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This is the new mandi package (v3.0.0a dated 2021-01-04), which creates a habitat specifically for introductory physics students. It provides consistent notation conventions that align with ISO 80000-2 recommendations. This document is a demonstration for the new package and should not be taken as official documentation. Features are not necessarily final and are still subject to change.

1 Fonts

1.1 Text Mode Fonts

1.1.1 Default Text Font Parameters

To begin with, let's look at the fonts we have at our disposal. Let's look at the default text mode font parameters first.

\encodingdefault	TU
\familydefault	lmr
\seriesdefault	\mathbf{m}
\shapedefault	\mathbf{n}
\rmdefault	lmr
\sfdefault	lms
\ttdefault	lmtt
\bfdefault	b
\updefault	up
\itdefault	it
\mddefault	\mathbf{m}
\sldefault	sl
\scdefault	sc

1.1.2 Text Mode Font Commands

Now let's look at the text mode commands for changing fonts and their accompanying results. Note that these commands require braced arguments and work only within the scope of the braces.

```
Text Mode Commands
The default normal text is \textnormal{...}.
abcdefghijklmnopgrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get roman letters, use \text{textrm}\{...\}.
abcdefghijklmnopgrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get san serif letters, use \textsf{...}.
abcdefghijklmnopgrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get typewriter letters, use \texttt{...}.
abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get medium letters, use \textmd{...}.
abcdefghijklmnopgrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get boldface letters, use \textbf{...}.
abc defghijklm nop qrstuvwxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789\\
Text up \textup{...}
abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get italic letters, use \textit{...}.
abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get slanted letters, use \textsl{...}.
abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
To get small capital letters, use \textsc{...}.
ABCDEFGHIJKLMNOPQRSTUVWXYZABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
```

Some of those text mode commands may seem redundant to you, and there are some you will never need to use, so don't worry if they look confusing. Remember that \textnormal{...} is the default and all you have to do to get it is start typing; no command is necessary unless you have changed something (and that's usually difficult to do). These text font commands can be used together if you remember to nest the braces correctly. Look at the following table.

Combined Text Mode Commands

To get boldface san serif letters, use \textbf{\textsf{...}}.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

To get boldface italic letters, use \textbf{\textit{...}}.

abcdefqhijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

To get boldface slanted letters, use \textbf{\textsl{...}}.

abc defghijk Imnop qrstuv wxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

1.1.3 Emphasizing Words in Text Mode

For semantic reasons, it's important to use \emph{...} when you want to emphasize a word. Use \emph{vector} to emphasize the word *vector* or \emph{momentum} to emphasize the word *momentum*. In most documents, \emph{...} defaults to italics, but it may default to something else when using a different document class. Let the document class do its work and you will have fewer things to remember.

1.1.4 Text Modal Font Commands

Next, let's look as the various text modal commands you can use. I like to think of them as *switches* rather than *commands* because they take effect immediately and stay in effect until you explicitly turn them off by activating another one, much like a light switch. As so, they do not take braced arguments, or indeed, any arguments at all. Look at the following table.

Text Modal Commands

Use \normalfont to switch to the default normal font.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \rmfamily to switch to roman letters.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \sffamily to switch to sans serif latters.

abcdefghijklmnopgrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \ttfamily to switch to typewriter letters.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \mdseries to switch to medium letters.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \bfseries to switch to boldface letters.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \upshape to switch to upright letters.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \itshape to switch to italic letters.

abcdefghijklmnop qrstuv wxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \slshape to switch to slanted letters.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

Use \scshape to switch to small capital letters.

ABCDEFGHIJKLMNOPQRSTUVWXYZABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

To illustrate how these switches work, the following unindented paragraph is in the default text font (it's just filler text). Lorem ipsum dolor sit amet, consectetur adipiscing elit. Duis egestas urna et dolor posuere, accumsan faucibus justo viverra. Pellentesque libero neque, maximus vitae placerat eu, luctus sit amet sapien. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos himenaeos. Aenean vel nisl massa. Sed id velit tellus. Vivamus eu elit a erat aliquam auctor nec sed mi. Orci varius natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Cras ut consequat purus. Fusce imperdiet scelerisque sagittis. Etiam maximus sagittis sapien. Proin mi metus, cursus a ex eget, maximus laoreet sapien. In hac habitasse platea dictumst. Morbi eget est dui. Cras posuere nisl quis leo facilisis, vel viverra augue sagittis. Nullam posuere, ex id efficitur mollis, velit nisi tincidunt augue, vel tempor orci nisi a justo.

The following unindented paragraph is the same filler text, but now preceded by the \sffamily switch.

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Duis egestas urna et dolor posuere, accumsan faucibus justo viverra. Pellentesque libero neque, maximus vitae placerat eu, luctus sit amet sapien. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos himenaeos. Aenean vel nisl massa. Sed id velit tellus. Vivamus eu elit a erat aliquam auctor nec sed mi. Orci varius natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Cras ut consequat purus. Fusce imperdiet scelerisque sagittis. Etiam maximus sagittis sapien. Proin mi metus, cursus a ex eget, maximus laoreet sapien. In hac habitasse platea dictumst. Morbi eget est dui. Cras posuere nisl quis leo facilisis, vel viverra augue sagittis. Nullam posuere, ex id efficitur mollis, velit nisi tincidunt augue, vel tempor orci nisi a justo.

Note that this (the current) paragraph is still typeset in sans serif letters because the \sffamily switch is still activated. We can deactivate it by activating another switch, like \normalfont to get back to normal default text, or like \bfseries to get bold letters, or even like \itshape to get italic letters. Note that we got both bold and italic letters in that last phrase, and in this sentence, because the \bfseries switch was still activated when we activated the \itshape switch. Activated switches can accumulate to give us new combinations of letter styles and shapes. We can return to the normal default font by activating the \normalfont switch just like this. Now everything is back to normal.

