CS1010FC — Programming Methodology School of Computing National University of Singapore

Re-Mid-Term Test

18 April 2015		Т	lime a	llowed	d: 1 ho	our 45	minutes		
Matriculation No:									

Instructions (please read carefully):

- 1. Write down your matriculation number on the **question paper**. DO NOT WRITE YOUR NAME ON THE QUESTION SET!
- 2. This is **an open-sheet test**. You are allowed to bring one A4 sheet of notes (written on both sides).
- 3. This paper comprises **FOUR** (4) **questions** and **NINETEEN** (19) **pages**. The time allowed for solving this test is 1 hour 45 minutes.
- 4. The maximum score of this test is **100 marks**. The weight of each question is given in square brackets beside the question number.
- 5. All questions must be answered correctly for the maximum score to be attained.
- 6. All questions must be answered in the space provided in the answer sheet; no extra sheets will be accepted as answers.
- 7. The back-sides of the sheets and the pages marked "scratch paper" in the question set may be used as scratch paper.
- 8. You are allowed to un-staple the sheets while you solve the questions. Please make sure you staple them back in the right order at the end of the test.
- 9. You are allowed to use pencils, ball-pens or fountain pens, as you like (no red color, please).

GOOD LUCK!

Question	Marks	Remark
Q1		
Q2		
Q3		
Q4		
Total		

Question 1: Python Expressions [30 marks]

There are several parts to this problem. Answer each part <u>independently and separately</u>. In each part, one or more Python expressions are entered into the interpreter (Python shell). Determine the response printed by the interpreter for the final expression entered. If the interpreter produces an error message, or enters an infinite loop, explain why.

```
A. x = 100
    for i in range(11, 21):
        if i % 3:
            x += 1
        elif i % 3 == 2:
            x -= 2
    print(x)
```

[5 marks]

```
D
```

```
B. x = 200
    y = 100
    def f(x, y):
        x = 5
        x = (x + y) // 3
        return x
    print(f(y, x))
```

[5 marks]

```
\mathbf{C}_{\bullet} def thrice(f):
         return f(f(f))
     def add1(x):
         return x+1
     print (thrice(thrice(add1))(3))
                                                                                 [5 marks]
\mathbf{D}_{\bullet} i = 2
    s = (0, 1)
     while i < 10:
         if i%3 != 0:
              s = s + (s[len(s)-2]+s[len(s)-1],)
         i += 1
     print(s[4] + len(s))
                                                                                 [5 marks]
```

```
\mathbf{E}_{\bullet} = (1, 2, 3)
    for i in range (1,5):
         x = x*i
    print(x[16:20])
                                                                                [5 marks]
F_{\bullet} x = 5
    y = 10
    z = 15
    def f(x, y):
         def g(y,z):
             def h(z, x):
                  return x + y + z
             return h(z,y)
         return g(y, x)
    print(f(y,x))
                                                                                [5 marks]
```

Question 2: Implementing Scheme Data Structures [24 marks]

In the Scheme programming language, the basic data structure is call a cons pair. In this question, we will simulate this data structure and work with it. Assume that the functions cons, car and cdr exist, such that:

```
car(cons(x,y)) = x

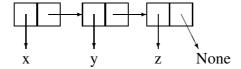
cdr(cons(x,y)) = y
```

cons (x, y) returns a pair object that joins two objects x and y. There is also a function is_pair that takes in one parameter and returns True if the input is a cons pair. You can assume that the order of growth for cons, car and cdr are all O(1) for both time and space.

The cons pair can be represented graphically as follows:



In order to combine more than two elements together, we create a chain of cons pairs called a Scheme list. A special property of a Scheme list is that the last element in the chain is always None. This is illustrated as follows:



The function mylist will create a new Scheme list object from an input sequence and the function length will return the number of elements in a Scheme list object. The function to_tuple will create a tuple corresponding to a Scheme list and the function reverse will reverse a Scheme list.

