

## Mid-Term Quiz

2 October 2013

**Time allowed:** 1 hour 45 minutes

**Matriculation No:**

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### Instructions (please read carefully):

1. Write down your matriculation number on the **question paper**. **DO NOT WRITE YOUR NAME ON THE QUESTION SET!**
2. This is **an open-sheet quiz**. You are allowed to bring one A4 sheet of notes (written on both sides).
3. This paper comprises **FOUR (4) questions** and **SIXTEEN (16) pages**. The time allowed for solving this quiz is **1 hour 45 minutes**.
4. The maximum score of this quiz is **100 marks**. The weight of each question is given in square brackets beside the question number.
5. All questions must be answered correctly for the maximum score to be attained.
6. All questions must be answered in the space provided in the answer sheet; no extra sheets will be accepted as answers.
7. The back-sides of the sheets and the pages marked “scratch paper” in the question set may be used as scratch paper.
8. You are allowed to un-staple the sheets while you solve the questions. Please make sure you staple them back in the right order at the end of the quiz.
9. You are allowed to use pencils, ball-pens or fountain pens, as you like (no red color, please).

## GOOD LUCK!

Question	Marks	Remark
Q1		
Q2		
Q3		
Q4		
<b>Total</b>		

**Question 1: Python Expressions [25 marks]**

There are several parts to this problem. Answer each part **independently and separately**. In each part, one or more Python expressions are entered into the interpreter (Python shell). Determine the response printed by the interpreter for the final expression entered. If the interpreter produces an error message, or enters an infinite loop, explain why.

**A.** `x = 0`  
`y = 5`  
`z = 4`  
`if x < y:`  
    `print(z)`  
`else:`  
    `print(y/x*z)`

[5 marks]

**B.** `x = 1`  
`y = 2`  
`def f(x):`  
    `if x <= y:`  
        `return x`  
    `else:`  
        `return good-grief`  
`print(f(2))`

[4 marks]

**C.**

```
count = 1
for i in range(10):
    if i == 0:
        continue
    elif i == 5:
        break
    else:
        count = count + 1
print(count)
```

[4 marks]

**D.**

```
a = 0
b = 10
while a < b:
    a = a + 1
    b = b - 1
print(a)
```

[4 marks]

**E.** `x = 4`  
`def f(y):`  
    `return g(x,y+x)`  
`def g(y,x):`  
    `return x`  
`print(f(x))`

[4 marks]

**F.** `def f(x,y):`  
    `return y(x(y(x(y))))`  
`def g(x):`  
    `return 5`  
`def h(x):`  
    `return x`  
`print(f(g,h))`

[4 marks]

**Question 2: Fibonacci Revisited [25 marks]**

The Fibonacci sequence is named after Leonardo Fibonacci. His 1202 book *Liber Abaci* introduced the sequence to Western European mathematics, although the sequence had been described earlier in Indian mathematics.

In mathematical terms, the sequence  $F_n$  of Fibonacci numbers is defined by the following recurrence relation:

$$F_n = F_{n-1} + F_{n-2}$$

with seed values:

$$F_0 = 0$$

$$F_1 = 1$$

**A. [Warm Up]** Write an iterative function `fib(n)` that returns the  $n$ th Fibonacci number. [6 marks]

**B.** What is the order of growth in terms of time and space for the function you wrote in Part (a) in terms of  $n$ . [4 marks]

Time:

Space:

**C.** Consider the the sequence  $G_n$  defined by the following recurrence relation:

$$G_n = G_{n-1}^2 + G_{n-2}^2$$

with seed values:

$$G_0 = 0$$

$$G_1 = 1$$

Write a function `fib_square(n)` that returns  $G_n$ .

[6 marks]

**D.** What is the order of growth in terms of time and space for the function you wrote in Part (c) in terms of  $n$ . [2 marks]

Time:

Space:

**E.** Consider the the sequence  $H_n$  defined by the following recurrence relation:

$$H_n = H_{n-1}^k + H_{n-2}^k$$

with seed values:

$$H_0 = a$$

$$H_1 = b$$

Write a function `create_fib(k, a, b)` that returns  $H_n$  for a specified value of  $k$ . In other words, suppose:

```
fib = create_fib(1, 0, 1)
```

```
fib_square = create_fib(2, 0, 1)
```

then, `fib` and `fib_square` would be equivalent to the functions that you wrote in Parts (a) and (c) respectively above. [7 marks]

