

Semantic Analysis of Advanced Programming Languages

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1 Introduction

There are two major problems growing in two areas. The first is in Computer Science, in particular software engineering. Software is becoming more and more complex, and hence more susceptible to software defects. Software bugs have two critical repercussions: they cost companies lots of money and time to fix, and they have the potential to cause harm.

The National Institute of Standards and Technology estimated that software errors cost the United State's economy approximately sixty billion dollars annually, while the Federal Bureau of Investigations estimated in a 2005 report that software bugs cost U.S. companies approximately sixty-seven billion a year [9, 14].

Software bugs have the potential to cause harm. In 2010 there were a approximately a hundred reports made to the National Highway Traffic Safety Administration of potential problems with the braking system of the 2010 Toyota Prius [1]. The problem was that the anti-lock braking system would experience a "short delay" when the brakes where pressed by the driver of the vehicle [13]. This actually caused some crashes. Toyota found that this short delay was the result of a software bug, and was able to repair the the vehicles using a software update [10]. Another incident where substantial harm was caused was in 2002 where two planes collided over Überlingen in Germany. A cargo plane operated by DHL collided with a passenger flight holding fifty-one passengers. Air-traffic control did not notice the intersecting traffic until less than a minute before the collision occurred. Furthermore, the on-board collision detection system did not alert the pilots until seconds before the collision. It was officially ruled by the German Federal Bureau of Aircraft Accidents Investigation that the on-board collision detection was indeed faulty [7].

The second major problem affects all of science. Scientific publications are riddled with errors. A portion of these errors are mathematical. In 2012 Casey Klein et al. used specialized computer software to verify the correctness of nine papers published in the proceedings of the International Conference on Functional Programming (ICFP). Two of the papers where used as a control which where known to have been formally verified before. In their paper [6] they show that all nine papers contained mathematical errors. This is disconcerting especially since most researchers trust published work and base their own work off of these papers. Kline's work shows that trusting published work might result in wasted time for the researchers basing their work off of these error prone publications. Faulty research hinders scientific progress.

Both problems outlined above have been the focus of a large body of research over the course of the last forty years. These challenges have yet to be completed successfully. The work I present here makes up the foundations of one side of the programs leading the initiative to build theory and tools which can be used to verify the correctness of software and mathematics. This program is called program verification using dependent type theories. The second program is automated theorem proving. In this program researchers build tools called model checkers and satisfiability modulo-theories solvers. These tools can be used to model and prove properties of large complex systems carrying out proofs of the satisfiability of certain constraints on the system nearly automatically, and in some cases fully automatically. As an example André Platzer and Edmund Clarke in 2009 used automated theorem proving to verify the correctness of the in flight collision detection systems used in airplanes. They actually found that there were cases where two plans could collide, and gave a way to fix the problem resulting in a fully verified algorithm for collision detection. That is he mathematically proved that there is no possible way for two plans to collide if the systems are

operational [8]. Automated theorem provers, however, are tools used to verify the correctness of software externally to the programming language and compiler one uses to write the software. In contrast with verification using dependent types we wish to include the ability to verify software within the programming language being used to write the software. Both programs have their merits and are very fruitful and interesting.

This report summarizes my dissertation by chapter, section, and subsection. Each section will be given the name of a chapter, and then the contents of the section will consist of a summary of that chapter. Similarly, for subsections. I make sure to include my already published work as well as on going work that needs to be done before my defense. My thesis will be broken into three main chapters. The first, gives a history of type theory, and the necessary background to facilitate understanding of the main results. The second chapter is on the design of new advanced functional programming languages. Finally, the third covers the meta-theoretic analysis of various type theories and functional programming languages.

2 Chapter 0: History and Background

This chapter provides a brief history of type theory as a foundation of mathematics and typed-functional programming languages. It begins with Bertrand Russell – the founder of type theory – and introduces key results up to the present. This chapter also serves as an introduction of all the necessary concepts to understand the remainder of the thesis. I make sure and present each type theory in its entirety and rigorously. In fact every language defined in the thesis will be formally defined in Ott [11]. Ott is a tool for writing definitions of programming languages, type theories, and λ -calculi. Ott generates a parser and a type checker which is used to check the accuracy of all objects definable within the language given to Ott as input. Ott’s strongest application is to check for syntax errors within research articles. Ott is a great example of a tool using the very theory I will present in my thesis. It clearly stands as a successful step towards the solution of the second major problem outlined in the introduction. Lastly, this history and background has all been written and was presented as my comprehensive exam.

