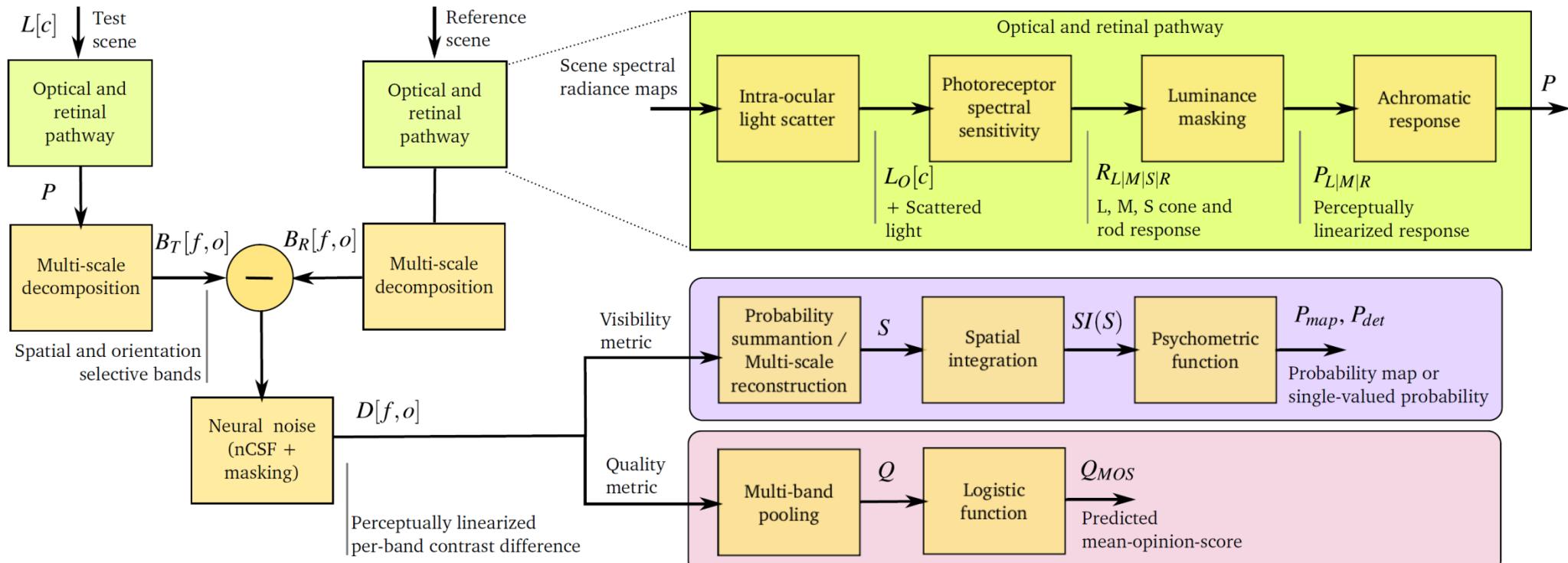
- **Visual quality is one of the component of QoE**
 - Especially important in the HDR *video delivery chain*
 - Measure the performance of video compression
 - Fidelity of tone mapping when HDR has to be shown on a LDR display
- **Full-reference vs. No-reference *quality metrics***
 - Perceptual fidelity vs. aesthetic judgements
- **Challenges w.r.t. LDR quality prediction**
 - HDR pixels encode scene luminance
 - Display rendering must be taken into account
 - The higher luminance renders noise more visible (contrast sensitivity is higher at higher)

Approaches for assessing HDR fidelity



HDR-VDP 2 (Visible Difference Predictor, Mantiuk'11)

- Accurate simulation of the early stages of HVS, including a new CSF
- Designed and calibrated to detect visibility of errors, it can be applied as a suprathreshold quality metric (MOS predictor)
- Generalizes to a broad range of viewing conditions (scotopic/photopic)



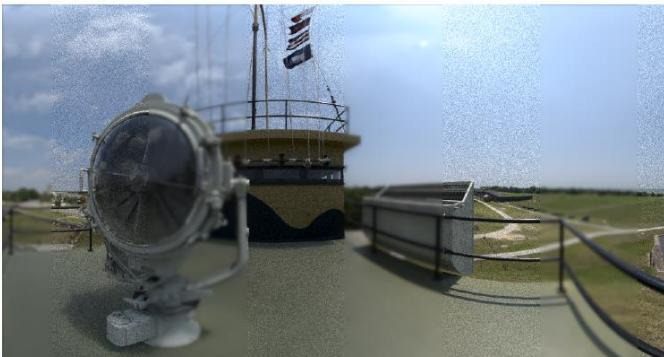
[Mantiuk et al., 2011]

HDR-VDP 2 – Output

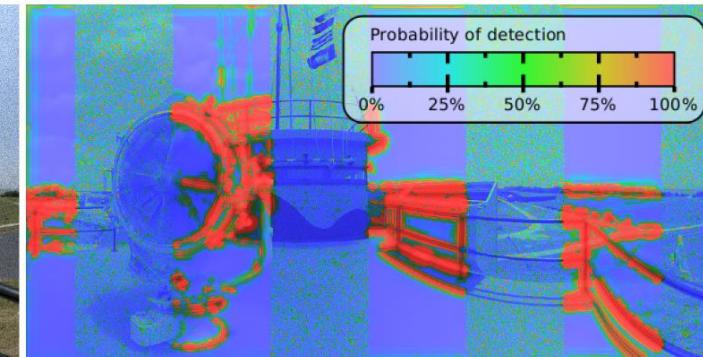
- **Visibility map (P_{map})**
 - Per pixel probability of detecting a difference
- **Global quality score (Q_{MOS})**
 - Value between 0 and 100
 - Obtained by pooling threshold-normalized subband differences
 - Pooling function obtained through model selection on two LDR training datasets
 - Version 2.2 of the metric has updated weights for the model computed on HDR content (Narwaria et al., 2015)



Reference Image



Test image



Probability of detection (screen, color)

