

termvar, *x*, *y*
funcname, **name**
indecies, *i*, *j*

$types, T, A, B, C$	$::=$ $ \quad \mathbf{Bool}$	Types
Γ	$::=$ $ \quad \emptyset$ $ \quad x_1 : T_1, \dots, x_i : T_i$	Typing Context
$program, p$	$::=$ $ \quad \mathbf{func name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{body\}$ $ \quad (p)$	Programs S
$body$	$::=$ $ \quad asgn; t$ $ \quad t$	Function Bodies Body with assignments Body without assignments
lv	$::=$ $ \quad \mathbf{let}$ $ \quad \mathbf{var}$	Assignment Tags Use x at least once Use x any number of times
$assignemnts, asgn$	$::=$ $ \quad lv_1 x_1 : T_1 = b_1; \dots; lv_j x_j : T_j = b_j$	Variable Assignments
t	$::=$ $ \quad x$ $ \quad T$ $ \quad \mathbf{F}$ $ \quad \mathbf{if } b_1 \mathbf{ then } t_1 \mathbf{ else } t_2$ $ \quad \mathbf{name}(b_1, \dots, b_i)$ $ \quad \mathbf{return } b$ $ \quad EC[t]$ $ \quad (t)$	Terms A variable Logical true Logical false Pattern Matching for booleans Function application Return of a term Plugging the hole in EC gives S
b	$::=$ $ \quad x$ $ \quad T$ $ \quad \mathbf{F}$ $ \quad \mathbf{if } b_1 \mathbf{ then } t_2 \mathbf{ else } t_3$ $ \quad \mathbf{name}(b_1, \dots, b_i)$ $ \quad EC[b]$ $ \quad (b)$	Basic Terms A variable Logical true Logical false Pattern Matching for booleans Function application Plugging the hole in EC gives S
v	$::=$ $ \quad T$ $ \quad \mathbf{F}$	Values
Δ	$::=$ $ \quad p_1$ $ \quad \Delta_1, \Delta_2$	Contexts of Function Definitions

TP	$::=$	List of Term Parameters
	\emptyset	Empty List
	b, TP	Term Argument
CP	$::=$	Evaluation Contexts for Parameters
	\emptyset	Empty List
	EC, TP	Context Evaluation Argument
	b, CP_2	Term Argument
$evalctx, EC$	$::=$	Evaluation Contexts
	\square	The hole (location of the evaluation point)
	T	
	F	
	if EC then t_2 else t_3	
	name (CP)	
	return b	
	(EC)	S

$\boxed{\Delta_1 \vdash \Delta_2}$ Type Checking for Definitions

$$\begin{array}{c}
\Delta; \Gamma, x_1 : T_1, \dots, x_i : T_i \vdash b_1 : A_1 \dots \Delta; \Gamma, x_1 : T_1, \dots, x_i : T_i, y_1 : A_1, \dots, y_{j-1} : A_{j-1} \vdash b_j : A_j \\
\Delta_1; x_1 : T_1, \dots, x_i : T_i, y_1 : A'_1, \dots, y_j : A'_j \vdash t : T \\
\hline
\Delta_1 \vdash \text{func name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{lv\ y_1 : A_1 = b_1; \dots; lv\ y_j : A_j = b_j; t\} \quad \text{DT_ASGN} \\
\\
\frac{\Delta_1; x_1 : T_1, \dots, x_i : T_i \vdash t : T}{\Delta_1 \vdash \text{func name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{t\}} \quad \text{DT_NASGN} \\
\\
\frac{\Delta_1 \vdash p_1 \quad \Delta_1, p_1 \vdash \Delta_2}{\Delta_1 \vdash p_1, \Delta_2} \quad \text{DT_EXT}
\end{array}$$

$\boxed{\Delta; \Gamma \vdash t : T}$ Type Checking for Terms

$$\begin{array}{c}
\frac{x : T \in \Gamma}{\Delta; \Gamma \vdash x : T} \quad \text{T_VAR} \\
\\
\frac{}{\Delta; \Gamma \vdash T : \text{Bool}} \quad \text{T_TRUE} \\
\\
\frac{}{\Delta; \Gamma \vdash F : \text{Bool}} \quad \text{T_FALSE} \\
\\
\frac{\Delta; \Gamma \vdash t_1 : T \quad \Delta; \Gamma \vdash t_2 : T \quad \Delta; \Gamma \vdash b_1 : \text{Bool}}{\Delta; \Gamma \vdash \text{if } b_1 \text{ then } t_1 \text{ else } t_2 : T} \quad \text{T_IF} \\
\\
\frac{\Delta; \Gamma \vdash b'_1 : T_1, \dots, \Delta; \Gamma \vdash b'_i : T_i \quad (\text{func name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{lv_1\ y_1 : A_1 = b_1; \dots; lv_j\ y_j : A_j = b_j; t\}) \in \Delta}{\Delta; \Gamma \vdash \text{name}(b'_1, \dots, b'_i) : T} \quad \text{T_APP} \\
\\
\frac{\Delta; \Gamma \vdash b : T}{\Delta; \Gamma \vdash \text{return } b : T} \quad \text{T_RETURN}
\end{array}$$

$\boxed{\Delta \vdash t_1 \rightsquigarrow t_2}$ Single-Step Reduction for Terms

$$\begin{array}{c}
\frac{}{\Delta \vdash \text{if } T \text{ then } t_1 \text{ else } t_2 \rightsquigarrow t_1} \quad \text{IFT} \\
\\
\frac{}{\Delta \vdash \text{if } F \text{ then } t_1 \text{ else } t_2 \rightsquigarrow t_2} \quad \text{IFF}
\end{array}$$

$$\begin{array}{c}
\overline{\Delta \vdash \text{return } b \rightsquigarrow b} \quad \text{RETURN} \\
\\
\frac{(\text{func name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{lv_1 y_1 : A_1 = b_1; \dots; lv_j y_j : A_j = b_j; t\}) \in \Delta}{\Delta \vdash \text{name}(v_1, \dots, v_i) \rightsquigarrow [v_1, \dots, v_i/x_1, \dots, x_i][b_1, \dots, b_j/y_1, \dots, y_j]t} \quad \text{BETA} \\
\\
\boxed{\Delta \vdash t_1 \rightsquigarrow^* t_2} \quad \text{Multi-Step Reduction for Terms} \\
\\
\frac{\Delta \vdash t_1 \rightsquigarrow t_2}{\Delta \vdash EC[t_1] \rightsquigarrow^* EC[t_2]} \quad \text{STEP} \\
\\
\frac{\Delta \vdash t_1 \rightsquigarrow t_2 \quad \Delta \vdash EC[t_2] \rightsquigarrow^* EC[t_3]}{\Delta \vdash EC[t_1] \rightsquigarrow^* EC[t_3]} \quad \text{MULT}
\end{array}$$

Definition rules: 15 good 0 bad
 Definition rule clauses: 28 good 0 bad