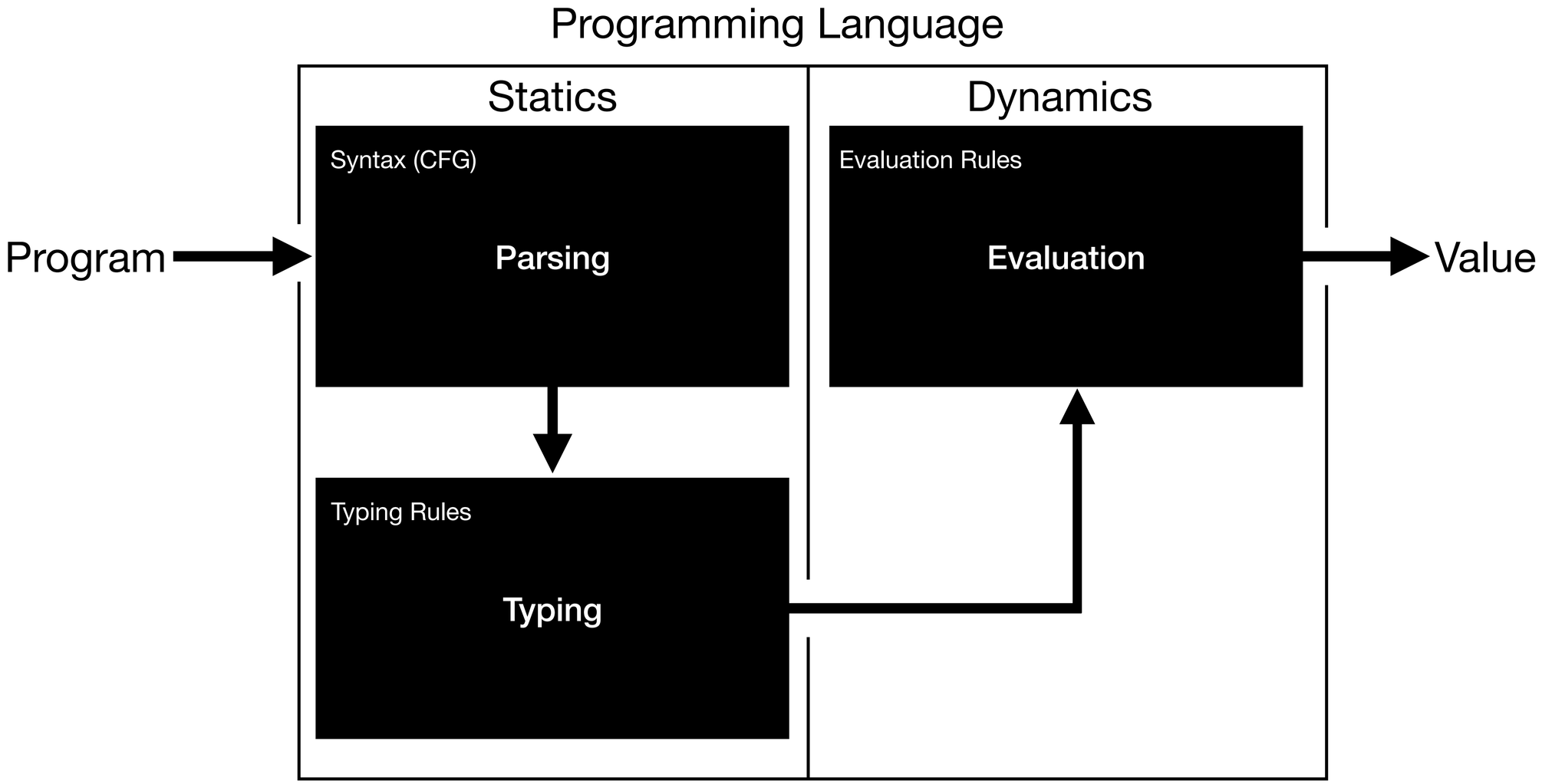
Object-Oriented Programming

Harley Eades III


Programming Language
Statics
Dynamics
Syntax (CFG)
Parsing
Evaluation Rules
Evaluation
Program
Value
Typing Rules
Typing