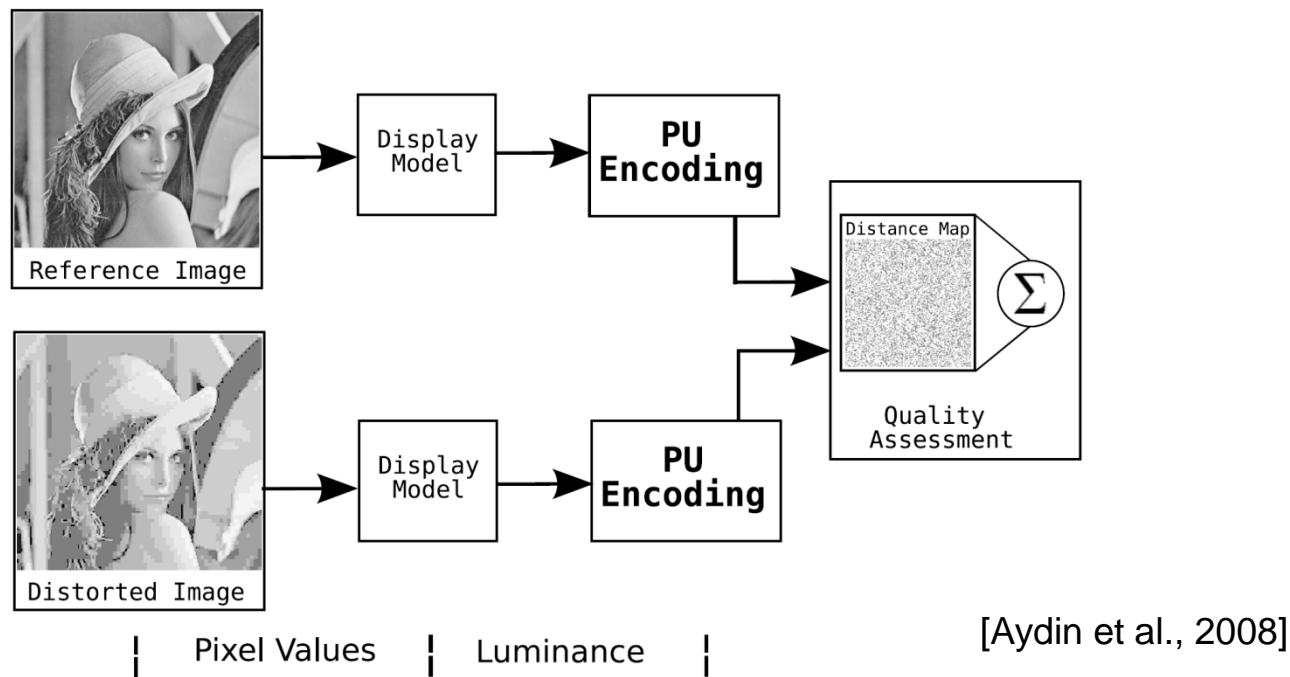
[Mantiuk et al., 2011]

LDR metrics on perceptually encoded pixels

- Many quality metrics used on LDR images compute operations or functions of pixel values
 - Hypothesis: pixels can be compared (e.g., differences can be computed) because they lie in a **perceptually uniform space**
 - Conventionally, LDR images are encoded with a gamma (BT.1886 EOTF, sRGB) that simulates the nonlinear response of HVS
- No longer true for HDR pixel values
 - Pixel values are proportional to physical luminance
 - Luminance masking and adaptation should be taken into account
- To be compared in a perceptually meaningful way, HDR pixels have to be **converted to perceptual units**
 - Luminance to brightness transformation
 - *Logarithm (Weber-Fechner law)*
 - *Power function (CIE LAB)*
 - *Perceptually uniform (PU) encoding* (Ayding et al., 2008)
 - CSF-based transfer functions (e.g., PQ)

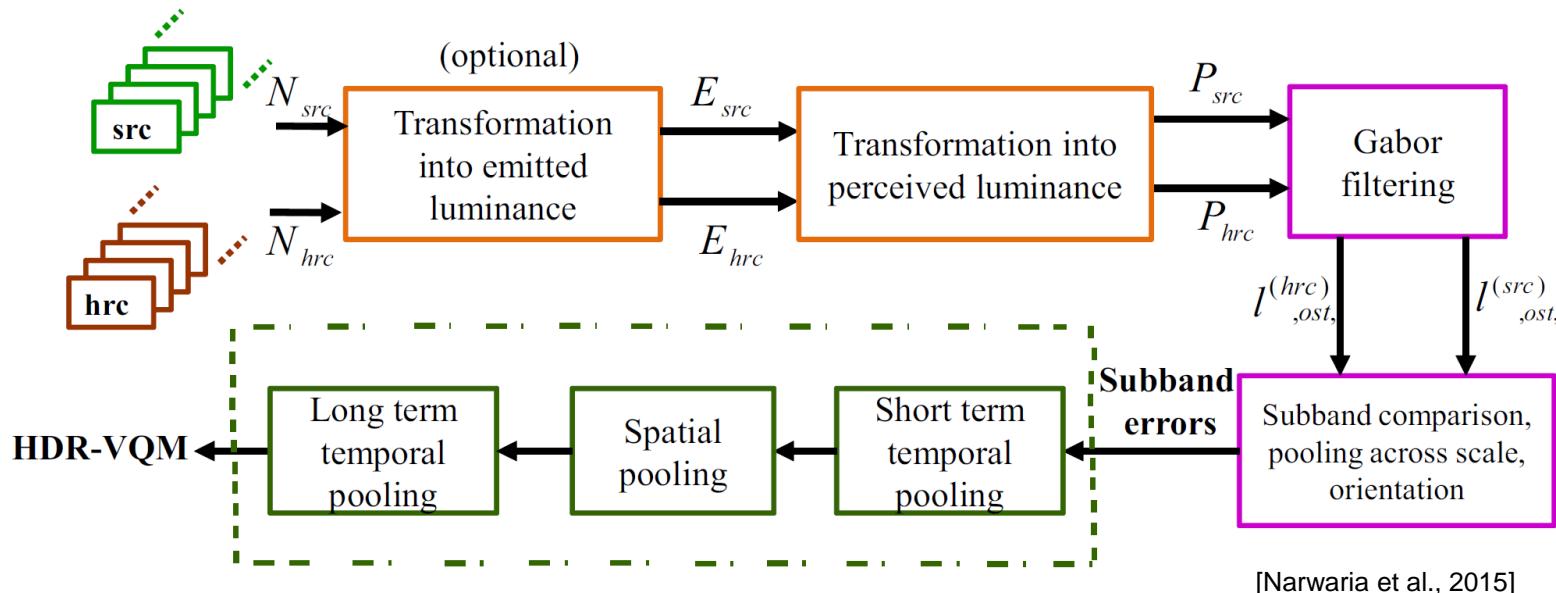
Extending LDR quality metrics to HDR

- Transform test and reference image pixels to perceptually uniform values before computing the quality metric
 - Differently from HDR-VDP, it is a simple luminance mapping
 - Computationally effective (look-up table)
 - The price to pay w.r.t. LDR is that the input of the mapping should be physical luminance in cd/m², i.e., a model of display is required