1.2 Math Mode Fonts

Now we need to discuss math mode fonts, which are considerably more complicated than text mode fonts. There are math mode font *commands*, but there are no math mode font *switches*. Math mode fonts sometimes include lowercase and/or uppercase Greek letters, which are frequently used in mathematical notation. Math mode fonts go into effect whenever you enter in-line math mode with \(\(\cdots\)\) or display math mode with \(\(\cdots\)\). Many IATEX tutorials use \$...\$ for in-line math mode and \$\$...\$\$ for display math mode. For various technical reasons, these are not recommended so please do not use them. Please consistently use \(\((\cdots\)\)\) for in-line math mode and \(\((\cdots\)\)\)]

1.2.1 Unicode Math Mode Font Commands

In math mode, we use the unicode-math package to create new font combinations that allow for greater flexibility than otherwise available. There is a tradeoff, and that is documents must be processed with the LualATeX engine. The math mode Unicode font commands available to you in this habitat are given in the following table. Note that all of these commands begin with \sym<...>. You may assume that characters not shown are not supported.

\(...\) or \[...\] or \symnormal{...} give the default math mode font. Use this for vector index notation.

abcdefghijklm nop qrstuvwxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

αβγδεεζηθθικλμυξοπωροσςτυφφχψωΔΓΘΛΞΠΣΥΦΨΩ

\symbf{...} gives boldface italic. Use this for coordinate-free vectors and matrices.

abcdef ghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ $\alpha\beta\gamma\delta\epsilon\varepsilon\zeta\eta\theta\vartheta\iota\kappa\lambda\mu\nu\xi o\pi\varpi\rho\varrho\sigma\varsigma\tau\upsilon\phi\varphi\chi\psi\omega\Delta\Gamma\Theta\Lambda\Xi\Pi\Sigma\Upsilon\Phi\Psi\Omega$

 $\sum_{\text{symup{...}}} \text{gives upright (roman) serif. Use this to name particles. } \sum_{\text{omega}} (\Omega) \text{ represents the ohm.}$

αβγδεεζηθθικλμυξοπωρρσςτυφφχψωΔΓΘΛΞΠΣΥΦΨΩ

\symbfup{...} gives boldface upright serif.

abcdefghijklm nop qrstuvwxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

 $\alpha\beta\gamma\delta\epsilon\epsilon\zeta\eta\theta\vartheta\iota\kappa\lambda\mu\nu\xi\sigma\pi\varpi\rho\varrho\sigma\varsigma\tau\upsilon\varphi\phi\chi\psi\omega\Delta\Gamma\Theta\Lambda\Xi\Pi\Sigma\Upsilon\Phi\Psi\Omega$

 \symmutes gives sans serif upright. Use this for physical dimensions.

abcdefghijklmnopqrstuvwxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

\symbfsfup{...} gives boldface sans serif upright.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789 αβγδεεζηθθικλμνξοπωρρσςτυφφχψω Δ Γ Θ Λ Ξ Π Σ Υ Φ Ψ Ω

\symsfit{...} gives sans serif italic. Use this for tensor index notation.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ

\symbfsfit{...} gives boldface sans serif italic. Use this for coordinate-free tensors.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ

\symcal{...} and\symbfcal{...} give calligraphic. Use these for points on a manifold or naming coordinate systems.

ABCDEFGHIJKLMNOPQRSTUVWXYZ

ABCDEFCHIJKLMNOPQRSTUVWXYZ

\symscr{...} and \symbfscr{...} give script. Use these for naming spacetime events.

abedefqhijklmnopqrstuvwxyxABCDEFGHIJXLMNOPQRSTUVWXYX

abcdefghijhlmnopqrstuvwxyzABCDEFGHJJKLMNOPQRSTUVWXYZ

\symtt{...} gives typewriter.

abcdefghijkl mnopqrstuvwxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

 $\verb|\symfrak{...}| and \verb|\symbffrak{...}| give Fraktur.$

abcdefghijklmnopgrstuvmrn3ABCDEFGHIJALMNDPQRGTUVWXN3

abcdefghijtlmnopqrstuvmrnzABCDEFGHIJALMNDPQAGTUVWXY3

\symbb{...} gives blackboard.

abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789

 $\verb|\symbbit{...}| gives blackboard italic. I have no idea why it's defined for only five letters.$

 $\mathit{deij}\, D$

The zero vector is \symbfup{0} or **0**. It is aliased as \zerovector, which also gives **0**. As you can see, many more characters are available using the Unicode commands. Also, notice the semantic naming of each typeface and style.

1.2.2 A Few More Mathematical Symbols

There's a handful of other mathematical symbols you will need, and here they are. Don't worry if you've never seen any or all of these before. The third row of symbols is unique to mandi.

$$\begin{array}{c} \nabla \, \square \, \partial \, \otimes \, \times \, \cdot \, \bullet \\ \nabla \, \partial \\ \nabla_{\boldsymbol{u}} \, \nabla_{\boldsymbol{u}} \\ \underline{\qquad \quad \boldsymbol{a}} \, \mathbb{C}_{(1,2)} \, \mathbb{C}_{(1,3)(2,4)} \, \mathsf{C}_{(1,2)} \, \mathsf{C}_{(1,3)(2,4)} \end{array}$$

1.2.3 Unicode Input

With Unicode support, you can use characters direction from your keyboard. It is important to remember that the glyphs (characters) you use must be present in the font you use for your document or they will not display correctly, if at all. The following example of Maxwell's equations uses characters typed directly from the keyboard.

$$\begin{split} \nabla \bullet \boldsymbol{E} &= \frac{\rho}{\varepsilon_o} \\ \nabla \bullet \boldsymbol{B} &= 0 \\ \nabla \times \boldsymbol{E} &= -\frac{\partial \boldsymbol{B}}{\partial t} \\ \nabla \times \boldsymbol{B} &= \mu_o \Big(I + \varepsilon_o \frac{\partial \boldsymbol{E}}{\partial t} \Big) \end{split}$$

There is an intelligent exterior derivative operator.

