CS1010S — Programming Methodology School of Computing National University of Singapore

Mid-Term Quiz

1 October 2014	October 2014			1	Time a	llowe	d: 1 ho	our 45	minutes
Matriculation No:									

Instructions (please read carefully):

- 1. Write down your matriculation number on the **question paper**. DO NOT WRITE YOUR NAME ON THE QUESTION SET!
- 2. This is **an open-sheet quiz**. You are allowed to bring one A4 sheet of notes (written on both sides).
- 3. This paper comprises FOUR (4) questions and NINETEEN (19) pages. The time allowed for solving this quiz is 1 hour 45 minutes.
- 4. The maximum score of this quiz is **100 marks**. The weight of each question is given in square brackets beside the question number.
- 5. All questions must be answered correctly for the maximum score to be attained.
- 6. All questions must be answered in the space provided in the answer sheet; no extra sheets will be accepted as answers.
- 7. The back-sides of the sheets and the pages marked "scratch paper" in the question set may be used as scratch paper.
- 8. You are allowed to un-staple the sheets while you solve the questions. Please make sure you staple them back in the right order at the end of the quiz.
- 9. You are allowed to use pencils, ball-pens or fountain pens, as you like (no red color, please).

GOOD LUCK!

Question	Marks	Remark
Q1		
Q2		
Q3		
Q4		
Total		

Question 1: Python Expressions [30 marks]

There are several parts to this problem. Answer each part <u>independently and separately</u>. In each part, one or more Python expressions are entered into the interpreter (Python shell). Determine the response printed by the interpreter for the final expression entered. If the interpreter produces an error message, or enters an infinite loop, explain why.

```
A_{\bullet} x = "0"
    if x:
        print("Yeah")
    elif not x:
        print("No!!")
    else:
        print("No idea!")
                                                                           [5 marks]
B. x = 3
    y = 5
    def f(x,y):
        x = 4
        return x + y
    print(f(y,x))
                                                                           [5 marks]
```

```
C_{\bullet} x = 1
    for i in range (2, 9):
         if i%2 == 0:
              x += i
         elif i>5:
              continue
         else:
              x -= 1
    print(x)
                                                                                [5 marks]
\mathbf{D}_{\bullet} x = 12345678
    y = 0
    while x > 0:
         y += 1
         x = x//10
    print(x + y)
                                                                                [5 marks]
```

Е.	<pre>def foo(x): return lambda y: x(x(y))</pre>	
	<pre>print(foo(foo)(lambda x:x+1)(2))</pre>	[5 marks]
車 力		
r.	<pre>def bar(x,y): return x + y</pre>	
	print(bar(((1,),),bar((1,2),(2,3))))	[5 marks]

Question 2: Alternating Series Galore [24 marks]

Consider the following alternating series s_{11} :

$$s_{11}(n) = 1 - 2 + 3 - 4 + \cdots n$$

A.	[Warm Up] Write an <u>recursive</u> function s11 (n) that returns the value for $s_{11}(n)$. [4 marks]
B. (A)	What is the order of growth in terms of time and space for the function you wrote in Part in terms of n . Explain your answer. [4 marks]
Ti	me:
Sp	pace:

D. What is the order of growth in terms of time and space for the function you wrote in Part (C) in terms of n. [2 marks] Time: Space:	C.	Write an <u>iterative</u> function s11 (n) that returns the value for $s_{11}(n)$.	[4 marks]
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
(C) in terms of <i>n</i> . [2 marks]			
Space:	Tiı	me:	
	Sp	pace:	

Now, consider the following alternating series s_{ij} where $i, j \ge 1$:

$$s_{21}(n) = 1+2-3+4+5-6+7+8-\cdots n$$

$$s_{12}(n) = 1 - 2 - 3 + 4 - 5 - 6 + 7 - 8 - \dots n$$

$$s_{31}(n) = 1 + 2 + 3 - 4 + 5 + 6 + 7 - 8 + \cdots n$$

Note that the subscript i denotes the number of terms with a positive sign and the subscript j denotes the number of terms with a negative sign. Basically these series will alternate between i positive terms and j negative terms.

