

# Ideal Quaternary Semantics of Attack Trees

Basic Properties for Sequence:

$$(A \triangleright_I A) \not\equiv A$$

$$(A \triangleright_I B) \not\equiv (B \triangleright_I A)$$

$$(A \triangleright_I (B \triangleright_I C)) \equiv ((A \triangleright_I B) \triangleright_I C)$$

$$\text{If } A \leq_4 C \text{ and } B \leq_4 D, \text{ then } (A \triangleright_I B) \leq_4 (C \triangleright_I D)$$

$$(A \triangleright_I (B \sqcup_I C)) \equiv ((A \triangleright_I B) \sqcup_I (A \triangleright_I C))$$

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Ideal Properties [Horne et al.:2016]:

$$((A \odot_I B) \triangleright_I (C \odot_I D)) \leq_4 ((A \triangleright_I C) \odot_I (B \triangleright_I D))$$

$$((A \odot_I B) \triangleright_I C) \leq_4 (A \odot_I (B \triangleright_I C))$$

$$(A \triangleright_I (B \odot_I C)) \leq_4 (B \odot_I (A \triangleright_I C))$$

$$(A \triangleright_I B) \leq_4 (A \odot_I B)$$

Note: Not equivalences!