Part 1:Pairs

New Syntactic Forms: Adding Pairs

Terms

$$
\begin{aligned}
t ::= \ & \mathsf{T} \\
\mid \ & \mathsf{F} \\
\mid \ & \mathsf{if}\ t_1\ \mathsf{then}\ t_2\ \mathsf{else}\ t_3 \\
\mid \ & x \\
\mid \ & \mathsf{fun}\, x : T \to \{t\} \\
\mid \ & t_1\, t_2 \\
\mid \ & (t_1, t_2) \\
\mid \ & t.1 \\
\mid \ & t.2 \\
\mid \ & \mathsf{let}\, x = t_1\, \mathsf{in}\, t_2
\end{aligned}
$$

Values

$$
\begin{aligned}
v ::= \ & \mathsf{T} \\
\mid \ & \mathsf{F} \\
\mid \ & \mathsf{fun}\, x : T \to \{t\} \\
\mid \ & (v_1, v_2)
\end{aligned}
$$

Types

$$
\begin{aligned}
T ::= \ & \mathsf{Bool} \\
\mid \ & (T_1, T_2) \\
\mid \ & T_1 \to T_2
\end{aligned}
$$

Example Programs

$$\begin{array}{l}\text{let twist} = \text{fun}\, p : (\text{Bool}, \text{Bool}) \to \{(p.2, p.1)\} \\ \qquad\qquad \text{in twist}\,(\text{T}, \text{F})\end{array}$$

$$\begin{array}{l}\text{let second} = \text{fun}\, p : (\text{Bool} \to \text{Bool}, \text{Bool}) \to \{\text{if}\, p.2\, \text{then}\, p.1\, \text{T}\, \text{else F}\} \\ \qquad\qquad\qquad \text{in second}\,(\text{fun}\, x : \text{Bool} \to \{\text{if}\, x\, \text{then F else T}\}, \text{T})\end{array}$$

Statics: Bools

$$\frac{\Gamma \vdash t_1 : \text{Bool} \qquad \Gamma \vdash t_2 : T \qquad \Gamma \vdash t_3 : T}{\Gamma \vdash \text{if } t_1 \text{ then } t_2 \text{ else } t_3 : T}\ \text{If}$$

$$\frac{}{\Gamma \vdash \text{T} : \text{Bool}}\ \text{T}$$

$$\frac{}{\Gamma \vdash \text{F} : \text{Bool}}\ \text{F}$$

Statics: Functions

$$\frac{}{\Gamma_1, x : T, \Gamma_2 \vdash x : T}\ \text{Var}$$

$$\frac{\Gamma, x : T_1 \vdash t : T_2}{\Gamma \vdash \mathsf{fun}\, x : T_1 \to \{t\} : T_1 \to T_2}\ \text{Fun}$$

$$\frac{\Gamma \vdash t_1 : T_1 \to T_2 \quad \Gamma \vdash t_2 : T_1}{\Gamma \vdash t_1\, t_2 : T_2}\ \text{App}$$

$$\frac{\Gamma \vdash t_1 : T_1 \qquad \Gamma, x : T_1 \vdash t_2 : T_2}{\Gamma \vdash \mathsf{let}\, x = t_1\, \mathsf{in}\, t_2 : T_2}\ \text{Let}$$

Statics: Pairs

$$\frac{\Gamma \vdash t_1 : T_1 \quad \Gamma \vdash t_2 : T_2}{\Gamma \vdash (t_1, t_2) : (T_1, T_2)}\ \text{Pair}$$

$$\frac{\Gamma \vdash t : (T_1, T_2)}{\Gamma \vdash t.1 : T_1}\ \text{First}$$

$$\frac{\Gamma \vdash t : (T_1, T_2)}{\Gamma \vdash t.2 : T_2}\ \text{Second}$$

Call-by-Value Dynamics: Bools

$$\frac{t_1 \rightsquigarrow t_1'}{\text{if } t_1 \text{ then } t_2 \text{ else } t_3 \rightsquigarrow \text{if } t_1' \text{ then } t_2 \text{ else } t_3}\ \text{If}$$

$$\frac{}{\text{if T then } t_2 \text{ else } t_3 \rightsquigarrow t_2}\ \text{IfT}$$

$$\frac{}{\text{if F then } t_2 \text{ else } t_3 \rightsquigarrow t_3}\ \text{IfF}$$

