# Department of Computer Science Duale Hochschule Baden-Wurttemberg Stuttgart



# Mission impossible: Disproving failed conjectures

### **Bachelor Thesis**

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This	is	to	certify	that:

- (i) the thesis comprises only my original work toward the Bachelor Degree
- (ii) due acknowlegement has been made in the text to all other material used

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# Acknowledgments

# Abstract

**Keywords:** Automated Theorem Proving, Model Construction, Effectively propositional logic, Range Restricting Transformations, Theorem Prover E, Bachmair and Ganzinger Model Construction Technique.

# Contents

A	cknov	wledgn	nents	III
1	Intr	oducti	on	1
2	Bac	kgroun	$\mathbf{1d}$	3
	2.1	First o	order logic (FOL)	3
		2.1.1	FOL overview and Example on it	4
		2.1.2	Decidability of FOL	4
		2.1.3	Universe of FOL	5
		2.1.4	Equality	5
	2.2	Effecti	vely propositional calculus (EPR)	5
		2.2.1	What is EPR	5
		2.2.2	Example on EPR	6
		2.2.3	Decidability and Universe of EPR	6
		2.2.4	Equality in EPR	6
	2.3	Proble	em Set	7
	2.4	The th	neorem prover E	9
		2.4.1	What is E	9
		2.4.2	What can E do	9
		2.4.3	The Code flow of E	9
		2.4.4	Latest results	10
3	Met	hodolo	ogy and Implementation	11
	3.1		formations	11
		3.1.1	Original transformations	11
		3.1.2	Simplified transformations	15
	3.2	Model	Construction	18
	3.3		FLow	23
4	Rela	ated W	Vork	25
	4.1		ent theorem provers	26
	4.2		Construction Techniques	26
	4.3		competition	27
	4.4		reasoning Techniques	30

	4.5	Range	Restricting Transformations	31
5	Test 5.1 5.2	Simpli: 5.1.1 5.1.2	alidation and Evaluation fied Transformations	32 32 33 33 33 33
6	<b>Res</b> : 6.1		g for termination	<b>34</b> 34
7	Con	clusion	1	36
8	Futu 8.1 8.2	8.1.1 8.1.2 8.1.3 8.1.4	nentational Future Work Extension for Transformations Adding Splitting Techniques Implement Other Model Construction Techniques More on Bachmair and Ganzinger Model Construction Technique and Evaluational Future Work Testing on a Server More Testing on the Transformations More Testing on the Bachmair and Ganzinger Model Construction Technique	37 37 37 38 38 38 38 38
Aı	ppen	$\operatorname{dix}$		40
A	List List	of Abbrof Figut	reviations	41 42 43 44
В	Syn	tax of	FOL	45
$\mathbf{C}$	Imp	lement	cation Details	47
D	Res	ults De	etails	48
Re	eferei	nces		57

# Chapter 1

# Introduction

Constructing Models has a huge importance in many fields specially in debugging tasks. It helps in modelling and highlighting the existence of bugs. And because of this it is used extensively in the field of Software and Hardware verification, also in analyzing and verifying Theorems.

So a concrete example to show its importance is the verification of Timsort algorithm, which was explained in details here [1]. Timsort is a hybrid sorting algorithm that was developed in 2002. It combines merge sort and insertion sort. And it was developed in the beginning to be used in python, but later on it was added to java. And today in Open JDK, Sun's JDK, and Android SDK it is the default sorting algorithm since it showed a great performance over real data. That resulted in using it in billions of devices because of the popularity of those platforms. In 2015, a formal verification for Timsort was tried to be done by a team using KeY, a verification tool for java programs that could be found here <a href="http://www.key-project.org/">http://www.key-project.org/</a>. And their analysis showed that the TimSort algorithm was broken and they found a bug and they corrected it, then after that they were able to formally verify the correction of the algorithm. And all the happened by the help of KeY. So it is really beneficial to be able to have models.

Having that importance in mind, we needed in this project to have an explicit model given to user when running problems on the theorem prover E, specifically for a sub-class of FOL named EPR. And in order to achieve that goal, Transformations have been applied to the problem specification to transform it to a certain form, namely range restricted form. Afterwards, Bachmair and Ganzinger Model Construction Technique is applied to extract the explicit model from the saturated set of the problem specification.

So a discussion of the work done will be given in the following order. We will have a background on the topic in chapter 2. Then in chapter 3 we will discuss the methodology followed and the implementation. Then an overview of related work will be

2

in chapter 4. Afterwards in chapter 5 we will explain the procedures followed to test the accuracy and efficiency of the implemented techniques. Moreover, A discussion of the results will be found in chapter 6. Then a conclusion will be given in chapter 7. And last but not least a discussion for related future work will be in chapter 8.

# Chapter 2

# Background

This chapter is devoted for introducing and familiarizing the reader to the theoretical concepts behind this project, and give the reader a background on the theorem prover E as well. So it will include the following sections:

- A background on First order logic (FOL) in section
- A background on Effectively propositional calculus (EPR) in section
- A background on E in section
- A background on Problem set in section

# 2.1 First order logic (FOL)

FOL, which is also known as first order predicate logic, is an expressive logic that allows us to formulate and encode most of our spoken language sentences in a defined way such that it could be further handled with rules such as simplification, inference rules. That allows automating the reasoning for FOL problems.

In order to have a general background on the topics of FOL, we will devote this section to that mission. So we are going to discuss the following points:

- Summary over FOL and Example on using it
- Decidability of FOL
- Herbrand Universe
- Equality

### 2.1.1 FOL overview and Example on it

### Overview on FOL

Quantifiers, variables, and functions are what signifies FOL over propositional logic. Having functions and being able to formulate "some", "all" is what added a lot to the expressiveness of FOL. So a review on the syntax and the structure of FOL, if needed, will be found here in appendix B.

### Example on FOL

A very famous example on FOL is the following:

Listing 2.1: Example on FOL

We want to formulate the following three sentences in FOL:

- (1) All Humans are mortals.
- (2) Socrates is a human.
- (3) Therefore, Socrates is mortal.

So in FOL syntax they are:

- (1)  $\forall X(Human(X) \rightarrow Mortal(X))$
- (2) Human(socrates)
- (3) Mortal(socrates)

Where *Human* and *Mortal* are predicates here since they represent properties over the elements of the domain. While *socrates* is a function symbol with arity 0 or in other words a constant

### 2.1.2 Decidability of FOL

The Problem of proving validity, or in other words unsatisfiability, of a formula in First order logic (FOL) had a lot of attention and experiments in the beginning. A lot of trials were made to prove that it is decidable as mentioned in [6]. But those trials were not successful. Later on, in the same year both [34, 7] proved that this problem in general is un-decidable.

