

$vars, n, a, x, y, z, w, m, o$

$ivar, i, k, j, l$

$R, S, T ::=$   
 $| 0$   
 $| S + T$   
 $| S - T$   
 $| HA$

$A, B, C ::=$   
 $| \perp$   
 $| A \oplus B$   
 $| A \bullet B$   
 $| JS$

$s, t ::=$   
 $| x$   
 $| \text{connect}_w \text{ to } t$   
 $| t_1 \cdot t_2$   
 $| \text{let } 0 = t_1 \text{ in } t_2$   
 $| x(t)$   
 $| \text{mkc}(t, x)$   
 $| \text{postp}(x \mapsto t_1, t_2)$   
 $| \text{inl } t$   
 $| \text{inr } t$   
 $| \text{case } t_1 \text{ of } x.t_2, y.t_3$   
 $| H e$   
 $| \text{let } J x = e \text{ in } t_2$   
 $| \text{let } H x = t_1 \text{ in } t_2$   
 $| (t) \quad S$

$e, u ::=$   
 $| x$   
 $| \text{connect}_\perp \text{ to } e$   
 $| \text{postp}_\perp e$   
 $| \text{connect to } e$   
 $| \text{postp}(x \mapsto e_1, e_2)$   
 $| \text{mkc}(e, x)$

|                  |       |                   |          |
|------------------|-------|-------------------|----------|
|                  |       | $x(e)$            |          |
|                  |       | $e_1 \oplus e_2$  |          |
|                  |       | <b>casel</b> $e$  |          |
|                  |       | <b>caser</b> $e$  |          |
|                  |       | <b>J</b> $t$      |          |
|                  |       | $(e)$             | <b>S</b> |
| $\Psi, \Pi$      | $::=$ |                   |          |
|                  |       | $\cdot$           |          |
|                  |       | $t : T$           |          |
|                  |       | $\Psi, \Pi$       |          |
|                  |       | $(\Psi)$          | <b>S</b> |
| $\Gamma, \Delta$ | $::=$ |                   |          |
|                  |       | $\cdot$           |          |
|                  |       | $e : A$           |          |
|                  |       | $\Gamma, \Gamma'$ |          |
|                  |       | $(\Gamma)$        | <b>S</b> |

$$\boxed{x : S \vdash_{\mathbf{C}} \Psi}$$

$$\begin{array}{c}
\frac{}{x : S \vdash_{\mathbf{C}} x : S} \text{C\_VAR} \\
\frac{s : T' \in \Psi}{x : S \vdash_{\mathbf{C}} \text{connect}_w \text{to } s : T, \Psi} \text{C\_WEAK} \\
\frac{x : S \vdash_{\mathbf{C}} t_1 : T, t_2 : T, \Psi}{x : S \vdash_{\mathbf{C}} t_1 \cdot t_2 : T, \Psi} \text{C\_CONTR} \\
\frac{x : S \vdash_{\mathbf{C}} t : 0, \Psi \quad x_1 : S_1 \vdash_{\mathbf{C}} \Psi_1 \dots x_i : S_i \vdash_{\mathbf{C}} \Psi_i}{x : S \vdash_{\mathbf{C}} \text{let } 0 = t \text{ in } \Psi_1, \dots, \text{let } 0 = t \text{ in } \Psi_i, \Psi} \text{C\_ZERO} \\
\frac{x : S \vdash_{\mathbf{C}} t : T_1, \Psi_1 \quad y : T_2 \vdash_{\mathbf{C}} \Psi_2}{x : S \vdash_{\mathbf{C}} \Psi_1, \text{mkc}(t, y) : T_1 - T_2, [y(t)/y]\Psi_2} \text{C\_SUBI} \\
\frac{x : S \vdash_{\mathbf{C}} t_1 : T_1 - T_2, \Psi_1 \quad y : T_1 \vdash_{\mathbf{C}} t_2 : T_2, \Psi_2}{x : S \vdash_{\mathbf{C}} \text{postp}(y \mapsto t_2, t_1), \Psi_1, [z(t_1)/z]\Psi_2} \text{C\_SUBE} \\
\frac{x : S \vdash_{\mathbf{C}} t : T_1, \Psi}{x : S \vdash_{\mathbf{C}} \text{inl } t : T_1 + T_2, \Psi} \text{C\_ORI1} \\
\frac{x : S \vdash_{\mathbf{C}} t : T_2, \Psi}{x : S \vdash_{\mathbf{C}} \text{inr } t : T_1 + T_2, \Psi} \text{C\_ORI2}
\end{array}$$