 ${\rm d}\omega$

2 The Unit Engine

The seven fundamental SI quantities are displacement (3 m), duration (3 s), mass (3 kg), electric current (3 A), thermodynamic temperature (3 K), amount (3 mol), and luminous intensity (3 cd).

```
rrent (3 A), thermodynamic temperature 4 \text{ m} \cdot \text{kg} \cdot \text{s}^{-1}, 4 \text{ N} \cdot \text{s}, 4 \text{ kg} \cdot \text{m/s}

4 \text{ m} \cdot \text{s}^{-2}, 4 \text{ N/kg}, 4 \text{ m/s}^2

4 \text{ kg} \cdot \text{s}^{-2} \cdot \text{A}^{-1}, 4 \text{ T}, 4 \text{ N/C} \cdot (\text{m/s})

4 \text{ m} \cdot \text{kg} \cdot \text{s}^{-1}, 4 \text{ m} \cdot \text{s}^{-2}, 4 \text{ kg} \cdot \text{s}^{-2} \cdot \text{A}^{-1}

4 \text{ N} \cdot \text{s}, 4 \text{ N/kg}, 4 \text{ T}

4 \text{ kg} \cdot \text{m/s}, 4 \text{ m/s}^2, 4 \text{ N/C} \cdot (\text{m/s})

\text{m} \cdot \text{kg} \cdot \text{s}^{-1}, \text{N} \cdot \text{s}, \text{kg} \cdot \text{m/s}
```

name	$\begin{array}{c} base \\ m \cdot s^{-2} \end{array}$	derived N/kg	alternate m/s ²
name	base mol	derived mol	alternate mol
${ m name}$ \angularvelocity	$\begin{array}{c} \text{base} \\ \text{rad} \cdot \text{s}^{-1} \end{array}$	derived rad/s	alternate rad/s
${\rm name} \\ {\tt \ \ \ \ \ \ }$	base $rad \cdot s^{-2}$	derived rad/s²	alternate rad/s ²
${ m name}$	$\begin{array}{c} \text{base} \\ \text{rad} \cdot \text{s}^{-1} \end{array}$	derived rad/s	alternate rad/s
name \angularimpulse	$\begin{array}{c} {\rm base} \\ {\rm m^2 \cdot kg \cdot s^{-1}} \end{array}$	$\begin{array}{c} \text{derived} \\ \text{J} \cdot \text{s} \end{array}$	$\begin{array}{c} \text{alternate} \\ \text{N} \cdot \text{m} \cdot \text{s} \end{array}$
name \angularmomentum	$\begin{array}{c} {\rm base} \\ {\rm m^2 \cdot kg \cdot s^{-1}} \end{array}$	$\frac{\text{derived}}{\text{kg} \cdot \text{m}^2/\text{s}}$	$\begin{array}{c} \text{alternate} \\ \text{N} \cdot \text{m} \cdot \text{s} \end{array}$
name \area	base m ²		$\underset{m^2}{\operatorname{alternate}}$
name \areamassdensity	base m ⁻² ·kg	derived kg/m²	alternate kg/m ²
name \areachargedensity	$\begin{array}{c} \text{base} \\ \text{m}^{-2} \cdot \text{s} \cdot \text{A} \end{array}$	derived C/m²	alternate C/m ²
name \capacitance	$\begin{array}{c} base \\ m^{-2} \cdot kg^{-1} \cdot s^4 \cdot A^2 \end{array}$	derived F	alternate C/V
name \charge	$\begin{array}{c} \text{base} \\ \text{A} \cdot \text{s} \end{array}$	derived C	alternate C

name	$\begin{array}{c} base \\ m \cdot kg \cdot s^{-3} \cdot A^{-1} \end{array}$	derived	alternate
\cmagneticfield		N/C	V/m
name	$\begin{array}{c} base \\ m^{-2} \cdot kg^{-1} \cdot s^3 \cdot A^2 \end{array}$	derived	alternate
\conductance		A/V	S
name \conductivity	$\begin{array}{c} base \\ m^{-3} \cdot kg^{-1} \cdot s^3 \cdot A^2 \end{array}$	$\frac{\mathrm{derived}}{(A/m^2)/(V/m)}$	alternate S/m
name \conventionalcurrent	base	derived	alternate
	A	A	C/s
name	base	derived	alternate
\current	A	A	A
name \currentdensity	$\begin{array}{c} base \\ m^{-2} \cdot A \end{array}$	derived A/m ²	$\begin{array}{c} {\rm alternate} \\ {\rm C\cdot s/m^2} \end{array}$
name \dielectricconstant	base	derived	alternate
name	base	derived	alternate
\displacement	m	m	m
name	base	derived	alternate
\duration	s	s	s
name	$\begin{array}{c} base \\ m \cdot s \cdot A \end{array}$	$\begin{array}{c} \text{derived} \\ \text{C} \cdot \text{m} \end{array}$	$\begin{array}{c} \text{alternate} \\ \text{C} \cdot \text{m} \end{array}$
name	$\begin{array}{c} base \\ m \cdot kg \cdot s^{-3} \cdot A^{-1} \end{array}$	derived	alternate
\electricfield		N/C	V/m
name \electricflux	$\begin{array}{c} base \\ m^3 \cdot kg \cdot s^{-3} \cdot A^{-1} \end{array}$	$\frac{\text{derived}}{N \cdot m^2/C}$	$\begin{array}{c} \text{alternate} \\ \text{V} \cdot \text{m} \end{array}$
name	$\begin{array}{c} base \\ m^2 \cdot kg \cdot s^{-3} \cdot A^{-1} \end{array}$	derived	alternate
\electricpotential		V	J/C
name	base s ⁻¹	derived	alternate
\electroncurrent		e/s	e/s
name	$\begin{array}{c} base \\ m^2 \cdot kg \cdot s^{-3} \cdot A^{-1} \end{array}$	derived	alternate
\emf		V	J/C
name \energy	$\begin{array}{c} base \\ m^2 \cdot kg \cdot s^{-2} \end{array}$	derived J	$\begin{array}{c} \text{alternate} \\ \text{N} \cdot \text{m} \end{array}$