Some algorithms were developed such that if the formula is unsatisfiable it will give a refutation, or proof in simpler words, however if it was not unsatisfiable then the algorithm may halt/terminate and give the correct result or may not halt/terminate at

all, so this problem is semi-decidable. An example for such procedure is resolution, with some refinements, in which its basic idea was first developed in [25]. So First order logic (FOL) is a semi-decidable logic.

### 2.1.3 Universe of FOL

Herbrand devised a procedure for generating the Universe of set of first order formulas; where the universe is the set of constants and grounded function symbols that represent terms in predicates. The procedure is defined recursively. So in most of the cases the Herbrand Universe of any set of first order formulas is infinite.

### 2.1.4 Equality

The Equality relation adds a lot of expressiveness and it is so intuitive to have it in logic. Adding equality to FOL is very beneficial such that it eases encoding problems to FOL, however it adds a burden for how it should be handled. So FOL with equality adds a distinguished predicate symbol = or  $\approx$  that represents equality to the set of predicate symbols. Moreover, it adds to the problem specification some axioms that helps in dealing with equality such as: reflexivity and symmetry.

In general, Equations are of the form:  $t1 \approx t2$ , Where each of the t1 and t2 is a term.

### 2.2 Effectively propositional calculus (EPR)

This section is discussing important points related to EPR, so the following points will be covered:

- subsection will explain what EPR is.
- Example on EPR will be given in subsection –.
- Universe and Decidability of EPR will discussed in subsection –.
- And last but not least in subsection we will talk about Equality in EPR.

### 2.2.1 What is EPR

Effectively propositional calculus (EPR) or sometimes known as Bernays-Schönfinkel class is a fragment of First order logic (FOL) in which all of its formulas follow the following format:

Listing 2.2: Format of EPR formula

$$\exists * \ \forall * \ F$$

where F is the formula.

Moreover, F has no proper functions symbols (all functions present are nullary ones "constants").

EPR fragment has a huge number of applications, e.g. Planning and Verification.

### 2.2.2 Example on EPR

Example for a formula in EPR:

Listing 2.3: Example for an EPR formula

$$\exists X \exists Y \forall Z (P(a, X, Y, Z))$$
.

Keeping ?? in mind, this will make every skolemized formula that originally was in EPR format have no proper function symbols. After transforming the above equation, it will be:

Listing 2.4: Example for a skolemized EPR formula

$$\forall Z (P(a,b,c,Z))$$
.

### 2.2.3 Decidability and Universe of EPR

Since the domain of EPR formulas contains only constants, and the number of constants in a formula is finite. So Herbrand universe of EPR formulas is finite. From that we could prove that EPR fragment is a decidable fragment in FOL, because of the finite number of ground interpretations it can have.

### 2.2.4 Equality in EPR

As we have mentioned before that EPR formulas will never contain proper function symbols. So terms will be one of two options:

- constant
- variable

And since Equality may be added to FOL as discussed in subsection –, then we should consider the case if the formulas are from the EPR fragment. Equations are in the following form  $t1 \approx t2$ , where t1 and t2 are terms. And since terms in EPR are only variables and constants. So the ground case of the Equation will contain only of constants. This result is important and we will refer to it later in chapter 3.

### 2.3 Problem Set

TPTP problems are first order problems, that are considered benchmarks to measure the performance of the different automated theorem provers. A description for TPTP could be found in [31], and the problem set could be downloaded from <a href="http://www.cs.miami.edu/~tptp/">http://www.cs.miami.edu/~tptp/</a>. TPTP problem set consists of different categories of problems, or divisions in other words, such as: PUZ, NLP, GRP. Those categories cames from the scientific meaning of the problems, e.g., NLP represents Natural language processing problems.

TPTP has its own language; TPTP for problems and TSTP for solutions. TPTP language could be written in two formats. The first of them is FOF, which is first order form. While the second form is CNF, which is clause normal form. Having a unified language for problems and solutions had a great impact on the field of Automated theorem proving (ATP). And this allows the integration of different ATP systems ,i.e., Automated theorem provers, since they have a specific language that could communicate in.

An example for a problem, i.e., GRP004-1 problem, from the TPTP problem set is given below in CNF format:

Listing 2.5: GRP004-1.p problem

```
%-
% File
            : GRP004-1 : TPTP v6.1.0. Released v1.0.0.
\% Domain
            : Group Theory
\% Problem
            : Left inverse and identity => Right inverse exists
% Version
            : [Cha70] axioms : Incomplete.
% English
            : In a group with left inverses and left identity every element
%
              has a right inverse.
% Refs
              [Luc68] Luckham (1968), Some Tree-paring Strategies for Theore
%
               [Cha70] Chang (1970), The Unit Proof and the Input Proof in Th
%
              [CL73]
                       Chang & Lee (1973), Symbolic Logic and Mechanical Theo
% Source
            : [Cha70]
% Names
            : Example 3 [Luc68]
%
            : Example 4 [Cha70]
%
            : Example 4 [CL73]
%
            : EX4 [SPRFN]
% Status
            : Unsatisfiable
            : 0.00 \text{ v}5.4.0, 0.11 \text{ v}5.3.0, 0.10 \text{ v}5.2.0, 0.00 \text{ v}2.1.0, 0.00 \text{ v}2
% Rating
    .0.0
% Syntax
            : Number of clauses
                                                  0 non-Horn;
                                                                  3 unit;
                                                                             3 RR)
                                           5 (
%
              Number of atoms
                                           11
                                                  0 equality)
%
              Maximal clause size
                                            4 (
                                                  2 average)
%
              Number of predicates
                                                  0 propositional; 3-3 arity)
                                            1 (
%
              Number of functors
                                            3 (
                                                  2 constant; 0-1 arity)
%
              Number of variables
                                           15 (
                                                  1 singleton)
%
              Maximal term depth
                                            2 (
                                                  1 average)
% SPC
            : CNF_UNS_RFO_NEQ_HRN
% Comments: [Luc68] is actually the right to left version.
cnf(left_inverse, axiom,
    ( product(inverse(X),X,identity))).
cnf(left_identity, axiom,
    ( product(identity, X, X) )).
cnf(associativity1, axiom,
    ( ~ product (X,Y,U)
        product (Y, Z, V)
        product (U, Z, W)
     product(X,V,W))).
cnf(associativity2, axiom,
      \sim product (X,Y,U)
      \tilde{p} product (Y, Z, V)
      \tilde{\phantom{a}} product (X,V,W)
     product(U,Z,W)).
cnf(prove_there_is_a_right_inverse, negated_conjecture,
    ( ~ product(a,X,identity) )).
```

### 2.4 The theorem prover E

### 2.4.1 What is E

E is a fully automatic theorem prover for FOL with equality implemented in ANSI-C that was released in 1998. Moreover, It is a saturation-based theorem prover. The Calculus implemented in E is variant of the superposition calculus proposed in [2].

