1

Implementation of a Carry Lookahead Fast Adder

Healy, Matthew mhealy@mst.edu Johnston, Jaxson jnjt37@mst.edu Grbesa, Lukas lgqq3@mst.edu

Abstract—Carry lookahead adders are one of the most common fast-adder architectures used in high performance computing to date. They allow for arbitrarily large summations with only $O(\log(n))$ complexity, rather than the O(n) complexity of a traditional ripple-carry adder.

The purpose of this project is to implement a simulation of the execution of a carry lookahead adder using the Intel 8051 architecture. Although this simulation cannot achieve the performance of a hardware implementation, it serves as a proof of concept for a carry lookahead adder.

I. Introduction

The carry lookahead adder was originally patented by IBM[1] in 1972. As time passed and technology improved, this method of addition was shown to be even more useful than originally thought, as it allows for the quick computation of numbers that would take a non-insignificant amount of time using the traditional ripple-carry method.

Our goal in this project is to implement a simulation of a carry lookahead adder on the 8051 microcontroller as a proof of concept. Since execution is serial, this simulation will not be faster than the built-in adding operations, as we are unable to calculate multiple things at once, as we could were we building a hardware model of a carry lookahead adder.

II. Approach

Since the carry value of a certain bit addition can be determined by looking at the previous pair of bits, finding their generate and propagate values, and comparing the propagate value to the carry of the previous bit operation. After a string of carries is created then all that must be done is two XOR operations because XORing the first input with the second input and XORing the result of that operation with the carry string gives the logical equivalent of adding the two numbers directly.

III. Results and Discussion

By first generating our Propogate(P) and Generate(G) strings from the input, and then stepping through our carry string and deriving each bit from the P and G strings and the previous carry bit, we emulate the stages of operation of a carry lookahead adder.

The P string is created by XORing each pair of respective input bits, and the G by ANDing together each pair of input bits. This would be done in hardware with blocks of two logic gates all operating in parallel, and would take approximately $2\Delta t$ to complete.

Operand 1	Operand 2	Sum	Time(clock pulses)
0x8A	0x25	0xAF	0xA0
0x1FFF	0xA222	0xC111	0x12E
0x3EFF	0x8AAA	0xC9A9	0x12E
0x254621	0xAAAAAA	0xCFF0CB	0x01D4
0x8532AA	0x243699	0xA96943	0x01D5
0x23456789	0x98765432	0xBBBBBBBBB	0x026A
0xABABABAB	0x111111111	0xBCBCBCBC	0x04C2
0xC1C1C1C1C1C1	0x1C1C1C1C1C1C	0xDDDDDDDDDDD	0x0300
0x123456789ABC	0x123456789ABC	0x2468ACF13578	0x0396
0x1234567C1C1C1C	0x11AAAAAAA8532AA	0x23DF0126A14EC6	0x042E

The next stage, wherein the P and carry bit are XORed together to create the sum, is emulated by a loop that XORs bytes of the carry string with bytes of the P string. While this adds another n time in the software solution, it would implement only another $2\Delta t$ in a hardware solution, since it would be only two more logic gates for each bit, all operating in parallel.

Algorithm 1 shows the basic implementation of this simulation:

Algorithm 1 Pseudocode for CLA Adder

 $\begin{array}{l} \mathrm{R3} \to \mathrm{carry\ string} \\ \mathrm{R6} \to \mathrm{Input\ A} \\ \mathrm{R7} \to \mathrm{Input\ B} \\ \mathrm{for\ all\ bytes}\ P_i \in P, G_i \in G, RX_i \in RX\ \mathrm{do} \\ P \leftarrow R6 \oplus R7 \\ G \leftarrow R6 \wedge R7 \\ \mathrm{end\ for} \\ \mathrm{for\ all\ bits}\ C_i \in C, P_i \in P, G_i \in G\ \mathrm{do} \\ C \leftarrow G \vee (P \wedge C) \\ \mathrm{end\ for} \\ \mathrm{for\ all\ bytes}\ SUM_i \in SUM, C_i \in C, P_i \in P\ \mathrm{do} \\ SUM_i \leftarrow C_i \oplus P_i \\ \mathrm{end\ for} \end{array}$

As can be seen in Fig. I, this software simulation falls far short of the speed of its hardware implementation. However, it does match very closely the speed of a ripple-carry add on the 8051 microcontroller, changing only the constant in the time-complexity.

IV. Summary and Conclusion

Upon testing we found that because the carry lookahead adder must be executed in serial, the simulation doesn't end up being any faster than simply adding the two values together. With that said, we were still successful in creating and implementing the carry lookahead adder, and, if given access to different hardware, we would be able to lower the execution time for the addition.