${ m name}$	$\begin{array}{c} base \\ m^{-1} \cdot kg \cdot s^{-2} \end{array}$	derived J/m³	alternate J/m ³
name \energyflux	base kg·s ⁻³	derived W/m²	$\begin{array}{c} {\rm alternate} \\ {\rm W/m^2} \end{array}$
name \entropy	$\begin{array}{c} base \\ m^2 \cdot kg \cdot s^{-2} \cdot K^{-1} \end{array}$	derived J/K	alternate J/K
name \frequency	$\begin{array}{c} \text{base} \\ s^{-1} \end{array}$	derived Hz	alternate Hz
name \force	$\begin{array}{c} \text{base} \\ \text{m} \cdot \text{kg} \cdot \text{s}^{-2} \end{array}$	derived N	alternate N
name \gravitationalfield	$\begin{array}{c} {\rm base} \\ {m \cdot s^{-2}} \end{array}$	derived N/kg	alternate N/kg
${\rm name} \\ {\tt \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	$\begin{array}{c} \text{base} \\ \text{m}^2 \cdot \text{s}^{-2} \end{array}$	derived J/kg	alternate J/kg
name \impulse	$\begin{array}{c} \text{base} \\ \text{m} \cdot \text{kg} \cdot \text{s}^{-1} \end{array}$	derived N·s	$\begin{array}{c} \text{alternate} \\ \text{N} \cdot \text{s} \end{array}$
name \indexofrefraction	base	derived	alternate
name \inductance	$\begin{array}{c} base \\ m^2 \cdot kg \cdot s^{-2} \cdot A^{-2} \end{array}$	derived H	$\begin{array}{c} \text{alternate} \\ V \cdot s/A \end{array}$
${\rm name} \\ {\tt linearchargedensity}$	$\begin{array}{c} \text{base} \\ m^{-1} \cdot s \cdot A \end{array}$	derived C/m	alternate C/m
name	$\begin{array}{c} base \\ m^{-1} \cdot kg \end{array}$	derived kg/m	alternate kg/m
name \luminous	base cd	derived cd	alternate cd
name \magneticcharge	$\begin{array}{c} \text{base} \\ \text{m} \cdot \text{A} \end{array}$		
name \magneticdipolemoment	$\begin{array}{c} base \\ m^2 \cdot A \end{array}$	$\begin{array}{c} \text{derived} \\ A \cdot m^2 \end{array}$	alternate J/T
name \magneticfield	$\begin{array}{c} base \\ kg \cdot s^{-2} \cdot A^{-1} \end{array}$	derived T	alternate $N/C \cdot (m/s)$

name	base	derived	alternate
$\mbox{\tt magneticflux}$	$m^2 \cdot kg \cdot s^{-2} \cdot A^{-1}$	$T\cdot m^2$	$V \cdot s$
name	base	derived	alternate
\mass	kg	kg	kg
name	base	derived	alternate
\mobility	$m^2 \cdot kg \cdot s^{-4} \cdot A^{-1}$	$m^2/V \cdot s$	(m/s)/(N/C)
\mobility	m ·kg·s ·A	III / V · S	(111/5)/(11/0)
name	base	derived	alternate
\momentum	$m\cdot kg\cdot s^{-1}$	$N \cdot s$	$kg \cdot m/s$
	1	1 . 1	1, ,
name	base	derived	alternate
\momentumflux	$m^{-1} \cdot kg \cdot s^{-2}$	N/m^2	N/m^2
name	base	derived	alternate
\momentofinertia	$\mathrm{m}^2\cdot\mathrm{kg}$	$\mathrm{m}^2\cdot\mathrm{kg}$	$J \cdot s^2$
•	3	3	J -
name	base	derived	alternate
\numberdensity	m^{-3}	$/\mathrm{m}^3$	$/m^3$
			•
name	base	derived	alternate
\permeability	$m\cdot kg\cdot s^{-2}\cdot A^{-2}$	$T\cdot m/A$	H/m
name	base	derived	alternate
\permittivity	$m^{-3} \cdot kg^{-1} \cdot s^{-4} \cdot A^2$	$C^2/N \cdot m^2$	F/m
A		5 /	- /
name	base	derived	alternate
\planeangle	$\mathrm{m}\cdot\mathrm{m}^{-1}$	rad	rad
	1	11	- 14 4 -
name	base $kq^{-1} \cdot s^4 \cdot A^2$	derived	alternate
\polarizability	kg · S· A	$C \cdot m^2/V$	$C \cdot m/(N/C)$
name	base	derived	alternate
\power	$m^2 \cdot kg \cdot s^{-3}$	W	J/s
-	-		
name	base	derived	alternate
\pressure	$m^{-1} \cdot kg \cdot s^{-2}$	Pa	N/m^2
nama	base	derived	alternate
name	base	derived	anemate
\relativepermeability			
name	base	derived	alternate
\relativepermittivity			
•			
name	base	derived	alternate
\resistance	$m^2 \cdot kg \cdot s^{-3} \cdot A^{-2}$	Ω	V/A