### 2.4.2 What can E do

Since superposition calculus is a refutation one. So the current state of E, that it could prove the un-satisfiability of set of axioms with the negation of the conjecture(s) by finding the empty clause, or returning the saturated set if the empty clause was not found and no more new clauses can be inferenced/simplified.

The returned saturated set is considered a model in the sense that it satisfies all the formulae in the give specification. However, an explicit model for the specification is not provided. Worth mentioning that it is not guaranteed in E to terminate/halt for EPR problems. This could be seen from the performance of E in EPR problems as it does not terminate in more than 50% of them.

### 2.4.3 The Code flow of E

This part is devoted from giving a brief on the main procedure in E. Figure 2.1 is a simplified version of the code flow in E.

### Code Flow of E

Take the input and transform its formulae to clausal normal form "CNF" by appling a clausification step on the problem.

Preprocess the transformed formulae to simplify them.

Select the suitable search parameters to the problem specification. And this is done by the automatic mode analyses.

Apply the saturation algorithm using the selected search parameters. And then return the saturation or the proof.

Obligatory steps

Optional steps

Figure 2.1: E Simplified code flow

### 2.4.4 Latest results

The latest results showed performance approaching 70% over all the CNF and FOF problems of the TPTP problem set and this is according to [27].

# Chapter 3

# Methodology and Implementation

Here in this chapter we will discuss the methods applied to extract an explicit model from an EPR problem specification. For how they are implemented using E's data structures and configurations, and how to run the program, please refer to chapter C in the appendix.

In order to achieve our goal, we had to transform the problems' clauses, which are the axioms of the specification and the negated conjectures (if found), to clauses in range restricted form through a simplified form of range restricted transformations. The original range restricted transformations and there simplified version will be discussed in section 3.1.

### 3.1 Transformations

The methods applied in the project to extract the models follows the transformations discussed in [4]. A brief on the original transformations will be given in 3.1.1.

Moreover, as mentioned before that this project is concerned with a sub-class of FOL which is EPR some simplifications to the transformations were made as the removed steps will have no meaning in the context of EPR problems. Those simplifications will be discussed in 3.1.2.

### 3.1.1 Original transformations

The original procedures discussed in [4] generally work for all sub-classes of FOL. Those procedures should be applied to a given set of axioms in a specific form called implication form, sometimes it is called a sequent as in here —ref—, which is explained here –, and here – to know how to transform to that form. Moreover, those transformations are guranteed to terminate for any given problem set, which is a gain for us since most of the EPR problems were not terminating in the original configurations of E.

### What are the Transformations

The Transformations are series of procedures, mainly about changing the clauses to certain form named range restricted form. Since the transformations deal with clauses in implication form, then we could define Clauses in range restricted form to be clauses in which all the variables that appear in the succeedent must exist in the anticedent as well.

An example for a range restricted clause is found below:

Listing 3.1: Range Restricted Clause Example

```
\forall X \forall Y (P(X) \land Q(Y) \longrightarrow R(X,Y)).
```

where the **antecedent** here is  $P(X) \wedge Q(Y)$ ; whereas the **succeedent** is R(X,Y).

### How do the transformations work

**Transformations** add a domain predicate to the specification that will help in finding the Model by saying what are the elements of the domain, or the elements of the universe in other words.

Moreover, There are three types of procedures in the transformations:

### • Range restricting transformations

are the first two transformations, and they are the most important type of them. All the rest were added to enhance and improve the range restricting ones. They are responsible for transforming the input clauses to the range restricted form and enumerating the universe/domain of the problem in a way or another. Only one of the two transformations should be applied, since they perform the same functionality but in different ways. The two transformations are:

- Classical Range Restricting Transformation (CRR): it enumerates the Herbrand Universe in a naive simple way.
- Range Restricting Transformation (RR): it was introduced to improve the naive implementation of the CRR. So it only adds elements to the domain only when it is needed.

### • Shifting transformations

are the second two transformations. They are optional to be used. They complement one another not replace each other. They were introduced mainly to prevent the non-termination of the transformations and to prevent generating redundant and unpleasant clauses from the steps in RR as well. And the two shifting transformations are:

- Basic Shifting Transformation (BS)
- Partial Flattening Transformation (PF)

### • Blocking Transformation (BL)

is the last transformation and it is optional as well. And It was introduced to detect periodicity that may occur because of function terms.

### Their order of application is:

- 1. One of the two range restricting CRR or RR
- 2. The Partial Flattening PF
- 3. The Basic Shifting BS
- 4. The Blocking BL

Where the output of a lower number transformation is the input to the higher one. A Flow Chart that summarizes what was explained will be found in Figure 3.1.

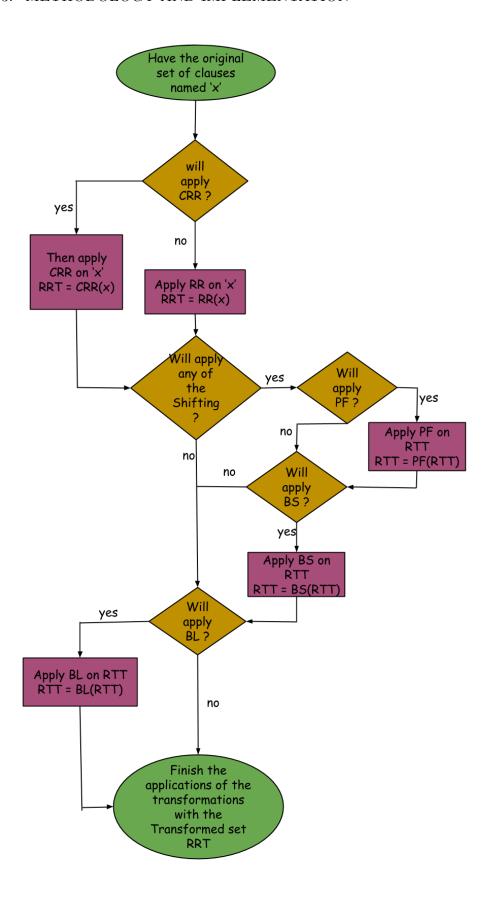


Figure 3.1: Flow of the original transformations

### 3.1.2 Simplified transformations

**This subsection** is concerned about discussing the simplifications that were added to the original transformations, that was explained in subsection 3.1.1. So this subsection will cover the following points:

- The reason for doing such simplifications.
- What are the Simplifications.
- The resulted simplified transformations.
- Examples for the Output of the transformations, or let's name it Intermediate Output.
- Discussion on the Output of the prover.

