



HeuristicLab  
A Paradigm-Independent and Extensible  
Environment for Heuristic Optimization

## Algorithm and Experiment Design with HeuristicLab

An Open Source Optimization Environment for  
Research and Education

S. Wagner, G. Kronberger  
Heuristic and Evolutionary Algorithms Laboratory (HEAL)  
School of Informatics/Communications/Media, Campus Hagenberg  
University of Applied Sciences Upper Austria



HEAL  
Heuristic and Evolutionary  
Algorithms Laboratory



fh  
OBERÖSTERREICH

Josef Ressel-Zentrum  
HEUREKA!

## Agenda

- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
- **Demonstration Part I: Working with HeuristicLab**
- **Demonstration Part II: Data-based Modeling**
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

3



## Instructor Biographies



- Stefan Wagner
  - Full professor for complex software systems (since 2009)
  - University of Applied Sciences Upper Austria
  - Co-founder of the HEAL research group
  - Project manager and chief architect of HeuristicLab
  - PhD in technical sciences (2009)
  - Johannes Kepler University Linz, Austria
  - Associate professor (2005 – 2009)
  - University of Applied Sciences Upper Austria
  - <http://heal.heuristiclab.com/team/wagner>



- Gabriel Kronberger
  - Full professor for business intelligence (since 2011)
  - University of Applied Sciences Upper Austria
  - Member of the HEAL research group
  - Architect of HeuristicLab
  - PhD in technical sciences (2010)
  - Johannes Kepler University Linz, Austria
  - Research assistant (2005 – 2011)
  - University of Applied Sciences Upper Austria
  - <http://heal.heuristiclab.com/team/kronberger>



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

2

## Objectives of the Tutorial



- Introduce general motivation and design principles of HeuristicLab
- Show where to get HeuristicLab
- Explain basic GUI usability concepts
- Demonstrate basic features
- Demonstrate editing and analysis of optimization experiments
- Demonstrate custom algorithms and graphical algorithm designer
- Demonstrate data-based modeling features
- Outline some additional features

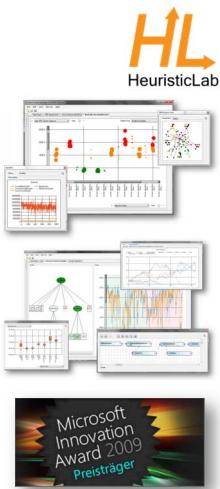
HeuristicLab Tutorial

<http://dev.heuristiclab.com>

4

## Introduction

- Motivation and Goals
  - graphical user interface
  - paradigm independence
  - multiple algorithms and problems
  - large scale experiments and analyses
  - parallelization
  - extensibility, flexibility and reusability
  - visual and interactive algorithm development
  - multiple layers of abstraction
- Facts
  - development of HeuristicLab started in 2002
  - based on Microsoft .NET and C#
  - used in research and education
  - second place at the *Microsoft Innovation Award 2009*
  - open source (GNU General Public License)
  - version 3.0 released on May 18th, 2010
  - latest version 3.3.6 released on January 3rd, 2012



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

5

## Where to get HeuristicLab?

- Download binaries
  - deployed as ZIP archives
  - latest stable version 3.3.6
    - released on January 3rd, 2012
  - daily trunk builds
  - <http://dev.heuristiclab.com/download>
- Check out sources
  - SVN repository
  - HeuristicLab 3.3.6 tag
    - <http://dev.heuristiclab.com/svn/hl/core/tags/3.3.6>
  - current development trunk
    - <http://dev.heuristiclab.com/svn/hl/core/trunk>
- License
  - GNU General Public License (Version 3)
- System requirements
  - Microsoft .NET Framework 4.0 Full Version
  - enough RAM and CPU power ;-)



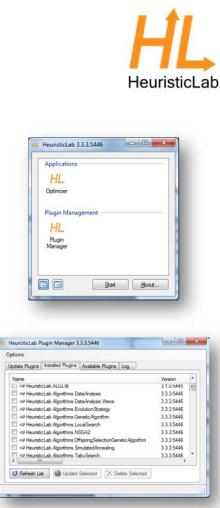
HeuristicLab Tutorial

<http://dev.heuristiclab.com>

6

## Plugin Infrastructure

- HeuristicLab consists of many assemblies
  - 94 plugins in HeuristicLab 3.3.6
  - plugins can be loaded or unloaded at runtime
  - plugins can be updated via internet
  - application plugins provide GUI frontends
- Extensibility
  - developing and deploying new plugins is easy
  - dependencies are explicitly defined, automatically checked and resolved
  - automatic discovery of interface implementations (service locator pattern)
- Plugin Manager
  - GUI to check, install, update or delete plugins

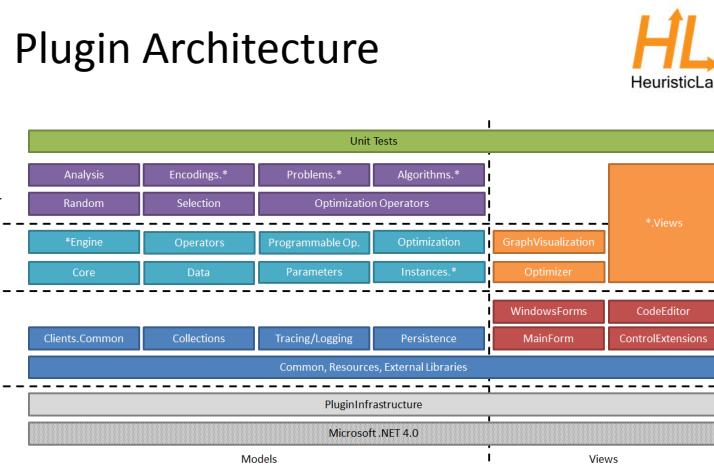


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

7

## Plugin Architecture



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

8

## Graphical User Interface



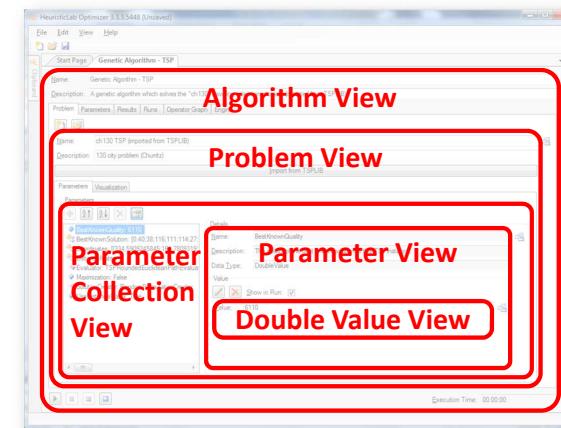
- HeuristicLab GUI is made up of views
  - views are visual representations of content objects
  - views are composed in the same way as their content
  - views and content objects are loosely coupled
  - multiple different views may exist for the same content
- Drag & Drop
  - views support drag & drop operations
  - content objects can be copied or moved (shift key)
  - enabled for collection items and content objects

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

9

## Graphical User Interface



HeuristicLab Tutorial

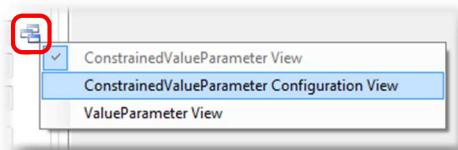
<http://dev.heuristiclab.com>

10

## Graphical User Interface



- ViewHost
  - control which hosts views
  - right-click on windows icon to switch views
  - double-click on windows icon to open another view
  - drag & drop windows icon to copy contents



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

11

## Available Algorithms & Problems



### Algorithms

- Evolution Strategy
- Genetic Algorithm
- Genetic Programming
- Island Genetic Algorithm
- Island Offspring Selection Genetic Algorithm
- Local Search
- NSGA-II
- Offspring Selection Genetic Algorithm
- Particle Swarm Optimization
- Robust Taboo Search
- SASEGASA
- Simulated Annealing
- Tabu Search
- User-defined Algorithm
- Variable Neighborhood Search
- Performance Benchmarks
- Cross Validation
- k-Means
- Linear Discriminant Analysis
- Linear Regression
- Multinomial Logit Classification
- Nearest Neighbor Regression and Classification
- Neural Network Regression and Classification
- Random Forest Regression and Classification
- Support Vector Regression and Classification

### Problems

- Artificial Ant
- Classification
- Clustering
- External Evaluation Problem
- Knapsack
- OneMax
- Quadratic Assignment
- Regression
- Single-Objective Test Function
- Symbolic Classification
- Symbolic Regression
- Traveling Salesman
- User-defined Problem
- Vehicle Routing

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

12

## Agenda

- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
- Demonstration Part I: Working with HeuristicLab
- Demonstration Part II: Data-based Modeling
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

13

## Demonstration Part I: Working with HeuristicLab

- Create, Parameterize and Execute Algorithms
- Save and Load Items
- Create Batch Runs and Experiments
- Multi-core CPUs and Parallelization
- Analyze Runs
- Analyzers
- Building User-Defined Algorithms

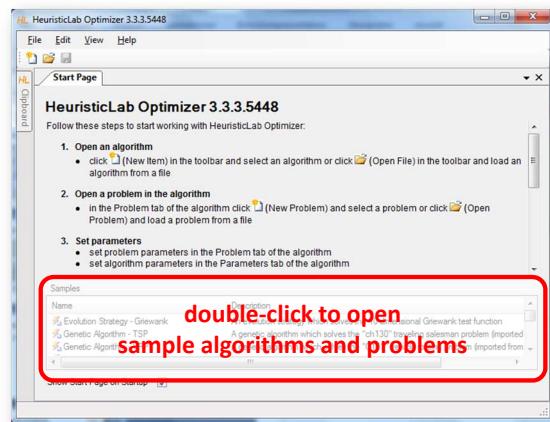


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

14

## HeuristicLab Optimizer

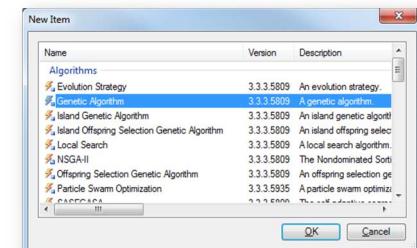
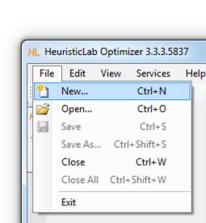