$$\begin{array}{c}
\frac{y : T_1 \vdash_C \Psi_2 \quad y : T_2 \vdash_C \Psi_3 \quad x : S \vdash_C t : T_1 + T_2, \Psi_1 \quad |\Psi_2| = |\Psi_3|}{x : S \vdash_C \Psi_1, \text{case } t \text{ of } y. \Psi_2, y. \Psi_3} \text{C\_ORE} \\
\\
\frac{x : S \vdash_C t : \text{HA}, \Psi_1 \quad x : A \vdash_L \cdot; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : S \vdash_C \Psi_1 \cdot (\text{let } H y = t \text{ in } \Psi_2)} \text{C\_HE} \\
\\
\boxed{x : A \vdash_L \Delta; \Psi} \\
\\
\frac{}{x : A \vdash_L x : A; \Psi} \text{L\_VAR} \\
\\
\frac{x : A \vdash_L \Delta; \Psi \quad e : B \in \Delta}{x : A \vdash_L \text{connect}_\perp \text{ to } e : \perp, \Delta; \Psi} \text{L\_PERPI} \\
\\
\frac{x : A \vdash_L e : \perp, \Delta; \Psi}{x : A \vdash_L \text{postp}_\perp e, \Delta; \Psi} \text{L\_PERPE} \\
\\
\frac{x : A \vdash_L \Delta_1, e : B; \Psi_1 \quad y : C \vdash_L \Delta_2; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta_1, \text{mkc}(e, y) : B \bullet C, [y(e)/y]\Delta_2; \Psi_1 \cdot [y(e)/y]\Psi_2} \text{L\_SUBI} \\
\\
\frac{x : A \vdash_L \Delta_1, e_1 : B \bullet C; \Psi_1 \quad y : C \vdash_L e_2 : B, \Delta_2; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta_1, \text{postp}(y \mapsto e_2, e_1), [y(e_1)/y]\Delta_2; \Psi_1 \cdot [y(e_1)/y]\Psi_2} \text{L\_SUBE} \\
\\
\frac{x : A \vdash_L \Delta_1, e_1 : B, e_2 : C, \Delta_2; \Psi}{x : A \vdash_L \Delta_1, e_1 \oplus e_2 : B \oplus C, \Delta_2; \Psi} \text{L\_PARI} \\
\\
\frac{y : B \vdash_L \Delta_2; \Psi_2 \quad |\Psi_2| = |\Psi_3| \quad z : C \vdash_L \Delta_3; \Psi_3 \quad x : A \vdash_L e : B \oplus C, \Delta_1; \Psi_1 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta_1, [\text{casel}(e)/y]\Delta_2, [\text{casel}(e)/z]\Delta_3; \Psi_1 \cdot [\text{casel}(e)/y]\Psi_2 \cdot [\text{casel}(e)/z]\Psi_3} \text{L\_PARE} \\
\\
\frac{x : A \vdash_L \Delta; t : T, \Psi}{x : A \vdash_L \Delta, \text{J } t : \text{J } T; \Psi} \text{L\_JI} \\
\\
\frac{x : A \vdash_L \Delta, e : \text{J } T; \Psi_1 \quad y : T \vdash_C \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_L \Delta; \Psi_1 \cdot \text{let } \text{J } y = e \text{ in } \Psi_2} \text{L\_JE} \\
\\
\frac{x : A \vdash_L \Delta, e : B; \Psi}{x : A \vdash_L \Delta; H e : H B, \Psi} \text{L\_HI}
\end{array}$$