### The Reason for doing the simplifications

As mentioned before in subsection 3.1.1, the original transformations is generic for all sub-classes of FOL. So naturally it contains many steps that deals with proper function symbols. However, what concerns us in this project is only the EPR sub-class of problems. And by keeping in mind the definition of EPR as mentioned here in 2.2.1, and by knowing that there is no existence of proper function symbols, and that there won't be even after the skolemization step in any EPR problem, So implementing the original transformations, as they were, didn't seem logical as it won't be used in any of the problems, and it would take much more time to implement it practically. So those were the motives for having such simplifications.

### What are the steps of the simplifications

The simplifications made were very simple, and they were applied to all procedures of the original transformations. The steps of the simplifications are:

- 1. Every step that only deals with proper function symbols is removed since they are not existing in EPR. Ex.: some steps in CRR and RR that loops on all the proper function symbols in the given problem.
- 2. Any step or procedure that was introduced because of the existence of proper function symbols in problems were removed as well. Ex.: BS, PF, and BL.

### The resulted simplified transformations

**After applying** the simplifications to the procedures of the transformations, the following steps were the only needed:

- Some steps in CRR.
- Some steps in RR.

For a chart representing the original CRR and what is removed from it, you can view Figure 3.2, while Figure 3.3 is for RR. And for a detailed explanation for the steps, you can check [4].

# Add the domain predicate to the signature of the problem & add a positive literal of that domain predicate to the set of clauses representing the problem Range restrict the unrestricted clauses Enumerate the Herbrand Universe by looping on the proper function terms in the signature and adding a rule for each of them remained after the simplifications removed after the simplifications

Figure 3.2: Original CRR with the kept and removed steps after the simplifications

The Steps of the original RR

### Add the domain predicate to the signature of the problem & add a positive literal of that 1 domain predicate to the set of clauses representing the problem. Add the domain elements from the Clause bodies by looping on the predicates in the antecedent of each clause and add their arguments. 3 Range restrict the unrestricted clauses. Add a rule to add domain elements of the 4 predicates found in the signature. Add a rule to add domain elements of the 5 proper function terms found in the signature. remained after the simplifications removed after the simplifications

Figure 3.3: Original RR with the kept and removed steps after the simplifications

### The Intermediate output

Here we name the output of applying the simplified transformations on a set of (counter) satisfiable set of clauses an **Intermediate output**, since the Output should be the returned explicit (counter) model. So In this part we give an example for a problem, and then show what is the Intermediate output of that problem from CRR, and RR.

Listing 3.2: Satisfiable CNF problem Example

Listing 3.3: CRR output Example

Listing 3.4: RR output Example

### Discussion on the Output of the prover

After applying the transformations on the clauses of a given problem, then this Intermediate output should be given as input to the normal proof procedure in E. And the final output for a (counter) satisfiable problem should be the saturated set, from which the explicit model should be extracted easily. However, this wasn't the case while running the problems, and the explicit model wasn't clear in the saturated set.

So a Model Construction Technique for saturation-based theorem provers was applied to the saturated set. And that Technique will be discussed in the following section 3.2

### 3.2 Model Construction

A Model Construction Technique had to be applied to the saturated set of clauses as discussed in the part related to the discussion on the output of the prover when the input was the range restricted version of the original set of clauses, and that was explained in subsection 3.1.2. Here in this section we will cover the following points:

- What is the Model Construction Technique used
- How does it work
- Discussion on the Output

### What is the used technique for Model Construction

The Model Construction Technique used is specific for resolution based theorem provers, and it is the ground positive case of Bachmair and Ganzinger Model Construction Technique that was devised here in [18]. This technique originated from the proof of Bachmair and Ganzinger that their resolution based theorem proving technique is complete. That proof will be found in [3].

### How does Bachmair and Ganzinger Model Construction Technique works

The chosen and implemented Bachmair and Ganzinger Model Construction Technique works for a saturated (counter) satisfiable set positive ground set of clauses. That has been generated using an ordered resolution system with simplification.

This Technique needs a term ordering that has been lifted to literals then lifted to clauses. That clause ordering should be total on ground clauses, and it should be the same one used in the saturation procedure.

### The algorithm works as follows:

- 1. sort the positive ground clauses using the ordering in an ascending order
- 2. sort the literals in each clause to define the maximal literal
- 3. for each of the clauses starting from the smaller in terms of the ordering if not already true by the chosen true literals, then add the its maximal literal to the set of the chosen true literals

A pseudo-code for the implemented version of the algorithm is given below:

Listing 3.5: Ground Positive Case for Bachmair and Ganzinger Model Construction

```
Input: clauses_set % saturated set of clauses
        , ordering % ordering used in the saturation
{
       % model is the set of positive literals in the
       % constructed model, at the beginning it is
       % an empty set of literals
        model = \{\}
       % this sorts the set of clauses ascendingly
        sort_clauses(clauses_set, ordering)
       % it marks the maximal literal in each clause
        mark_maximal_literals(clauses_set, ordering)
        for clause:clause_set do:
         % here it checks whether the current clause
         % is true by the partial model we have or not
          if not is_clause_true_by_model(clause, model) then:
                % if not true yet the it gets the marked
                % maximal literal and adds it to model
                model = model + get_maximal_literal(clause)
          end_if
        end_{-}for
Output: model
```

**An Example** for applying the Bachmair and Ganzinger Model Construction Technique is given below:

Listing 3.6: Example for applying Bachmair and Ganzinger Model Construction Technique

```
Let the unordered saturated set of clauses be:  \{ & R(a,b)|Q(b)\,, \\ P(a)\,, & P(a)|Q(b)\,, \\ R(b,b) \}  Let the order of the present clauses:  \{ & P(a) < Q(b) < R(a\,,\,b) < R(b\,,\,b) \}  % the left most literal in each of the % ordered clauses is the maximal
```

Table 3.1: Table to test captions and labels

```
Then the explicit Model:  \{ \\ P(a) \, , \\ R(a,b) \, , \\ R(b,b) \\ \}
```

### Discussion on the Output

The output of the Model Construction Technique is the final one. It gives back the positive literals in the constructed explicit model. An Example for the output is given below in 3.7.

