CS1010S — Programming Methodology School of Computing National University of Singapore

Mid-Term Test

30 September 2015			1	Time a	llowe	d: 1 ho	our 45	minutes
Matriculation No:								

Instructions (please read carefully):

- Write down your matriculation number on the question paper. DO NOT WRITE YOUR NAME ON THE QUESTION SET!
- 2. This is **an open-sheet test**. You are allowed to bring one A4 sheet of notes (written on both sides).
- 3. This paper comprises **FOUR (4) questions** and **EIGHTEEN (18) pages**. The time allowed for solving this test is **1 hour 45 minutes**.
- 4. The maximum score of this test is **100 marks**. The weight of each question is given in square brackets beside the question number.
- 5. All questions must be answered correctly for the maximum score to be attained.
- 6. All questions must be answered in the space provided in the answer sheet; no extra sheets will be accepted as answers.
- 7. The back-sides of the sheets and the pages marked "scratch paper" in the question set may be used as scratch paper.
- 8. You are allowed to un-staple the sheets while you solve the questions. Please make sure you staple them back in the right order at the end of the test.
- 9. You are allowed to use pencils, ball-pens or fountain pens, as you like (no red color, please).

GOOD LUCK!

Question	Marks	Remark
Q1		
Q2		
Q3		
Q4		
Total		

Question 1: Python Expressions [30 marks]

There are several parts to this problem. Answer each part independently and separately. In each part, one or more Python expressions are entered into the interpreter (Python shell). Determine the response printed by the interpreter for the final expression entered. If the interpreter produces an error message, or enters an infinite loop, explain why. Partial marks will be awarded for workings if the final answer is wrong.

```
A. y = 10

x = 2

def f(x):

x = 13 * x

y = 12

return x + y

print(f(y) + x)
```

```
C. def foo(x, y):
                                                                        [5 marks]
        return x + y
   def bar(x):
        return x + x
   print(foo((1, 2), bar((bar(3), (4,)))))
D. x = 10
                                                                        [5 marks]
   y = 20
   if x > y:
       print("Good")
   elif x < y:
       print("Bad")
   if x <= y:</pre>
       print("Maybe")
```

```
\mathbf{E}_{\bullet} def boo(x):
                                                                                   [5 marks]
         return lambda y: x(x(y))
    print(boo(boo)(lambda x:x+1)(5))
\mathbf{F}_{\bullet} s = "How_are_you?"
                                                                                   [5 marks]
   x = 0
   while len(s) > x:
        x = x + 1
        if x % 2 == 0:
             continue
        s = s[x:]
   print(s)
```

Question 2: Digital Sums [24 marks]

The digit sum of an non-negative integer is simply the sum of all its digits. For example, the digit sum of 65536 is 6+5+5+3+6=25.

A. [Warm-up] Write a function digit_sum which takes in a non-negative integer n and returns the digit sum of n. [4 marks]

<pre>def digit_sum(n):</pre>	
B. What is the order of growth in terms of time and space for the function (A) in terms of n . Explain your answer.	you wrote in Part
<i>Hint</i> : The number of digits of an integer n is $\lfloor \log_{10} n \rfloor + 1$	[4 marks]
Time:	
Space:	

C. A digital root or also known as a repeated digital sum, of a non-negative integer is the single digit value obtained by repeatedly summing the digits, using the result from the previous iteration to compute the digit sum. This process continues until a single-digit number is reached	18	
For example, the digital root of 65536 is 7. Because $6+5+5+3+6=25$ and then $2+5=7$.		
Write a <u>recursive</u> function $digital_root$ which takes in a non-negative integer n and return the digital root of n .	ıs	
You may if you wish, reuse the function you defined in part A. [4 marks	s]	
<pre>def digital_root(n):</pre>		
D. What is the order of growth in terms of time and space for the function you wrote in Pa (C) in terms of n . Briefly explain your answer.	rt	
Remember to account for the function you defined in part A if you had used it. [4 marks	s]	
Time:		
Space:		

