(Simplified) Bounded Linear Logic

$$\frac{\Gamma_1, \Gamma_2 \vdash B}{\Gamma_1, !_0 A, \Gamma_2 \vdash B} \ W$$

$$\frac{\Gamma_1, !_{p_1}A, !_{p_2}A, \Gamma_2 \vdash B}{\Gamma_1, !_{p_1+p_2}A, \Gamma_2 \vdash B} C$$

$$\frac{!\overrightarrow{p}\Gamma \vdash B}{!_{p*}\overrightarrow{p}\Gamma \vdash !_{p}B} P$$

$$\frac{\Gamma, A \vdash B}{\Gamma, !_1 A \vdash B} \ D$$

(Simplified) Bounded Linear Logic

$$\frac{\Gamma_1, \Gamma_2 \vdash B}{\Gamma_1, !_0 A, \Gamma_2 \vdash B} \ W$$

$$\frac{\Gamma_1, !_{p_1}A, !_{p_2}A, \Gamma_2 \vdash B}{\Gamma_1, !_{p_1+p_2}A, \Gamma_2 \vdash B} C$$

The precursor to graded comonads.

$$\frac{!_{\overrightarrow{p}}\Gamma \vdash B}{!_{p*\overrightarrow{p}}\Gamma \vdash !_{p}B} P$$

$$\frac{\Gamma, A \vdash B}{\Gamma, !_1 A \vdash B} \ D$$