Call-by-Value Dynamics: Functions

$$\frac{t_1 \rightsquigarrow t_1'}{t_1\, t_2 \rightsquigarrow t_1'\, t_2}\ \text{App1}$$

$$\frac{t_2 \rightsquigarrow t_2'}{v_1\, t_2 \rightsquigarrow v_1\, t_2'}\ \text{App2}$$

$$\frac{t_1 \rightsquigarrow t_1'}{\mathsf{let}\, x = t_1\, \mathsf{in}\, t_2 \rightsquigarrow \mathsf{let}\, x = t_1'\, \mathsf{in}\, t_2}\ \text{Let}$$

$$\frac{}{\mathsf{let}\, x = v\, \mathsf{in}\, t \rightsquigarrow [v/x]t}\ \text{Let}\beta$$

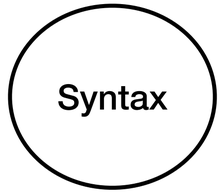
$$\frac{}{(\mathsf{fun}\, x : T \to \{t\})\, v \rightsquigarrow [v/x]t}\ \beta$$

Call-by-Value Dynamics: Pairs

$$\frac{t_1 \rightsquigarrow t_1'}{(t_1, t_2) \rightsquigarrow (t_1', t_2)}\ \text{Pair1} \qquad \frac{t \rightsquigarrow t'}{t.1 \rightsquigarrow t'.1}\ \text{Proj1} \qquad \frac{}{(v_1, v_2).1 \rightsquigarrow v_1}\ \text{Pair}\beta_1$$

$$\frac{t_2 \rightsquigarrow t_2'}{(v_1, t_2) \rightsquigarrow (v_1, t_2')}\ \text{Pair2} \qquad \frac{t \rightsquigarrow t'}{t.2 \rightsquigarrow t'.2}\ \text{Proj2} \qquad \frac{}{(v_1, v_2).2 \rightsquigarrow v_2}\ \text{Pair}\beta_2$$

Core Design Concepts:



Part 2:Unit

New Syntactic Forms: Adding Unit

Terms

$$
\begin{aligned}
t ::= \ & \mathsf{T} \\
\mid \ & \mathsf{F} \\
\mid \ & \mathsf{if}\ t_1\ \mathsf{then}\ t_2\ \mathsf{else}\ t_3 \\
\mid \ & x \\
\mid \ & \mathsf{fun}\, x : T \to \{t\} \\
\mid \ & t_1\, t_2 \\
\mid \ & () \\
\mid \ & \mathsf{match}\ t_1 \{() \to t_2\} \\
\mid \ & (t_1, t_2) \\
\mid \ & t.1 \\
\mid \ & t.2 \\
\mid \ & \mathsf{let}\, x = t_1\ \mathsf{in}\ t_2
\end{aligned}
$$

Values

$$
\begin{aligned}
v ::= \ & \mathsf{T} \\
\mid \ & \mathsf{F} \\
\mid \ & \mathsf{fun}\, x : T \to \{t\} \\
\mid \ & (v_1, v_2) \\
\mid \ & ()
\end{aligned}
$$

Types

$$
\begin{aligned}
T ::= \ & \mathsf{Bool} \\
\mid \ & () \\
\mid \ & (T_1, T_2) \\
\mid \ & T_1 \to T_2
\end{aligned}
$$

Example: Sequence

$$t_1; t_2 = (\mathsf{let}\, x = t_1\, \mathsf{in}\, t_2)$$

$$\frac{\Gamma \vdash t_1 : T_1 \qquad \Gamma \vdash t_2 : ()}{\Gamma \vdash t_1; t_2 : ()}\ \text{Seq}$$

$$\mathsf{let}\, x = t_1; t_2 = (\mathsf{let}\, x = t_1\, \mathsf{in}\, t_2)$$

$$\frac{\Gamma \vdash t_1 : T_1 \qquad \Gamma, x : T_1 \vdash t_2 : ()}{\Gamma \vdash \mathsf{let}\, x = t_1; t_2 : ()}\ \text{Define}$$

Example: Sequencing Programs

$$\frac{\Gamma \vdash t : \text{String}}{\Gamma \vdash \text{print}\, t : ()}\ \text{Print}$$