\mathbf{E}_{\bullet} Write an <u>iterative</u> function digital_root which takes in a non-negative integer n and returns the digital root of n .		
You may if you wish, reuse the function you defined in part A.	[4 marks]	
<pre>def digital_root(n):</pre>		
\mathbf{F} . What is the order of growth in terms of time and space for the function you wrote in terms of n . Briefly explain your answer.	e in Part (E)	
Remember to account for the function you defined in part A if you had used it.	[4 marks]	
Time:		
Space:		
брасс.		

Question 3: Higher-Order Function [24 marks]

Consider the following higher-order function that we call tail:

```
def tail(f, n, a, b, c):
    if a > b:
        return c
    else:
        return tail(f, n, n(a), b, f(a, c))
```

A. Suppose the function $sum_integers(n)$ computes the sum of integers from 1 to n (inclusive) and $sum_integers(n)$ is defined as follows:

Please provide possible implementations for the terms T1, T2, T3, T4 and T5. You may also optionally define other helper functions in <PRE> if needed. [6 marks]

optional <pre>:</pre>	
<t1>:</t1>	
<t2>:</t2>	
<t3>:</t3>	
<t4>:</t4>	
<t5>:</t5>	

B. Suppose the function $sum_even_integers(n)$ computes the sum of even integers from 1 to n (inclusive) and $sum_even_integers(n)$ is defined as follows:

Please provide possible implementations for the terms T6, T7, T8, T9 and T10. You may also optionally define other helper functions in <PRE> if needed. [6 marks]

*optional <pre>:</pre>	
<t6>:</t6>	
<t7>:</t7>	
<t8>:</t8>	
<t9>:</t9>	
<t10>:</t10>	

C. We can also express the sum function presented in lecture (reproduced in the Appendix) in terms of tail as follows:

Please provide possible implementations for the terms T11, T12, T13, T14 and T15. You may also optionally define other helper functions in <PRE> if needed. [6 marks]

*optional <pre>:</pre>	
<t11>:</t11>	
<t12>:</t12>	
<t13>:</t13>	
<t14>:</t14>	
<t15>:</t15>	

D. [Warning: HARD!] We can also express digit_sum (described in part A) in terms of tail as follows:

Without using the digit_sum function, provide a possible implementation for the terms T16, T17, T18, T19 and T20. You may also optionally define other helper functions in <PRE> if needed.

Hint: It might be useful to define a function that returns the i^{th} digit of a number. [6 marks]

		_
*optional <pre>:</pre>		
<t16>:</t16>		
<t17>:</t17>		
<t18>:</t18>		
<t19>:</t19>		
<t20>:</t20>		

Question 4: Ballot Boxes [22 marks]

Warning: Please read the entire question clearly before you attempt this problem!!

For the upcoming elections, the Elections Committee has decided to use an electronic voting system. You task is to model the ballot boxes which are used to store the ballots, or votes. In addition, each ballot box also identifies the names of the contesting candidates.

A ballot box is created with the function create_empty_box which takes as input a tuple of candidates and returns an empty ballot box.

The function get_candidates takes as input a ballot box and returns a tuple of candidates contesting in the ballot box, and the function get_contents will return a tuple of the ballots in the box in any order.

The function add_vote takes as inputs a vote, which is represented represented by a String and a ballot box, and returns a ballot box with the ballot added to its contents. A voter can supply any string in his vote, even leaving it blank.

The function count_votes takes as input a ballot box and returns the total number of votes it contains.