name \resistivity	$\begin{array}{c} base \\ m^3 \cdot kg \cdot s^{-3} \cdot A^{-2} \end{array}$	$\operatorname*{derived}_{\Omega\cdot\mathbf{m}}$	alternate $(V/m)/(A/m^2)$
name	$\begin{array}{c} \text{base} \\ \text{m}^2 \cdot \text{m}^{-2} \end{array}$	derived	alternate
\solidangle	m⁻ · m	sr	sr
name	base	derived	alternate
\specificheatcapacity	$m^2 \cdot s^{-2} \cdot K^{-1}$	$J/K \cdot kg$	$J/K \cdot kg$
name	base	derived	alternate
\springstiffness	$\mathrm{kg}\cdot\mathrm{s}^{-2}$	N/m	N/m
name	base	derived	alternate
\springstretch	m	m	m
name	base	derived	alternate
\stress	$m^{-1} \cdot kg \cdot s^{-2}$	Pa	N/m ²
name	base	derived	alternate
\strain			
name	base	derived	alternate
\temperature	K	K	K
name	base	derived	alternate
\torque	$m^2 \cdot kg \cdot s^{-2}$	$N\cdot m$	$N\cdot m$
name	base	derived	alternate
\velocity	$m\cdot s^{-1}$	$m\cdot s^{-1}$	m/s
name	base	derived	alternate
\volume	m^3	m^3	m^3
name	base	derived	alternate
\volumechargedensity	$m^{-3} \cdot s \cdot A$	C/m ³	C/m ³
name	base	derived	alternate
\volumemassdensity	$m^{-3}\cdot kg$	kg/m ³	kg/m^3
name	base	derived	alternate
\wavelength	m	m	m
name	base	derived	alternate
\wavenumber	m^{-1}	/m	/m
name	base	derived	alternate
\work	$m^2 \cdot kg \cdot s^{-2}$	J	$N\cdot m$
name	base	derived	alternate
\youngsmodulus	$m^{-1} \cdot kg \cdot s^{-2}$	Pa	N/m^2

3 Column and Row Vectors

3.1 Column Vectors

$$\begin{pmatrix} 0 \\ 1 \\ 2 \\ 3 \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \\ a_2 \end{pmatrix}$$

3.2 Row Vectors

$$(0 \quad 1 \quad 2 \quad 3)(a_1 \quad a_2 \quad a_2)$$

4 Symbolic Vectors

4.1 Notation Conventions

Typesetting symbolic vectors is ubiquitous in in physics, yet most sources are not consistent in notation compared to other sources. Using arrows to denote vector quantities, as with \vec*{p}} (note the *), which gives \vec{p} , seems the standard in introductory physics courses, but this isn't seen in higher level resources, and certainly not in published articles. The standard, which doesn't seem to be observed, is that vectors are typeset in boldface italic, as with $\vee ec\{p\}$, which gives p. Physics teachers know students struggle with using arrows to denote vector quantities, and most students never correctly learn it. After all, why should they learn something that isn't used consistently, or even at all? There is really just one practical reason for using arrows rather than boldface, and that is the quaint notion of writing on a whiteboard (or a chalkboard if anyone remembers those). We really should move with the times and enforce the professional convention for our students. So in mandi we do exactly this, but allow flexibility in notation for those who insist upon having it. By default, the standard LATFX \vec{...} command is redefined to, by default, typeset symbols for vector quantities in boldface italic. The starred form of the command, \vec*{...}, typesets them with arrows. Note that getting arrow notation is a bit more difficult (because you must type the *) than the default boldface italic notation, and this is a subtle psychological tactic on my part; the new notation takes less effort.

4.2 Symbolic Notation

The command \dirvect{...} typesets the symbol for a vector's direction. \dirvect{r} gives \hat{r} and as you might expect by now \dirvect*{r} gives \hat{r} . A vector's magnitude is typeset with \norm{...}. As you may predict, \norm{\vec{r}} gives ||r|| and \norm{\vec*{r}} gives $||\hat{r}||$. Any vector can be factored into its magnitude and direction. So $\mathbf{p} = ||\mathbf{p}||\hat{\mathbf{p}}$ or $\vec{p} = ||\hat{p}||\hat{p}$.

The command $\mbox{magvect{r}}$ typesets the symbol for a vector's magnitude. $\mbox{magvect{r}}$ gives $\|r\|$ and of course $\mbox{magvect*{r}}$ gives $\|\vec{r}\|$.

Finally, the command $\D\text{vect}\{...\}$ typesets the symbol for the change in a vector. $\D\text{vect}\{r\}$ gives Δr . For arrow notation, use the starred form. $\D\text{vect}\{r\}$ gives $\Delta \vec{r}$.

4.3 Embellishments

Again, I state that notation should help the reader and for physics students, unambiguously help guide one's thinking. This frequently requires use of embellishments, or additions to basic notation. For example, consider a rock moving through space. One can speak of the rock's momentum, and notate it as \vec{p}_{frock}, which gives

$$\mathbf{p}_{rock}$$

as predicted. But wait, the subscript doesn't look right. It is typeset in italic when it shouldn't be. So instead, we write \vec{p}_{\mathup{rock}}, which gives

$\boldsymbol{p}_{\mathrm{rock}}$

which looks much better. Why does this make a difference? The answer is that the \vec{...} command internally takes place in *math mode*, which means all characters are, by default, typeset in italic. Words are not intended to be written in math mode. So if we want to typeset an actual piece of text, you must mark it up as such using a \mathup{...} command.

