National University of Singapore
School of Computing
CS1010S: Programming Methodology
Semester I, 2022/2023

Side Quest 8.2
Cheryl's Birthday

Release date: 19th September 2022
Due: 4th October 2022, 23:59

Required Files

- sidequest08.2-template.py

Background

Albert and Bernard just became friends with Cheryl, and they want to know when her birthday is. Cheryl gives them a list of 10 possible dates. Cheryl then tells Albert and Bernard separately the month and the day of her birthday respectively.

May 15	May 16	May 19
June 17	June 18	
July 14	July 16	
Aug 14	Aug 15	Aug 17

Passing by, you overhear the conversation between Albert and Bernard.

Albert   I don't know Cheryl's birthday, but I know that Bernard doesn't know too.
Bernard   At first I didn't know when Cheryl's birthday is, but I know now.
Albert   Then I also know when Cheryl's birthday is.

Using the information given by Albert and Bernard as constraints, you realize that you can create a program that can filter out the invalid cases, and identify Cheryl's birthday.

You begin by arranging all possible birthdays into a neat table, and you can observe that some dates may contain a unique `day` or a unique `month`, or both, among all other possible dates. If Albert is given such a `month` where only one of the possible birthdays is in that month, he will know Cheryl's birthday immediately. Similarly, if Bernard is given such a unique `day`, he will also know Cheryl's birthday immediately.

	14	15	16	17	18	19
May		×	×			×
June				×	×	
July	×		×			
Aug	×	×		×		

Administrivia

For this sidequest, `birthday` refers to a tuple containing two strings: the `month`, followed by the `day`. The term `month` refers to the month of the `birthday` while `day` refers to the day of the `birthday`.

For example, for the `birthday` (`"May"`, `"15"`), `month` is represented by the string `"May"` and `day` is represented by the string `"15"`.

All the possible `birthdays` are stored in a bigger tuple, named `possible_birthdays`. The `possible_birthdays` provided by Cheryl in the beginning has been given in the template file.

This mission consists of **three** tasks.

Task 1: Unique days and months (3 marks)

You would like to find out if a given `day` or `month` appears only once among all possibilities of birthdays.

(a) The function `unique_day` takes in a string `day` and a tuple of `possible_birthdays` and returns `True` if the `day` is unique for the particular set of possible birthdays. Otherwise, it returns `False`. Implement `unique_day`. (1 mark)

(b) The function `unique_month` takes in a string `month` and a tuple of `possible_birthdays` and returns `True` if the `month` is unique for the particular set of possible birthdays. Otherwise, it returns `False`. Implement `unique_month`. (1 mark)

(c) The function `contains_unique_day` takes in a string `month` and a tuple of `possible_birthdays` and returns `True` if there is a unique `day` in the `month` for the particular set of possible birthdays. Otherwise, it returns `False`.

Implement `contains_unique_day`. (1 mark)

For example, suppose that the value of the tuple `possible_birthdays` is ((`"May"`, `"16"`), (`"May"`, `"17"`), (`"June"`, `"16"`)).

- `17` is a **unique day** because `17` appears only once across all the possible birthdays.
- `June` is a **unique month** because it only has one day whereas `May` has two.
- `May` contains a **unique day** (`"May"`, `"17"`).
- `June` does not contain a unique day because in the set of `possible_birthdays`, the month `June` only has day `16` which is **not a unique day**.

Task 2: Setting up the constraints (6 marks)

(a) *I don't know Cheryl's birthday, but I know that Bernard doesn't know too.*
Analyze the first statement from the conversation, and you will realize that Albert is essentially saying that his given month is **not** unique. Also, for his given month, all the days are **not unique**, so Bernard cannot know the birthday either.

The function `statement1` takes in a tuple `birthday` and a set of `possible_birthdays`. Then, it will return `True` if the `month` of the `birthday` is not unique, and that particular `month` does not contain a unique `day` either in the given set of possible birthdays. Otherwise, it will return `False`. Implement `statement1`. (2 marks)

(b) *At first I didn't know when Cheryl's birthday was, but I know now.*
Analyze the second statement from the conversation, and you will realize that the `day` that Cheryl told Bernard is a unique `day` from the remaining possible birthdays. The function `statement2` takes in a tuple `birthday` and a set of `possible_birthdays`, and will return `True` if the `day` of the given `birthday` is unique in the set of `possible_birthdays`. Otherwise, it will return `False`. Implement `statement2`. (2 marks)

(c) *Then I also know when Cheryl's birthday is.*
Analyze the third statement from the conversation, and you will realize that the `month` Albert has heard is a unique `month` from the remaining possible birthdays. The function `statement3` takes in a tuple `birthday` and a set of `possible_birthdays`. It will return `True` if the `month` of the `birthday` is unique for the particular set of possible birthdays. Otherwise, it will return `False`. Implement `statement3`. (2 marks)

Task 3: And now I know her birthday, too! (1 mark)

Implement the function `get_birthday` that will take in a tuple `possible_birthdays` and will return a tuple containing the `birthdays` that are still valid after being filtered through the constraints. If done correctly, the result should be a single element tuple consisting of Cheryl's `birthday` only.

(Hint: Make use of `filter` to shortlist a subset of the previous list of `possible_birthdays` using one constraint each time.)