

$vars, n, a, x, y, z, w, m, o$

$ivar, i, k, j, l$

$R, S, T ::=$
 $| 0$
 $| S + T$
 $| S - T$
 $| HA$

$A, B, C ::=$
 $| \perp$
 $| A \oplus B$
 $| A \bullet B$
 $| JS$

$s, t ::=$
 $| x$
 $| \text{connect}_w \text{ to } t$
 $| t_1 \cdot t_2$
 $| \text{let } 0 = t_1 \text{ in } t_2$
 $| x(t)$
 $| \text{mkc}(t, x)$
 $| \text{postp}(x \mapsto t_1, t_2)$
 $| \text{inl } t$
 $| \text{inr } t$
 $| \text{case } t_1 \text{ of } x.t_2, y.t_3$
 $| He$
 $| \text{let } Jx = e \text{ in } t_2$
 $| \text{let } Hx = t_1 \text{ in } t_2$
 $| (t) \quad S$

$e, u ::=$
 $| x$
 $| \text{connect}_\perp \text{ to } e$
 $| \text{postp}_\perp e$
 $| \text{connect to } e$
 $| \text{postp}(x \mapsto e_1, e_2)$
 $| \text{mkc}(e, x)$

		$x(e)$	
		$e_1 \oplus e_2$	
		casel e	
		caser e	
		J t	
		(e)	S
Ψ, Π	$::=$		
		\cdot	
		$t : T$	
		Ψ, Π	
		(Ψ)	S
Γ, Δ	$::=$		
		\cdot	
		$e : A$	
		Γ, Γ'	
		(Γ)	S

$$\boxed{x : S \vdash_{\mathbf{C}} \Psi}$$

$$\begin{array}{c}
\frac{}{x : S \vdash_{\mathbf{C}} x : S} \text{C_VAR} \\
\frac{s : T' \in \Psi}{x : S \vdash_{\mathbf{C}} \text{connect}_w \text{to } s : T, \Psi} \text{C_WEAK} \\
\frac{x : S \vdash_{\mathbf{C}} t_1 : T, t_2 : T, \Psi}{x : S \vdash_{\mathbf{C}} t_1 \cdot t_2 : T, \Psi} \text{C_CONTR} \\
\frac{x : S \vdash_{\mathbf{C}} t : 0, \Psi \quad x_1 : S_1 \vdash_{\mathbf{C}} \Psi_1 \dots x_i : S_i \vdash_{\mathbf{C}} \Psi_i}{x : S \vdash_{\mathbf{C}} \text{let } 0 = t \text{ in } \Psi_1, \dots, \text{let } 0 = t \text{ in } \Psi_i, \Psi} \text{C_ZERO} \\
\frac{x : S \vdash_{\mathbf{C}} t : T_1, \Psi_1 \quad y : T_2 \vdash_{\mathbf{C}} \Psi_2}{x : S \vdash_{\mathbf{C}} \Psi_1, \text{mkc}(t, y) : T_1 - T_2, [y(t)/y]\Psi_2} \text{C_SUBI} \\
\frac{x : S \vdash_{\mathbf{C}} t_1 : T_1 - T_2, \Psi_1 \quad y : T_1 \vdash_{\mathbf{C}} t_2 : T_2, \Psi_2}{x : S \vdash_{\mathbf{C}} \text{postp}(y \mapsto t_2, t_1), \Psi_1, [z(t_1)/z]\Psi_2} \text{C_SUBE} \\
\frac{x : S \vdash_{\mathbf{C}} t : T_1, \Psi}{x : S \vdash_{\mathbf{C}} \text{inl } t : T_1 + T_2, \Psi} \text{C_ORI1} \\
\frac{x : S \vdash_{\mathbf{C}} t : T_2, \Psi}{x : S \vdash_{\mathbf{C}} \text{inr } t : T_1 + T_2, \Psi} \text{C_ORI2}
\end{array}$$