So now you can correctly typeset an initial momentum and final momentum symbolically as \vec{p}_{\mathbb{p}_{\mathbf{j}}}, which give

$$\boldsymbol{p}_{\text{initial}}$$
 and $\boldsymbol{p}_{\text{final}}$

exactly as expected. If you want something other than actual text as a subscript, just supply it without additional markup. So you could write, for example, \vec{p}_{1} and get

\boldsymbol{p}_1

as expected. The braces around the subscript are strictly not required if the subscript is just one character, but it is a good habit to write them all the time, so I do.

You can add superscripts just as easily as you can add subscripts, using a caret (^) to denote the superscript. Writing \vec{p}^{\mathup{rock}} gives

$$p^{\text{rock}}$$

just like that. All the comments about subscripts above apply to superscripts. The best part is that you can effortlessly mix subscripts and superscripts. Writing

\vec{p}^{\mathup{rock}}_{\mathup{final}} gives

$$m{p}_{\mathrm{final}}^{\mathrm{rock}}$$
 and $m{p}_{\mathrm{final}}^{\mathrm{rock}}$

and note that the order of the flourishes doesn't matter. The underlying LATEX3 programming layer makes this almost trivial to implement in mandi now. Using text to embellish a symbolic vector takes a bit more effort, which is a subtle warning to use it sparingly. Simply changing \vec{...} to \vec*{...} gives the same results with arrow notation and gives

$$\overrightarrow{p}_{\mathrm{final}}^{\mathrm{rock}}$$
 and $\overrightarrow{p}_{\mathrm{final}}^{\mathrm{rock}}$

as expected.

It is very important to always that when in math mode, always, without exception, wrap words used in subscripts and superscripts in \mathup{...}. This does not apply to mathematical symbols, only to actual words or any text that is not mathematical notation.

Of course you can mix mathematical notation and text in the flourishes. As an example, one could represent an alpha particle's final momentum by writing \vec{p}_{\symmp{\lambdalpha},\mathup{final}} which typesets as

$\boldsymbol{p}_{\alpha \text{ final}}$

as beautifully as expected. If you want arrow notation, you would write \vec*{p}_{\symup{\alpha},\mathup{final}} which typesets as

$$\vec{p}_{\alpha, \text{final}}$$

as expected. For many reasons, I think the boldface notation looks better. Finally, note that \symup{...} is used here since upright Greek letters are used to name subatomic particles.

$$\| \boldsymbol{p}_{\text{final}} \| \qquad \left(\frac{1}{4\pi\varepsilon_{o}} \right)$$

$$\Delta \boldsymbol{r} = \boldsymbol{r}_{\text{final}} - \boldsymbol{r}_{\text{initial}} \qquad \text{definition} \qquad \qquad (1)$$

$$\text{Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi.} \qquad (2)$$

$$\Delta \mathbf{r} = \mathbf{r}_{\text{final}} - \mathbf{r}_{\text{initial}} \qquad \text{definition}$$
 (3)

$$\Delta \mathbf{r} = \mathbf{r}_{\text{final}} - \mathbf{r}_{\text{initial}} \qquad \text{definition}$$

$$\|\mathbf{r}\| = \sqrt{\mathbf{r} \cdot \mathbf{r}} \tag{5}$$

4.4 Coordinate-Free Notation

The arrow notation used in introductory physics is a compromise between a notation that ostensibly helps students remember the quantity in question had an associate direction and a notation that is easily reproducible by hand on a whiteboard. As hard as we try, students rarely use arrow notation for vectors correctly, if at all. You don't find arrow notation for vectors much at all in the literature outside of introductory textbooks. Most sources use boldface, and while that is harder to use on a whiteboard, it's trivial to do in IATEX so why not adopt it as the expectation?

Use the \veccomp{...} command to get coordinate-free notation for vectors. \veccomp{p} gives **p**. This notation isn't intended to be used with embellishments, but it can be done as long as you are in math mode.

4.5 Index Notation

Use the \veccomp*{...} command to get index notation for vectors. \veccomp*{p} gives p. Where is the index? You have to supply it using the \indices{...} command from the tensor package, which mandi loads for you. So to get the symbol for momentum in index notation you would use \veccomp*{p}\indices{^i} which gives p^i . Now, you may realize that \veccomp*{p}^i gives the same result, and it does indeed give p^i as expected, so why bother with the \indices{...} command? The answer is that the \indices{...} command plays an important role in tensor index notation, which includes vector index notation, and you need to be comfortable using it. Use \veccomp{e} to get a basis vector, which gives e as expected. Basis vectors must be labeled, and I recommend using the indices{...} command, but both \veccomp{e}\indices{_i} and \veccomp{e}_i give the same result, e_i as expected. So to get the full symbol for a vector in a particular basis you would use

5 Highlighting Mathematics

A new feature to mandi is a command for highlighting mathematics.

$$(\Delta s)^{2} = -(\Delta t)^{2} + (\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}$$

$$(\Delta s)^{2} = -(\Delta t)^{2} + (\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}$$

$$(\Delta s)^{2} = -(\Delta t)^{2} + (\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}$$

$$(\Delta s)^{2} = -(\Delta t)^{2} + (\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}$$

$$(\Delta s)^{2} = -(\Delta t)^{2} + (\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}$$

Here is another example.

$$\Delta \mathbf{p} = \mathbf{F}_{\text{net,sys}} \Delta t$$

Highlighting also works in in-line math mode like $a^2 + b^2 = c^2$.

6 Tensor Notation

A tensor has a valence $\binom{m}{n}$ by definition. A vector is a $\binom{1}{0}$ tensor and a one-form is a $\binom{0}{1}$ tensor.