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

15

## Create Algorithm

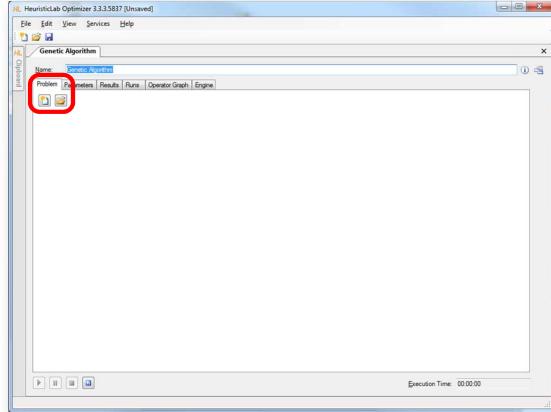


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

16

## Create or Load Problem

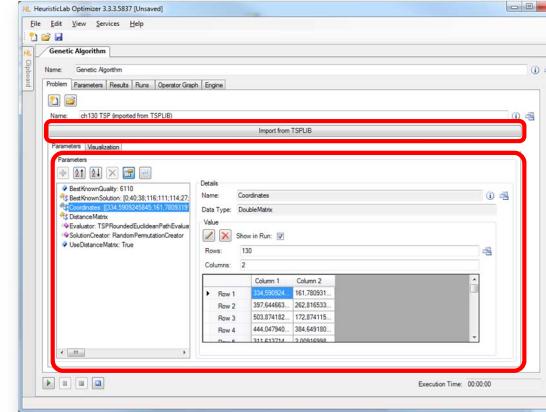


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

17

## Import or Parameterize Problem Data

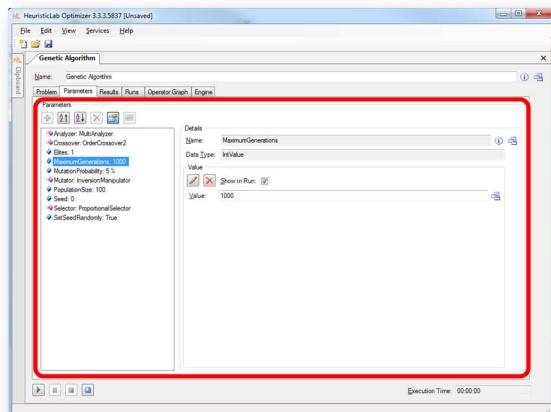


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

18

## Parameterize Algorithm

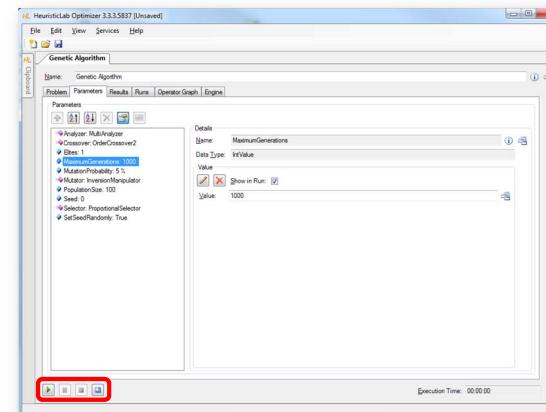


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

19

## Start, Pause, Resume, Stop and Reset

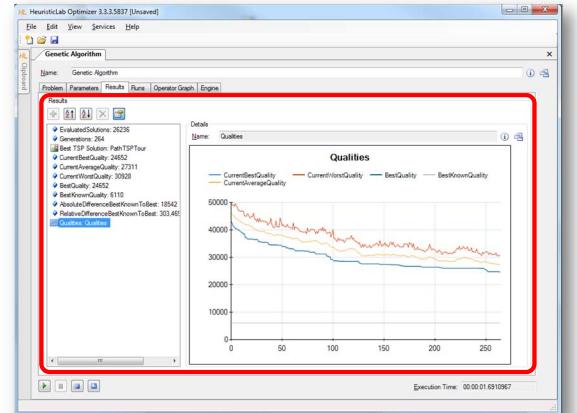


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

20

## Inspect Results



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

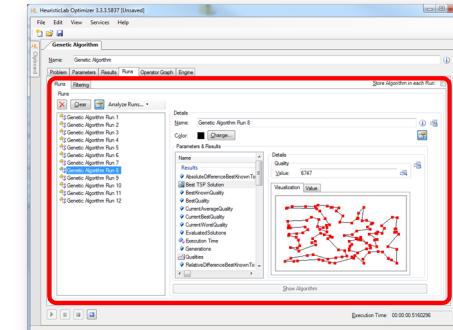


HeuristicLab

21

## Compare Runs

- A run is created each time when the algorithm is stopped
  - runs contain all results and parameter settings
  - previous results are not forgotten and can be compared



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

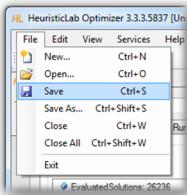


HeuristicLab

22

## Save and Load

- Save to and load from disk
  - HeuristicLab items (i.e., algorithms, problems, experiments, ...) can be saved to and loaded from a file
  - algorithms can be paused, saved, loaded and resumed
  - data format is custom compressed XML
  - saving and loading files might take several minutes
  - saving and loading large experiments requires some memory



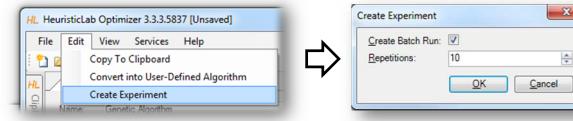
HeuristicLab Tutorial

<http://dev.heuristiclab.com>

23

## Create Batch Runs and Experiments

- Batch runs
  - execute the same optimizer (e.g. algorithm, batch run, experiment) several times
- Experiments
  - execute different optimizers
  - suitable for large scale algorithm comparison and analysis
- Experiments and batch runs can be nested
- Generated runs can be compared afterwards



HeuristicLab Tutorial

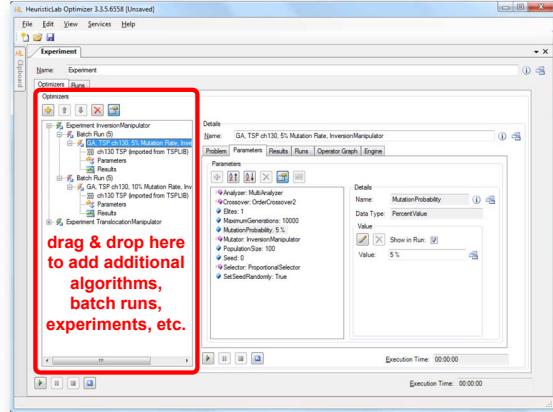
<http://dev.heuristiclab.com>



HeuristicLab

24

## Create Batch Runs and Experiments



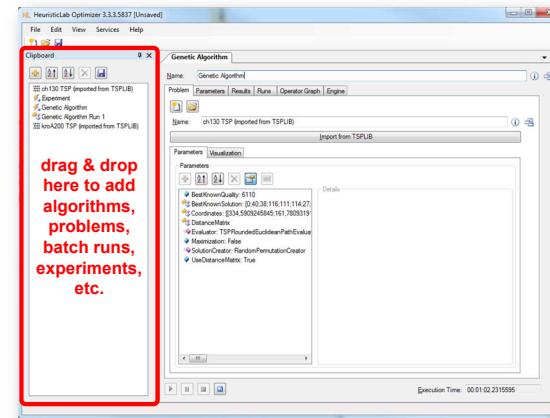
HeuristicLab Tutorial

<http://dev.heuristiclab.com>



25

## Clipboard



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

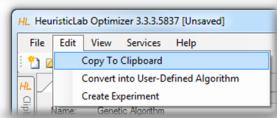


26

## Clipboard



- Store items
  - click on the buttons to add or remove items
  - drag & drop items on the clipboard
  - use the menu to add a copy of a shown item to the clipboard



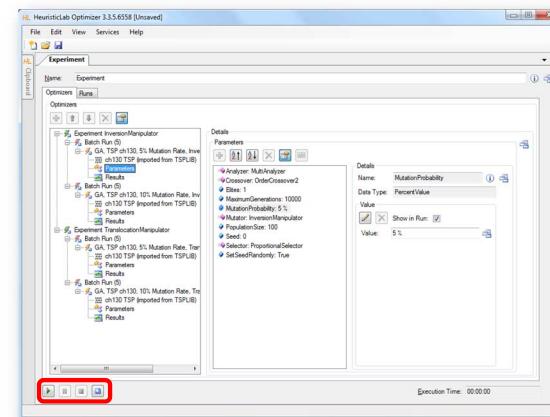
- Show items
  - double-click on an item in the clipboard to show its view
- Save and restore clipboard content
  - click on the save button to write the clipboard content to disk
  - clipboard is automatically restored when HeuristicLab is started the next time

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

27

## Start, Pause, Resume, Stop, Reset

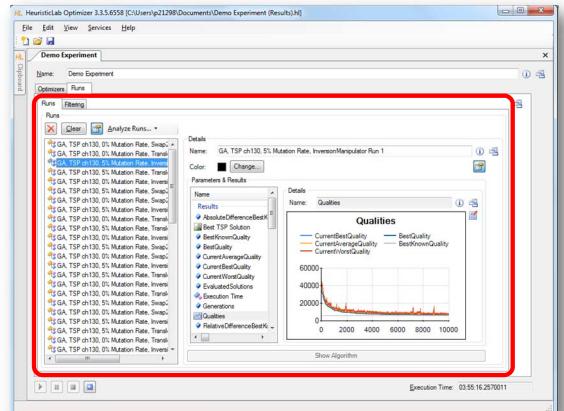


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

28

## Compare Runs



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

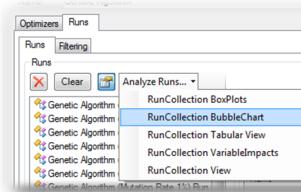
29

## Analyze Runs



HeuristicLab

- HeuristicLab provides interactive views to analyze and compare all runs of a run collection
  - textual analysis
    - RunCollection Tabular View
  - graphical analysis
    - RunCollection BubbleChart
    - RunCollection BoxPlots
- Filtering is automatically applied to all open run collection views



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

30

## RunCollection Tabular View

The screenshot shows the 'RunCollection Tabular View' dialog. The table has 48 rows and 6 columns. The columns are: BestKnownQuality, BestKnownSolution, BestQuality, Coordinates, Crossover, and CurrentAverageQuality. The table lists various runs of a Genetic Algorithm, each with a unique ID (Run 13 to Run 30) and specific numerical values for the other columns.

HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

31

## RunCollection Tabular View



HeuristicLab

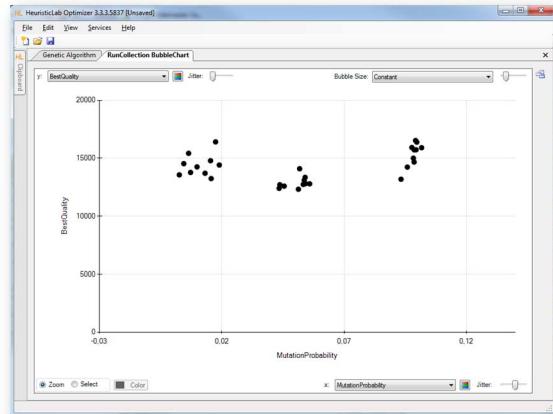
- Sort columns
  - click on column header to sort column
  - Ctrl-click on column header to sort multiple columns
- Show or hide columns
  - right-click on table to open dialog to show or hide columns
- Compute statistical values
  - select multiple numerical values to see count, sum, minimum, maximum, average and standard deviation
- Select, copy and paste into other applications

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

32

## RunCollection BubbleChart



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

33

## RunCollection BubbleChart



HeuristicLab

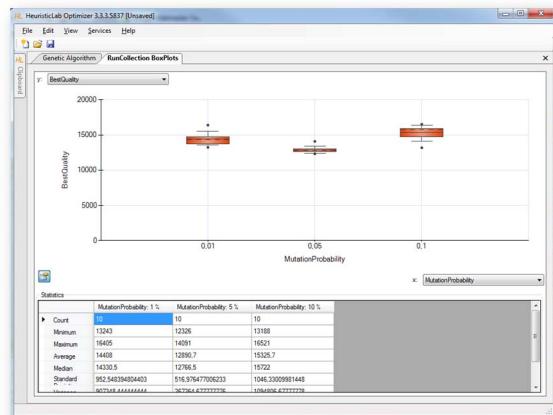
- Choose values to plot
  - choose which values to show on the x-axis, the y-axis and as bubble size
  - possible values are all parameter settings and results
- Add jitter
  - add jitter to separate overlapping bubbles
- Zoom in and out
  - click on Zoom and click and drag in the chart area to zoom in
  - double click on the chart area background or on the circle buttons beside the scroll bars to zoom out
- Color bubbles
  - click on Select, choose a color and click and drag in the chart area to select and color bubbles
  - applying automatically by clicking on the axis coloring buttons
- Show runs
  - double click on a bubble to open its run
- Export image
  - right-click to open context menu to copy or save image
  - save image as pixel (BMP, JPG, PNG, GIF, TIF) or vector graphics (EMF)
- Show box plots
  - right-click to open context menu to show box plots view