Listing 3.7: Example for the returned Model

```
dom(t).
bird(t).
fly(t).
```

Moreover, we augmented the output with a visual part. It prints out a dot graph representing the positive clauses linked with the positive literal, that belongs to the model, that makes them true or satisfiable in other words. Example of the returned dot graph will be listed in 3.8, and a rendered Figure for the same graph will be in 3.4.

Listing 3.8: Example of returned dot graph

```
digraph model {
 rankdir=LR;
subgraph cluster_model {
  label="Model";
 0 [shape=ellipse, fillcolor=lightskyblue1, style=filled, label="
     fly(t)"]
 1 [shape=ellipse, fillcolor=lightskyblue1, style=filled, label="
     bird(t)"]
 2 [shape=ellipse, fillcolor=lightskyblue1, style=filled, label="
    dom(t)"]
subgraph cluster_clauses {
 label="Positive Ground Clauses";
 3 [shape=box, fillcolor=lightpink1, style=filled, label="cnf(
     i_0_3, plain, (fly(t))."
 3 -> 0
 4 [shape=box, fillcolor=lightpink1, style=filled, label="cnf(
     i_0_1, plain, (bird(t))."
 4 -> 1
 5 [shape=box, fillcolor=lightpink1, style=filled, label="cnf(
     i_0_2, plain, (dom(t))."
 5 -> 2
 }
```

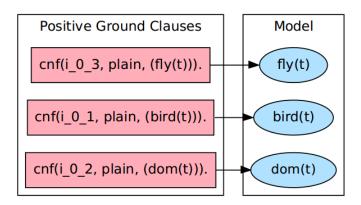


Figure 3.4: Rendered dot graph of Model

### 3.3 Code FLow

**So a small summary** for the flow of the code is given below, and simplified flow chart is in Figure 3.5:

- 1. The input is an EPR (counter) satisfiable problem.
- 2. Simplified Range Restricted Transformations got applied on the input.
- 3. The intermediate output from the transformations act as input for the normal proof procedure.
- 4. The output from the prover, which is the saturated set of clauses, is the input for the Bachmair and Ganzinger Model Construction Technique.
- 5. Then the final output is the positive literals of the explicit Model for the given problem.

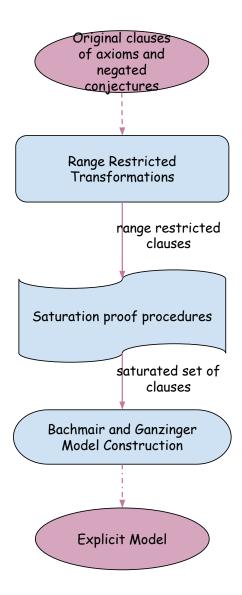


Figure 3.5: Simplified Flow chart for the code flow

# Chapter 4

# Related Work

Automated Theorem Proving has many applications in various fields, e.g., Mathematical Reasoning, Knowledge Representation, Planning and Scheduling. First we mention a defintion for ATP, according to [17], we could define ATP to be "is the use of a computer to prove to prove non-numerical results, i.e. determine their truth (validiy)".

The main process in automated theorem proving is proving the validity of a conjecture given a set of axioms, or if we are talking from the context of refutation-based theorem proving then the main process is proving the unsatisfiability of a given specification. And a lot of work and research was done to develop and enhance different calculi for that process.

The dual task for proving, or process in other words, is disproving, where a (counter) model is returned from the disproving procedure. Despite of the importance of the disproving process, less work ,compared to the proving process, were devoted for its development.

In this chapter we will discuss the related work to the topic and bit of literature review over it. So it divied into the following sections:

- Different Theorem provers
- Model Construction Techniques
- CASC competition
- Reasoning in EPR
- More on Range Restricting Transformations

### 4.1 Different theorem provers

A lot of classifications can be done to automated theorem provers. One may target the different calculi applied by each of them such as Model Evolution Calculus as applied in Darwin for example or Instantiation-based theorem provers as in iProver or Resolution based as implemented in E.

Other classification may target the output of each, where a distinction between the goal of each prover is considered. E.g., E is a refutation-based theorem prover that proves unsatisfiability, or in simpler words it proves the validity of a conjecture. However, The main goal for iProver is to give a (counter) model for unvalid conjectures. It is notable to say that some automated theorem provers give both output according to the given problem.

Another Taxonomy for automated theorem provers relies on whether they are fully automated or interactive. Interactive automated theorem provers needs hints from human beings, however in the case of fully automated theorem proving no assistance is needed from humans. An example for a fully automated one is E, Vampire and Dawrin. On the other hand, IMPS [9] is an interactive example for a proof system.

### 4.2 Model Construction Techniques

Model Construction, or building, can be done using different approaches that depends on the type of logic it relates to. E.g., A very famous procedure for propositional logic is DPLL algorithm, which stands for Davis-Putnam-Logemann-LoveLand algorithm, it is mainly used to decide the satisfiability of a logical formula. In propositional logic, this problem can be reduced to the SAT problem, boolean satisfiability problem. Model evolution calculus is another example that its idea is based on DPLL, however it lifts DPLL in order to be applied for first order logic problems.

Another technique that is applied is Instantiation-based techniques, where it applies instantiation on the active clauses and then give the grounded set to a SAT solver, if the SAT solver detected the un-satisfiability of the clause set then it terminates, however if not then it generates new clauses using inference rules then repeats the whole process until saturation is reached.

Another set of tool that helps in the process of Model Generation, are Model finders. The functionality of those type of tools is mainly giving back a model for a satisfiable set of clauses with specifying the number of domain elements that you need to find for. Those tools is used for example in some Model evolution based theorem provers such as FM-Darwin.

There are different styles of model finders such as MACE-style and SEM-style model finders. MACE-style model finders work by transforming the first order problem to an equivalent propositional one considering the size of the domain while doing the transformation. And then use a SAT-solver on the transformed set. On the other hand,

SEM-style model finders depends on searching and backtracking. An example for a MACE-style model finder is Paradox. However, Finder is an example for a SEM-style model finder. [8]

### 4.3 CASC competition

Nowadays, Automated theorem provers have a yearly competition named CASC competition [21, 29]. It is held on CADE or IJCAR conferences. In CASC different automated theorem provers compete to prove its efficiency over other theorem provers. The CASC competition's problems are chosen from the TPTP problem set. There are various division in the Competition, e.g. FOF, which is first order form non-propositional theorems, another one is SAT, which is clause normal form really non-propositional non theorems. The criteria for judgement is average time needed to solve problems, the number of solved problems, the numbers of problems solved + a solution output . Each division has its own contestants, and its own winners.