V. Source Code

```
MOV 40H, #00H
MOV 41H, #00H
MOV 42H, #00H
MOV 43H, #00H
                                          ; Input A
              MOV 44H, #00H
MOV 45H, #00H
MOV 46H, #00H
MOV 47H, #00H
              MOV 48H, #00H
MOV 49H, #00H
MOV 4AH, #00H
MOV 4BH, #00H
MOV 4CH, #00H
MOV 4DH, #00H
                                        ; Input B
              MOV 4EH, #00H
MOV 4FH, #00H
              MOV R2, #8H ; Length of longest operand in bytes
              MOV R0, #40H
MOV R1, #48H
MOV A, R2
MOV R5, A
                                         ; length of operands stored in R2
SETUP: MOV SCON, #10000010B
MOV TMOD, #00010000B
              MOV TL1, #00H; start timer at 0
MOV TH1, #00H; start timer at 0
INPUTA: JNB TI. $
                                        ; wait until ready to transmit
              CLR TI
MOV A, @R0
MOV C, P
MOV TB8, C
                                         ; set odd parity bit
; output byte of A
; move to next byte
              MOV SBUF, A ;
INC R0 ;
DJNZ R5, INPUTA
              MOV R0, #40H
                                       ; reset to beginning of A
MOV A, R2
MOV R5, A
INPUTB: JNB TI, $
CIR TI
MOV A, @R1
MOV C, P
                                        ; reset counter
                                        ; wait until ready to transmit
              MOV TB8, C ;
MOV SBUF, A ;
INC R1
DJNZ R5, INPUIB
                                        ; set odd parity bit
; output byte of B
                                        ; reset to beginning of B
              MOV R1, #48H
              SETB TR1
                                         ; start timer
              MOV A, R2
MOV R5, A
MOV A, @R0
MOV R4, A
MOV A, @R0
XRL A, @R1
MOV @R0, A
                                         ; init counter
                                         ; temp hold for byte of R6 data
              MOV A, @R1
ANL A, R4
MOV @R1, A
              INC R0
INC R1
                                         : move to next bit of P
                                          ; move to next bit of G
              DJNZ R5, LOAD
              MOV A. R2
                                        : reset R5
              MOV R5, A
CLR C
MOV A, R2
                                        ; C will be used as Ci in boolean equation
              MOV A, R2
DEC A
ADD A, #40H
MOV R0, A
MOV A, R2
DEC A
ADD A, #48H
MOV R1, A
                                         ; point at least significant byte
                                         ; point at least significant byte
CARRY: MOV B, @R1
MOV A, @R0
MOV R4, #81
MOV 0D6H, C
BITE: ANL C, 0E0H
ORL C, 0F0H
                                          ; set counter for 8 rotations
                                         ; store carry—in
; intermediate = Ci AND P(i+1)
              MOV 0F0H, C
RR A
MOV @R1, A
MOV A, B
                                          ; save Ci into C as well as R3.0
                                           save Ci into C as well as F
rotate P byte
store P byte in men
move G/C to A for rotation
rotate G/C byte
replace byte in R3
reload P from men
              RR.A
              MOV B, A ; replace byte in R3
MOV A, @R1 ; reload P from mem
DINZ R4, BITE ; repeat for whole byte
              MOV A, B
MOV 0D5H, C
CLR C
                                        ; store carry-out
              RLCA ; rotate C/G string to align carrys over correct bits MOV C, ODSH ; restore carry—out JNB ODSH, NOINC INC A
                                        ; increment if there was a carry—in
NOINC MOV@R1, A
                                         ; replace C/G in memory
              DEC RO
              DEC R1
              DJNZ R5, CARRY
              MOV R0, #40H
MOV R1, #48H
MOV A, R2
MOV R5, A
                                        ; return to beginning of P
; return to beginning of C/G
```

MOV A, @R0 XRL A, @R1 MOV @R0, A SUM: ; compute final sum ; move to next bit of P ; move to next bit of Carry string INC R0 INC R1 DJNZ R5, SUM : stop timer CLR TR1 ; wait until ready to transmit TIME: JNB TI, \$ JNB TI, \$
CLR TI
MOVA, THI
MOVC, P
MOVTB8, C
MOVSBUF, A
JNB TI, \$
CLR TI
MOVA, TLI
MOVC, P
MOVTB8, C ; set odd parity bit ; output high byte of time ; wait until ready to transmit ; set odd parity bit MOV TB8. C. MOV SBUF, A ; output low byte of time MOVA, R2 MOV R5, A MOV R0, #40H JNB TI, \$ reset R0 to beginning of result string OUT: ; wait until ready to transmit CLR TI MOV A, @R0 MOV C, P MOV TB8, C ; set odd parity bit ; output byte of result MOV SBUF, A INC BO DJNZ R5, OUT FLUSH: MOV A, #FFH MOV C, P MOV TB8, C MOV SBUF, A ; output dummy byte to flush output END

References

 Franz, S. and Dieter, S. Parallel binary carry look-ahead adder system. [US Patent 3,700,875]. https://www.google.com/patents/US3700875 1972.