$\text{let twist} = \text{fun}\, p : (\text{Bool}, \text{Bool}) \to \{(p.2, p.1\};$
$\text{let second} = \text{fun}\, p : (\text{Bool} \to \text{Bool}, \text{Bool}) \to \{\text{if}\, p.2\, \text{then}\, p.1\ \text{T}\ \text{else}\ \text{F}\};$
$\text{if}\ (\text{second}\ (\text{fun}\, x : \text{Bool} \to \{x\}, \text{T}))\ \text{then print "True" else print "False"}$

Statics: Bools

$$\frac{\Gamma \vdash t_1 : \text{Bool} \qquad \Gamma \vdash t_2 : T \qquad \Gamma \vdash t_3 : T}{\Gamma \vdash \text{if } t_1 \text{ then } t_2 \text{ else } t_3 : T}\ \text{If}$$

$$\frac{}{\Gamma \vdash \text{T} : \text{Bool}}\ \text{T}$$

$$\frac{}{\Gamma \vdash \text{F} : \text{Bool}}\ \text{F}$$

Statics: Functions

$$\frac{}{\Gamma_1, x : T, \Gamma_2 \vdash x : T}\ \text{Var}$$

$$\frac{\Gamma, x : T_1 \vdash t : T_2}{\Gamma \vdash \mathsf{fun}\, x : T_1 \to \{t\} : T_1 \to T_2}\ \text{Fun}$$

$$\frac{\Gamma \vdash t_1 : T_1 \to T_2 \quad \Gamma \vdash t_2 : T}{\Gamma \vdash t_1\, t_2 : T_2}\ \text{App}$$

$$\frac{\Gamma \vdash t_1 : T_1 \qquad \Gamma, x : T_1 \vdash t : T_2}{\Gamma \vdash \mathsf{let}\, x = t_1\, \mathsf{in}\, t_2 : T}\ \text{Let}$$

Statics: Pairs

$$\frac{\Gamma \vdash t_1 : T_1 \quad \Gamma \vdash t_2 : T_2}{\Gamma \vdash (t_1, t_2) : (T_1, T_2)}\ \text{Pair}$$

$$\frac{\Gamma \vdash t : (T_1, T_2)}{\Gamma \vdash t.1 : T_1}\ \text{First}$$

$$\frac{\Gamma \vdash t : (T_1, T_2)}{\Gamma \vdash t.2 : T_2}\ \text{Second}$$

Statics: Unit

$$\frac{}{\Gamma \vdash () : ()}\ \text{Unit} \qquad \frac{\Gamma \vdash t_1 : () \qquad \Gamma \vdash t_2 : T}{\Gamma \vdash \mathsf{match}\ t_1 \{() \to t_2\} : T}\ \text{Match}$$

Call-by-Value Dynamics: Bools

$$\frac{t_1 \rightsquigarrow t_1'}{\text{if } t_1 \text{ then } t_2 \text{ else } t_3 \rightsquigarrow \text{if } t_1' \text{ then } t_2 \text{ else } t_3}\ \text{If}$$

$$\frac{}{\text{if T then } t_2 \text{ else } t_3 \rightsquigarrow t_2}\ \text{IfT}$$

$$\frac{}{\text{if F then } t_2 \text{ else } t_3 \rightsquigarrow t_3}\ \text{IfF}$$

Call-by-Value Dynamics: Functions

$$\frac{t_1 \rightsquigarrow t_1'}{t_1\, t_2 \rightsquigarrow t_1'\, t_2}\ \text{App1}$$

$$\frac{t_2 \rightsquigarrow t_2'}{v_1\, t_2 \rightsquigarrow v_1\, t_2'}\ \text{App2}$$

$$\frac{t_1 \rightsquigarrow t_1'}{\mathsf{let}\, x = t_1\, \mathsf{in}\, t_2 \rightsquigarrow \mathsf{let}\, x = t_1'\, \mathsf{in}\, t_2}\ \text{Let}$$

$$\frac{}{\mathsf{let}\, x = v\, \mathsf{in}\, t \rightsquigarrow [v/x]t}\ \text{Let}\beta$$

$$\frac{}{(\mathsf{fun}\, x : T \to \{t\})\, v \rightsquigarrow [v/x]t}\ \beta$$

Call-by-Value Dynamics: Pairs

$$\frac{t_1 \rightsquigarrow t_1'}{(t_1, t_2) \rightsquigarrow (t_1', t_2)}\ \text{Pair1} \qquad \frac{t \rightsquigarrow t'}{t.1 \rightsquigarrow t'.1}\ \text{Proj1} \qquad \frac{}{(v_1, v_2).1 \rightsquigarrow v_1}\ \text{Pair}\beta_1$$

