CS1010S — Programming Methodology School of Computing National University of Singapore

Re-Mid-Term Quiz

17 October 2014			$\Gamma \mathrm{ime}$	allow	ved: 1	l hour	45 m	inutes
Matriculation No:								

Instructions (please read carefully):

- 1. Write down your matriculation number on the **question paper**. DO NOT WRITE YOUR NAME ON THE QUESTION SET!
- 2. This is **an open-sheet quiz**. You are allowed to bring one A4 sheet of notes (written on both sides).
- 3. This paper comprises FOUR (4) questions and NINETEEN (19) pages. The time allowed for solving this quiz is 1 hour 45 minutes.
- 4. The maximum score of this quiz is **100 marks**. The weight of each question is given in square brackets beside the question number. Note however that the final grade will be capped at **60 marks** because this is a re-exam.
- 5. All questions must be answered correctly for the maximum score to be attained.
- 6. All questions must be answered in the space provided in the answer sheet; no extra sheets will be accepted as answers.
- 7. The back-sides of the sheets and the pages marked "scratch paper" in the question set may be used as scratch paper.
- 8. You are allowed to un-staple the sheets while you solve the questions. Please make sure you staple them back in the right order at the end of the quiz.
- 9. You are allowed to use pencils, ball-pens or fountain pens, as you like (no red color, please).

GOOD LUCK!

Question	Marks	Remark
Q1		
Q2		
Q3		
Q4		
Total		

Question 1: Python Expressions [30 marks]

There are several parts to this problem. Answer each part <u>independently and separately</u>. In each part, one or more Python expressions are entered into the interpreter (Python shell). Determine the response printed by the interpreter for the final expression entered. If the interpreter produces an error message, or enters an infinite loop, explain why.

```
A. x = 0
     if x <= 0:
         print("Yeah")
     elif x \ge 0:
         print("No!!")
     if x == 0:
         print("No idea!")
                                                                       [5 marks]
В.
     def t(a,b):
         return (b,)+(a)
     print(t(t((1,2),2),3))
                                                                       [5 marks]
```

```
C. x = 5
    y = 7
     def g(y):
         return x + y
     def f(x):
         y = 4
         return g(x-y)
    print(f(y))
                                                                     [5 marks]
D.
     sum = 60
     for i in range(1,10):
         if i % 3:
             continue
         if sum < 10:
             break
         sum //= i
     print(sum)
                                                                     [5 marks]
```

```
\mathbf{E}.
    a = "Happy"
     b = "Birthday!"
     while (a):
         b += a[0]
         a = a[1:]
     print(b)
                                                                         [5 marks]
\mathbf{F}.
    once = lambda f: lambda x: f(x)
     twice = lambda f: lambda x: f(f(x))
     thrice = lambda f: lambda x: f(f(f(x)))
     print(once(twice(thrice(lambda x:2*x)))(2))
                                                                         [5 marks]
```

Question 2: Palindromic numbers [22 marks]

A palindromic number is a number that remains the same when its digits are reversed. For example, 27372 is a palindromic number, i.e. it is "symmetrical".

The first 20 palindromic numbers (starting from 1) are:

$1,\ 2,\ 3,\ 4,\ 5,\ 6,\ 7,\ 8,\ 9,\ 11,\ 22,\ 33,\ 44,\ 55,\ 66,\ 77,\ 88,\ 99,\ 101,\ 111$	
A. Write a <u>recursive</u> function is_palindromic(n) that returns True if n dromic number and return False otherwise.	is a palin-
(Hint: It might be helpful to use strings.)	[5 marks]

B. What is the order of growth in terms of time and space for the function you wrote in Part (A) in terms of n? **Explain** your answer, state your assumptions (if any). (Hint: String slicing takes O(k) space and time where k is the length of the returned string. Adding two strings takes $O(k_1 + k_2)$ space and time where k_1 and k_2 are the lengths of the two strings.)

Time:	
Space:	

${\bf C.}$ Write an <u>iterative</u> function is_palindromic(n) that returns True if n dromic number and return False otherwise.	is a palin- [5 marks]
\mathbf{D}_{\bullet} What is the order of growth in terms of time and space for the function in Part (C) in terms of n ?	you wrote [2 marks]
Time:	
Space:	

here						$77, 88, 99$ t^{th} palindro	, 101, 111 omic numb	er.
	Write a f	function n	th_palind	lrome(n)	that retur	rns the n th	palindron	nic number. [6 marks]

Question 3: Higher-Order Functions [22 marks]

Consider the following sum S(i,j,k) where i,j,k are integers and k>0:

$$S(i,j,k) = i + (i+k) + (i+2k) + \cdots + (i+nk)$$
, where $i + nk \le j < i + (n+1)k$

A. Suppose the function compute_s(i,j,k) will return the sum S(i,j,k). We can express S(i,j,k) in terms of sum (see Appendix) as follows:

def compute_s(i,j,k):
 return sum(<T1>, <T2>, <T3>, <T4>)

Please provide possible implementations for the terms T1, T2, T3, and T4. [5 marks]

T1: [1 mark]	
T2: [1 mark]	
T3: [2 marks]	
T4: [1 mark]	

B. We	can also express $S(i,j,k)$ in terms of fold (see Appendix) as follows:	
	oute_s(i,j,k): urn fold(<t5>, <t6>, <t7>)</t7></t6></t5>	
Please pr	ovide possible implementations for the terms T5, T6, and T7.	[5 marks]
T5: [1 mark]		
T6: [2 marks]		
T7: [2 marks]		