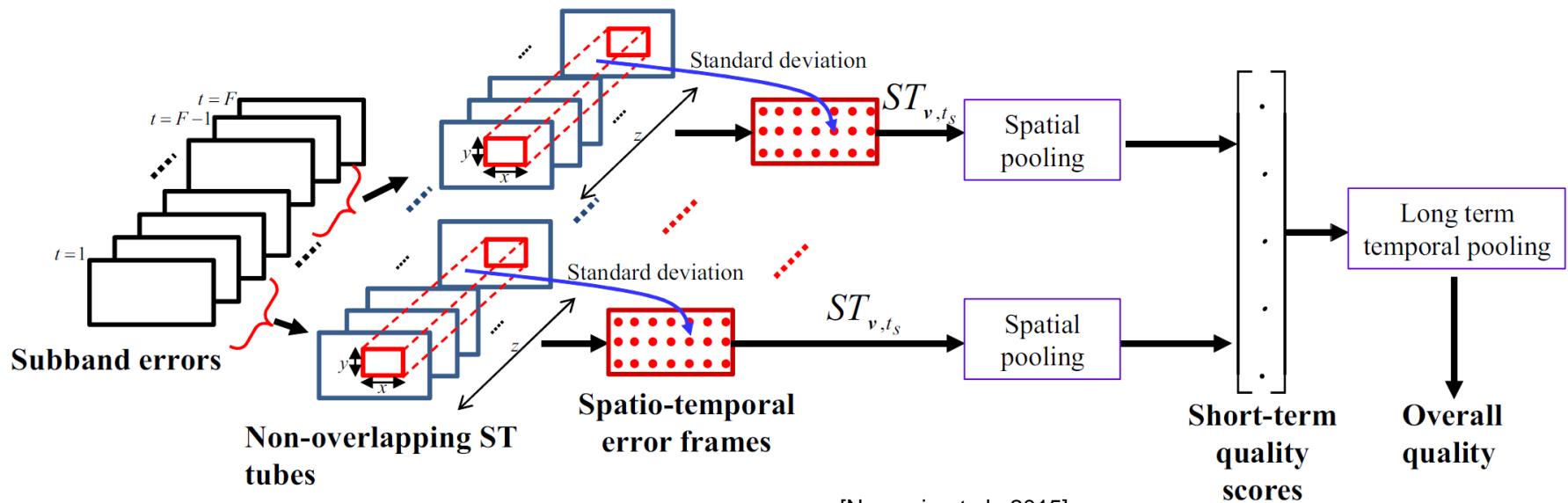
Extensions to video – HDR-VQM (Narwaria'15)

- Suprathreshold video quality metric based on perceptually uniform encoded HDR pixel values
- Compute errors in frequency subbands, similar to HDR-VDP
 - Much simpler modeling (no retinal image, no inter-band contrast, etc.)
 - Much faster
- Spatio-temporal pooling



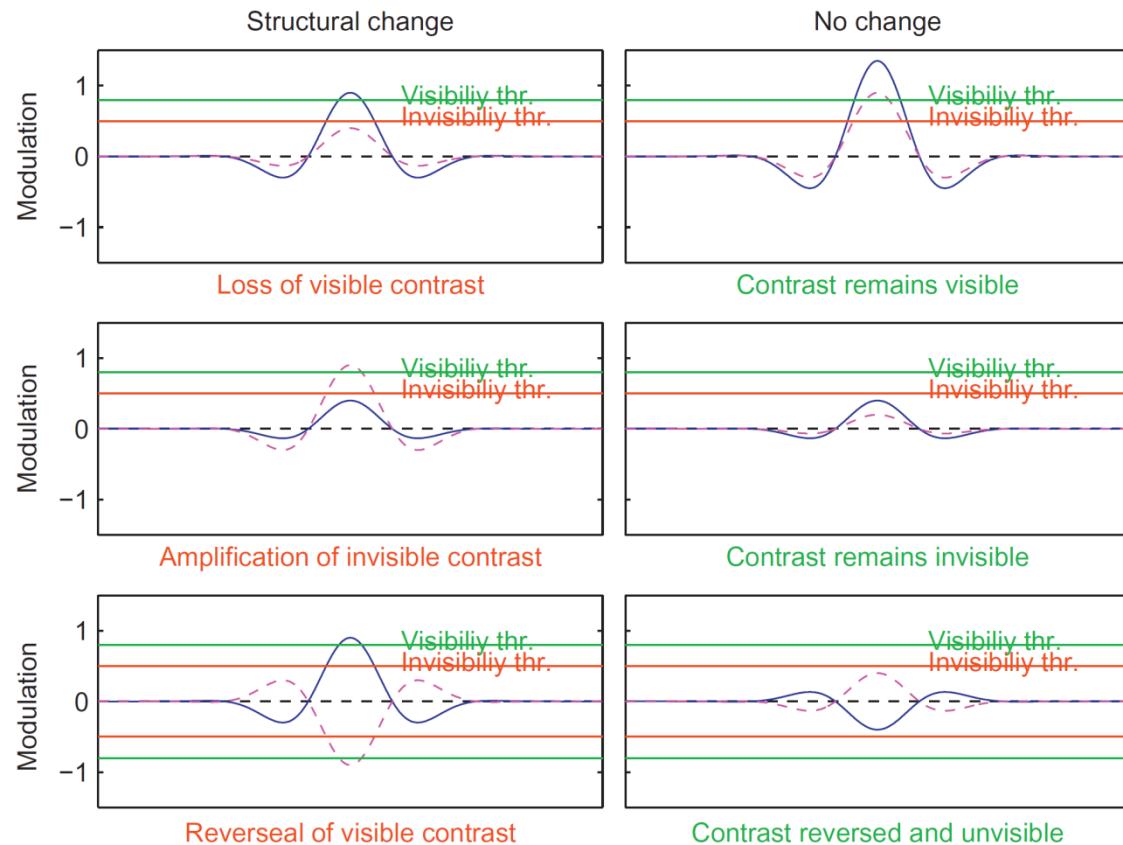
HDR-VQM Spatio-Temporal pooling

- Video divided in non-overlapping short-term spatio-temporal tubes
 - Spatial support to cover foveation area (approx. 2° of visual angle)
 - Temporal support: 300-500 ms
 - Standard deviation for short-term temporal pooling
- Spatial and long-term temporal pooling performed by excluding largest values from short-term temporal pooling