7 GlowScript and VPython Program Listings

7.1 The glowscriptblock Environment

GlowScript program listings are improved and look better. Clicking anywhere on the actual code takes the reader to the relevant source code on GlowScript.org for read-only access using the URL provided by the user. To minimize the chances of a program being broken over a pagebreak, each listing begins on a new page. This is a big change from the previous version of mandi and may be annoying for small programs, but I think the clarity of beginning a new listing on a new page is important. I recommend using a URL shortening utility to keep the URL from getting unruly, and don't forget to manually prepend either http:// or https:// (preferably the latter) to the URL. Note that GlowScript ignores the from vpython import * line.

```
GlowScript 3.0 VPython
1
    from vpython import *
2
   scene.width = 400
4
   scene.height = 760
5
   # constants and data
   g = 9.8
                # m/s^2
   mball = 0.03 \# kg
   Lo = 0.26
               # m
10
    ks = 1.8
                  # N/m
    deltat = 0.01 #s
11
12
   # objects (origin is at ceiling)
13
    ceiling = box(pos=vector(0,0,0), length=0.2, height=0.01, width=0.2)
14
    ball = sphere(pos=vector(0,-0.3,0), radius=0.025, color=color.orange)
15
    spring = helix(pos=ceiling.pos, axis=ball.pos-ceiling.pos,
16
             color=color.cyan,thickness=0.003,coils=40,radius=0.010)
17
18
   # initial values
19
    pball = mball * vector(0,0,0)
                                        # kg m/s
20
    Fgrav = mball * g * vector(0,-1,0) # N
21
22
   # improve the display
24
                                   # turn off automatic camera zoom
25
    scene.autoscale = False
    scene.center = vector(0, -Lo, 0) # move camera down
26
    scene.waitfor('click')
                                   # wait for a mouse click
27
28
   # initial calculation loop
29
   # calculation loop
30
   while t < 10:
31
        rate(100)
32
        # we need the stretch
33
        s = mag(ball.pos) - Lo
34
35
        # we need the spring force
        Fspring = ks * s * -norm(spring.axis)
36
        Fnet = Fgrav + Fspring
37
        pball = pball + Fnet * deltat
38
        ball.pos = ball.pos + (pball / mball) * deltat
39
        spring.axis = ball.pos - ceiling.pos
40
        t = t + deltat
41
```

Listing 1: A GlowScript program.

nameref-link to listing: A GlowScript program ref-link to listing: 1 pageref-link to listing: 18 autoref-link to listing: Listing 1

It may be annoying for a small program listing like this, but again, I think the clarity is important, especially for beginners.

Listing 2: 79 Columns

nameref-link to listing: 79 Columns ref-link to listing: 2 pageref-link to listing: 20 autoref-link to listing: Listing 2

7.2 The glowscriptblock Environment With VPython Programs

VPython programs are also nicely formatted but lack the hyperlink capability because they live on the user's local computer and not online. Since the glowscriptblock environment turns the code into a hyperlink, it makes no sense semantically to use this environment for VPython programs. Still, it is sometimes helpful to show a block of code this way without turning the code into a hyperlink. Use glowscriptblock without the optional argument to typeset a block of VPython code. In this example, note that the GlowScript 3.0 VPython line is omitted because VPython does not ignore it.

```
from vpython import *
1
2
   scene.width = 400
3
   scene.height = 760
   # constants and data
5
    g = 9.8
                # m/s^2
   mball = 0.03 \# kg
   Lo = 0.26
                 # m
   ks = 1.8
                 # N/m
9
10
    deltat = 0.01 #s
11
    # objects (origin is at ceiling)
12
    ceiling = box(pos=vector(0,0,0), length=0.2, height=0.01, width=0.2)
13
    ball = sphere(pos=vector(0,-0.3,0), radius=0.025, color=color.orange)
14
    spring = helix(pos=ceiling.pos, axis=ball.pos-ceiling.pos,
15
             color=color.cyan,thickness=0.003,coils=40,radius=0.010)
16
17
   # initial values
18
    pball = mball * vector(0,0,0)
                                      # kg m/s
19
    Fgrav = mball * g * vector(0,-1,0) # N
20
21
    t = 0
22
   # improve the display
23
   scene.autoscale = False
                                   # turn off automatic camera zoom
24
25
    scene.center = vector(0, -Lo, 0) # move camera down
   scene.waitfor('click')
                                   # wait for a mouse click
26
27
   # initial calculation loop
28
   # calculation loop
29
   while t < 10:
30
        rate(100)
31
        # we need the stretch
32
        s = mag(ball.pos) - Lo
33
        # we need the spring force
34
35
        Fspring = ks * s * -norm(spring.axis)
        Fnet = Fgrav + Fspring
36
        pball = pball + Fnet * deltat
37
        ball.pos = ball.pos + (pball / mball) * deltat
38
        spring.axis = ball.pos - ceiling.pos
39
        t = t + deltat
```

Listing 3: A VPython program

```
nameref-link to listing: A VPython program ref-link to listing: 3 pageref-link to listing: 21 autoref-link to listing: Listing 3
```

7.3 In-line GlowScript and VPython Code

In-line code can be included as before using \glowscriptline{...} or \vpythonline{...}, depending on which is semantically appropriate. Using

```
\glowscriptline{Earth = sphere(color=color.blue)} gives
Earth = sphere(pos=vector(1,1,1), radius=2, color=color.blue) and
\vpythonline{Sun = sphere(pos=vector(1,1,1), radius=2, color=color.yellow)} gives
Sun = sphere(pos=vector(1,1,1), radius=2, color=color.yellow).
```

