Example: Graded Environment Monad

$$M: \mathscr{P}(E) \to [\mathsf{Set}, \mathsf{Set}]$$

$$\eta_A:A\to M_{\varnothing}A$$

$$M_X(A) = X \Rightarrow A$$

$$\mu_A: M_X M_Y A \to M_{X \cup Y} A$$

$$>>=: M_{\chi}A \rightarrow (A \rightarrow M_{Y}B) \rightarrow M_{\chi \cup Y}B$$

Towards a Formal Theory of Graded Monads

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Abstract. We is pose is to adapt by Street in the emonad can be factally along a left adjoint struction general construction general

articular that every graded a strict action transported n what sense the first construction while the second tion. Finally, we illustrate

the Eilenberg-Moore construction on the graded state monad induced by any object V in a symmetric monoidal closed category \mathscr{C} .