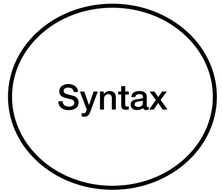
$$\frac{t_2 \rightsquigarrow t_2'}{(v_1, t_2) \rightsquigarrow (v_1, t_2')}\ \text{Pair2} \qquad \frac{t \rightsquigarrow t'}{t.2 \rightsquigarrow t'.2}\ \text{Proj2} \qquad \frac{}{(v_1, v_2).2 \rightsquigarrow v_2}\ \text{Pair}\beta_2$$

Call-by-Value Dynamics: Unit

$$\frac{t_1 \rightsquigarrow t_1'}{\mathsf{match}\ t_1\{() \to t_2\} \rightsquigarrow \mathsf{match}\ t_1'\{() \to t_2\}}\ \text{Match}$$

$$\frac{}{\mathsf{match}\ ()\{() \to t_2\} \rightsquigarrow t_2}\ \text{Unit}\beta$$

Core Design Concepts:



Part 3:Tuples

New Syntactic Forms: Adding Tuples

Terms

$$
\begin{aligned}
t ::= \ & \mathsf{T} \\
\mid \ & \mathsf{F} \\
\mid \ & \mathsf{if}\ t_1\ \mathsf{then}\ t_2\ \mathsf{else}\ t_3 \\
\mid \ & x \\
\mid \ & \mathsf{fun}\, x : T \to \{t\} \\
\mid \ & t_1\, t_2 \\
\mid \ & (t_1, \ldots, t_i) \\
\mid \ & \mathsf{match}\ t_1 \{(x_1, \ldots, x_i) \to t_2\} \\
\mid \ & \mathsf{let}\, x = t_1\ \mathsf{in}\ t_2
\end{aligned}
$$

Values

$$
\begin{aligned}
v ::= \ & \mathsf{T} \\
\mid \ & \mathsf{F} \\
\mid \ & \mathsf{fun}\, x : T \to \{t\} \\
\mid \ & (v_1, \ldots, v_i)
\end{aligned}
$$

Types

$$
\begin{aligned}
T ::= \ & \mathsf{Bool} \\
\mid \ & (T_1, \ldots, T_i) \\
\mid \ & T_1 \to T_2
\end{aligned}
$$

Example: Tuple

(T, F, T, F, F)

```
fun (p : (Bool, Bool, Bool)) → {
    match p {
        (x, y, z) → if x
                    then if y
                         then z
                         else False
                    else False
    }
}
```

Statics: Bools

$$\frac{\Gamma \vdash t_1 : \text{Bool} \qquad \Gamma \vdash t_2 : T \qquad \Gamma \vdash t_3 : T}{\Gamma \vdash \text{if } t_1 \text{ then } t_2 \text{ else } t_3 : T}\ \text{If}$$

$$\frac{}{\Gamma \vdash \text{T} : \text{Bool}}\ \text{T}$$

$$\frac{}{\Gamma \vdash \text{F} : \text{Bool}}\ \text{F}$$

Statics: Functions

$$\frac{}{\Gamma_1, x : T, \Gamma_2 \vdash x : T}\ \text{Var}$$

$$\frac{\Gamma, x : T_1 \vdash t : T_2}{\Gamma \vdash \mathsf{fun}\, x : T_1 \to \{t\} : T_1 \to T_2}\ \text{Fun}$$

$$\frac{\Gamma \vdash t_1 : T_1 \to T_2 \quad \Gamma \vdash t_2 : T}{\Gamma \vdash t_1\, t_2 : T_2}\ \text{App}$$

$$\frac{\Gamma \vdash t_1 : T_1 \qquad \Gamma, x : T_1 \vdash t : T_2}{\Gamma \vdash \mathsf{let}\, x = t_1\, \mathsf{in}\, t_2 : T}\ \text{Let}$$