An Important division in the CASC competition, that is so related to that topic, is the EPR division, which represents effectively propositional clause normal form theorems and non-theorems. Moreover, EPR division has two sub-divisions, and they are:

- EPT: which have the theorems related problems, or in other words the unsatisfiable set of problems.
- EPS: which have the non-theorems, that is the satisfiable problems.

The latest CASC competition, that was CASC-J7, was held during the 7th International Joint Conference on Automated Reasoning (IJCAR) on 20th July 2014 <a href="http://cs.nyu.edu/ijcar2014/">http://cs.nyu.edu/ijcar2014/</a>. The latest results for the EPR division is summarized in the following Figure 4.1:

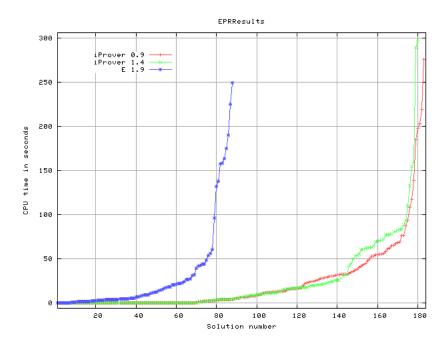


Figure 4.1: EPR division results taken from http://www.cs.miami.edu/~tptp/CASC/J7/WWWFiles/ResultsPlots.html

Moreover, latest results for the sub-divisions of EPR is given in Figure 4.2; where sub-figure 4.2b shows the EPS results, while sub-figure 4.2a shows the EPT results. And Table 4.1 is a summary for the results.

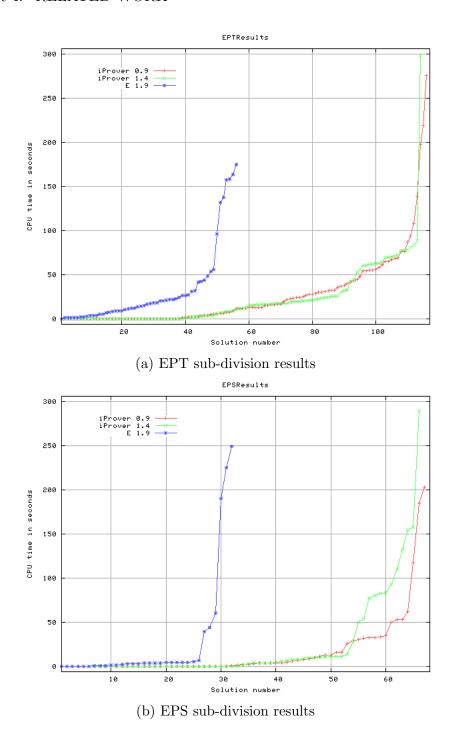


Figure 4.2: EPR sub-divisions results both taken from http://www.cs.miami.edu/~tptp/CASC/J7/WWWFiles/ResultsPlots.html

	88
	00
Average-CPU-time   22.96   22.80   31	1.02
Solutions 62 174	88
New-Solved $(10)$ 10 9	5

Table 4.1: Summary for EPR division results

### 4.4 EPR reasoning Techniques

Reasoning in EPR is very interesting, since it is a fragment of FOL that could be transformed to propositional logic with some processing such as grounding techniques. So both reasoning techniques done for FOL and propositional logic are valid for EPR fragment, however for the propositional case further handling will be required.

According to [20], we could classify some of the methods used in reasoning for EPR fragment into two categories:

- Grounding based methods, which are mainly techniques applied to limit the number
  of generated clauses in the grounding step, afterwards normal methods of reasoning
  for propositional calculus could be applied as the EPR problem will be reduced to
  a propositional one. Some of those grounding based methods are mentioned below:
  - Splitting
  - Pure Predicates
  - Linking restrictions
  - Sort inference
  - Incremental Search
- Non-grounding based methods, which are methods using normal inference systems and calculi used for generic FOL.
  - Resolution Calculus, which was first proposed in [25]
  - Model evolution Calculus, which was proposed by [5]
  - Instantiation Calculus, which was proposed in [12]

Resolution is the oldest one of all the three calculi. In the beginning the results mentioned in [13] showed that it is difficult to be able to decide EPR fragment using a resolution procedure. Later on, a resolution procedure was found to be able to decide EPR [10]. However, resolution is inefficient at least practically for EPR and this could viewed from the results of the EPR division in the yearly CASC competition.

Model evolution calculus has the same decidability for FOL as resolution with saturation as proposed here in [3]. So it is refutationally complete and sound. But it has an advantage over resolution, since it is in general a decision procedure for EPR fragment, however this is not the case with most resolution procedures. And practically the automated theorem provers that implement the Model evolution calculus have better results in the CASC competition for EPR division.

Instantiation Calculus has the same decidability for FOL as resolution with saturation and model evolution calculus. And it is decision procedure for EPR fragment like Model evolution calculus. And the automated theorem provers that depends on Instantiation calculus have a very good results in the CASC competition for the EPR division [32, 33], at least the first on this division in the last CASC competition. CASC-J7. is an Instantiation based theorem prover.

Table 4.2 found below summarizes the comparison between the three Non-grounding methods for reasoning in EPR.

Point of Comparison	Resolution	Model Evolution	Instantiation
Relatively New	No	Yes	Yes
Semi-decidable for FOL	Yes	Yes	Yes
Decidable for EPR	No, in general	Yes	Yes
Practically proved efficiency in EPR division	No	Yes	Yes
Example for Prover	E	Darwin	iProver
II			

Table 4.2: Summary for Non-grounding methods for reasoning in EPR

#### 4.5 Range Restricting Transformations

According to [4], The range restricted transformations implemented in this project, that was originally devised in [4], were also added to other theorem provers MSPASS and KRHyper. And the results showed improvement and effectiveness in trying them over the satisfiable set problems in TPTP, specifically Version 3.1.1.

## Chapter 5

# Testing, Validation and Evaluation

Here in this chapter, we explain what was done for validating the output and Evaluating the program. So we divide this chapter into two sections:

- Validating and Evaluating the Simplified Transformations.
- Validating and Evaluating the Implementation of Bachmair and Ganzinger Model Construction Technique.