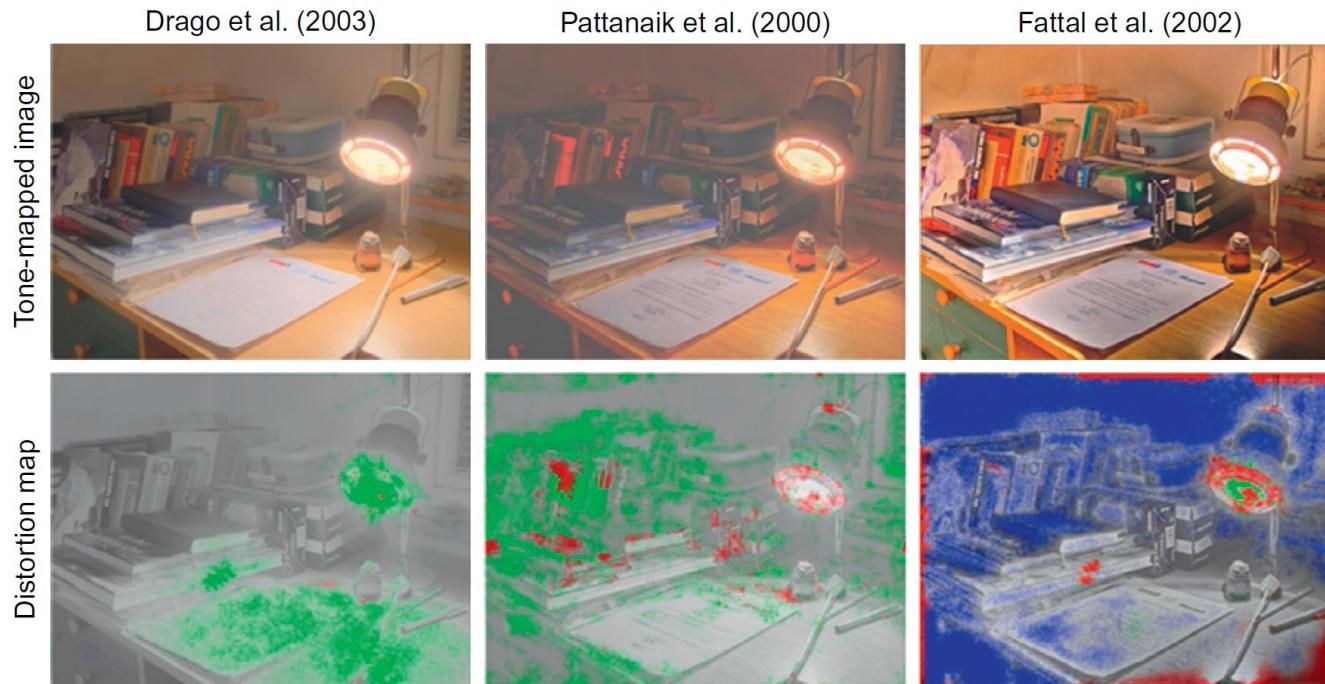
Dynamic range-independent metrics

- **Dynamic Range Independent (DRI) metric (Aydin et al., 2008)**
 - Visibility predictor
 - Adapted to evaluate images of different luminance and dynamic range (TMO's, iTMO's, display rendering)
- **3 structural changes can affect quality:**
 - Loss of visible contrast
 - Amplification of invisible contrast
 - Reversal of visible contrast
- **Thresholds values:**
 - Visibility > 95%
 - Invisibility < 50%



DRI metric: evaluation of TMO's

- **Output: distortion map**
 - Green: loss of visible contrast (e.g., details)
 - Blue: amplification of invisible noise (e.g., noise)
 - Red: contrast reversal (e.g., halos)
- **Suitable for visual inspection and qualitative evaluation**
- **Does not produce a global quality score**



[Aydin et al., 2008]

Tone-Mapped Image Quality Index (Yeganeh and Wang, 2013)

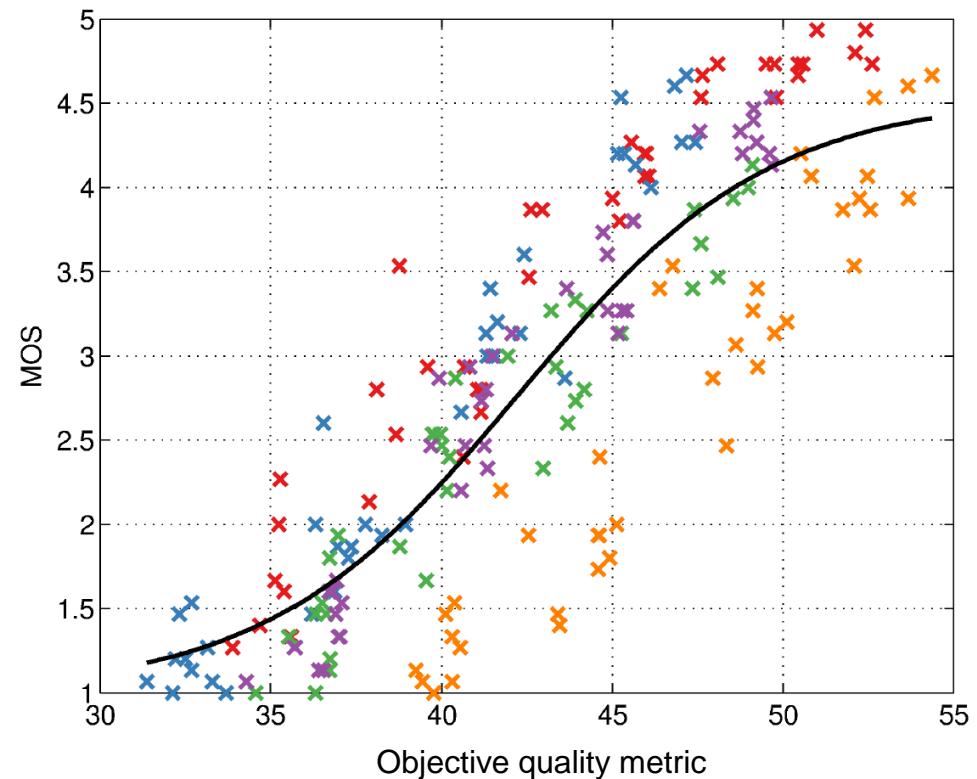
- Predicts overall quality of a tone-mapped image w.r.t. an HDR reference
- Structural similarity S :
 - Modified SSIM index without luminance component
 - Contrast component adapted to detect only cases in which invisible contrast becomes visible or vice versa (similar to DRI)
 - Visual model employing a CSF and a psychometric function
- Naturalness N :
 - Similarity between the histogram of tone-mapped image and the “average” histogram of LDR images
- TMQI metric is the combination of the two terms:

$$Q = aS^\alpha + (1 - a)N^\beta$$

- Spearman rank-order correlation coefficient (monotonicity of predictions) ~ 0.8

Measuring performance of fidelity metrics

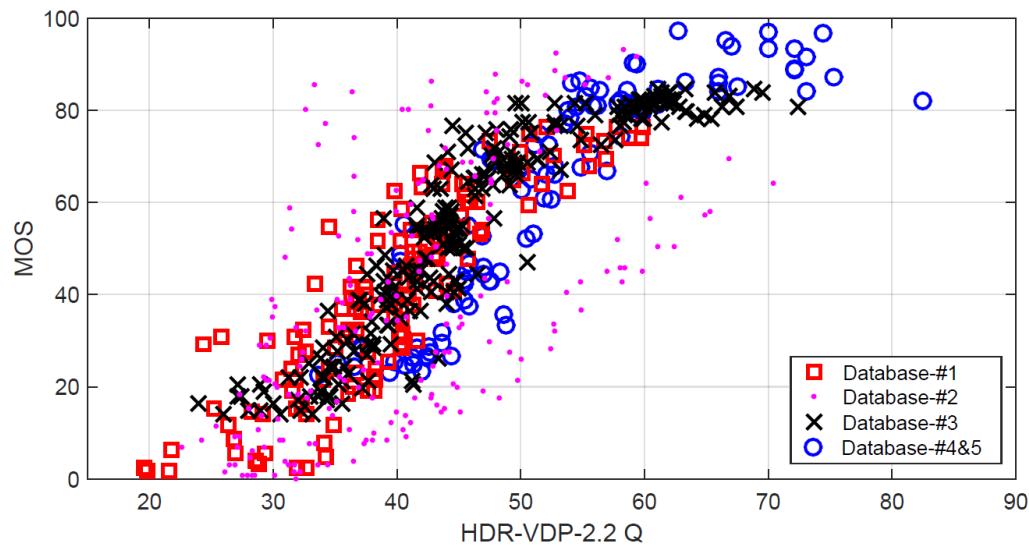
- Mean opinion scores predicted by quality metrics can be compared to actual MOS values collected in subjective studies
- Statistical evaluation of metrics predictions (ITU-T P.1401)
 - Accuracy – Pearson's correlation coefficient (PCC), root mean square error (RMSE)
 - Monotonicity – Spearman's rank-order correlation coefficient (SROCC)
 - Consistency – Outlier Ratio (OR)



