

$vars, n, a, x, y, z, w, m, o$

$ivar, i, k, j, l$

$R, S, T ::=$   
 $| 0$   
 $| S + T$   
 $| S - T$   
 $| HA$

$A, B, C ::=$   
 $| \perp$   
 $| A \oplus B$   
 $| A \bullet B$   
 $| JS$

$s, t ::=$   
 $| x$   
 $| \text{connect}_w \text{ to } t$   
 $| t_1 \cdot t_2$   
 $| \text{false } t$   
 $| x(t)$   
 $| \text{mkc}(t, x)$   
 $| \text{postp}(x \mapsto t_1, t_2)$   
 $| \text{inl } t$   
 $| \text{inr } t$   
 $| \text{case } t_1 \text{ of } x.t_2, y.t_3$   
 $| He$   
 $| \text{let } Jx = e \text{ in } t_2$   
 $| \text{let } Hx = t_1 \text{ in } t_2$   
 $| (t) \quad S$

$e, u ::=$   
 $| x$   
 $| \text{connect}_\perp \text{ to } e$   
 $| \text{postp}_\perp e$   
 $| \text{connect to } e$   
 $| \text{postp}(x \mapsto e_1, e_2)$   
 $| \text{mkc}(e, x)$

$$\begin{array}{lcl}
& | & x(e) \\
& | & e_1 \oplus e_2 \\
& | & \text{casel } e \\
& | & \text{caser } e \\
& | & \mathbf{J} t \\
& | & (e) \quad \mathbf{S} \\
\\
\Psi, \Pi & ::= & \\
& | & \cdot \\
& | & t : T \\
& | & \Psi, \Pi \\
& | & (\Psi) \quad \mathbf{S} \\
\\
\Gamma, \Delta & ::= & \\
& | & \cdot \\
& | & e : A \\
& | & \Gamma, \Gamma' \\
& | & (\Gamma) \quad \mathbf{S}
\end{array}$$

$$\boxed{x : S \vdash_{\mathbf{C}} \Psi}$$

$$\begin{array}{c}
\frac{}{x : S \vdash_{\mathbf{C}} x : S} \text{C\_VAR} \\
\\
\frac{s : T' \in \Psi \quad x : S \vdash_{\mathbf{C}} \Psi}{x : S \vdash_{\mathbf{C}} \text{connect}_w \text{to } s : T, \Psi} \text{C\_WEAK} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t_1 : T, t_2 : T, \Psi}{x : S \vdash_{\mathbf{C}} t_1 \cdot t_2 : T, \Psi} \text{C\_CONTR} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t : 0, \Psi \quad x_1 : S_1 \vdash_{\mathbf{C}} \Psi_1 \dots x_i : S_i \vdash_{\mathbf{C}} \Psi_i}{x : S \vdash_{\mathbf{C}} [\text{false } t/x_1] \Psi_1, \dots, [\text{false } t/x_i] \Psi_i, \Psi} \text{C\_ZERO} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t : T_1, \Psi_1 \quad y : T_2 \vdash_{\mathbf{C}} \Psi_2}{x : S \vdash_{\mathbf{C}} \Psi_1, \text{mkc}(t, y) : T_1 - T_2, [y(t)/y] \Psi_2} \text{C\_SUBI} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t_1 : T_1 - T_2, \Psi_1 \quad y : T_1 \vdash_{\mathbf{C}} t_2 : T_2, \Psi_2}{x : S \vdash_{\mathbf{C}} \text{postp}(y \mapsto t_2, t_1), \Psi_1, [y(t_1)/y] \Psi_2} \text{C\_SUBE} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t : T_1, \Psi}{x : S \vdash_{\mathbf{C}} \text{inl } t : T_1 + T_2, \Psi} \text{C\_ORI1} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t : T_2, \Psi}{x : S \vdash_{\mathbf{C}} \text{inr } t : T_1 + T_2, \Psi} \text{C\_ORI2}
\end{array}$$

