

# Graded Modal Simple Type Theory (GMSTT)

August 13, 2018

## 1 Introduction

## 2 Graded Modal Simple Type Theory (GMSTT)

## 3 Graded Linear Exponential Comonad

## 4 Double Categorical Analysis

**Lemma 4.1** (Duplication in **SMC**). *The absorption and distribution axioms from the definition of a graded linear exponential comonad (Definition ?) can be replaced by the following statement: for every  $r \in \mathcal{R}$ , both*

$$\delta_{-,r} : D(- * r) \rightarrow D(-); D(r) \quad \delta_{-,s} : D(s * -) \rightarrow D(s); D(-)$$

*are 2-cells of the following type in **SMC**:*

$$\begin{array}{ccc} \mathcal{R}^+ & \xrightarrow{r * -} & \mathcal{R}^+ \\ \downarrow D & \searrow \delta_{r,-} & \downarrow D \\ [\mathcal{C}, \mathcal{C}]_l & \xrightarrow{-; D(r)} & [\mathcal{C}, \mathcal{C}]_l \end{array} \quad \begin{array}{ccc} \mathcal{R}^+ & \xrightarrow{- * s} & \mathcal{R}^+ \\ \downarrow D & \searrow \delta_{-,s} & \downarrow D \\ [\mathcal{C}, \mathcal{C}]_l & \xrightarrow{D(s); -} & [\mathcal{C}, \mathcal{C}]_l \end{array}$$