Benchmark of HDR image/video quality metrics

- **Several studies on benchmarking HDR quality metrics**
 - Different datasets
 - Different kinds of distortion (compression algorithms, TMO's)
 - Different experimental procedures
 - Different conclusions!
- **Extensive performance evaluation on 690 HDR images**
 - 5 subjectively annotated datasets with aligned scores (Pinson and Wolf, 2003)

Database	Obs.	Meth.	Stim.	Compr.	TMO
#1 [18]	27	ACR-HR	140	JPEG ¹	iCAM06 [27]
#2 [28]	29	ACR-HR	210	JPEG 2000 ¹	AS [29] RG [30] RL [30] DR [31] Log
#3 [32]	24	DSIS	240	JPEG-XT	RG [30] MT [33]
#4 [16]	15	DSIS	50	JPEG ¹ JPEG 2000 ¹ JPEG-XT	Mai [34]
#5	15	DSIS	50	JPEG ¹ JPEG 2000 ¹	Mai [34] PQ [21], [35]



Benchmark of HDR image/video quality metrics

Metric	PCC						OR					
	Database #1	Database #2	Database #3	Database #4&5	Combined	Except Database #2	Database #1	Database #2	Database #3	Database #4&5	Combined	Except Database #2
Photometric-MSE	0.4051	0.1444	0.7080	0.5095	0.3742	0.6292	0.750	0.933	0.787	0.830	0.830	0.762
Photometric-PSNR	0.4409	0.2564	0.7132	0.5594	0.4967	0.6507	0.771	0.905	0.767	0.820	0.813	0.717
Photometric-SSIM	0.5016	0.3583	0.8655	0.6708	0.6220	0.7596	0.821	0.938	0.679	0.780	0.786	0.694
Photometric-IFC	0.7781	0.8234	0.9183	0.8195	0.8153	0.8132	0.750	0.871	0.546	0.610	0.661	0.596
Photometric-UQI	0.7718	0.8208	0.8846	0.7876	0.8102	0.8113	0.707	0.871	0.558	0.640	0.658	0.623
Photometric-VIF	0.7603	0.5076	0.8666	0.6144	0.6450	0.7916	0.679	0.948	0.617	0.800	0.787	0.652
PU-MSE	0.4824	0.3309	0.8559	0.8024	0.6100	0.7710	0.857	0.933	0.633	0.680	0.755	0.615
PU-PSNR	0.5297	0.3269	0.8606	0.8009	0.6093	0.7763	0.779	0.919	0.579	0.660	0.764	0.619
PU-SSIM	0.8661	0.7049	0.9532	0.9201	0.8352	0.9098	0.714	0.948	0.404	0.560	0.632	0.452
PU-IFC	0.7910	0.8422	0.9201	0.8566	0.8371	0.8446	0.750	0.886	0.500	0.610	0.642	0.575
PU-MSSIM	0.8847	0.7236	0.9564	0.9038	0.8515	0.9281	0.607	0.933	0.388	0.570	0.587	0.390
PU-UQI	0.7823	0.8507	0.8768	0.7777	0.8181	0.8077	0.664	0.848	0.583	0.680	0.643	0.613
PU-VIF	0.7845	0.7583	0.9349	0.9181	0.8449	0.8923	0.700	0.943	0.450	0.520	0.655	0.540
Log-MSE	0.6114	0.5314	0.8856	0.8820	0.6464	0.7953	0.843	0.924	0.592	0.570	0.693	0.588
Log-PSNR	0.6456	0.5624	0.8870	0.8819	0.6671	0.8011	0.786	0.919	0.588	0.580	0.751	0.598
Log-SSIM	0.8965	0.8035	0.9235	0.8255	0.8235	0.8656	0.643	0.876	0.525	0.570	0.671	0.535
Log-IFC	0.7919	0.8366	0.9167	0.8551	0.8322	0.8448	0.750	0.833	0.529	0.610	0.646	0.575
Log-UQI	0.7837	0.8268	0.8786	0.7830	0.8065	0.8052	0.671	0.843	0.579	0.630	0.662	0.613
Log-VIF	0.5079	0.6202	0.8354	0.7065	0.5919	0.7169	0.807	0.924	0.654	0.730	0.843	0.683
HDR-VDP-2.2 Q	0.9048	0.5980	0.9499	0.9407	0.8163	0.9385	0.564	0.919	0.346	0.520	0.587	0.421
HDR-VQM	0.8949	0.8059	0.9589	0.9333	0.8871	0.9383	0.514	0.895	0.383	0.530	0.575	0.410
mPSNR	0.6545	0.6564	0.8593	0.8587	0.7209	0.7974	0.771	0.895	0.667	0.610	0.706	0.633
tPSNR-YUV	0.5784	0.4524	0.8319	0.7789	0.6440	0.7675	0.800	0.952	0.625	0.670	0.752	0.646
CIE ΔE 2000	0.6088	0.2553	0.7889	0.6082	0.4971	0.7550	0.743	0.924	0.675	0.760	0.828	0.688

Perspectives and challenges

- **Color**

- All the metrics discussed above are color blind
- Color difference metrics such as CIE ΔE_{2000} have been designed for LDR content
- Do not take into account color appearance phenomena

- **Aesthetic quality**

- Artistic intent (in TMO, content grading for display, etc.)
- Automatic optimization of these tasks
- Estimation of aesthetic attributes (Aydin et al., 2015)
- In the case of HDR, predicting the perceived dynamic range and colorfulness (Hulusic et al., 2016)

- **Visual fatigue**

- HDR viewing may increase visual fatigue and discomfort
- Dependency on ambient illumination and display peak luminance (Rempel et al., 2009)

WRAP-UP

Perspectives and challenges

- **HDR imaging technology is quite mature**
 - Perceptual phenomena and their impact on Quality of Experience are well understood
 - Many tools for image acquisition and reproduction
- **Still many challenges to solve for video**
 - Efficient video coding, standardization, backward compatibility
 - Real-time high-quality display
 - Video tone mapping and inverse tone mapping
 - Color management
 - Quality of Experience and aesthetic evaluation, etc.
- **HDR is a fundamental requirement for true immersive entertainment and communication**
 - New and fascinating artistic choices in digital media creation
 - Increasing diffusion of HDR content
 - Big players in streaming, cinema and broadcasting actively involved in standardization