### Question 3: Higher Order Functions [22 marks]

Consider the following higher-order function that we call `flutter`:

```
def flutter(f, op, n):
    result = f(0)
    for i in range(n):
        result = op(f(i), result)
    return result
```

**A.** Write down the expression corresponding to the expression that `flutter` computes. You can use  $\oplus$  to represent `op` in your expression. [4 marks]

**B.** Suppose the function `sum_integers(n)` computes the sum of integers from 1 to  $n$  (inclusive) and `sum_integers(n)` is defined as follows:

```
def sum_integers(n):
    return flutter(<T1>,
                  <T2>,
                  <T3>)
```

Please provide possible implementations for the terms `T1`, `T2`, and `T3`. [6 marks]

`T1`:  
[2 marks]

`T2`:  
[2 marks]

`T3`:  
[2 marks]



**C.** Suppose the function `product_integers(n)` computes the product of integers from 1 to  $n$  (inclusive) and `product_integers(n)` is defined as follows:

```
def product_integers(n):
    return flutter(<T4>,
                  <T5>,
                  <T6>)
```

Please provide possible implementations for the terms T4, T5, and T6.

[6 marks]

T4:  
[2 marks]

T5:  
[2 marks]

T6:  
[2 marks]

**D. [Pyramid Sum]** We define the pyramid sum  $P_n$  as follows:

$$P_1 = 1 \quad (1)$$

$$P_2 = 1 + 2 + 1 \quad (2)$$

$$P_3 = 1 + 2 + 3 + 2 + 1 \quad (3)$$

$$\vdots = \vdots \quad (4)$$

$$P_n = 1 + \cdots + n - 1 + n + n - 1 + \cdots + 1 \quad (5)$$

Suppose we define `pyramid_sum(n)` in terms of `flutter` as follows:

```
def pyramid_sum(n):
    def pyramid(x):
        <T7>
    def op(a,b):
        <T8>
    return flutter(pyramid,
                  op,
                  n+1)
```

Please provide possible implementations for the terms T7 and T8.

[6 marks]

T7:  
[3 marks]

T8:  
[3 marks]

**Question 4: Rabbits!! [28 marks]**

In this question, you will learn how to model rabbits.

**A. [Warm Up]** Write function `create_rabbit(gender, father, mother)` that will take 3 arguments, the gender of a rabbit as well as the parents of a rabbit respectively and return a new *rabbit* object. [3 marks]

**B.** Write the following accessors: `get_gender`, `get_father` and `get_mother` for the rabbit object that you defined in Part (a) above. [6 marks]

**C.** Assume that there are only two valid inputs for gender: "Male" and "Female" (strings). Write a function `mate(rabbit1, rabbit2)` that will take as arguments two rabbit objects. `mate` will return a new rabbit object if and only if `rabbit1` and `rabbit2` are of different gender, or `None` otherwise. Also, if `mate` does return a new rabbit, the rabbit has a 50% chance of being either male or female. **Hint:** The `random()` function will return a random value between 0 and 1. [6 marks]

**D.** Write a function `is_parent(a,b)` that will return `True` if `b` is a parent of `a`, where both `a` and `b` are rabbit objects, or `False` otherwise. [4 marks]

**E.** Write a function `is_sibling(a,b)` that will return `True` if `a` and `b` are siblings, i.e. they share at least one parent, where both `a` and `b` are rabbit objects, or `False` otherwise. [4 marks]

**F.** Write a function `get_grandparents(a)` that will return a tuple containing **all** the grandparents of a rabbit object `a`. Note also that there **should not** be any duplicates in the returned tuple. [5 marks]

## Appendix

The following are some functions that were introduced in class. For your reference, they are reproduced here.

```
def sum(term, a, next, b):
    if (a>b):
        return 0
    else:
        return term(a) + sum(term, next(a), next, b)

def fold(op, f, n):
    if n==0:
        return f(0)
    else:
        return op(f(n), fold(op, f, n-1))

def enumerate_interval(low, high):
    return tuple(range(low,high+1))

def filter(pred, seq):
    if seq == ():
        return ()
    elif pred(seq[0]):
        return (seq[0],) + filter(pred, seq[1:])
    else:
        return filter(pred, seq[1:])

def accumulate(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(seq[0], accumulate(fn, initial, seq[1:]))
```

Scratch Paper

— END OF PAPER —