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

34

## RunCollection BoxPlots



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

35

## RunCollection BoxPlots



HeuristicLab

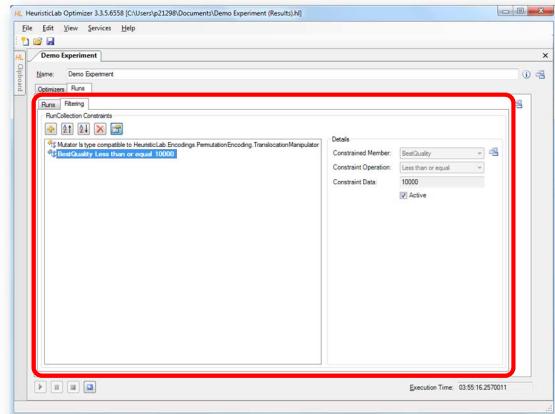
- Choose values to plot
  - choose which values to show on the x-axis and y-axis
  - possible values are all parameter settings and results
- Zoom in and out
  - click on Zoom and click and drag in the chart area to zoom in
  - double click on the chart area background or on the circle buttons beside the scroll bars to zoom out
- Show or hide statistical values
  - click on the lower left button to show or hide statistical values
- Export image
  - right-click to open context menu to copy or save image
  - save image as pixel (BMP, JPG, PNG, GIF, TIF) or vector graphics (EMF)

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

36

## Filter Runs



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

37

## Multi-core CPUs and Parallelization

- Parallel execution of optimizers in experiments
  - optimizers in an experiment are executed sequentially from top to bottom per default
  - experiments support parallel execution of their optimizers
  - select a not yet executed optimizer and start it manually to utilize another core
  - execution of one of the next optimizers is started automatically after an optimizer is finished
- Parallel execution of algorithms
  - HeuristicLab provides special operators for parallelization
  - engines decide how to execute parallel operations
  - sequential engine executes everything sequentially
  - parallel engine executes parallel operations on multiple cores
  - Hive engine (under development) executes parallel operations on multiple computers
  - all implemented algorithms support parallel solution evaluation

HeuristicLab Tutorial

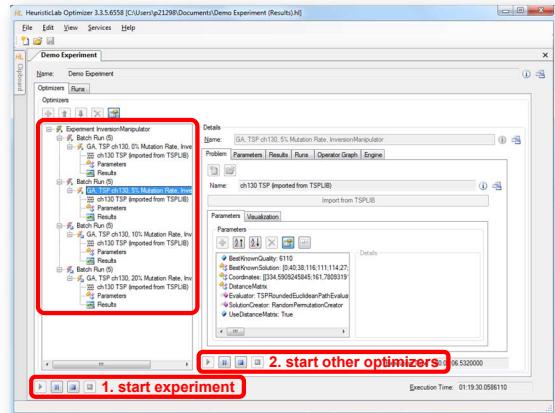
<http://dev.heuristiclab.com>



HeuristicLab

38

## Parallel Execution of Experiments



HeuristicLab Tutorial

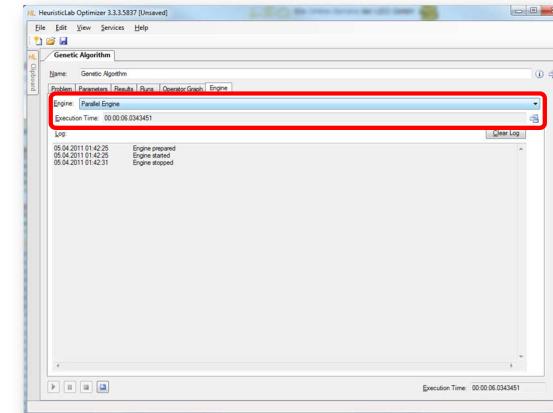
<http://dev.heuristiclab.com>



HeuristicLab

39

## Parallel Execution of Algorithms



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

40

## Analyzers



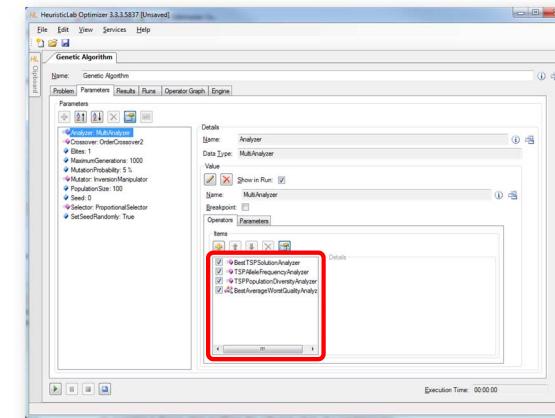
- Special operators for analysis purposes
  - are executed after each iteration
  - serve as general purpose extension points of algorithms
  - can be selected and parameterized in the algorithm
  - perform algorithm-specific and/or problem-specific tasks
  - some analyzers are quite costly regarding runtime and memory
  - implementing and adding custom analyzers is easy
- Examples
  - TSPAlleleFrequencyAnalyzer
  - TSPPopulationDiversityAnalyzer
  - SuccessfulOffspringAnalyzer
  - SymbolicDataAnalysisVariableFrequencyAnalyzer
  - SymbolicRegressionSingleObjectiveTrainingBestSolutionAnalyzer
  - ...

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

41

## Analyzers

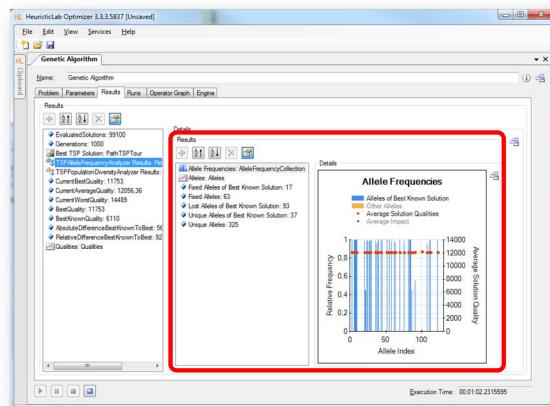


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

42

## TSPAlleleFrequencyAnalyzer

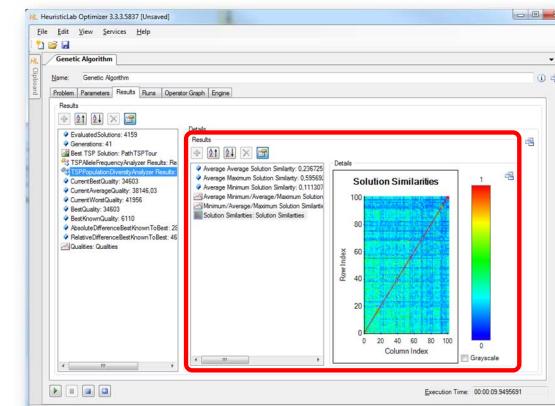


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

43

## TSPPopulationDiversityAnalyzer



HeuristicLab Tutorial

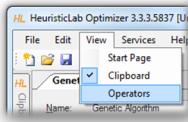
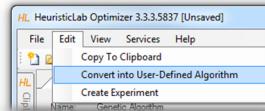
<http://dev.heuristiclab.com>

44

## Building User-Defined Algorithms



- Operator graphs
  - algorithms are represented as operator graphs
  - operator graphs of user-defined algorithms can be changed
  - algorithms can be defined in the graphical algorithm designer
  - use the menu to convert a standard algorithm into a user-defined algorithm



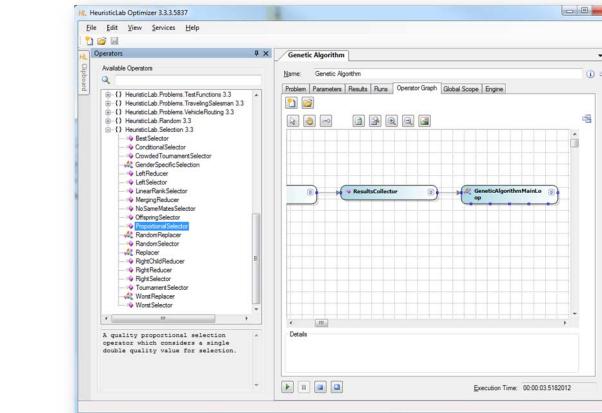
- Operators sidebar
  - drag & drop operators into an operator graph
- Programmable operators
  - add programmable operators in order to implement custom logic in an algorithm
  - no additional development environment needed
- Debug algorithms
  - use the debug engine to obtain detailed information during algorithm execution

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

45

## Building User-Defined Algorithms

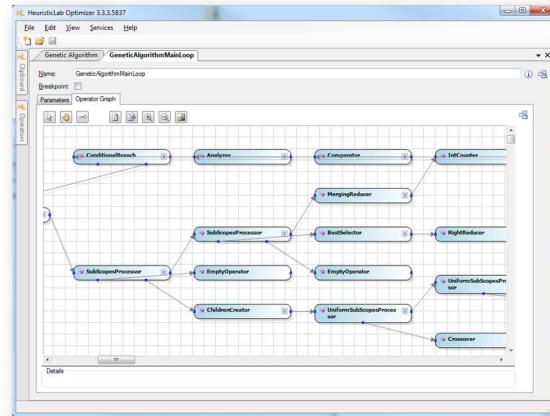


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

46

## Building User-Defined Algorithms



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

47

## Programmable Operators



```

public class ProgrammableSingleSuccessorOperator : IOperation
{
    public static IOperation Execute(ProgrammableSingleSuccessorOperator op,
        IExecutionContext context)
    {
        return op.Successor == null ? null : context.CreateOperation(op.Successor);
    }
}

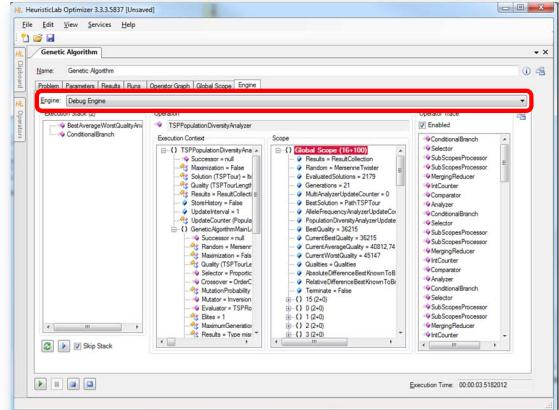
```

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

48

## Debugging Algorithms



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



49

## Agenda

- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
- Demonstration Part I: Working with HeuristicLab
- Demonstration Part II: Data-based Modeling
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

50

## Demonstration Part II: Data-based Modeling

- Introduction
- Regression with HeuristicLab
- Model simplification and export
- Variable relevance analysis
- Classification with HeuristicLab



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

51

## Introduction to Data-based Modeling

- Dataset: Matrix  $(x_{i,j})_{i=1..N, j=1..K}$ 
  - N observations of K input variables
  - $x_{i,j}$  = i-th observation of j-th variable
  - Additionally: Vector of labels  $(y_1 \dots y_N)^T$
- Goal: learn association of input variable values to labels
- Common tasks
  - Regression (real-valued labels)
  - Classification (discrete labels)
  - Clustering (no labels, group similar observations)



