

# Example : Graded Environment Monad

$$M : \mathcal{P}(E) \rightarrow [\text{Set}, \text{Set}]$$

$$\eta_A : A \rightarrow M_{\emptyset} A$$

$$M_X(A) = X \Rightarrow A$$

$$\mu_A : M_X M_Y A \rightarrow M_{X \cup Y} A$$

$$>>= : M_x A \rightarrow (A \rightarrow M_y B) \rightarrow M_{x \cup y} B$$

# Towards a Formal Theory of Graded Monads

**Soichiro Fujii**

, Shin-ya Katsumata<sup>2</sup>, and Paul-André Melliès<sup>3</sup>

<sup>1</sup> Department

<sup>3</sup> Laboratoire

**Abstract.** We propose is to adapt by Street in the monad can be fact along a left adjoint construction general construction general the Eilenberg-Moore construction on the graded state monad induced by any object  $V$  in a symmetric monoidal closed category  $\mathcal{C}$ .