#### 5.1 Simplified Transformations

#### 5.1.1 Evaluating Memory Efficiency

The first part of the implementation which is related to applying the transformations to the the clause set introduces no memory leaks to the whole program.

Tools to check this:

1. Script implemented in E for giving a summary on the allocated and de-allocated memory structures, and the results showed that they are equal.

2. Tool named 'valgrind' which also showed the same results as the above script.

#### 5.1.2 Accuracy of the transformations

In all tested problems, The results of the Transformations were the same as an implemented program called Yarralumla http://users.cecs.anu.edu.au/~baumgart/systems/yarralumla/, implemented by Peter Baumgartner, one of the authors of [4]. So we believe it is correct.

# 5.2 Bachmair and Ganzinger Model Construction Technique

#### 5.2.1 Evaluating Memory Efficiency

The same tools mentioned for The Transformations in 5.1.1 part were used. And the same results were achieved for the Implemented Model Construction Technique.

#### 5.2.2 Accuracy of Implementation

To Be added later

## Chapter 6

### Results

#### 6.1 Testing for termination

The tests ran over all the (counter) satisfiable EPR problems in TPTP v6.1.0, and they were 267 problem. Only 109 were terminated within 5 minutes time limit. Tables D.1 and D.2 show detailed results of running all the 267 problem with the time needed to terminate the problem.

6.1 pie chart shows the distribution of the terminated 109 problems with respect of rating of the problem.



Figure 6.1: Distribution of terminated problems over different ratings

Some random problems were chosen to be tested thoroughly. SYN867-1 was one of them that gave interesting and weird results. The normal problem specification given to the prover terminated, however, when the transformed set was given to the prover, it did not terminate till the 5 minutes passed. So this shows

## Chapter 7

### Conclusion

So we can conclude from the results of testing that the saturated output did not have a significant difference after applying the range restricting transformations for the problem specification. Most of the solved problems were almost range restricted problems from the beginning. So no clear benefit from the transformations were gained.

However, Something that was not tested thoroughly was the effect of termination in general for EPR problems since in testing a time limit of three minutes were given to halt if it did not achieve results before it. As it was mentioned before that resolution based reasoning systems do not guarantee termination. However, The transformations guarantee termination for EPR. So this needs to be checked out without a time limit.

At the end, Minimal explicit model was given after applying the Bachmair and Ganzinger Model Construction Technique for the saturated set. Another addition was the extension of Bachmair and Ganzinger Model Construction Technique to handle equality in EPR formulae.

## Chapter 8

### Future Work

This project has a fertile environment were many aspects could be added and extended in a simple way. And those points will be discussed in the sections of this chapter in details. Moreover, those points could be viewed in two different categories, the first of them is implementation view and it will be discussed further in section 8.1, while the other is a testing and evaluational view and this will be presented in section 8.2.

#### 8.1 Implementational Future Work

This section is devoted to discuss the related enhancements and implementations that could be added in E to achieve the goal of model construction. Most of those points will also help in evaluating the implemented technique in a way or another.

Some Points include modifications for the implemented part such as sub-section 8.1.1, while others will need a whole new implementation as in sub-section 8.1.4.

#### 8.1.1 Extension for Transformations

As discussed before the original transformations mentioned were simplified because it was only intended for EPR sub-class in FOL. So a great extension that could be done is to extend the transformations to all sub-classes of FOL instead of only EPR by adding the simplified steps in the implemented crr and rr procedures on one hand, and by adding the shifting and blocking transformations on the other hand.

#### 8.1.2 Adding Splitting Techniques

Another addition for that project that could be added is implementing splitting techniques. Since it was one of the limitations that did not make the implemented Transformations work on their own and needed further handling by augmenting it with the Bachmair and Ganzinger Model construction Technique.

So this could be done by adding a suitable splitting technique with backtracking, and in this case the Bachmair and Ganzinger Model Construction Technique won't be enabled, however another part for further handling would be needed to extract the explicit model from the saturated splitted set of clauses.

#### 8.1.3 Implement Other Model Construction Techniques

Augmenting E with other Model Construction Techniques would add a value for it. As well as, it will make us have a good evaluation on the implemented Bachmair and Ganzinger Model Construction Technique since we will have a meaningful comparison on the performance and the effect of each of the different techniques.

# 8.1.4 More on Bachmair and Ganzinger Model Construction Technique

Adding the General case for Bachmair and Ganzinger Model Construction Technique that deals with the non ground case for the saturated set of clauses, as explained here in [18], may have a good output since the transformations will not be used in this case and it will act directly on the saturated set without having them acting. And this will be a good research point to compare the effect of the transformations as a Model Construction Technique.

#### 8.2 Testing and Evaluational Future Work

Testing is very important to be able to evaluate any project. So the coming points are of a great importance to have a fair judgement on the implemented techniques and to discover the limitations of applying them in saturation-based theorem provers.

#### 8.2.1 Testing on a Server

Testing medium sized and large sized problems on a large server would be of a great importance. Since only a personal computer of 4 GB RAM were used in the testing so only small sized problems were able to run on it without crashing. And the results of these problems is important to have a full overview on the performance and the impact of the project specially on those problems in the EPR set that were not terminating in the original configurations. Only after that we could have a fair evaluation on the project.

#### 8.2.2 More Testing on the Transformations

More Testing on the Transformations is needed with consideration of the prover itself to know why the transformations alone did not perform what it was supposed to do. Then after knowing the reason that could be enhanced accordingly.

# 8.2.3 More Testing on the Bachmair and Ganzinger Model Construction Technique

Also More Testing on the implemented Bachmair and Ganzinger Model Construction Technique is of major importance at least to know the limitations of applying it in saturation-based theorem provers.