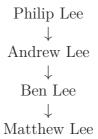
	des sum and fold, map and reduce (see Appendix) are higher-order functions ommonly used in practice.	
It turns ou	at that we can also express $S(i,j,k)$ in terms of map and reduce:	
	te_s(i,j,k): n reduce(<t8>, <t9> , map(<t10> , tuple(range(<t11>))))</t11></t10></t9></t8>	
Please pro	vide possible implementations for the terms T8, T9, T10, and T11. [6 marks]	
T8: [1 mark]		
T9: [1 mark]		
T10: [2 marks]		
T11: [2 marks]		

	ed, the functions map and reduce are very handy. For example, we can use them e the factorial of a non-negative number n :
def facto	rial(n): rn reduce(T<15> , <t16> , map(<t17>, tuple(range(<t18>))))</t18></t17></t16>
Recall that	$t factorial(n) = 1 \times 2 \times 3 \times \times n.$
Please pro	vide possible implementations for the terms T15, T16, T17, and T18. [6 marks]
T15: [2 marks]	
T16: [1 mark]	
T17: [1 mark]	
T18: [2 marks]	

Question 4: Genealogy [26 marks]

Warning: Please read the question description clearly before you attempt this problem!!

Genealogy is the study of families and the tracing of their lineages and history. For this question, we will specialize in studying the lineage of fathers, which is called a patriline. In other words, it is a family line of fathers. For example, this is a 4 generation patriline of the Lee family:



You will create a family patriline with the function make_patriline(family, ancestor), where family is the family name and ancestor is the first name of the first ancestor of this line. Thereafter, sons can be added to the patriline with the function begat(patriline, name), where patriline is the patriline and name is the name of the next son in line. For example, the Lee's patriline can be created by:

```
>>> lee = make_patriline("Lee", "Philip")
>>> lee2 = begat(lee, "Andrew")
>>> lee3 = begat(lee2, "Ben")
>>> lee4 = begat(lee3, "Matthew")
```

The function get_length(patriline) returns the number of generations in the patriline, and the function get_person(patriline, n) is used to get the nth person of the patriline, with the first ancestor being n = 1.

Example:

```
>>> get_length(lee4)
4
>>> get_person(lee4, 2)
'Andrew'
>>> get_person(lee4, 5)
None
```

Α.	Describe how you will represent a patriline using a tuple.	[3 marks]
B. bega	Please provide a possible implementation for the constructor make_patrt.	[4 marks]
def	<pre>make_patriline(family, ancestor):</pre>	
def	begat(patriline, name):	

	Please provide a possible implementation for the accessors functions get_length and _person. [6 marks]
def	<pre>get_length(patriline):</pre>
def	<pre>get_person(patriline, n):</pre>

D. Bob, a genealogist, would like to use Python for his work. In particular, he wants to examine the patrilines that we have created. One function that he needs in his work is to get the name of the father of a given person in the patriline.

For example:

```
>>> get_father(lee4, "Ben")
'Andrew'
>>> get_father(lee4, "Amos")
None
>>> get_father(lee4, "Philip")
None
```

Give a possible implementation of the function get_father, bearing in mind that Bob has no knowledge of your patriline state. You may assume that no two persons in the patriline have the same name.

[3 marks]

def	<pre>get_father(patriline,</pre>	name):

E. Now it is entirely possible for a father to have several sons, in which case a patriline might be split from a common ancestor. For example, consider the Tan's patriline:

```
>>> tan = make_patriline("Tan", "John")
>>> tan2 = begat(tan, "Samuel")
>>> tan3 = begat(tan2, "Elvis")
>>> tan4 = begat(tan2, "Elvin")
>>> tan5 = begat(tan4, "Brian")
```

where Samuel has two sons, Elvis and Elvin, thus forking the Tan patriline into two.

When studying patrilines, it is important to know where patrilines have forked. Help Bob write a function to find the lowest common ancestor of two patrilines, provided that they are of the same family and origin. You may assume that two patrilines with a common ancestry will both have the same first ancestor.

[6 marks]

Example:

```
>>> lowest_common_ancestor(tan4, tan5)
'Samuel'
>>> lowest_common_ancestor(lee3, tan3)
None
```

```
def lowest_common_ancestor(p1, p2):
```

F . Oh no! In his research, Bob has discovered that "Tan" is a very common family name. It is entirely possible to have different patrilines of two different persons with the same name! For example:		
<pre>>>> atan = make_patriline("Tan", "John") >>> atan1 = begat(atan, "Mark")</pre>		
Since there are two different persons named John Tan, the correct output should be:		
>>> lowest_common_ancestor(tan3, atan1) None		
Does your implementation of lowest_common_ancestor(p1, p2) produce the correct result? If yes, please explain why? If no, please explain what can be done to change it. Hint: The is comparison operator on strings does not guarantee consistent results. [4 marks]		

Appendix

The following are some functions that were introduced in class. For your reference, they are reproduced here.

```
def sum(term, a, next, b):
  if (a>b):
    return 0
  else:
    return term(a) + sum(term, next(a), next, b)
def fold(op, f, n):
  if n==0:
    return f(0)
  else:
    return op(f(n), fold(op, f, n-1))
def map(fn, seq):
    if seq == ():
        return ()
    else:
        return (fn(seq[0]), ) + map(fn, seq[1:])
def reduce(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(seq[0], reduce(fn, initial, seq[1:]))
def enumerate_interval(low, high):
    return tuple(range(low,high+1))
def filter(pred, seq):
    if seq == ():
        return ()
    elif pred(seq[0]):
        return (seq[0],) + filter(pred, seq[1:])
    else:
        return filter(pred, seq[1:])
```

Scratch Paper

- END OF PAPER -