3 Chapter I: Design

This chapter presents the design of a two general-purpose dependently-typed functional programming languages called Freedom of Speech, and Separation of Proof from Program, and a new constructive type theory with constructive control called Dualized Type Theory. This chapter will have a section per language. All the work with respect to the first two languages is complete although mostly unpublished. The language of Dualized Type Theory is stabilizing, but its analysis is on going work [12].

The TRELLYS project is a collaboration between the University of Iowa, University of Pennsylvania, and Portland State University to design a new general-purpose dependently-typed functional programming language that supports type-based verification. What sets TRELLYS apart from other similar projects is that it contains a number of advanced features within the same language. For example, mixing type-based verification with general recursion is not well understood. This mixture is one of the primary aims of this project. TRELLYS was designed from the bottom up. We started with a small trusted language called the core, and then, after the core was finished, we would build a surface language on top of it. Then the latter would elaborate into the former. My primary contribution to this project was to the design and analysis of the core. I helped with the design and analysis of two core languages. The first is Freedom of Speech.

3.1 Freedom of Speech

The main objective of the TRELLYS project is to design a functional programming language with two discernible fragments: a logical fragment, and a programmatic fragment. The programmatic fragment is a general purpose dependently-type functional programming language. This is a Turing-complete language with general recursion. In addition it contains the type in type axiom which leads to paradoxes [2, 3]. This axiom allows for the definition of generic programs. Now the logical

fragment is the fragment that can be used to prove properties about the programs defined in the programmatic fragment. In order for this fragment to be considered a logic it must terminate. Meaning every program written in the this fragment must terminate in general. This property guarantees that the logic is consistent.

Recall that the three perspectives of computation¹ tell us that programs are proofs and their types are propositions. The most significant feature of Freedom of Speech is that logical types can contain programs from the programmatic fragment, but they are never allowed to be applied to any arguments. Thus, the logical fragment is allowed to “talk” about the programmatic fragment. This property we call free speech.

This section introduces the Freedom of Speech language and discusses its design. The analysis of this language greatly influenced its design. I discuss the analysis in Section 4.1.1. Interesting properties of this design include: implicit arguments, the free speech property, a collapsed syntax, and judgmental fragmentation into the logical and programmatic fragment. This design is complete and formalized in Ott, but was never published.

3.2 Separation of Proof from Program (SepPP)

One of the key features of the Freedom of Speech language is that it has a collapsed language where terms and types are apart of the same syntactic category. This makes for a very elegant design, but due to having to fragment the language into a logical fragment and a programmatic fragment using the typing judgment the language very hard to reason about. This is especially true when we want to extend the Freedom of Speech language with additional features. For example, algebraic data types. To overcome this problem we (the University of Iowa group) proposed to separate the logical fragment from the programmatic fragment into two distinct languages. Then provide the necessary linkage to allow for the logical fragment to contain the free speech property.

In this section the full design of SepPP is detailed and discussed. We did not carry out any analysis of this language, but only explored its design, and its use in writing real-world programs [5, 4]. Then full design of SepPP has never been published, however, its design is completely written up, and an implementation² exists.

3.3 Dualized Type Theory (DTT)

Constructive control operators are control operators – operators that have the ability to discard evaluation contexts – that have been restricted to discarding only certain context so as to remain constructive.

¹Also known as the Curry-Howard correspondence, and the propositions-as-types proofs-as-programs correspondence.

²SepPP’s implementation was authored by Garrin Kimmel.

4 Chapter II: Analysis

4.1 Basic Analysis

4.1.1 Free Speech

4.1.2 Dualized Type Theory

4.2 Normalization by Hereditary Substitution

4.2.1 Stratified System F (SSF) and its Extensions

4.2.2 The $\lambda\Delta$ -Calculus

4.3 Categorical Semantics

4.3.1 Semi-Bilinear Logic

4.3.2 Split Bi-Intuitionistic Logic

4.3.3 Dualized Type Theory

4.3.4 Nested Bi-Intuitionistic Logic

5 Conclusion

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