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

52

## Data-based Modeling Algorithms in HeuristicLab



- Symbolic regression and classification based on genetic programming
- External Libraries:
  - Support Vector Machines for Regression and Classification
  - Linear Regression
  - Linear Discriminate Analysis
  - K-Means clustering

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

53

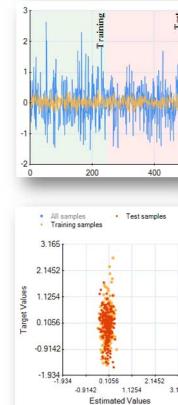
## Case Studies

- Demonstration
  - problem configuration
    - data import
    - target variable
    - input variables
    - data partitions (training and test)
  - analysis of results
    - accuracy metrics
    - visualization of model output



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



54

## Case Study: Regression



- Poly-10 benchmark problem dataset
  - 10 input variables  $x_1 \dots x_{10}$
  - $y = x_1 \cdot x_2 + x_3 \cdot x_4 + x_5 \cdot x_6 + x_1 \cdot x_7 \cdot x_9 + x_3 \cdot x_6 \cdot x_{10}$
  - non-linear modeling approach necessary
  - frequently used in GP literature
  - download <http://dev.heuristiclab.com/AdditionalMaterial#GECCO2012>

HeuristicLab Tutorial

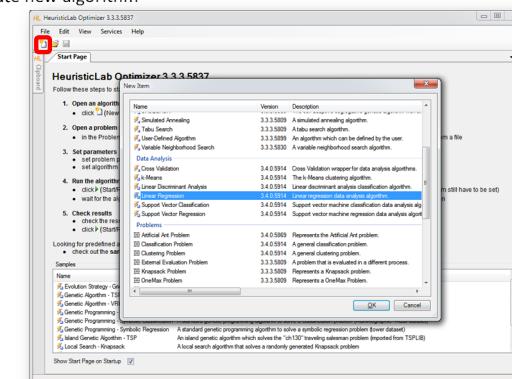
<http://dev.heuristiclab.com>

55

## Linear Regression



- Create new algorithm

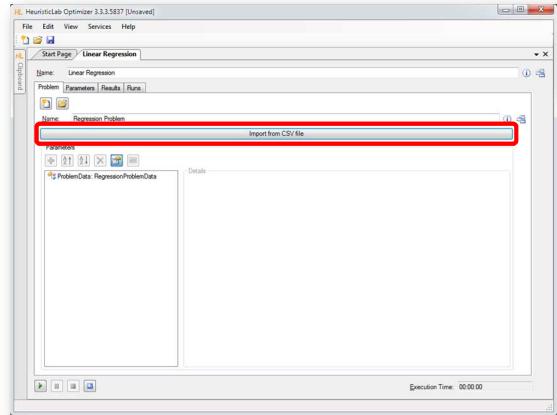


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

56

## Import Data from CSV-File

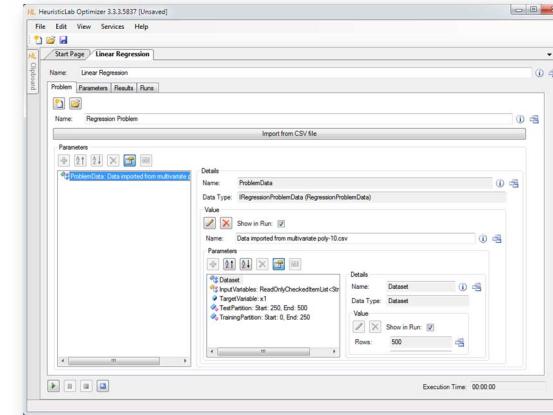


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

57

## Inspect and Configure Dataset

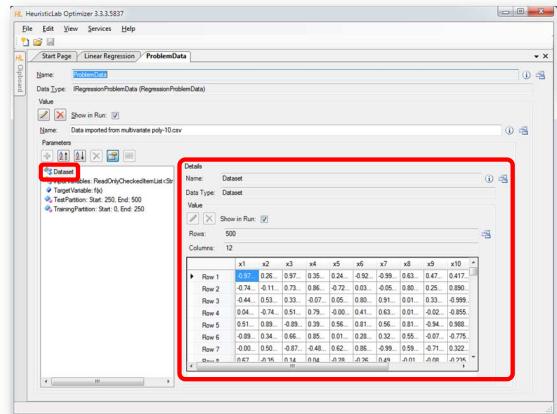


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

58

## Inspect Imported Data

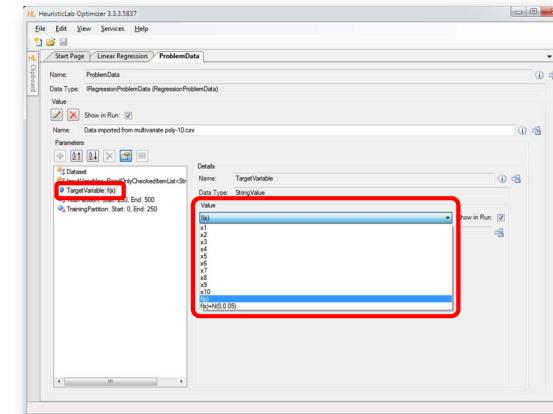


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

59

## Set Target Variable

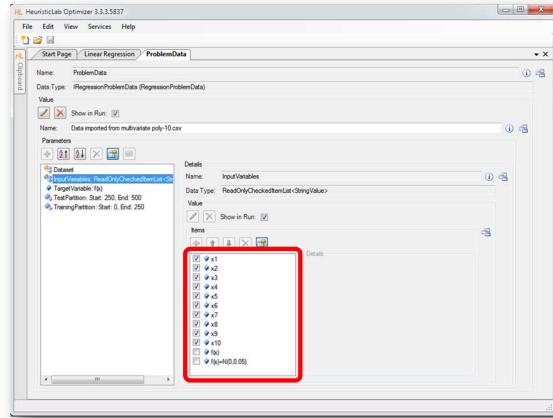


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

60

## Select Input Variables

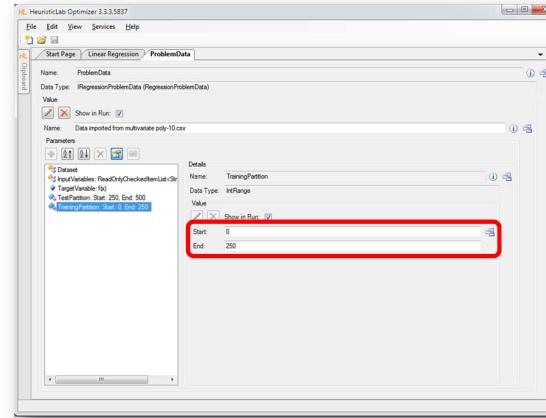


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

61

## Configure Training and Test Partitions

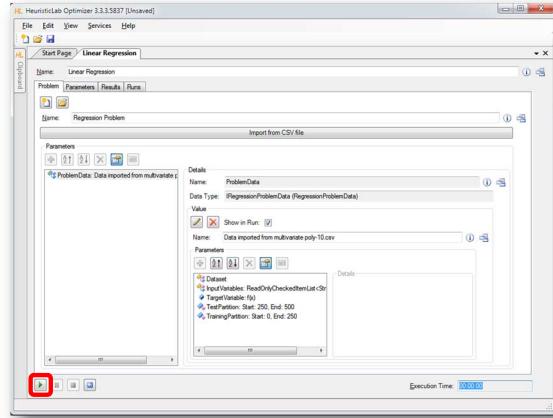


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

62

## Run Linear Regression

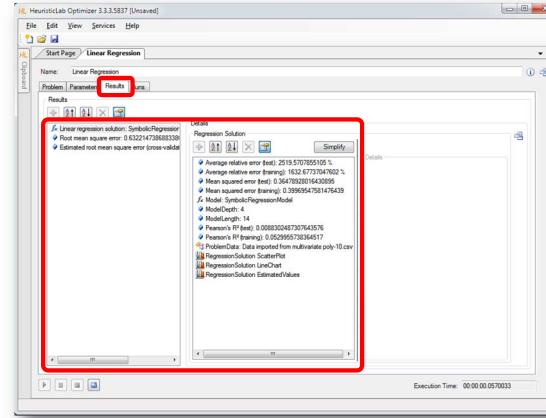


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

63

## Inspect Results

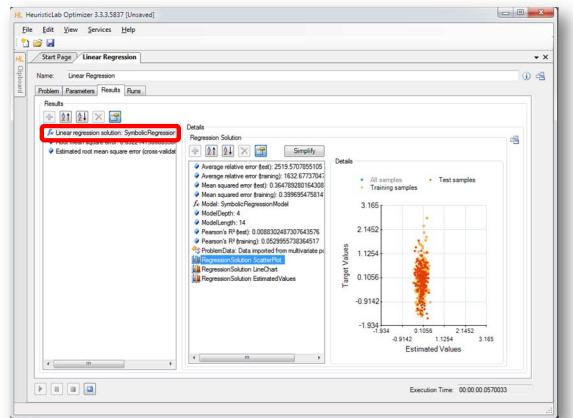


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

64

## Inspect Scatterplot of Predicted and Target Values



HeuristicLab Tutorial

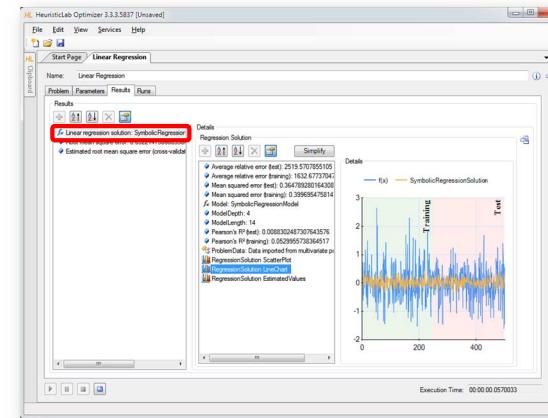
<http://dev.heuristiclab.com>



HeuristicLab

65

## Inspect Linechart



HeuristicLab Tutorial

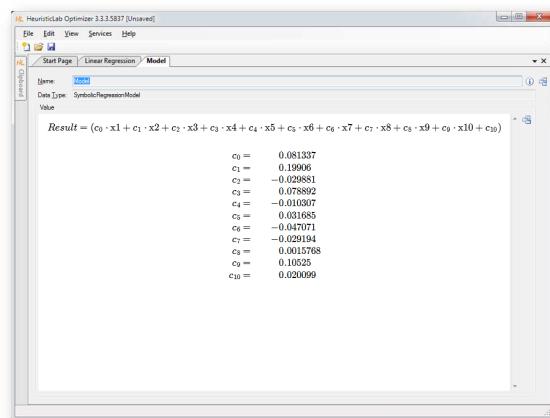
<http://dev.heuristiclab.com>



HeuristicLab

66

## Inspect the Model



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



HeuristicLab

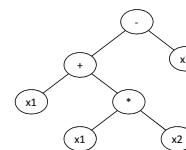
67

## Symbolic Regression with HeuristicLab



HeuristicLab

- Linear regression produced an inaccurate model.
- Next: produce a nonlinear symbolic regression model using genetic programming
- Genetic programming
  - evolve variable-length models
  - model representation: symbolic expression tree
  - structure and model parameters are evolved side-by-side
  - white-box models



