

termvar, *x*, *y*
funcname, **name**
indecies, *i*, *j*

$types, T, A, B, C$	$::=$ $ \quad \mathbf{Bool}$	Types
Γ	$::=$ $ \quad \emptyset$ $ \quad x_1 : T_1, \dots, x_i : T_i$	Typing Context
$program, p$	$::=$ $ \quad \mathbf{func\ name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{body\}$ $ \quad p_1\ p_2$ $ \quad (p)$	Programs
$body$	$::=$ $ \quad asgn; t$ $ \quad t$	Function Bodies Body with assignments Body without assignments
lv	$::=$ $ \quad \mathbf{let}$ $ \quad \mathbf{var}$	Assignment Tags Use x at least once Use x any number of times
$assignemnts, asgn$	$::=$ $ \quad lv_1\ x_1 : T_1 = b_1; \dots; lv_j\ x_j : T_j = b_j$	Variable Assignments
t	$::=$ $ \quad x$ $ \quad T$ $ \quad \mathbf{F}$ $ \quad \mathbf{if\ } b_1 \mathbf{\ then\ } t_1 \mathbf{\ else\ } t_2$ $ \quad \mathbf{name}(b_1, \dots, b_i)$ $ \quad \mathbf{return\ } b$ $ \quad EC[t]$ $ \quad (t)$	Terms A variable Logical true Logical false Pattern Matching for booleans Function application Return of a term Plugging the hole in EC gives
b	$::=$ $ \quad x$ $ \quad T$ $ \quad \mathbf{F}$ $ \quad \mathbf{if\ } b_1 \mathbf{\ then\ } t_2 \mathbf{\ else\ } t_3$ $ \quad \mathbf{name}(b_1, \dots, b_i)$ $ \quad EC[b]$ $ \quad (b)$	Basic Terms A variable Logical true Logical false Pattern Matching for booleans Function application Plugging the hole in EC gives
v	$::=$ $ \quad T$ $ \quad \mathbf{F}$	Values
Δ	$::=$ $ \quad p_1$ $ \quad \Delta_1, \Delta_2$	Contexts of Function Definitions

TP	$::=$	List of Term Parameters
	\emptyset	Empty List
	b, TP	Term Argument
CP	$::=$	Evaluation Contexts for Parameters
	\emptyset	Empty List
	EC, TP	Context Evaluation Argument
	b, CP_2	Term Argument
$evalctx, EC$	$::=$	Evaluation Contexts
	\square	The hole (location of the evaluation point)
	T	
	F	
	if EC then t_2 else t_3	
	name (CP)	
	return b	
	(EC)	S

$\boxed{\Gamma \vdash t : T}$ Type Checking

$$\frac{x : T \in \Gamma}{\Gamma \vdash x : T} \quad \text{T_VAR}$$

$\boxed{\Delta \vdash t_1 \rightsquigarrow t_2}$ Single-Step Reduction for Terms

$$\overline{\Delta \vdash \text{if } T \text{ then } t_1 \text{ else } t_2 \rightsquigarrow t_1} \quad \text{IFT}$$

$$\overline{\Delta \vdash \text{if } F \text{ then } t_1 \text{ else } t_2 \rightsquigarrow t_2} \quad \text{IFF}$$

$$\overline{\Delta \vdash \text{return } b \rightsquigarrow b} \quad \text{RETURN}$$

$$\frac{(\text{func name}(x_1 : T_1, \dots, x_i : T_i) \rightarrow T\{lv_1 y_1 : A_1 = b_1; \dots; lv_j y_j : A_j = b_j; t\}) \in \Delta}{\Delta \vdash \text{name}(v_1, \dots, v_i) \rightsquigarrow [v_1, \dots, v_i/x_1, \dots, x_i][b_1, \dots, b_j/y_1, \dots, y_j]t} \quad \text{BETA}$$

$\boxed{\Delta \vdash t_1 \rightsquigarrow^* t_2}$ Multi-Step Reduction for Terms

$$\frac{\Delta \vdash t_1 \rightsquigarrow t_2}{\Delta \vdash EC[t_1] \rightsquigarrow^* EC[t_2]} \quad \text{STEP}$$

$$\frac{\Delta \vdash t_1 \rightsquigarrow t_2 \quad \Delta \vdash EC[t_2] \rightsquigarrow^* EC[t_3]}{\Delta \vdash EC[t_1] \rightsquigarrow^* EC[t_3]} \quad \text{MULT}$$

Definition rules: 7 good 0 bad
Definition rule clauses: 11 good 0 bad