Statics: Tuples

$$\frac{\Gamma \vdash t_1 : T_1 \quad \cdots \quad \Gamma \vdash t_i : T_i}{\Gamma \vdash (t_1, t_2) : (T_1, T_2)}\ \text{Tuple}$$

$$\frac{\Gamma \vdash t_1 : (T_1, \ldots, T_i) \qquad \Gamma, x_1, \ldots, x_i \vdash t_2 : T}{\Gamma \vdash \mathsf{match}\ t_1 \{(x_1, \ldots, x_i) \rightarrow t_2\} : T}\ \text{Match}$$

Call-by-Value Dynamics: Bools

$$\frac{t_1 \rightsquigarrow t_1'}{\text{if } t_1 \text{ then } t_2 \text{ else } t_3 \rightsquigarrow \text{if } t_1' \text{ then } t_2 \text{ else } t_3}\ \text{If}$$

$$\frac{}{\text{if T then } t_2 \text{ else } t_3 \rightsquigarrow t_2}\ \text{IfT}$$

$$\frac{}{\text{if F then } t_2 \text{ else } t_3 \rightsquigarrow t_3}\ \text{IfF}$$

Call-by-Value Dynamics: Functions

$$\frac{t_1 \rightsquigarrow t_1'}{t_1\, t_2 \rightsquigarrow t_1'\, t_2}\ \text{App1}$$

$$\frac{t_2 \rightsquigarrow t_2'}{v_1\, t_2 \rightsquigarrow v_1\, t_2'}\ \text{App2}$$

$$\frac{t_1 \rightsquigarrow t_1'}{\mathsf{let}\, x = t_1\, \mathsf{in}\, t_2 \rightsquigarrow \mathsf{let}\, x = t_1'\, \mathsf{in}\, t_2}\ \text{Let}$$

$$\frac{}{\mathsf{let}\, x = v\, \mathsf{in}\, t \rightsquigarrow [v/x]t}\ \text{Let}\beta$$

$$\frac{}{(\mathsf{fun}\, x : T \to \{t\})\, v \rightsquigarrow [v/x]t}\ \beta$$

Call-by-Value Dynamics: Tuples

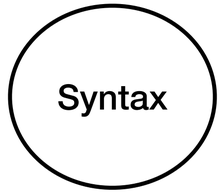
$$\frac{t_{i+1} \rightsquigarrow t'_{i+1}}{(v_1, \ldots, v_i, t_{i+1}, \ldots, t_j) \rightsquigarrow (v_1, \ldots, v_i, t'_{i+1}, \ldots, t_j)}\ \text{Tuple}$$

Call-by-Value Dynamics: Tuples

$$\frac{t_1 \rightsquigarrow t_1'}{\mathsf{match}\ t_1\{(x_1, \ldots, x_i) \to t_2\} \rightsquigarrow \mathsf{match}\ t_1'\{(x_1, \ldots, x_i) \to t_2\}}\ \text{Match}$$

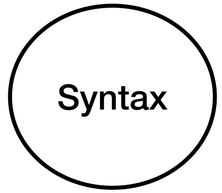
$$\frac{}{\mathsf{match}\ (v_1, \ldots, v_i)\{(x_1, \ldots, x_i) \to t_2\} \rightsquigarrow [v_1/x_1]\cdots[v_i/x_i]t_2}\ \text{Tuple}\beta$$

Core Design Concepts:



Part 3:Records

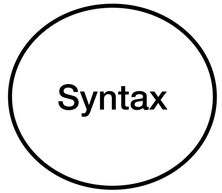
Core Design Concepts:



Part ?: OOP in OCaml

What is OCaml?

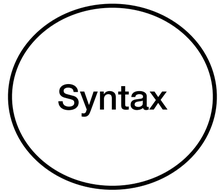
Core Design Concepts:



An object oriented, imperative, functional programming language.

What is OCaml?

Core Design Concepts:



An object oriented, imperative, functional programming language.

OCaml mixes all of these paradigms together.

What is OCaml?