HeuristicLab Tutorial

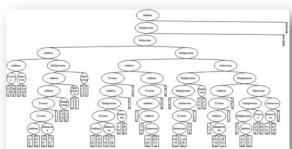
<http://dev.heuristiclab.com>

68

## Symbolic Regression with HeuristicLab



- Demonstration
  - problem configuration
  - function set and terminal set
  - model size constraints
  - Evaluation
- Algorithm configuration
  - selection
  - Mutation
- Analysis of results
  - model accuracy
  - model structure and parameters

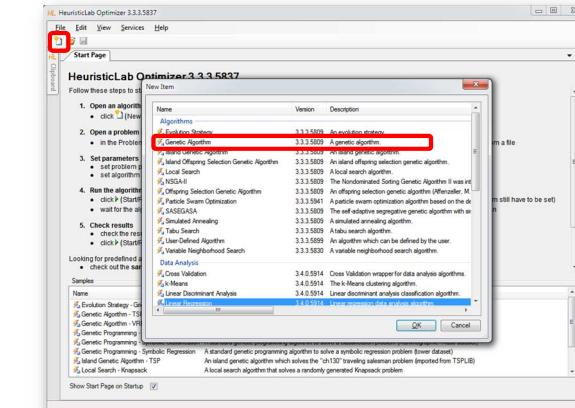


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

69

## Create New Genetic Algorithm

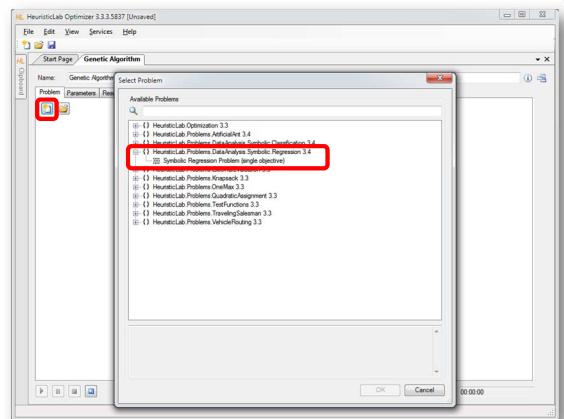


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

70

## Create New Symbolic Regression Problem

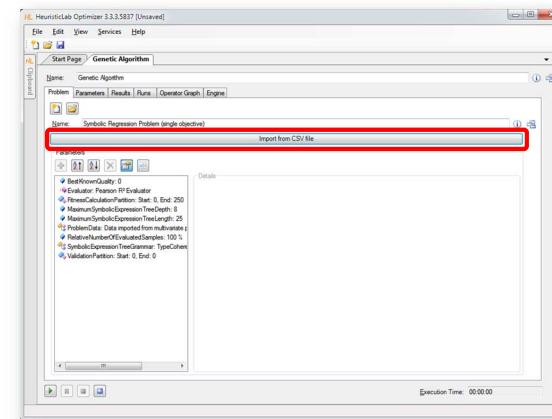


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

71

## Import Data

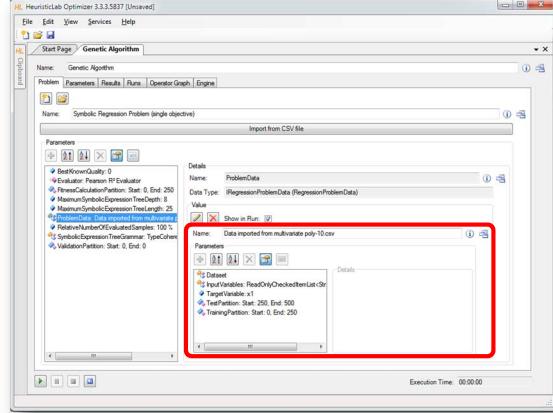


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

72

## Inspect Data and Configure Dataset



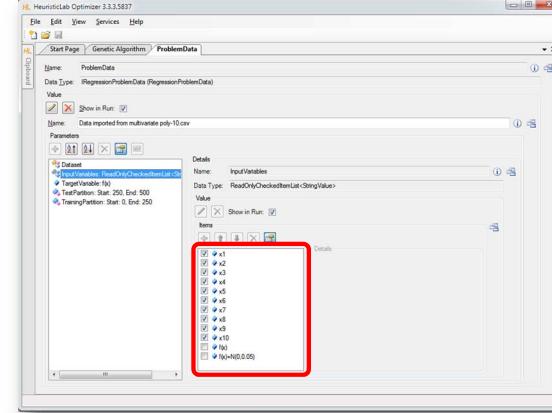
HeuristicLab Tutorial

<http://dev.heuristiclab.com>



73

## Set Target and Input Variables



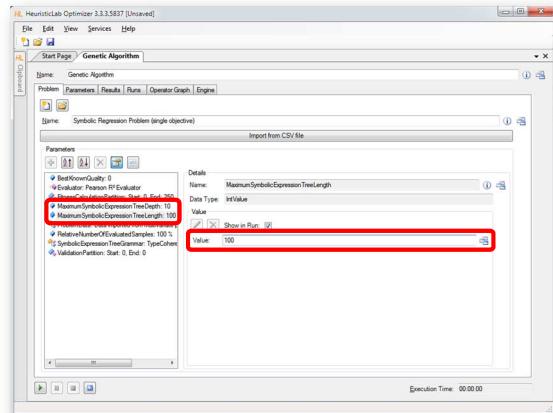
HeuristicLab Tutorial

<http://dev.heuristiclab.com>



74

## Configure Maximal Model Depth and Length



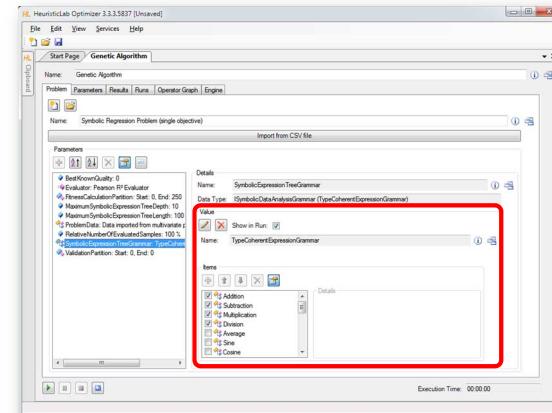
HeuristicLab Tutorial

<http://dev.heuristiclab.com>



75

## Configure Function Set (Grammar)



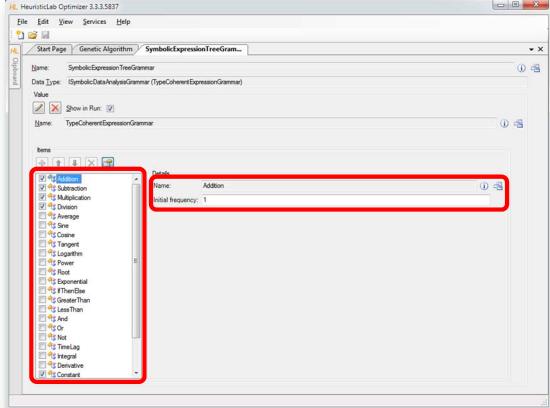
HeuristicLab Tutorial

<http://dev.heuristiclab.com>



76

## Configure Function Set (Grammar)



HeuristicLab Tutorial

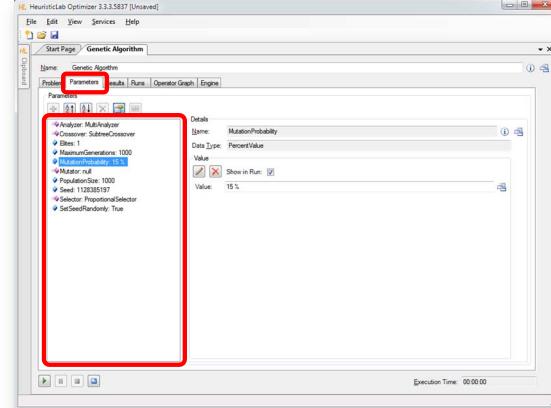
<http://dev.heuristiclab.com>



HeuristicLab

77

## Configure Algorithm Parameters



HeuristicLab Tutorial

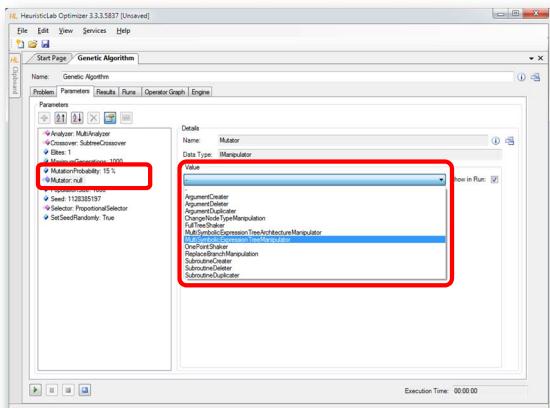
<http://dev.heuristiclab.com>



HeuristicLab

78

## Configure Mutation Operator



HeuristicLab Tutorial

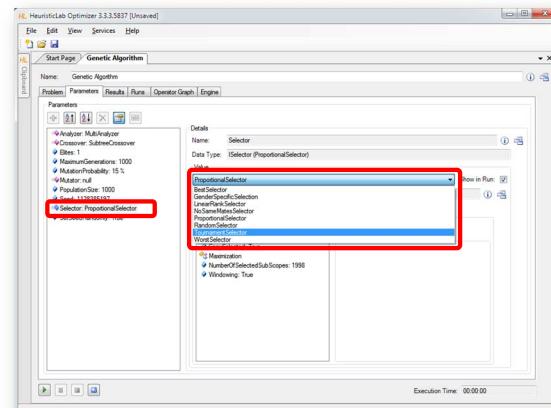
<http://dev.heuristiclab.com>



HeuristicLab

79

## Configure Selection Operator



HeuristicLab Tutorial

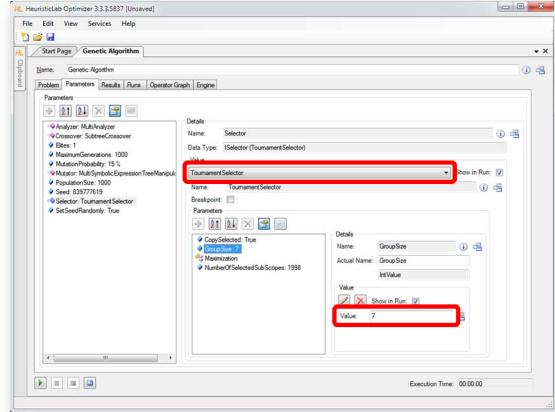
<http://dev.heuristiclab.com>



HeuristicLab

80

## Configure Tournament Group Size



HeuristicLab Tutorial

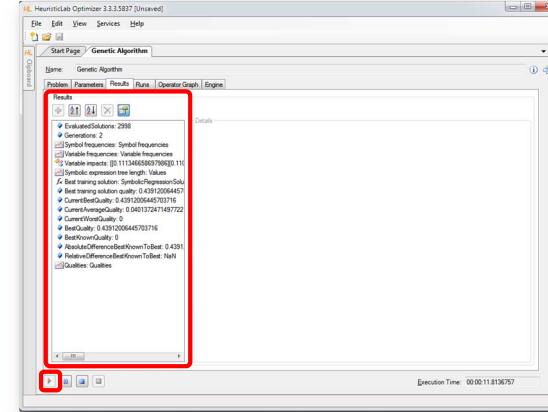
<http://dev.heuristiclab.com>



HeuristicLab

81

## Start Algorithm and Inspect Results



HeuristicLab Tutorial

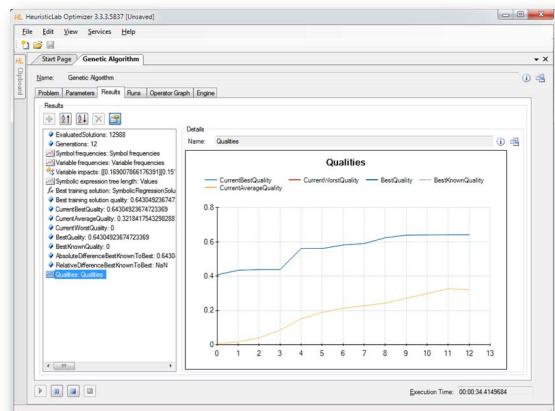
<http://dev.heuristiclab.com>



HeuristicLab

82

## Inspect Quality Chart



HeuristicLab Tutorial

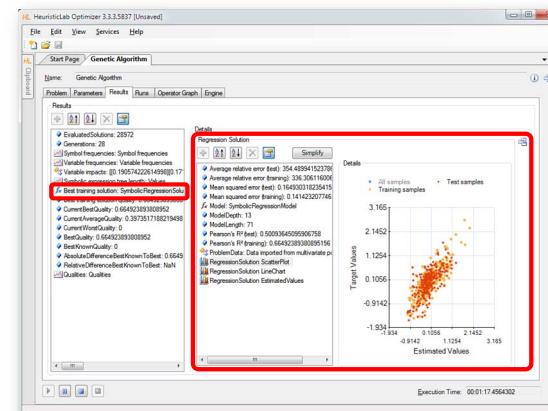
<http://dev.heuristiclab.com>



HeuristicLab

83

## Inspect Best Model on Training Partition



HeuristicLab Tutorial

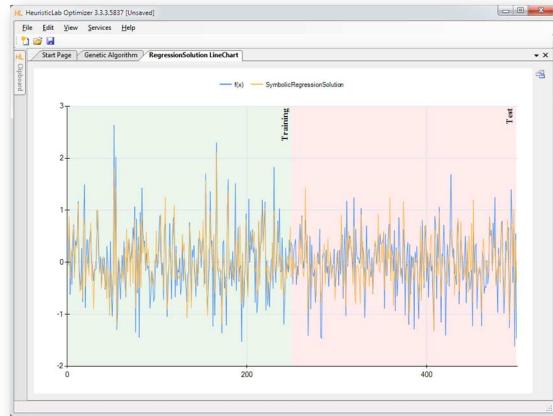
<http://dev.heuristiclab.com>



HeuristicLab

84

## Inspect Linechart of Best Model on Training Partition

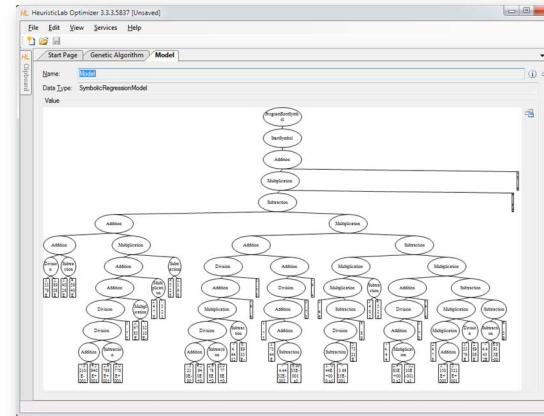


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

85

## Inspect Structure of Best Model on Training Partition



HeuristicLab Tutorial

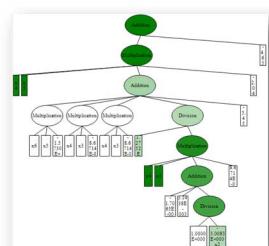
<http://dev.heuristiclab.com>

86

## Model Simplification and Export



- Demonstration
  - automatic simplification
  - visualization of node impacts
  - manual simplification
    - online update of results
  - model export
    - MATLAB
    - LaTeX



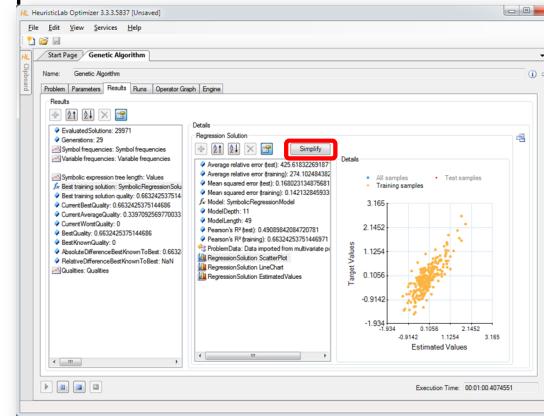
$$\text{Result} = x_0(t) \cdot x_3(t) \cdot c_{20} \cdot \left( x_6(t) \cdot x_5(t) \cdot c_4 + x_4(t) \cdot x_3(t) \cdot c_7 + x_4(t) \cdot x_3(t) \cdot c_{10} + \frac{c_{11}x_2(t)}{x_4(t) \cdot x_3(t) \cdot (c_{14}x_4(t) + c_{15}x_5(t) + \frac{1}{c_{16}x_2(t)})} + c_{21} \right)$$