7.4 Including a VPython File

A VPython file can be included using \vpythonfile{...}{...}. The file should be in the same folder as the document being typeset, and a caption and a reference label must be provided. Again, the typeset listing begins on a new page. Note that this example contains the exact same code as the example above, but it is read from a file.

```
from vpython import *
   scene.width = 400
3
    scene.height = 760
4
   # constants and data
   q = 9.8
                 # m/s^2
   mball = 0.03 \# kg
   Lo = 0.26
                 # m
    ks = 1.8
                  # N/m
9
    deltat = 0.01 #s
10
11
    # objects (origin is at ceiling)
12
    ceiling = box(pos=vector(0,0,0), length=0.2, height=0.01, width=0.2)
13
    ball = sphere(pos=vector(0,-0.3,0),radius=0.025,color=color.orange)
14
    spring = helix(pos=ceiling.pos, axis=ball.pos-ceiling.pos,
15
             color=color.cyan,thickness=0.003,coils=40,radius=0.010)
16
17
   # initial values
18
    pball = mball * vector(0,0,0)
                                        # kg m/s
19
    Fgrav = mball * g * vector(0,-1,0) # N
20
21
22
   # improve the display
23
                                    # turn off automatic camera zoom
    scene.autoscale = False
    scene.center = vector(0, -Lo, 0) # move camera down
25
   scene.waitfor('click')
                                    # wait for a mouse click
26
27
   # initial calculation loop
28
29
    # calculation loop
   while t < 10:
30
        rate(100)
31
        # we need the stretch
32
        s = mag(ball.pos) - Lo
33
34
        # we need the spring force
        Fspring = ks * s * -norm(spring.axis)
35
        Fnet = Fgrav + Fspring
36
        pball = pball + Fnet * deltat
37
        ball.pos = ball.pos + (pball / mball) * deltat
38
        spring.axis = ball.pos - ceiling.pos
39
        t = t + deltat
40
```

Listing 4: Sample Program

```
nameref-link to listing: Sample Program ref-link to listing: 4 pageref-link to listing: 23 autoref-link to listing: Listing 4
```

8 Commands Specific to Matter & Interactions

These commands are defined in an optional accessory package called mandiexp. That package's name is subject to change.

$$\begin{split} \Delta \boldsymbol{p}_{\text{sys}} &= \boldsymbol{F}_{\text{sys,net}} \, \Delta t & \text{momentum principle} \\ \boldsymbol{p}_{\text{sys,final}} &= \boldsymbol{p}_{\text{sys,initial}} + \boldsymbol{F}_{\text{sys,net}} \, \Delta t & \text{momentum principle,} \\ \Delta E_{\text{sys}} &= W_{\text{ext}} + Q & \text{energy principle} \\ E_{\text{sys,final}} &= E_{\text{sys,initial}} + W_{\text{ext}} + Q & \text{energy principle, update} \\ \Delta \boldsymbol{L}_{A,\text{sys}} &= \boldsymbol{\tau}_{A,\text{sys,net}} \, \Delta t & \text{angular momentum} \\ \boldsymbol{L}_{A,\text{sys,final}} &= \boldsymbol{L}_{A,\text{sys,initial}} + \boldsymbol{\tau}_{A,\text{sys,net}} \, \Delta t & \text{angular momentum} \\ & \text{principle, update form} \end{split}$$

$$E_{\rm sys} \quad E_{\rm sys,final} \quad E_{\rm sys,initial} \quad \Delta E_{\rm sys}$$

$$E_{\rm particle} \quad E_{\rm particle,final} \quad E_{\rm particle,initial} \quad \Delta E_{\rm particle}$$

$$E_{\rm rest} \quad E_{\rm rest,final} \quad E_{\rm rest,initial} \quad \Delta E_{\rm rest}$$

$$E_{\rm internal} \quad E_{\rm internal,final} \quad E_{\rm internal,initial} \quad \Delta E_{\rm internal}$$

$$E_{\rm chem} \quad E_{\rm chem,final} \quad E_{\rm chem,initial} \quad \Delta E_{\rm chem}$$

$$E_{\rm therm} \quad E_{\rm therm,final} \quad E_{\rm therm,initial} \quad \Delta E_{\rm therm}$$

$$E_{\rm photon} \quad E_{\rm photon,final} \quad E_{\rm photon,initial} \quad \Delta E_{\rm photon}$$

$$E_{\rm electron} \quad E_{\rm electron,final} \quad E_{\rm electron,initial} \quad \Delta E_{\rm electron}$$

$$E_{\beta} \quad E_{\beta, {\rm final}} \quad E_{\beta, {\rm initial}} \quad \Delta E_{\beta}$$

$$K_{\rm trans} \quad K_{\rm trans,final} \quad K_{\rm trans,initial} \quad \Delta K_{\rm trans}$$

$$E_{\rm K} \quad E_{\rm K,final} \quad E_{\rm K,initial} \quad \Delta E_{\rm K}$$

$$K_{\rm rot} \quad K_{\rm rot,final} \quad K_{\rm rot,initial} \quad \Delta E_{\rm rot}$$

$$E_{\rm rot} \quad E_{\rm rot,final} \quad E_{\rm rot,initial} \quad \Delta E_{\rm rot}$$

$$K_{\rm vib} \quad K_{\rm vib,final} \quad K_{\rm vib,initial} \quad \Delta E_{\rm vib}$$

$$E_{\rm vib} \quad E_{\rm vib,final} \quad E_{\rm vib,initial} \quad \Delta U_{\rm g}$$

$$U_{\rm e} \quad U_{\rm e,final} \quad U_{\rm e,initial} \quad \Delta U_{\rm e}$$

$$U_{\rm e} \quad U_{\rm e,final} \quad U_{\rm e,initial} \quad \Delta U_{\rm e}$$

$$U_{\rm s. initial} \quad \Delta U_{\rm s.}$$

These commands are intended to be semantically helpful.