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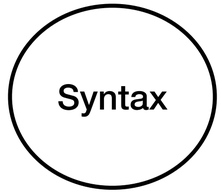

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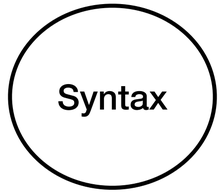

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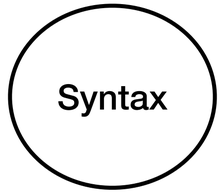

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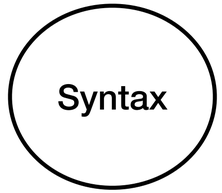
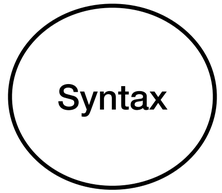


An object oriented, imperative, functional programming language.

OCaml mixes all of these paradigms together.

Class Definitions

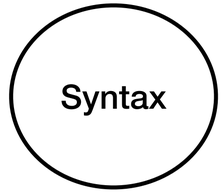
Core Design Concepts:




```
class name = object (self) … end
```

Class Definitions

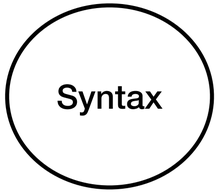
Core Design Concepts:




```
class stack_of_ints =
  object (self)
    val mutable the_list = ([] : int list)
     …
  end;;
```

Class Definitions

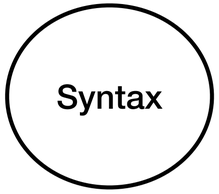
Core Design Concepts:




```
class stack_of_ints =
  object (self)
    val mutable the_list = ([] : int list)
    method push x = …
    method pop = …
    method peek = …
    method size = …
  end;;
```

Class Definitions

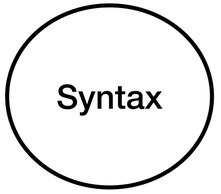
Core Design Concepts:




```
class stack_of_ints =
  object (self)
    val mutable the_list = ([] : int list)
    method push x = the_list <- Cons(x, the_list)
    method pop = …
    method peek = …
    method size = …
  end;;
```

Class Definitions

Core Design Concepts:

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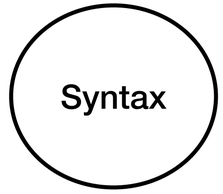
class stack_of_ints =
  object (self)
    val mutable the_list = ([] : int list)
    method pop =
      let result = head the_list in
      the_list <- tail the_list;
      result
    method push x = …
    method peek = …
    method size = …
  end;;
```

Class Definitions

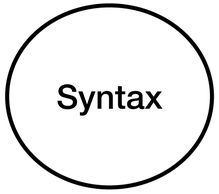
Core Design Concepts:




```
class stack_of_ints =
  object (self)
    val mutable the_list = ([] : int list)
    method push x = …
    method pop = …
    method peek = head the_list
    method size = …
  end;;
```

Class Definitions

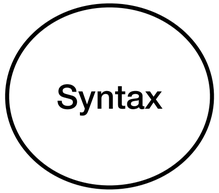
Core Design Concepts:




```
class stack_of_ints =
  object (self)
    val mutable the_list = ([] : int list)
    method push x = …
    method pop = …
    method peek = …
    method size = length the_list
  end;;
```

Class Definitions

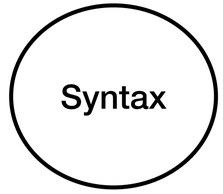
Core Design Concepts:




```
class stack_of_ints =
  object (self) …
end;;
class stack_of_ints :
  object
    val mutable the_list : int list
    method peek : int
    method pop : int
    method push : int -> unit
    method size : int
  end
```

Accessing fields and methods

Core Design Concepts:

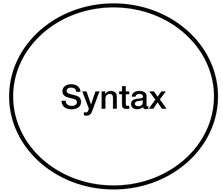



```
# let s = new stack_of_ints;;

val s : stack_of_ints = <obj>
```

Accessing fields and methods

Core Design Concepts:

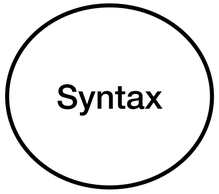



```
s#fieldName

s#methodName
```

Accessing fields and methods

Core Design Concepts:




```
# for i = 1 to 10 do
    s#push i
  done;;
- : unit = ()
# while s#size > 0 do
    Printf.printf "Popped %d off the stack.\n" s#pop
  done;;
…
Popped 10 off the stack.
Popped 9 off the stack.
Popped 8 off the stack.
- : unit = ()
```