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

87

## Detailed Model Analysis and Simplification

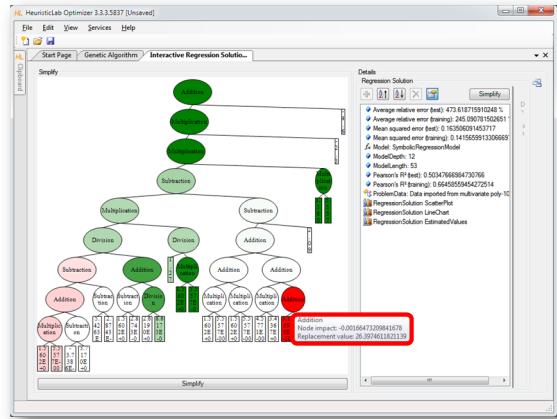


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

88

## Symbolic Simplification and Node Impacts

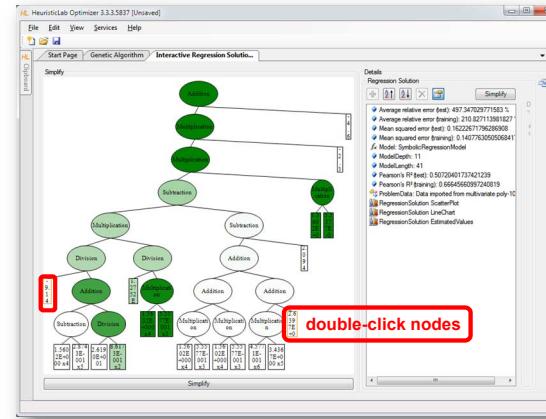


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

89

## Manual Simplification

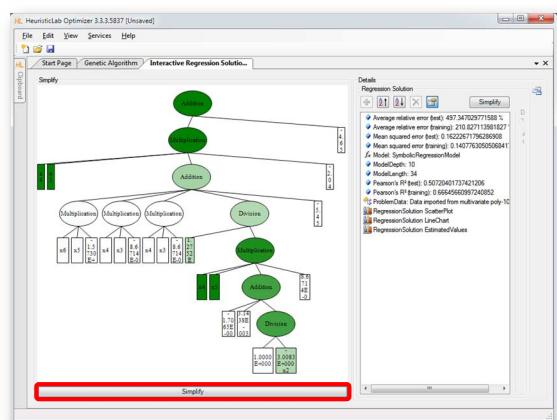


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

90

## Automatic Symbolic Simplification



HeuristicLab Tutorial

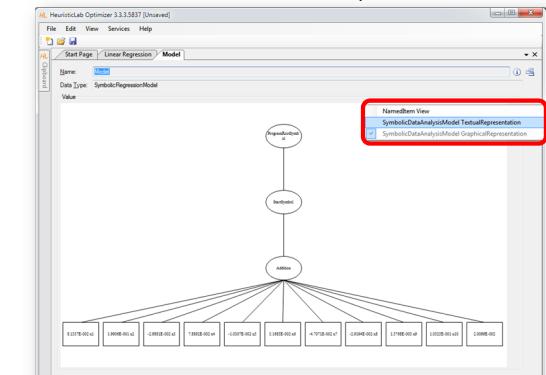
<http://dev.heuristiclab.com>

91

## Textual Representations Are Also Available



- Use ViewHost to switch to textual representation view.



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

92

## Default Textual Representation for Model Export



```
HeuristicLab Optimizer 3.3.3.5837 [Unsaved]
File Edit View Services Help
HL Start Page | Linear Regression > Model
Name: Model
Data Type: SymbolicRegressionModel
Value:
Formatter: Default String Formatter
(PolynomialSymbol
(StartSymbol
Addition
(B.1137E-002*x)
(1.0000E+000*x)
(-2.9881E-002*x)
(7.0000E-001*x)
(-1.0007E-002*x)
(0.0000E+000*x)
(-4.7016E-002*x)
(2.0000E+000*x)
(1.9765E-003*x)
(1.0000E+000*x)
(2.0099E-002*x)
)
)
```

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

93

## Textual Representation for Export to LaTeX



```
HeuristicLab Optimizer 3.3.3.5837 [Unsaved]
File Edit View Services Help
HL Start Page | Linear Regression > Model
Name: Model
Data Type: SymbolicRegressionModel
Value:
Formatter: LaTeX String Compiler
\needs{upackage{amsmath}}
\begin{aligned}
&\text{Result} = (c_1 x_{11}) + c_1 x_{21} (t) + c_1 x_{31} (t) + c_1 x_{41} (t) + c_1 x_{51} (t) + c_1 x_{61} (t) + c_1 x_{71} (t) + c_1 x_{81} (t) + c_1 x_{91} (t) + c_1 x_{101} (t) + c_1 x_{111} (t) \\
&+ c_2 x_{12} + 0.0113722424739 \cdot x_{12}^2 + c_3 x_{13} + c_4 x_{14} + c_5 x_{15} + c_6 x_{16} + c_7 x_{17} + c_8 x_{18} + c_9 x_{19} + c_{10} \cdot \log(t) \\
&+ c_{11} x_{22} + c_{12} x_{23} + c_{13} x_{24} + c_{14} x_{25} + c_{15} x_{26} + c_{16} x_{27} + c_{17} x_{28} + c_{18} x_{29} + c_{19} x_{30} + c_{20} \cdot \log(t) \\
&+ c_{21} x_{31} + c_{22} x_{32} + c_{23} x_{33} + c_{24} x_{34} + c_{25} x_{35} + c_{26} x_{36} + c_{27} x_{37} + c_{28} x_{38} + c_{29} x_{39} + c_{30} \cdot \log(t) \\
&+ c_{31} x_{41} + c_{32} x_{42} + c_{33} x_{43} + c_{34} x_{44} + c_{35} x_{45} + c_{36} x_{46} + c_{37} x_{47} + c_{38} x_{48} + c_{39} x_{49} + c_{40} \cdot \log(t) \\
&+ c_{41} x_{51} + c_{42} x_{52} + c_{43} x_{53} + c_{44} x_{54} + c_{45} x_{55} + c_{46} x_{56} + c_{47} x_{57} + c_{48} x_{58} + c_{49} x_{59} + c_{50} \cdot \log(t) \\
&+ c_{51} x_{61} + c_{52} x_{62} + c_{53} x_{63} + c_{54} x_{64} + c_{55} x_{65} + c_{56} x_{66} + c_{57} x_{67} + c_{58} x_{68} + c_{59} x_{69} + c_{60} \cdot \log(t) \\
&+ c_{61} x_{71} + c_{62} x_{72} + c_{63} x_{73} + c_{64} x_{74} + c_{65} x_{75} + c_{66} x_{76} + c_{67} x_{77} + c_{68} x_{78} + c_{69} x_{79} + c_{70} \cdot \log(t) \\
&+ c_{71} x_{81} + c_{72} x_{82} + c_{73} x_{83} + c_{74} x_{84} + c_{75} x_{85} + c_{76} x_{86} + c_{77} x_{87} + c_{78} x_{88} + c_{79} x_{89} + c_{80} \cdot \log(t) \\
&+ c_{81} x_{91} + c_{82} x_{92} + c_{83} x_{93} + c_{84} x_{94} + c_{85} x_{95} + c_{86} x_{96} + c_{87} x_{97} + c_{88} x_{98} + c_{89} x_{99} + c_{90} \cdot \log(t) \\
&+ c_{91} x_{101} + c_{92} x_{102} + c_{93} x_{103} + c_{94} x_{104} + c_{95} x_{105} + c_{96} x_{106} + c_{97} x_{107} + c_{98} x_{108} + c_{99} x_{109} + c_{100} \cdot \log(t)
\end{aligned}
```