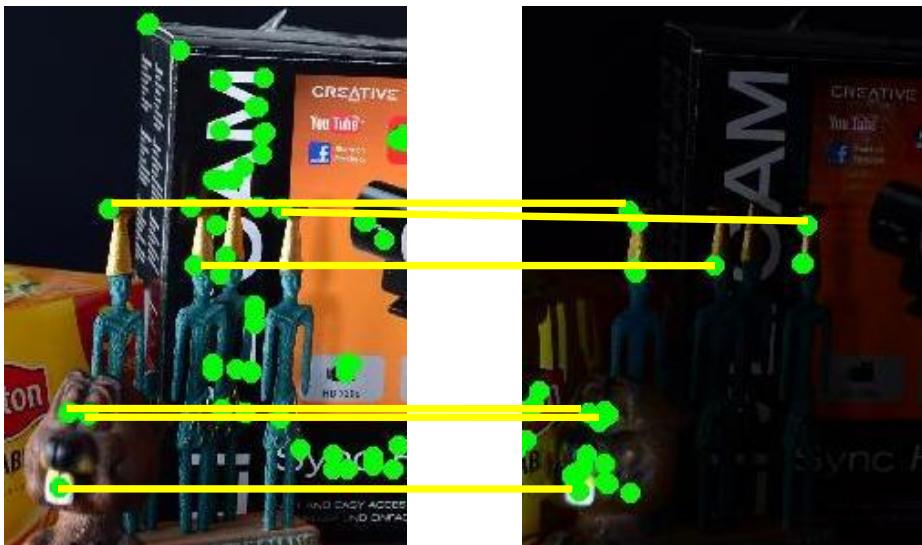
HDR beyond entertainment

- **High potential for a number of applications**
- **Computer vision**
 - Capture of dark and bright details for video surveillance
 - Automated driving and driver assistance systems
- **Simulation**
 - Realistic driving simulation
 - Virtual reality
- **Medical imaging**
 - Importance of accurate reproduction of gray levels
 - Design of novel luminance mapping for dark details

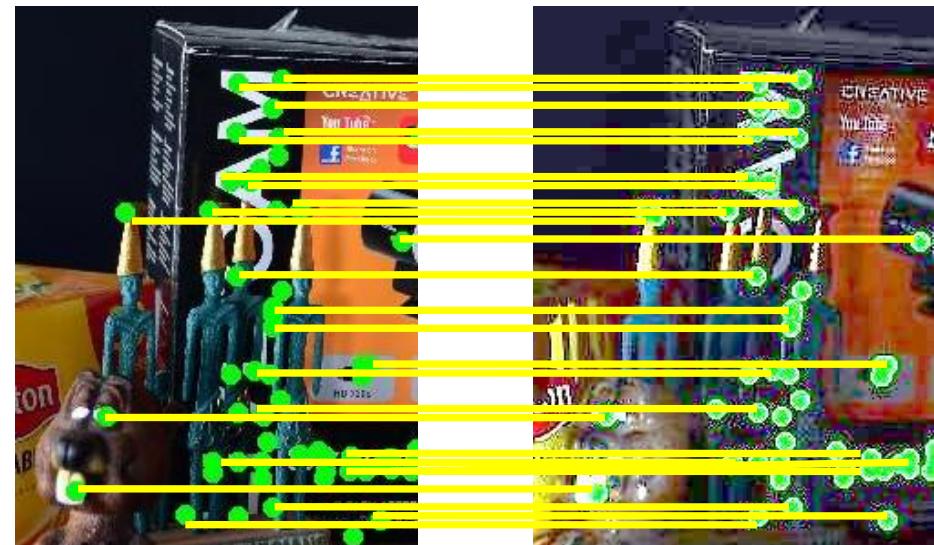


HDR for computer vision: image matching

- Illumination changes constitute a major challenge in video surveillance and analysis applications
 - Image matching is seriously affected by drastic changes in illumination
 - HDR can help to increase keypoint repeatability and descriptor matching
 - TMO's have to be optimized for this purpose



LDR



HDR

A. Rana, G. Valenzise, F. Dufaux, Evaluation of Feature Detection in HDR Based Imaging Under Changes in Illumination Conditions, ISM 2015

Safety in automated driving

- Florida, 30th of June 2016: first fatal Tesla car accident
- The autopilot sensors on the Model S failed to distinguish a white tractor-trailer crossing the highway against a bright sky



FURTHER READING AND RESOURCES

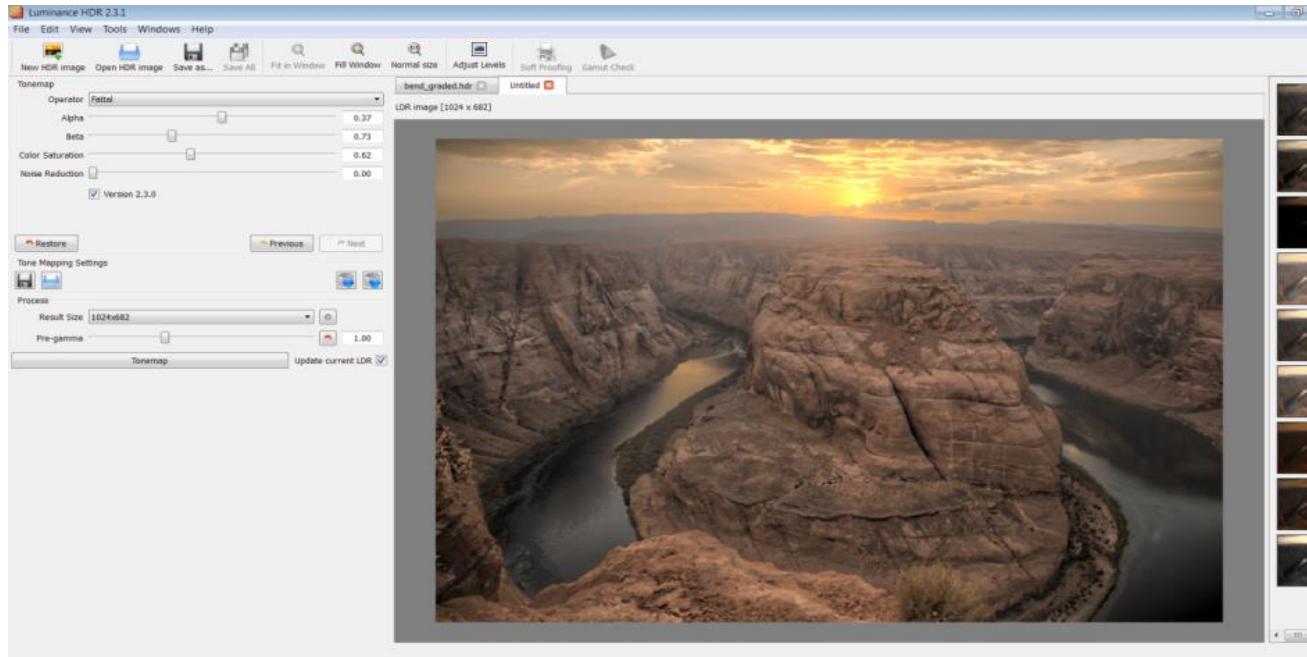
- **OpenEXR**
 - Developed by Industrial Light & Magic
 - I/O for .exr format
- **PFSTools**
 - Command line tools and C/Matlab libraries
 - HDR I/O, tone mapping, viewing utilities
- **Matlab HDR Toolbox**
 - HDR functions for tone mapping, inverse tone mapping and utilities
- **Piccante**
 - Open source C++ library
 - HDR image processing



