$\begin{array}{c} termvar, \, x, \, y \\ funcname, \, \texttt{name} \\ indecies, \, i, \, j \end{array}$ 

```
types, T, A, B, C
                                                                                       Types
                            ::=
                                  Bool
                             Γ
                            ::=
                                                                                       Typing Context
                                  x_1: T_1, \ldots, x_i: T_i
                                                                                       Programs
program, p
                                  func name(x_1: T_1, \ldots, x_i: T_i) \rightarrow T\{body\}
                                                                                   S
body
                            ::=
                                                                                       Function Bodies
                                                                                          Body with assignments
                                  asgn;t
                                                                                          Body without assignments
lv
                            ::=
                                                                                       Assignment Tags
                                                                                          Use x at least once
                                  let
                                  var
                                                                                          Use x any number of times
                                                                                       Variable Assignments
assignemnts, asgn
                                  lv_1 x_1 : T_1 = b_1; ...; lv_i x_i : T_i = b_i
t
                                                                                       Terms
                            ::=
                                  \boldsymbol{x}
                                                                                          A variable
                                  T
                                                                                          Logical true
                                                                                          Logical false
                                  if b_1 then t_1 else t_2
                                                                                          Pattern Matching for booleans
                                  name(b_1, \ldots, b_i)
                                                                                          Function application
                                  \operatorname{return} b
                                                                                          Return of a term
                                  EC[t]
                                                                                          Plugging the hole in EC gives
                                                                                   S
                                  (t)
                                                                                       Basic Terms
b
                                                                                          A variable
                                  \boldsymbol{x}
                                  T
                                                                                          Logical true
                                                                                          Logical false
                                  if b_1 then t_2 else t_3
                                                                                          Pattern Matching for booleans
                                  name(b_1, \ldots, b_i)
                                                                                          Function application
                                  EC[b]
                                                                                          Plugging the hole in EC gives
                                  (b)
                                                                                   S
                                                                                       Values
v
                                  T
                                  F
                                                                                       Contexts of Function Definitions
\Delta
                                  p_1
```

```
TP
                                                                                              List of Term Parameters
                                                                                                   Empty List
                                              b, TP
                                                                                                   Term Argument
 CP
                                                                                              Evaluation Contexts for Parameters
                                                                                                   Empty List
                                              EC, TP
                                                                                                   Context Evaluation Argument
                                              b, CP_2
                                                                                                   Term Argument
evalctx, EC
                                                                                              Evaluation Contexts
                                                                                                   The hole (location of the evaluation point)
                                             if EC then t_2 else t_3
                                             \mathtt{name}(\mathit{CP})
                                              return b
                                                                                       S
                                              (EC)
                       Type Checking for Definitions
\Delta_1 \vdash \Delta_2
\Delta; \Gamma, x_1 : T_1, \ldots, x_i : T_i \vdash b_1 : A_1 \ldots \Delta; \Gamma, x_1 : T_1, \ldots, x_i : T_i, y_1 : A_1, \ldots, y_{j-1} : A_{j-1} \vdash b_j : A_j
\begin{array}{c} \Delta_1; x_1: T_1, \, \dots, x_i: T_i, y_1: A_1', \, \dots, y_j: A_j' \vdash t: T \\ \\ \Delta_1 \vdash \mathsf{func} \, \mathsf{name}(x_1: T_1, \, \dots, x_i: T_i) \to T\{\mathit{lv} \, y_1: A_1 = b_1; \, \dots; \mathit{lv} \, y_j: A_j = b_j; t\} \end{array}
                                                                                                                                                                                                 DT_Asgn
                                      \frac{\Delta_1; x_1: T_1, \dots, x_i: T_i \vdash t: T}{\Delta_1 \vdash \mathsf{func}\,\mathsf{name}(x_1: T_1, \dots, x_i: T_i) \to T\{t\}} \quad \mathsf{DT\_NAsgN}
                                                                                                                                               DT_{-}Empty
                       <<no parses (char 3): e***mptyset |- emptyset >>
                                                            \frac{\Delta_1 \vdash p_1 \quad \Delta_1, p_1 \vdash \Delta_2}{\Delta_1 \vdash p_1, \Delta_2} \quad \text{DT-Ext}
 \Delta; \Gamma \vdash t : T
                                Type Checking for Terms
                                                                          \frac{x:T\in\Gamma}{\Delta;\Gamma\vdash x:T} T_VAR
                                                                                                      T_{-}T_{RUE}
                                                                     \overline{\Delta;\Gamma\vdash T:\mathsf{Bool}}
                                                                                                       T_FALSE
                                                                     \overline{\Delta : \Gamma \vdash \mathsf{F} : \mathsf{Bool}}
                                                          \Delta; \Gamma \vdash t_1 : T
                                                         \frac{\Delta; \Gamma \vdash t_2 : T \quad \Delta; \Gamma \vdash b_1 : \mathsf{Bool}}{\Delta; \Gamma \vdash \mathsf{if} \ b_1 \ \mathsf{then} \ t_1 \ \mathsf{else} \ t_2 : T} \quad \mathsf{T} \mathsf{\bot} \mathsf{IF}
       \Delta; \Gamma \vdash b'_1 : T_1, \ldots, \Delta; \Gamma \vdash b'_i : T_i
       \frac{(\mathsf{func}\,\mathsf{name}(x_1:T_1,\,\dots,x_i:T_i)\to T\{lv_1\,y_1:A_1=b_1;\,\dots;lv_j\,y_j:A_j=b_j;t\})\in\Delta}{\Delta;\Gamma\vdash\mathsf{name}(b_1',\,\dots,b_i'):T}
                                                               \frac{\Delta; \Gamma \vdash b : T}{\Delta; \Gamma \vdash \mathsf{return} \ b : T} \quad \mathsf{T\_RETURN}
 \Delta \vdash t_1 \leadsto t_2
                               Single-Step Reduction for Terms
                                                              \overline{\Delta \vdash \text{if } T \text{ then } t_1 \text{ else } t_2 \leadsto t_1}
```

$$\frac{}{\Delta \vdash \mathsf{if} \, \mathsf{F} \, \mathsf{then} \, t_1 \, \mathsf{else} \, t_2 \leadsto t_2} \quad \mathsf{IFF}$$

$$\frac{}{\Delta \vdash \mathsf{return} \; b \leadsto b} \quad \mathsf{RETURN}$$

$$\frac{(\mathsf{func}\,\mathsf{name}(x_1:T_1,\,\ldots,x_i:T_i)\to T\{\mathit{lv}_1\,y_1:A_1=b_1;\,\ldots;\mathit{lv}_j\,y_j:A_j=b_j;t\})\in\Delta}{\Delta\vdash\mathsf{name}(v_1,\,\ldots,v_i)\leadsto[v_1,\,\ldots,v_i/x_1,\,\ldots,x_i][b_1,\,\ldots,b_j/y_1,\,\ldots,y_j]t}\quad\mathsf{Beta}$$

 $\Delta \vdash t_1 \leadsto^* t_2$  Multi-Step Reduction for Terms

$$\frac{\Delta \vdash t_1 \leadsto t_2}{\Delta \vdash EC[t_1] \leadsto^* EC[t_2]} \quad \text{Step}$$

$$\frac{\Delta \vdash t_1 \leadsto t_2 \quad \Delta \vdash EC[t_2] \leadsto^* EC[t_3]}{\Delta \vdash EC[t_1] \leadsto^* EC[t_3]} \quad \text{Multi-$$

Definition rules: 15 good 1 bad Definition rule clauses: 28 good 1 bad