Sample execution:

```
>>> ml = mylist((1,2,3))
>>> car(ml)
1
>>> car(cdr(ml))
2
>>> car(cdr(cdr(ml)))
3
>>> cdr(cdr(cdr(ml)))
None
>>> length(ml)
3
>>> to_tuple(ml)
(1, 2, 3)
```

```
>>> rl = reverse(ml)
>>> car(rl)
>>> car(cdr(rl))
>>> car(cdr(cdr(rl)))
>>> cdr(cdr(cdr(rl)))
None
A. Please provide a possible implementation for mylist.
                                                                           [4 marks]
def mylist(seq):
B. Please provide a possible implementation for length.
                                                                           [4 marks]
def length(slst):
```

C. What is the order of growth in terms of time and space for the f (B) in terms of <i>n</i> where <i>n</i> is the length of slst.	function you wrote in Part [2 marks]
Time:	
Space:	
D. If your function length in Part(B) was implemented as a recusival possible iterative implementation for length. If it were iterative, plimplementation.	
<pre>def length(slst):</pre>	

E. What is the order of growth in terms of time and space for the func D) in terms of n where n is the length of slst.	tion you wrote in Part [2 marks]
Time:	
Space:	
F. Please provide a possible implementation for to_tuple.	[4 marks]
def to_tuple(slst):	

G.	Please provide a possible implementation for reverse.	[4 marks]
def	reverse(slst):	

Question 3: Higher-Order Functions [22 marks]

A. [Warm-up] Consider the following sum:

$$a(1) + a(2) + ... + a(n)$$

where a is a function. Suppose the function asum(a,n) computes this sum for $n \ge 1$ and is defined in terms of sum (see Appendix) as follows:

Please provide possible implementations for T1, T2, T3, and T4.

[6 marks]

_	
<t1>: [2 marks]</t1>	
<t2>: [1 mark]</t2>	
<t3>: [2 marks]</t3>	
<t4>: [1 mark]</t4>	

B. Next, sur Appendix) as f	ppose the function $asum(a,n)$ from Part (A) is defined in terms of fold (follows:	see
def asum(a,r return f	n): Fold(<t5>,</t5>	
Please provide	possible implementations for T5, T6, and T7. [6 mar	:ks]
<t5>: [2 marks]</t5>		
<t6>: [2 marks]</t6>		
<t7>: [2 marks]</t7>		
C. Consider	the following expression:	
	$(((\cdots(b(0)/b(1))/b(2))/\cdots)/b(n)$	
	tient (b, n) computes this expression (for $n \ge 0$), i.e. bquotient (b, 0) = $b(0)/b(1)$, etc. and it is defined in terms of fold as follows:	(0),
def bquotien return f	<pre>int(b,n): Fold(<t8>,</t8></pre>	
Please provide	possible implementations for T8, T9, and T10. [4 mar	ks]
<t8>: [2 marks]</t8>		
<t9>: [1 mark]</t9>		
<t10>:</t10>		

[1 mark]

D. Consider the following continued fraction	D.	Consider	the	following	continued	fraction
---	----	----------	-----	-----------	-----------	----------

$$\frac{1}{1 + \frac{2}{1 + \frac{\dots}{1 + n}}}$$

Suppose cfraction (n) computes this expression (for $n \ge 1$), i.e. cfraction (1) = 1, cfraction (2) = $\frac{1}{1+2}$, cfraction (3) = $\frac{1}{1+\frac{2}{1+3}}$, etc. and it is defined in terms of fold as follows:

Please provide possible implementations for T11, T12, and T13.

[6 marks]

_	
<t11>: [2 marks]</t11>	
<t12>: [2 marks]</t12>	
<t13>: [2 marks]</t13>	

[4 marks]

Question 4: Chocolate Packing [24 marks]

You work for a chocolate factory that makes 2 types of chocolates, a small 1×1 chocolate and a big 2×2 chocolate. The chocolates are packed in square boxes of length n. i.e. of size $n \times n$. Each box can contain both small and big chocolates. For example, a box of length 2 (i.e. 2×2) can fit either one big chocolate or 4 small ones. A box of length 3 (i.e. 3×3) can fit either one big chocolate and 5 small ones or 9 small chocolates. Your goal is to model boxes of chocolates using the following functions:

- make_box(n,b,s) will create a box of length n, containing b big chocolates and s small chocolates.
- size (b) will return the length of box *b*.
- $get_big(b)$ will return the number of big chocolates in box b.

make_box(n,b,s), size(b), get_big(b) and get_small(b).

• get_small(b) will return the number of small chocolates in box *b*.

Note: You are limited to using <u>tuples</u> for this question, i.e. you cannot use lists and other Python data structures.