HDR Applications

- **Luminance HDR**

- Based on PFS tools with QT interface
- Cross-platform
- HDR merging, tone mapping



HDR Applications

- **HDRshop**
 - Developed by Paul Debevec
- **Pictureaut**
 - Developed by Christian Bloch
 - Image based lighting, HDR Panorama creation
- **HDREfex Pro**
 - Plugin for Photoshop/Lightroom/Aperture
 - Creative photo effects
- **Photomatix**
 - HDR alignment and merging

HDR Content

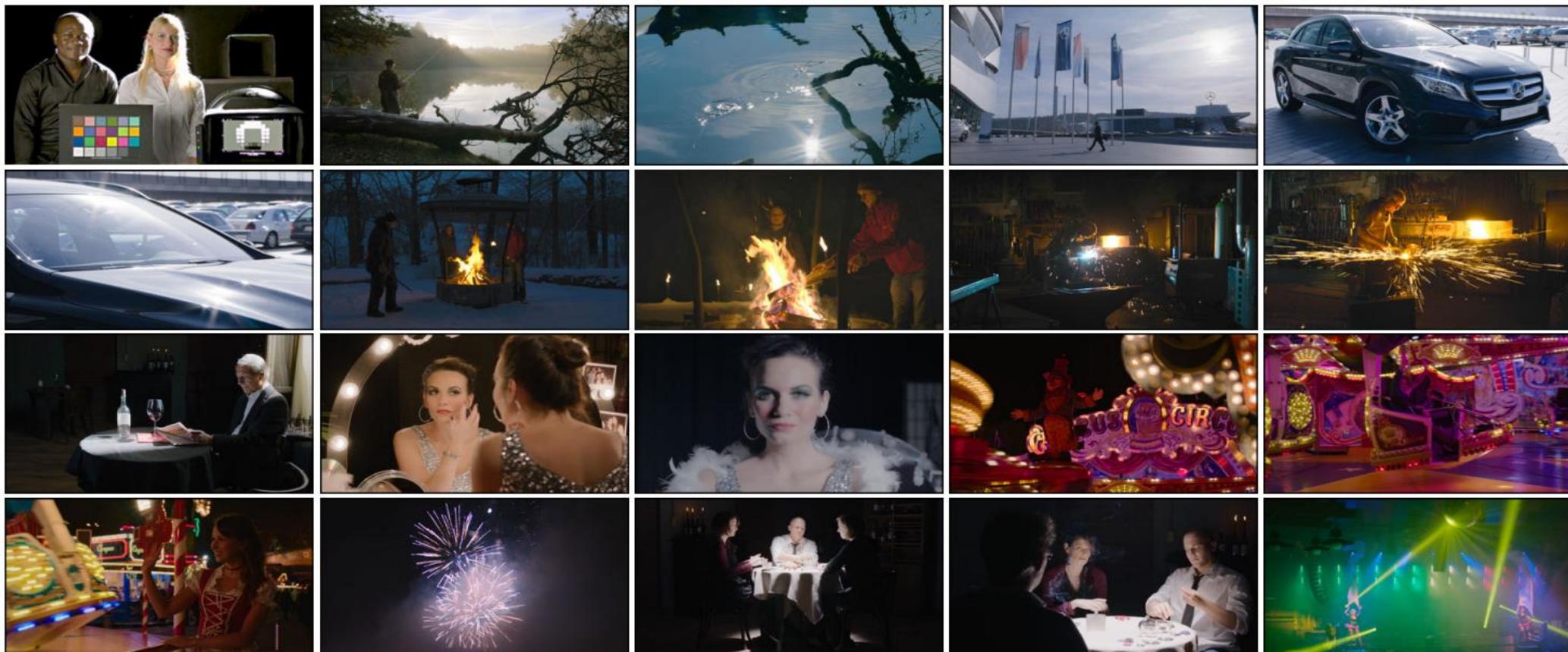
- **HDR Photographic Survey**
 - Almost 100 HDR photographs
 - Radiometrically calibrated
 - Colorimetric measurements for several images



HDR Content

- **Stuttgart HDR Video Dataset**

- Videos of challenging scenes with cinematic staging
- Captured using mirror rig – 2 exposures



References

- F. Dufaux, P. Le Callet, R. Mantiuk, M. Mrak, High Dynamic Range Video - From Acquisition, to Display and Applications, Academic Press, 2016
- F. Banterle, A. Artusi, K. Debattista, and A. Chalmers, Advanced High Dynamic Range Imaging, AK Peters / CRC Press, 2011
- E. Reinhard, G. Ward, P. Debevec, S. Pattanaik, W. Heidrich and K. Myszkowski, High Dynamic Range Imaging, 2nd edition, Morgan Kaufmann Publishers, 2010

References – Perception

- Fairchild, M.D., 2013. *Color appearance models*. John Wiley & Sons.
- Barten, P.G., 1999. *Contrast sensitivity of the human eye and its effects on image quality* (Vol. 72). SPIE press.
- T. Kunkel, S. Daly, S. Miller, J. Froehlich, 2016. Perceptual design for high dynamic range systems. In *High Dynamic Range Video: From Acquisition to Display and Applications*.
- Mantiuk, R., Myszkowski, K. and Seidel, H.P., 2006, February. Lossy compression of high dynamic range images and video. In *Electronic Imaging 2006* (pp. 60570V-60570V). International Society for Optics and Photonics.

References – Capture

- **HDR Capture / Sensors**
 - Hoefflinger, B. ed., 2007. *High-dynamic-range (HDR) vision*. Springer Berlin Heidelberg.
- **Ghost removal:**
 - Tursun, O.T., Akyüz, A.O., Erdem, A. and Erdem, E., 2015, May. The state of the art in HDR deghosting: A survey and evaluation. In *Computer Graphics Forum* (Vol. 34, No. 2, pp. 683-707).
 - Hafner, D., Demetz, O. and Weickert, J., 2014, August. Simultaneous HDR and Optic Flow Computation. In *ICPR* (pp. 2065-2070).

References – Tone mapping

- **Video Tonemapping**

- Eilertsen, G., Wanat, R., Mantiuk, R.K. and Unger, J., 2013, October. Evaluation of Tone Mapping Operators for HDR-Video. In *Computer Graphics Forum* (Vol. 32, No. 7, pp. 275-284).
- Boitard, R., Bouatouch, K., Cozot, R., Thoreau, D. and Gruson, A., 2012, October. Temporal coherency for video tone mapping. In *SPIE Optical Engineering+ Applications* (pp. 84990D-84990D). International Society for Optics and Photonics.
- Kang, S.B., Uyttendaele, M., Winder, S. and Szeliski, R., 2003, July. High dynamic range video. In *ACM Transactions on Graphics (TOG)* (Vol. 22, No. 3, pp. 319-325). ACM.