Е.	Write a function s21 (n) that returns the value for $s_{21}(n)$.	[5 marks]

= make_s(1,1) = make_s(1,2)	
_ 、	[5 mark

Question 3: Higher-Order Alternating Functions [23 marks]

Consider the following alternating series F_{ij} where $i, j \ge 1$:

$$F_{11}(n) = f(n,1) - f(n,2) + f(n,3) - f(n,4) + f(n,5) - f(n,6) + f(n,7) - f(n,8) + \cdots + f(n,n)$$

$$F_{21}(n) = f(n,1) + f(n,2) - f(n,3) + f(n,4) + f(n,5) - f(n,6) + f(n,7) + f(n,8) + \cdots + f(n,n)$$

$$F_{12}(n) = f(n,1) - f(n,2) - f(n,3) + f(n,4) - f(n,5) - f(n,6) + f(n,7) - f(n,8) + \cdots + f(n,n)$$

$$F_{31}(n) = f(n,1) + f(n,2) + f(n,3) - f(n,4) + f(n,5) + f(n,6) + f(n,7) - f(n,8) + \cdots + f(n,n)$$

 F_{ij} is similar to s_{ij} from Question 2(e). The only difference is that each term is now a function instead of a simple integer. Suppose the function make_f(f,i,j) will return a function that computes $F_{ij}(n)$. In other words, s_{11} from Question 2(a) can be expressed as:

$$s11 = make_f(lambda n, x: x, 1, 1)$$

A. Consider the following alternating series to estimate ln 2:

$$\ln 2 = 1 - 1/2 + 1/3 - 1/4 + \dots + (-1)^{n+1} 1/n$$

and the function ln2(n) which gives the estimate to n terms as follows:

$$ln2 = make_f(, ,)$$

Please provide possible implementations for the terms T1, T2, and T3.

[5 marks]

T1: [3 marks]		
T2: [1 marks]		
T3: [1 marks]		

B. Consider the following alternating series t_{ij} :

$$t_{11}(n) = n - (n-1) + (n-2) - (n-3) + (n-4) - (n-5) + (n-6) - (n-7) + \cdots 1$$

$$t_{21}(n) = n + (n-1) - (n-2) + (n-3) + (n-4) - (n-5) + (n-6) + (n-7) - \cdots 1$$

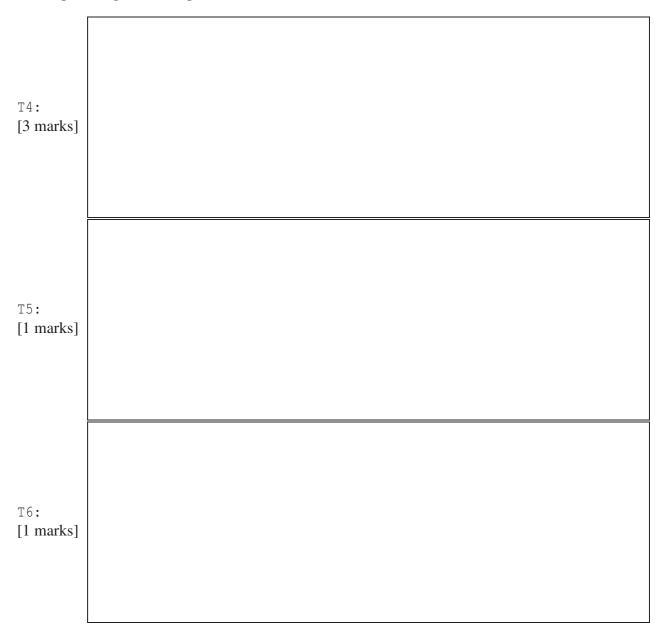
$$t_{12}(n) = n - (n-1) - (n-2) + (n-3) - (n-4) - (n-5) + (n-6) - (n-7) - \cdots 1$$

$$t_{13}(n) = n - (n-1) - (n-2) - (n-3) + (n-4) - (n-5) - (n-6) - (n-7) + \cdots 1$$

which is very similar to s_{ij} except the terms are reversed. Suppose the function make_t computes $t_{ij}(n)$ as follows:

```
def make_t(i,j):
    return make_f(<T4>, <T5>, <T6>)
```

Please provide possible implementations for the terms T4, T5, and T6. [5 marks]



from 1 up to and including n, and that:		
intsum = make_f(<t7>, <t8>, <t9>)</t9></t8></t7>		
Please prov	vide possible implementations for the terms T7, T8, and T9.	[5 marks]
T7: [3 marks]		
T8: [1 marks]		
T9: [1 marks]		

Now suppose that the function intsum(n) will compute the sum of all positive integers

C.