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

94

## LaTeX Export



```
HeuristicLab Optimizer 3.3.3.5837 [Unsaved]
File Edit View Services Help
HL Start Page | Genetic Algorithm > Interactive Regression Solution > Model
Name: Model
Data Type: SymbolicRegressionModel
Value:
Formatter: LaTeX String Formatter
\needs{upackage{amsmath}}
\begin{aligned}
\text{Result} &= (c_1 x_{11}) + c_1 x_{21} (t) + c_1 x_{31} (t) + c_1 x_{41} (t) + c_1 x_{51} (t) + c_1 x_{61} (t) + c_1 x_{71} (t) + c_1 x_{81} (t) + c_1 x_{91} (t) + c_1 x_{101} (t) \\
&+ c_2 x_{12} + 0.014411481469 \cdot x_{12}^2 + c_3 x_{13} + c_4 x_{14} + c_5 x_{15} + c_6 x_{16} + c_7 x_{17} + c_8 x_{18} + c_9 x_{19} + c_{10} \cdot \log(t) \\
&+ c_{11} x_{22} + c_{12} x_{23} + c_{13} x_{24} + c_{14} x_{25} + c_{15} x_{26} + c_{16} x_{27} + c_{17} x_{28} + c_{18} x_{29} + c_{19} x_{30} + c_{20} \cdot \log(t) \\
&+ c_{21} x_{31} + c_{22} x_{32} + c_{23} x_{33} + c_{24} x_{34} + c_{25} x_{35} + c_{26} x_{36} + c_{27} x_{37} + c_{28} x_{38} + c_{29} x_{39} + c_{30} \cdot \log(t) \\
&+ c_{31} x_{41} + c_{32} x_{42} + c_{33} x_{43} + c_{34} x_{44} + c_{35} x_{45} + c_{36} x_{46} + c_{37} x_{47} + c_{38} x_{48} + c_{39} x_{49} + c_{40} \cdot \log(t) \\
&+ c_{41} x_{51} + c_{42} x_{52} + c_{43} x_{53} + c_{44} x_{54} + c_{45} x_{55} + c_{46} x_{56} + c_{47} x_{57} + c_{48} x_{58} + c_{49} x_{59} + c_{50} \cdot \log(t) \\
&+ c_{51} x_{61} + c_{52} x_{62} + c_{53} x_{63} + c_{54} x_{64} + c_{55} x_{65} + c_{56} x_{66} + c_{57} x_{67} + c_{58} x_{68} + c_{59} x_{69} + c_{60} \cdot \log(t) \\
&+ c_{61} x_{71} + c_{62} x_{72} + c_{63} x_{73} + c_{64} x_{74} + c_{65} x_{75} + c_{66} x_{76} + c_{67} x_{77} + c_{68} x_{78} + c_{69} x_{79} + c_{70} \cdot \log(t) \\
&+ c_{71} x_{81} + c_{72} x_{82} + c_{73} x_{83} + c_{74} x_{84} + c_{75} x_{85} + c_{76} x_{86} + c_{77} x_{87} + c_{78} x_{88} + c_{79} x_{89} + c_{80} \cdot \log(t) \\
&+ c_{81} x_{91} + c_{82} x_{92} + c_{83} x_{93} + c_{84} x_{94} + c_{85} x_{95} + c_{86} x_{96} + c_{87} x_{97} + c_{88} x_{98} + c_{89} x_{99} + c_{90} \cdot \log(t) \\
&+ c_{91} x_{101} + c_{92} x_{102} + c_{93} x_{103} + c_{94} x_{104} + c_{95} x_{105} + c_{96} x_{106} + c_{97} x_{107} + c_{98} x_{108} + c_{99} x_{109} + c_{100} \cdot \log(t)
\end{aligned}
```

HeuristicLab Tutorial

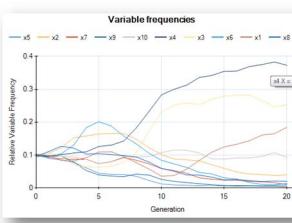
<http://dev.heuristiclab.com>

95

## Variable Relevance Analysis



- Which variables are important to predict classes correctly?
- Demonstration
  - Variable frequency analyzer
  - symbol frequency analyzer
  - variable impacts



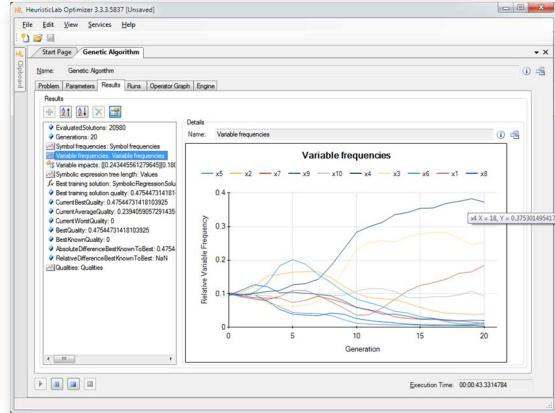
HeuristicLab Tutorial

<http://dev.heuristiclab.com>

	Relative variable relevance
x4	0.302803859106054
x3	0.241170172985569
x1	0.179112369714678
x10	0.0589664719249172
x2	0.054455184742382
x6	0.0446774403657897
x8	0.0436011597048278
x7	0.0331173502974243
x5	0.0226252246461621
x9	0.01946242278034

96

## Inspect Variable Frequency Chart

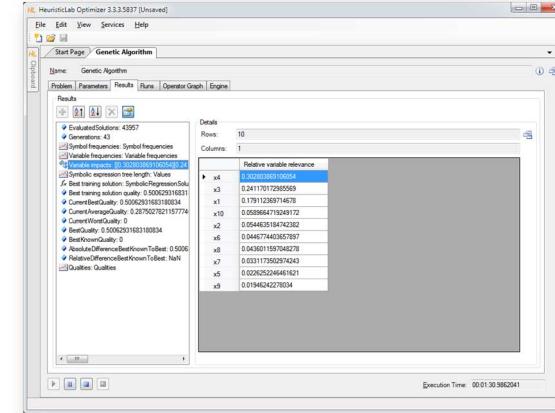


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

97

## Inspect Variable Impacts

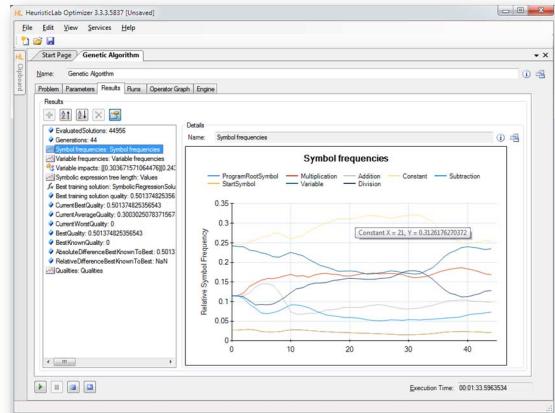


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

98

## Inspect Symbol Frequencies



HeuristicLab Tutorial

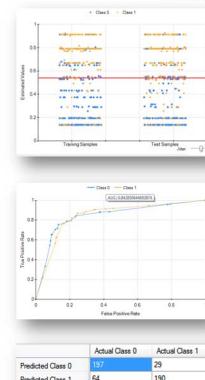
<http://dev.heuristiclab.com>

99

## Classification with HeuristicLab



- Symbolic classification
  - evolve discriminating function using GP
  - find thresholds to assign classes
- Demonstration
  - real world medical application
  - model accuracy
  - visualization of model output
    - discriminating function output
    - ROC-curve
    - confusion matrix



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

100

## Case Study: Classification



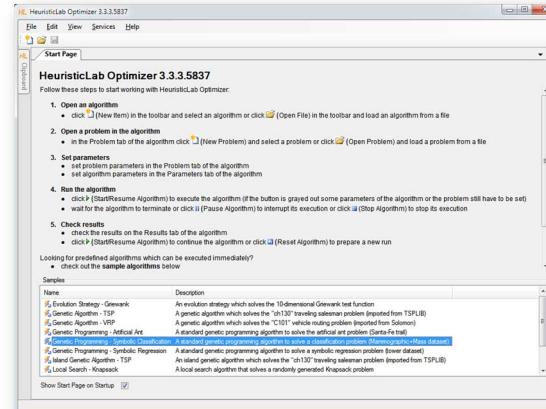
- Real world medical dataset (*Mammographic Mass*) from UCI Machine Learning Repository
  - data from non-invasive mammography screening
  - variables:
    - patient age
    - visual features of inspected mass lesions: shape, margin, density
  - target variable: severity (malignant, benign)
- download  
<http://dev.heuristiclab.com/AdditionalMaterial#GECCO2012>