Decide on an implementation for the chocolate box object and implement the functions

L				

otherwise.	[6 marks]

B. Implement the function is_valid that takes in one parameter and returns True if the input is a valid box object (i.e. the format is correct and all the chocolates will fit inside), or False

C. The functions $add_big(b,n)$ and $add_small(b,n)$ add n big and small chocolates to a box b, respectively, and return a <u>new</u> box. If it is not possible to add n chocolates, False is returned instead. Provide possible implementations of add_big and add_small. Note that you are allowed to define helper functions if you think they would be helpful. [6 marks]

Sample execution:

```
>>> b1 = make_box(3,0,0)
>>> size(b1)
3
>>> get_big(b1)
0
>>> get_small(b1)
0
>>> add_big(b1,2)
False
>>> add_small(b1,10)
False
```

```
>>> b2 = add_big(b1,1)
>>> size(b2)
3
>>> get_big(b2)
1
>>> get_small(b2)
0

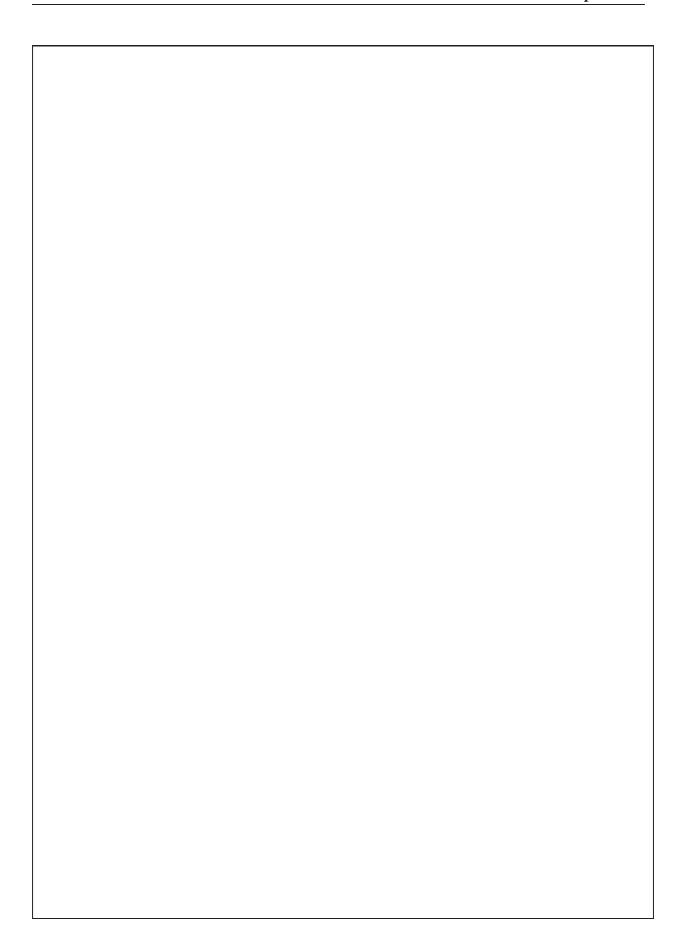
>>> b3 = add_small(b2,5)
>>> size(b3)
3
>>> get_big(b3)
1
>>> get_small(b3)
5

>>> add_big(b3,2)
False
>>> add_small(b3,10)
False
```

D. The functions add_big_fit(b,n) and add_small_fit(b,n) add n big and small chocolates to a box b, respectively, and always return a <u>new</u> box. If the additional chocolates, the new box will be of the minimal size to fit the additional chocolates. You can assume that the functions sqrt and ceil are available. sqrt(n) returns the square root of n and ceil(n) returns integer larger than n if n is not an integer. [8 marks]

Sample execution:

```
>>> b4 = add_big_fit(b3,3)
>>> size(b4)
5
>>> get_big(b4)
4
>>> get_small(b4)
5
>>> b5 = add_small_fit(b4,5)
>>> size(b5)
6
>>> get_big(b5)
4
>>> get_small(b5)
10
```



Appendix

The following are some functions that were introduced in class. For your reference, they are reproduced here.

```
def sum(term, a, next, b):
  if (a > b):
   return 0
  else:
    return term(a) + sum(term, next(a), next, b)
def fold(op, f, n):
 if n==0:
   return f(0)
  else:
    return op(f(n), fold(op, f, n-1))
def enumerate_interval(low, high):
    return tuple(range(low, high+1))
def filter(pred, seq):
    if seq == ():
        return ()
    elif pred(seq[0]):
        return (seq[0],) + filter(pred, seq[1:])
    else:
        return filter(pred, seq[1:])
def accumulate(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(seq[0], accumulate(fn, initial, seq[1:]))
```

Scratch Paper