D. It turns out that we can express make_f in terms of fold (see Appendix) as follows: def make_f(f,i,j): def op(x, y): <T10> def f1(n,x):<T11> def helper(n): return fold(op, lambda x: f1(n,x), <T12>) return helper Please provide possible implementations for the terms T10, T11, and T12. [8 marks] T10: [2 marks] T11: [4 marks] T12: [2 marks]

Question 4: Espionage [23 marks]

Warning: Please read the question description clearly before you attempt this problem!!

You are working for a spy agency and you have been tasked with building a multi-level encryption system for the agency. The way this system works is that you create a message m with the function <code>make_message(msg)</code>, where <code>msg</code> is a String. A message <code>msg</code> is read with the read(<code>msg)</code> function.

After that you can encrypt your message m with the function encrypt (m, password) to return a new encrypted message m'. Any attempts to read the encrypted message m' will return the string "*ENCRYPTED*". decrypt (m', password) will recover the message m. If the wrong password is used in the decryption, the returned message will be messed up and which will return the string "*GARBLED*" for any attempts to read it. encrypt can be applied multiple times and an equal number of decrypt with the passwords applied in strict reverse order will be required to recover the original message. Attempts to decrypt a non-encrypted message will have no effect.

Sample Execution:

```
>>> m1 = make_message("CS1010S is cool!")
>>> m1
<function make_message.<locals>.secret at 0x104074170>
>>> read(m1)
'CS1010S is cool!'
>>> m2 = encrypt (m1, 12345)
>>> read(m2)
'*ENCRYPTED*'
>>> m3 = decrypt (m2, 54321)
>>> read(m3)
'*GARBLED*'
>>> m4 = decrypt (m2, 12345)
>>> read(m4)
'CS1010S is cool!'
>>> m5 = encrypt (m2, 54321)
>>> read(m5)
'*ENCRYPTED*'
>>> m6 = decrypt (m5, 54321)
>>> read(m6)
'*ENCRYPTED*'
>>> m7 = decrypt (m6, 12345)
>>> read(m7)
'CS1010S is cool!'
```

>>>	m8 = decrypt(m1,12345) read(m8) 1010S is cool!'	
A.	Describe how you will keep track of the state of a message using a tuple.	[3 marks]
and (A). mes	Write a function make_message (msg) that will take in a String representing return a new message object that will be implemented according to your descr. Note that you cannot simply return an unobfuscated tuple because if not, the sage would be free for all to see. One simple approach to get around this is sect inside a function, but you are welcome to use another method to obfuscate marks]	iption in Part en the secret s to wrap the

C.	Please provide a possible implementation for the accessor function read.	[4 marks]
D.	Please provide a possible implementation for the function encrypt that will sage in a manner consistent with your description in Part (A).	ll encrypt the [4 marks]

Please provide a possible implementation for the function decrypt lessage that was encrypted by the encrypt function in Part (D) above.	that will decrypt the [4 marks]

Suppose now that we want the secret message to be decrypted by applying the required numer of decrypt with the correct passwords <i>in any order</i> , though the decrypting of the message ith any wrong password will garble the message. Explain how your implementation(s) in Parts (C) to (E) would need to be updated to implement this and write the required code. [4 marks]					

Appendix

The following are some functions that were introduced in class. For your reference, they are reproduced here.

```
def sum(term, a, next, b):
 if (a>b):
   return 0
 else:
    return term(a) + sum(term, next(a), next, b)
def fold(op, f, n):
 if n==0:
    return f(0)
 else:
    return op(f(n), fold(op, f, n-1))
def enumerate interval(low, high):
    return tuple(range(low, high+1))
def filter(pred, seq):
    if seq == ():
        return ()
    elif pred(seq[0]):
        return (seq[0],) + filter(pred, seq[1:])
    else:
        return filter(pred, seq[1:])
def accumulate(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(seq[0], accumulate(fn, initial, seq[1:]))
```

Scratch Paper

— END OF PAPER —