



## Lab #1

Instructor: Dr. Ha Viet Uyen Synh.

Duration: 3 hours

### Report Submission:

Submit a single .docx or .pdf file containing:

#### 1. Source Code:

- Code from Part 1 (computing  $e^x$ ).
- Code from Part 2 (computing and plotting  $\sin(x)$ ).
- Code from Part 3 (error analysis and computing  $\cos(x)$ ).

#### 2. Results Obtained:

- Approximation and actual values of  $e^x$ ,  $\sin(x)$ , and  $\cos(x)$  at  $x=1$ .
- Three plots: `sin_taylor.png`, `sin_error.png`, `cos_taylor.png`.
- Error analysis for  $\sin(x)$  (location of largest error and explanation).
- A short paragraph comparing the convergence of  $\sin(x)$  and  $\cos(x)$ .

### Lab Procedure

#### Part 1:

- Compute the first 4 terms of the Taylor Series for  $e^x$  around  $x=0$ .
- Run the code and record the output (approximation and actual value) in your report.

#### Part 2:

- Write a function to compute the Taylor Series approximation of  $\sin(x)$ .
- Run the code and copy the results into your report.
- Plot the actual  $\sin(x)$  against its Taylor approximations with 1, 3, and 5 terms.
- Save the plot as `sin_taylor.png` and include it in your report.

#### Part 3:

- Compute and plot the absolute error of the Taylor approximation for  $\sin(x)$  with 5 terms.
- Save the plot as `sin_error.png` and include it in your report.
- Where is the error largest? Why?
- Implement the Taylor Series for  $\cos(x)$  with 4 terms around  $x=0$ .
- Run the code, record the results in your report, and save the plot as `cos_taylor.png` for inclusion.
- Write a short paragraph (5-7 sentences) in your report: Compare the convergence of the Taylor Series for  $\sin(x)$  and  $\cos(x)$ .