$$\begin{array}{c}
\frac{y : T_1 \vdash_C \Psi_2 \quad y : T_2 \vdash_C \Psi_3 \quad x : S \vdash_C t : T_1 + T_2, \Psi_1 \quad |\Psi_2| = |\Psi_3|}{x : S \vdash_C \Psi_1, \text{case } t \text{ of } y. \Psi_2, y. \Psi_3} \text{C\_ORE} \\
\\
\frac{x : S \vdash_C t : \mathsf{HA}, \Psi_1 \quad x : A \vdash_L \cdot; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : S \vdash_C \Psi_1 \cdot (\text{let } \mathsf{H} y = t \text{ in } \Psi_2)} \text{C\_HE}
\end{array}$$

$$\boxed{x : A \vdash_L \Delta; \Psi}$$

$$\begin{array}{c}
\frac{}{x : A \vdash_L x : A; \Psi} \text{L\_VAR} \\
\\
\frac{s : T' \in \Psi \quad x : A \vdash_L \Delta; \Psi}{x : A \vdash_L \Delta; \text{connect}_w \text{ to } s : T, \Psi} \text{L\_WEAK} \\
\\
\frac{x : A \vdash_L \Delta; t_1 : T, t_2 : T, \Psi}{x : A \vdash_L \Delta; t_1 \cdot t_2 : T, \Psi} \text{L\_CONTR} \\
\\
\frac{x : A \vdash_L \Delta; \Psi \quad e : B \in \Delta}{x : A \vdash_L \text{connect}_\perp \text{ to } e : \perp, \Delta; \Psi} \text{L\_PERPI} \\
\\
\frac{x : A \vdash_L e : \perp, \Delta; \Psi}{x : A \vdash_L \text{postp}_\perp e, \Delta; \Psi} \text{L\_PERPE} \\
\\
\frac{x : A \vdash_L \Delta_1, e : B; \Psi_1 \quad y : C \vdash_L \Delta_2; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta_1, \text{mkc}(e, y) : B \bullet C, [y(e)/y]\Delta_2; \Psi_1 \cdot [y(e)/y]\Psi_2} \text{L\_SUBI} \\
\\
\frac{x : A \vdash_L \Delta_1, e_1 : B \bullet C; \Psi_1 \quad y : C \vdash_L e_2 : B, \Delta_2; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta_1, \text{postp}(y \mapsto e_2, e_1), [y(e_1)/y]\Delta_2; \Psi_1 \cdot [y(e_1)/y]\Psi_2} \text{L\_SUBE} \\
\\
\frac{x : A \vdash_L \Delta_1, e_1 : B, e_2 : C, \Delta_2; \Psi}{x : A \vdash_L \Delta_1, e_1 \oplus e_2 : B \oplus C, \Delta_2; \Psi} \text{L\_PARI} \\
\\
\frac{y : B \vdash_L \Delta_2; \Psi_2 \quad |\Psi_2| = |\Psi_3| \quad z : C \vdash_L \Delta_3; \Psi_3 \quad x : A \vdash_L e : B \oplus C, \Delta_1; \Psi_1 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta_1, [\text{case}_l(e)/y]\Delta_2, [\text{case}_r(e)/z]\Delta_3; \Psi_1 \cdot [\text{case}_l(e)/y]\Psi_2 \cdot [\text{case}_r(e)/z]\Psi_3} \text{L\_PARE} \\
\\
\frac{x : A \vdash_L \Delta; t : T, \Psi}{x : A \vdash_L \Delta, \mathsf{J} t : \mathsf{J} T; \Psi} \text{L\_JI} \\
\\
\frac{x : A \vdash_L \Delta, e : \mathsf{J} T; \Psi_1 \quad y : T \vdash_C \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta; \Psi_1 \cdot \text{let } \mathsf{J} y = e \text{ in } \Psi_2} \text{L\_JE} \\
\\
\frac{x : A \vdash_L \Delta, e : B; \Psi}{x : A \vdash_L \Delta; \mathsf{H} e : \mathsf{H} B, \Psi} \text{L\_HI}
\end{array}$$