References – Tone mapping

- **Inverse Tonemapping**

- Rempel, A.G., Trentacoste, M., Seetzen, H., Young, H.D., Heidrich, W., Whitehead, L. and Ward, G., 2007, August. Ldr2hdr: on-the-fly reverse tone mapping of legacy video and photographs. In *ACM Transactions on Graphics (TOG)* (Vol. 26, No. 3, p. 39). ACM.
- Banterle, F., Ledda, P., Debattista, K. and Chalmers, A., 2006, November. Inverse tone mapping. In *Proceedings of the 4th international conference on Computer graphics and interactive techniques in Australasia and Southeast Asia* (pp. 349-356). ACM.

References – Color Management

- **Color Spaces**
 - Fairchild, M.D. and Wyble, D.R., 2010, January. hdr-CIELAB and hdr-IPT: Simple models for describing the color of high-dynamic-range and wide-color-gamut images. In *Color and Imaging Conference* (Vol. 2010, No. 1, pp. 322-326). Society for Imaging Science and Technology.
- **Color Appearance Modeling**
 - Fairchild, M.D., 2013. *Color appearance models*. John Wiley & Sons.
 - Kuang, J., Johnson, G.M. and Fairchild, M.D., 2007. iCAM06: A refined image appearance model for HDR image rendering. *Journal of Visual Communication and Image Representation*, 18(5), pp.406-414.
 - Reinhard, E., Pouli, T., Kunkel, T., Long, B., Ballestad, A. and Damberg, G., 2012. Calibrated image appearance reproduction. *ACM Transactions on Graphics (TOG)*, 31(6), p.201.

References – Color Management

- **Gamut Management**

- Sidukova, E., Pouli, T., Artusi, A., Akyuz, A. O., Banterle, F., Reinhard, E., Mazlumoglu, Z., ‘A Gamut Mapping Framework for Color-Accurate Reproduction of HDR Images’, IEEE Computer Graphics and Applications, 36(4), 2016

References – Video Compression

- Sullivan, G. J.; Ohm, J.-R.; Han, W.-J.; Wiegand, T. Overview of the High Efficiency Video Coding (HEVC) Standard, *IEEE Transactions on Circuits and Systems for Video Technology*, 22 (12), 1649-1668, Dec. 2012.
- S. Miller, M. Nezamabadi and S. Daly, Perceptual signal coding for more efficient usage of bit codes, in Annual Technical Conference Exhibition, SMPTE 2012, pp. 1–9, Oct. 2012.
- T. Borer and A. Cotton, A. A “Display Independent” High Dynamic Range Television System, BBC White Paper, Sept. 2015.
- Z. Mai, H. Mansour, R. Mantiuk, P. Nasiopoulos, R. Ward, and W. Heidrich, “Optimizing a Tone Curve for Backward-Compatible High Dynamic Range Image and Video Compression”, *IEEE Transactions on Image Processing*, vol. 20, no. 6, pp. 1558-1571, June 2011
- A. Koz and F. Dufaux, Methods for Improving the Tone Mapping for Backward Compatible High Dynamic Range Image and Video Compression, *Signal Processing: Image Communication*, vol. 29, no. 2, pp. 274-292, February 2014.

References – Display

- Seetzen, H., Heidrich, W., Stuerzlinger, W., Ward, G., Whitehead, L., Trentacoste, M., Ghosh, A. and Vorozcova, A., 2004. High dynamic range display systems. *ACM Transactions on Graphics (TOG)*, 23(3), pp.760-768.
- Trentacoste, M., Heidrich, W., Whitehead, L., Seetzen, H. and Ward, G., 2007. Photometric image processing for high dynamic range displays. *Journal of Visual Communication and Image Representation*, 18(5), pp.439-451.
- Zerman, E., Valenzise, G., De Simone, F., Banterle, F. and Dufaux, F., 2015, September. Effects of display rendering on HDR image quality assessment. In *SPIE Optical Engineering+ Applications* (pp. 95990R-95990R). International Society for Optics and Photonics.
- Zerman, E., Valenzise, G. and Dufaux, F., 2016, July. A dual modulation algorithm for accurate reproduction of high dynamic range video. In *IEEE 12th Image, Video, and Multidimensional Signal Processing Workshop (IVMSP)* (pp. 1-5). IEEE.
- Burini, N., Nadernejad, E., Korhonen, J., Forchhammer, S. and Wu, X., 2013. Modeling power-constrained optimal backlight dimming for color displays. *Journal of Display Technology*, 9(8), pp.656-665.
- Narwaria, M., da Silva, M.P. and Le Callet, P., 2016. Dual modulation for LED-backlit HDR displays. *High Dynamic Range Video: From Acquisition, to Display and Applications*.
- Kunkel, T., Daly, S., Miller, S., and Froehlich, J., 2016. Perceptual design for high dynamic range systems. *High Dynamic Range Video: From Acquisition, to Display and Applications*.
- Chalmers A., Karr B., Suma R., and Debattista K., 2016. Fifty shades of HDR. In *IEEE Digital Media Industry and Academic Forum*

References – Quality of Experience

- Yeganeh, H. and Wang, Z., 2013. Objective quality assessment of tone-mapped images. *IEEE Transactions on Image Processing*, 22(2), pp.657-667.
- Valenzise, G., De Simone, F., Lauga, P. and Dufaux, F., 2014, September. Performance evaluation of objective quality metrics for HDR image compression. In *SPIE Optical Engineering+ Applications* (pp. 92170C-92170C). International Society for Optics and Photonics.
- Aydin, T.O., Mantiuk, R., Myszkowski, K. and Seidel, H.P., 2008. Dynamic range independent image quality assessment. *ACM Transactions on Graphics (TOG)*, 27(3), p.69.
- Mantiuk, R., Kim, K.J., Rempel, A.G. and Heidrich, W., 2011, August. HDR-VDP-2: a calibrated visual metric for visibility and quality predictions in all luminance conditions. In *ACM Transactions on Graphics (TOG)* (Vol. 30, No. 4, p. 40). ACM.

References – Quality of Experience

- Aydn, T.O., Mantiuk, R. and Seidel, H.P., 2008, February. Extending quality metrics to full luminance range images. In *Electronic Imaging 2008* (pp. 68060B-68060B). International Society for Optics and Photonics.
- Narwaria, M., Da Silva, M.P. and Le Callet, P., 2015. HDR-VQM: An objective quality measure for high dynamic range video. *Signal Processing: Image Communication*, 35, pp.46-60.
- Rempel, A.G., Heidrich, W., Li, H. and Mantiuk, R., 2009, September. Video viewing preferences for HDR displays under varying ambient illumination. In *Proceedings of the 6th Symposium on Applied Perception in Graphics and Visualization* (pp. 45-52). ACM.
- Aydn, T.O., Smolic, A. and Gross, M., 2015. Automated aesthetic analysis of photographic images. *IEEE transactions on visualization and computer graphics*, 21(1), pp.31-42.
- Hulusic, V., Valenzise, G., Provenzi, E., Debattista, K. and Dufaux, F., 2016, June. Perceived dynamic range of HDR images. In *2016 Eighth International Conference on Quality of Multimedia Experience (QoMEX)* (pp. 1-6). IEEE.