Example:

```
>>> box = create_empty_box(('Mouse', 'Tiger'))
>>> count_votes(box)
0

>>> box = add_vote('Tiger', box)
>>> box = add_vote('Mouse', box)
>>> box = add_vote('Ben', box)
>>> box = add_vote('Mouse', box)
>>> box = add_vote('', box)
>>> count_votes(box)
5

>>> get_candidates(box)
('Mouse', 'Tiger')
>>> get_contents(box)
('Tiger', 'Mouse', 'Ben', 'Mouse', '')
```

A. Explain how you will represent the state of a ballot box.

[2 marks]

В.	Provide an implementation for the functions	<pre>create_empty_box, get_candi</pre>	dates and
get.	_contents.		[4 marks]

def	<pre>create_empty_box(candidates):</pre>
def	<pre>get_candidates(box):</pre>
def	<pre>get_contents(box):</pre>

C. Provide an implementation for the functions add_vote and count_votes. [4 marks]

```
def add_vote(vote, box):

def count_votes(box):
```

D. When counting the votes, it is also essential to know how many spoilt votes there are. Write a function count_spoilt_votes that takes as input a ballot box and return the number of spoilt votes, i.e., the vote is not equal to any of the candidates. [4 marks]

Example:

```
>>> count_spoilt_votes(box)
2
>>> box2 = create_empty_box(('Mouse', 'Tiger'))
>>> box2 = add_vote('Tiger', box2)
>>> box2 = add_vote('Lion', box2)
>>> box2 = add_vote('Mickey', box2)
>>> box2 = add_vote('#whatever', box2)
>>> count_spoilt_votes(box2)
3
```

```
def count_spoilt_votes(box):
```

E. At the counting station, there is a need to combine the votes from two ballot boxes together into a bigger box for easier storage. Write a function combine_boxes which takes as inputs two ballot boxes, and returns one ballot box containing the combined votes, provided that both boxes have the same contesting candidates. Otherwise, if the candidates differ, an empty ballot box with no candidates is returned.

You may assume that the candidate lists are always in alphabetical order. [4 marks]

```
Example:
```

```
>>> count_votes(box)
5
>>> count_votes(box2)
4
>>> box3 = combine_boxes(box, box2)
>>> count_votes(box3)
9
>>> box4 = create_empty_box(('Cow', 'Tiger'))
>>> box5 = combine_boxes(box3, box4)
>>> count_votes(box5)
0
>>> get_candidates(box5)
()
```

```
def combine_boxes(box1, box2):
```

F. On no! Instead of using combine_boxes, some idi0t has been putting ballot boxes into boxes using add_vote! Nooooo... What happens now is that we have a ballot box that, in addition to votes, also contains other boxes! Now our count_votes function might not be correct!

Write a function unpack_boxes that takes as input a ballot box and unpacks all the inner boxes and return a ballot box that only contains the votes of all the boxes.

You may assume that all the inner boxes have the same candidates.

[4 marks]

Example:

```
>>> bad_box = add_vote(box2, box)
>>> count_votes(bad_box)
6 # This is an incorrect result

>>> fixed_box = unpack_boxes(bad_box)
>>> count_votes(fixed_box)
9

>>> get_contents(fixed_box)
('Tiger', 'Mouse', 'Ben', 'Mouse', '', 'Tiger', 'Lion', 'Mickey', '#whatever')
```

```
def unpack_boxes(box):
```

Appendix

The following are some functions that were introduced in class. For your reference, they are reproduced here.

```
def sum(term, a, next, b):
  if (a > b):
    return 0
  else:
    return term(a) + sum(term, next(a), next, b)
def product(term, a, next, b):
 if a > b:
    return 1
  else:
    return term(a) * product(term, next(a), next, b)
def fold(op, f, n):
  if n==0:
    return f(0)
  else:
    return op(f(n), fold(op, f, n-1))
def enumerate_interval(low, high):
    return tuple(range(low,high+1))
def filter(pred, seq):
    if seq == ():
        return ()
    elif pred(seq[0]):
        return (seq[0],) + filter(pred, seq[1:])
    else:
        return filter(pred, seq[1:])
def accumulate(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(seq[0], accumulate(fn, initial, seq[1:]))
```

Scratch Paper