$$\begin{array}{c}
\frac{y : T_1 \vdash_{\mathbf{C}} \Psi_2 \quad y : T_2 \vdash_{\mathbf{C}} \Psi_3 \quad x : S \vdash_{\mathbf{C}} t : T_1 + T_2, \Psi_1 \quad |\Psi_2| = |\Psi_3|}{x : S \vdash_{\mathbf{C}} \Psi_1, \text{case } t \text{ of } y.\Psi_2, y.\Psi_3} \quad \mathbf{C_ORE} \\
\\
\frac{x : S \vdash_{\mathbf{C}} t : \mathbf{H}A, \Psi_1 \quad x : A \vdash_{\mathbf{L}} \cdot; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : S \vdash_{\mathbf{C}} \Psi_1 \cdot (\text{let } \mathbf{H}y = t \text{ in } \Psi_2)} \quad \mathbf{C_HE}
\end{array}$$

$$\boxed{x : A \vdash_{\mathbf{L}} \Delta; \Psi}$$

$$\begin{array}{c}
\frac{}{x : A \vdash_{\mathbf{L}} x : A; \Psi} \quad \mathbf{L_VAR} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta; \Psi \quad e : B \in \Delta}{x : A \vdash_{\mathbf{L}} \text{connect}_{\perp} \text{ to } e : \perp, \Delta; \Psi} \quad \mathbf{L_PERPI} \\
\\
\frac{x : A \vdash_{\mathbf{L}} e : \perp, \Delta; \Psi}{x : A \vdash_{\mathbf{L}} \text{postp}_{\perp} e, \Delta; \Psi} \quad \mathbf{L_PERPE} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta_1, e : B; \Psi_1 \quad y : C \vdash_{\mathbf{L}} \Delta_2; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_{\mathbf{L}} \Delta_1, \text{mkc}(e, y) : B \bullet C, [y(e)/y]\Delta_2; \Psi_1 \cdot \Psi_2} \quad \mathbf{L_SUBI} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta_1, e_1 : B \bullet C; \Psi_1 \quad y : C \vdash_{\mathbf{L}} e_2 : B, \Delta_2; \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_{\mathbf{L}} \Delta_1, \text{postp}(y \mapsto e_2, e_1), [y(e_1)/y]\Delta_2; \Psi_1 \cdot \Psi_2} \quad \mathbf{L_SUBE} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta_1, e_1 : B, e_2 : C, \Delta_2; \Psi}{x : A \vdash_{\mathbf{L}} \Delta_1, e_1 \oplus e_2 : B \oplus C, \Delta_2; \Psi} \quad \mathbf{L_PARI} \\
\\
\frac{y : B \vdash_{\mathbf{L}} \Delta_2; \Psi_2 \quad z : C \vdash_{\mathbf{L}} \Delta_3; \Psi_3 \quad x : A \vdash_{\mathbf{L}} e : B \oplus C, \Delta_1; \Psi_1 \quad |\Psi_2| = |\Psi_3| \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_{\mathbf{L}} \Delta_1, [\text{casel}(e)/y]\Delta_2, [\text{caser}(e)/z]\Delta_3; \Psi_1 \cdot \Psi_2 \cdot \Psi_3} \quad \mathbf{L_PARE} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta; t : T, \Psi}{x : A \vdash_{\mathbf{L}} \Delta, \mathbf{J}t : \mathbf{J}T; \Psi} \quad \mathbf{L_JI} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta, e : \mathbf{J}T; \Psi_1 \quad y : T \vdash_{\mathbf{C}} \Psi_2 \quad |\Psi_1| = |\Psi_2|}{x : A \vdash_{\mathbf{L}} \Delta; \Psi_1 \cdot \text{let } \mathbf{J}y = e \text{ in } \Psi_2} \quad \mathbf{L_JE} \\
\\
\frac{x : A \vdash_{\mathbf{L}} \Delta, e : B; \Psi}{x : A \vdash_{\mathbf{L}} \Delta; \mathbf{H}e : \mathbf{H}B, \Psi} \quad \mathbf{L_HI}
\end{array}$$