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

101

## Open Sample

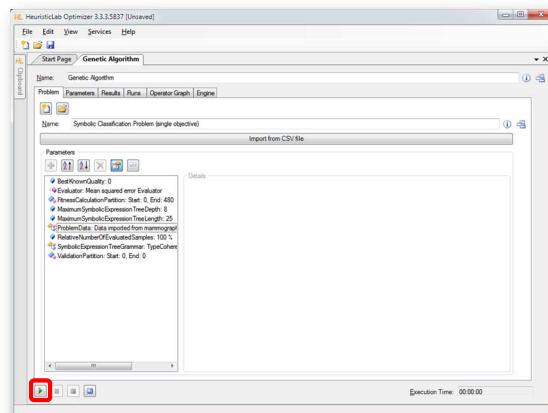


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

102

## Configure and Run Algorithm

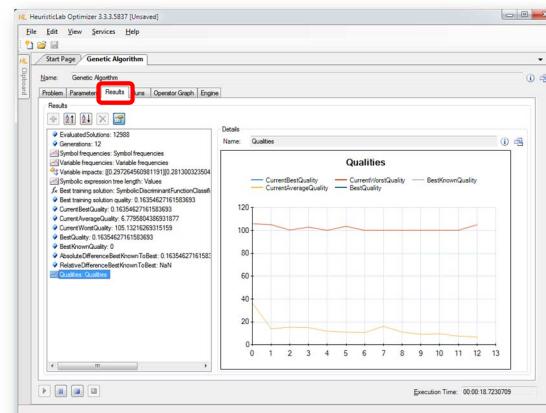


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

103

## Inspect Quality Linechart

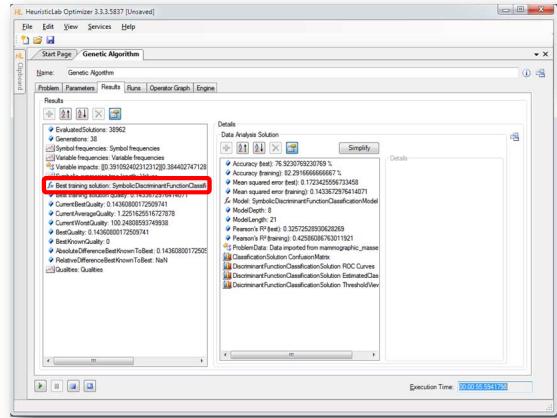


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

104

## Inspect Best Training Solution

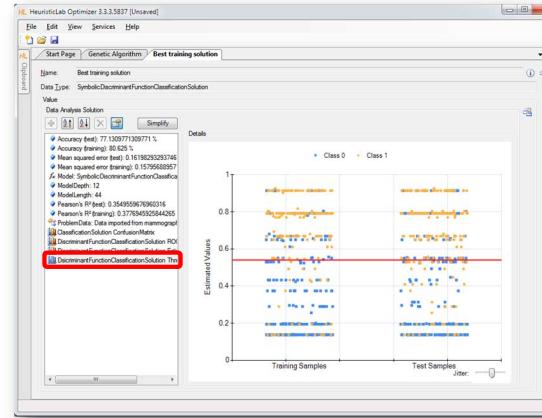


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

105

## Inspect Model Output and Thresholds

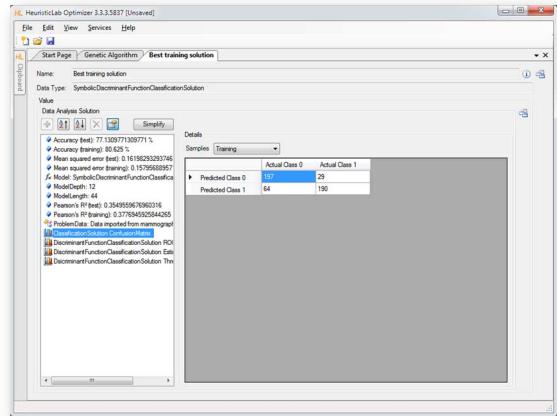


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

106

## Inspect Confusion Matrix

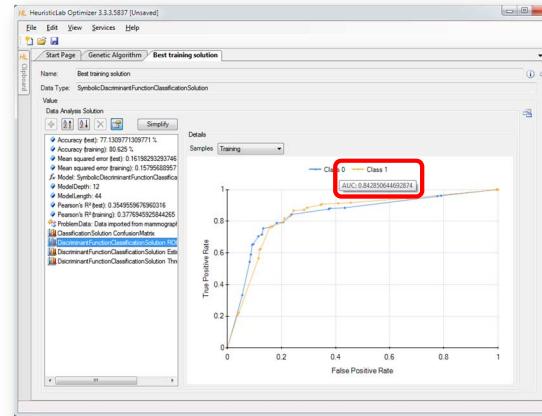


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

107

## Inspect ROC Curve



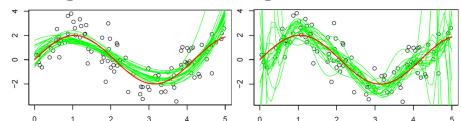
HeuristicLab Tutorial

<http://dev.heuristiclab.com>

108

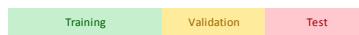
## Validation of Results

- Overfitting = memorizing data

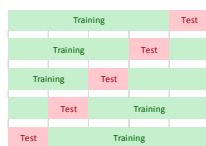


- Strategies to reduce overfitting

– validation partition



– cross-validation



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

109

## Validation of Results

- Demonstration

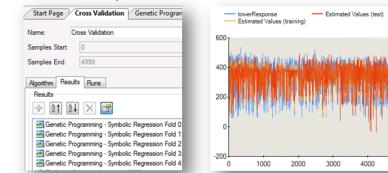
– Configuration of a validation set

– Inspection of best solution on validation set

– Analysis of training- and validation fitness correlation

- Cross-validation

- Configuration
- Analysis of results



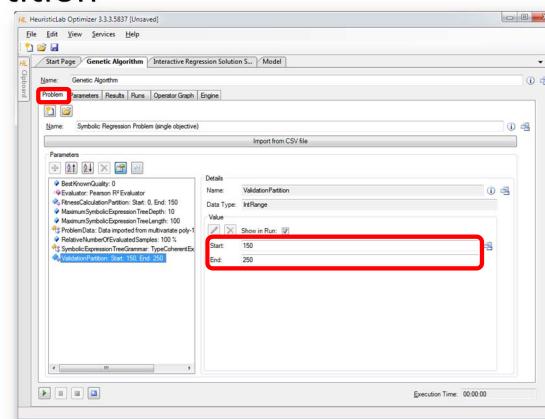
HeuristicLab Tutorial

<http://dev.heuristiclab.com>



110

## Configuration of Validation Partition

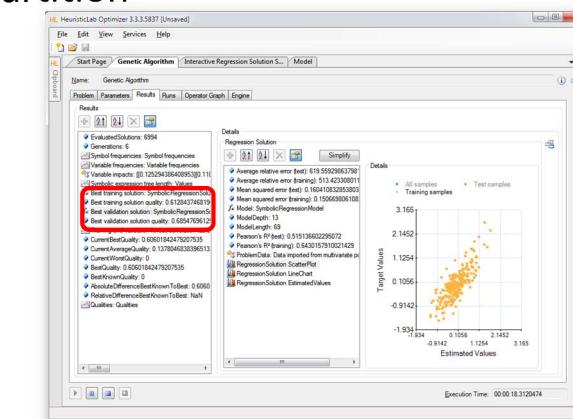


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

111

## Inspect Best Model on Validation Partition

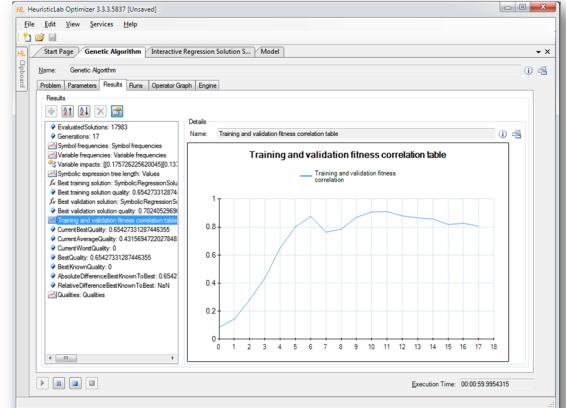


HeuristicLab Tutorial

<http://dev.heuristiclab.com>

112

## Inspect Linechart of Correlation of Training and Validation Fitness



HeuristicLab Tutorial

<http://dev.heuristiclab.com>



113

## Agenda

- Objectives of the Tutorial
- Introduction
- Where to get HeuristicLab?
- Plugin Infrastructure
- Graphical User Interface
- Available Algorithms & Problems
- **Demonstration Part I: Working with HeuristicLab**
- **Demonstration Part II: Data-based Modeling**
- Some Additional Features
- Planned Features
- Team
- Suggested Readings
- Bibliography
- Questions & Answers



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

114

## Some Additional Features

- HeuristicLab Hive
  - parallel and distributed execution of algorithms and experiments on many computers in a network
- Optimization Knowledge Base (OKB)
  - database to store algorithms, problems, parameters and results
  - open to the public
  - open for other frameworks
  - analyze and store characteristics of problem instances and problem classes
- External solution evaluation and simulation-based optimization
  - interface to couple HeuristicLab with other applications (MATLAB, AnyLogic, ...)
  - supports different protocols (command line parameters, TCP, ...)
- Parameter grid tests and meta-optimization
  - automatically create experiments to test large ranges of parameters
  - apply heuristic optimization algorithms to find optimal parameter settings for heuristic optimization algorithms



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

115

## Planned Features

- Algorithms & Problems
  - steady-state genetic algorithm
  - unified tabu search for vehicle routing
  - scatter search
  - ...
- Cloud Computing
  - port HeuristicLab Hive to Windows Azure
- Linux
  - port HeuristicLab to run on Mono and Linux machines
- Have a look at the HeuristicLab roadmap
  - <http://dev.heuristiclab.com/trac/hl/core/roadmap>
- Any other ideas, requests or recommendations?
  - join our HeuristicLab Google group [heuristiclab@googlegroups.com](mailto:heuristiclab@googlegroups.com) or
  - write an e-mail to [support@heuristiclab.com](mailto:support@heuristiclab.com)



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

116

## HeuristicLab Team



Heuristic and Evolutionary Algorithms Laboratory (HEAL)  
School of Informatics, Communications and Media  
University of Applied Sciences Upper Austria

Softwarepark 11  
A-4232 Hagenberg  
AUSTRIA

WWW: <http://heal.heuristiclab.com>



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

117

## Suggested Readings

- S. Voß, D. Woodruff (Edts.)  
**Optimization Software Class Libraries**  
Kluwer Academic Publishers, 2002



- M. Affenzeller, S. Winkler, S. Wagner, A. Beham  
**Genetic Algorithms and Genetic Programming  
Modern Concepts and Practical Applications**  
CRC Press, 2009



HeuristicLab Tutorial

<http://dev.heuristiclab.com>

118

## Bibliography



- S. Wagner, M. Affenzeller  
HeuristicLab: A generic and extensible optimization environment  
Adaptive and Natural Computing Algorithms, pp. 538-541  
Springer, 2005
- S. Wagner, S. Winkler, R. Braune, G. Kronberger, A. Beham, M. Affenzeller  
Benefits of plugin-based heuristic optimization software systems  
Computer Aided Systems Theory - EUROCAST 2007, Lecture Notes in Computer Science, vol. 4739, pp. 747-754  
Springer, 2007
- S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
Modeling of heuristic optimization algorithms  
Proceedings of the 20th European Modeling and Simulation Symposium, pp. 106-111  
DIPTEM University of Genova, 2008
- S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
Model driven rapid prototyping of heuristic optimization algorithms  
Computer Aided Systems Theory - EUROCAST 2009, Lecture Notes in Computer Science, vol. 5717, pp. 729-736  
Springer, 2009
- S. Wagner  
Heuristic optimization software systems - Modeling of heuristic optimization algorithms in the HeuristicLab software environment  
Ph.D. thesis, Johannes Kepler University Linz, Austria, 2009.
- S. Wagner, A. Beham, G. Kronberger, M. Kommeda, E. Pitzer, M. Kofler, S. Vonolfen, S. Winkler, V. Dorfer, M. Affenzeller  
HeuristicLab 3.3: A unified approach to metaheuristic optimization  
Actas del séptimo congreso español sobre Metaheurísticas, Algoritmos Evolutivos y Bioinspirados (MAEB'2010), 2010
- Detailed list of all publications of the HEAL research group: <http://research.fh-ooe.at/de/orgunit/detail/356#showpublications>

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

119

## Questions & Answers



<http://dev.heuristiclab.com>

[heuristiclab@googlegroups.com](mailto:heuristiclab@googlegroups.com)

HeuristicLab Tutorial

<http://dev.heuristiclab.com>

120