# Appendix

# Appendix A

# Lists

**FOL** First order logic

**ATP** Automated theorem proving

**EPR** Effectively propositional calculus

**CRR** Classical Range Restricting Transformation

**RR** Range Restricting Transformation

**BS** Basic Shifting Transformation

**PF** Partial Flattening Transformation

**BL** Blocking Transformation

# List of Figures

2.1	E Simplified code flow	10
3.1	Flow of the original transformations	14
3.2	Original CRR with the kept and removed steps after the simplifications .	16
3.3	Original RR with the kept and removed steps after the simplifications	17
3.4	Rendered dot graph of Model	23
3.5	Simplified Flow chart for the code flow	24
4.1	EPR division results taken from http://www.cs.miami.edu/\protect\unhbox\voidb@x\penalty\@M\{}tptp/CASC/J7/WWWFiles/ResultsPlots.html	28
4.2	EPR sub-divisions results both taken from http://www.cs.miami.edu/ \protect\unhbox\voidb@x\penalty\@M\{}tptp/CASC/J7/WWWFiles/Resulthtml	ltsPlots 29
6.1	Distribution of terminated problems over different ratings	34

# List of Tables

3.1	Table to test captions and labels	21
4.1	Summary for EPR division results	30
4.2	Summary for Non-grounding methods for reasoning in EPR	31
D.1	Results of Sat EPR TPTP problems	54
D.2	More Solved Sat EPR TPTP problems	54

# Listings

2.1	Example on FOL
2.2	Format of EPR formula
2.3	Example for an EPR formula
2.4	Example for a skolemized EPR formula
2.5	GRP004-1.p problem
3.1	Range Restricted Clause Example
3.2	Satisfiable CNF problem Example
3.3	CRR output Example
3.4	RR output Example
3.5	Ground Positive Case for Bachmair and Ganzinger Model Construction . 20
3.6	Example for applying Bachmair and Ganzinger Model Construction Tech-
	nique
3.7	Example for the returned Model
3.8	Example of returned dot graph

## Appendix B

## Syntax of FOL

#### Syntax of FOL

The syntax of FOL consists of:

- Predicates, which is a mapping for properties in a language. Moreover, the symbols used for representing predicates are finite and specific for each problem.
- Terms, which consists of functions and variables as shown below:
  - Functions, which itself can be divided according to the arity of the function symbol as follows:
    - \* if (arity == 0), then it is considered a constant
    - \* if (arity > 0), then it is a proper function symbol
  - Variables, and they are infinite list of symbols
- Special symbols
  - $-\perp$  which represents false
  - $\top$  which represents true

Atoms which are the basic building blocks of a formula, follow the following format:

where p is a predicate symbols, any ti is a term, and k is the arity of the predicate symbol p. A Literal is an atom or a negated atom. A formula consists of only one atom is called an Atomic formula.

Compound formulas are formed by:

• Connectives, and they are divided into:

 $- \rightarrow$ : implication

 $-\neg \text{ or } \sim : \text{ negation}$ 

 $- \vee \text{ or } | : \text{ disjunction}$ 

 $- \wedge \text{ or } \& : \text{ conjunction}$ 

 $- \equiv$ : equivalence

- Quantifiers, and they are the following two:
  - $\forall$  which is the universal quantifier
  - $\exists$  which is the existential quantifier

A Clause is a disjunction of Literals. A ground clause is a clause having no variables. A positive clause is a clause who has no negated atoms. While a negative clause is a clause who contains only negated atoms. A mixed clause is a clause who consists of both atoms and negated atoms. A unit clause is a clause containing one Literal.

# Appendix C

# Implementation Details

# Appendix D

### Results Details

Here in this chapter of the appendix, we give details for the results of the tests. For the tests, we had a bash script running the transformations in the beginning then the normal prover then the model extraction part. Also it prints the time taken by each step. Moreover, time limit of 3 minutes and memory limit of 1GB were given to the 2nd step which is the normal prover itself. Only 107 of the problems were able to terminate within the time limit. The tests were done on a server with 8 GB RAM and 8 CPUs.

The below table D.1 gives the details of running the script over all the (counter) satisfiable EPR problems:

Problem	rating	transformations t.	terminated	saturation t.	model extraction t.
GRP123-1.005.p	0.17	0.003s	no	_	-
GRP123-2.005.p	0.17	0.003s	no	_	_
GRP123-3.004.p	0.17	0.008s	yes	0.349s	0.014s
GRP123-4.004.p	0.17	0.004s	yes	2.023s	0.050s
GRP123-6.005.p	0.17	0.004s	no	_	_
GRP123-7.005.p	0.33	0.003s	no	_	_
GRP123-8.004.p	0.17	0.003s	yes	0.871s	0.029s
GRP123-9.004.p	0.17	0.003s	yes	0.506s	0.031s
GRP124-1.005.p	0.17	0.006s	no	_	_
GRP124-2.005.p	0.17	0.003s	no	_	_
GRP124-3.005.p	0.17	0.004s	no	_	_
GRP124-4.005.p	0.17	0.003s	no	_	_
GRP124-6.005.p	0.17	0.007s	no	_	_
GRP124-7.005.p	0.33	0.003s	no	_	_
GRP124-8.005.p	0.33	0.003s	no	_	_
GRP124-9.005.p	0.33	0.004s	no	_	_
GRP125-1.004.p	0.17	0.003s	yes	0.424s	0.014s
GRP125-2.004.p	0.17	0.003s	yes	0.081s	0.004s
GRP125-3.004.p	0.17	0.005s	yes	0.486s	0.007s

11 -		I	1	1	
GRP125-4.004.p	0.17	0.002s	yes	2.288s	0.030s
GRP126-1.005.p	0.17	0.004s	no	_	_
GRP126-2.005.p	0.17	$0.007\mathrm{s}$	no	_	_
GRP126-3.005.p	0.17	0.003s	no	_	_
GRP126-4.005.p	0.17	0.003s	no	_	_
GRP127-1.005.p	0.17	0.003s	no	_	_
GRP127-2.005.p	0.17	0.004s	yes	0.431s	0.004s
GRP127-3.005.p	0.17	0.009 s	no	_	_
GRP127-4.005.p	0.17	0.008s	no	_	_
GRP128-1.004.p	0.17	0.003s	yes	2.084s	0.032s
GRP128-2.004.p	0.17	0.002s	yes	0.337s	0.004 s
GRP128-3.004.p	0.17	0.003s	yes	0.806s	0.014s
GRP128-4.004.p	0.17	0.003s	yes	59.517s	0.096s
GRP129-1.005.p	0.17	0.002s	no	_	_
GRP129-2.005.p	0.17	0.008s	no	_	_
GRP129-3.005.p	0.33	0.004s	no	_	_
GRP129-4.005.p	0.17	0.002s	no	_	_
GRP130-1.005.p	0.17	0.002s	no	_	_
GRP130-2.005.p	0.17	0.004s	no	_	_
GRP130-3.004.p	0.17	0.006s	yes	2.495s	0.006s
GRP130-4.004.p	0.17	0.005s	yes	1 m 8.226 s	0.104s
GRP131-1.005.p	0.17	0.003s	no	_	_
GRP131-2.005.p	0.17	0.005s	no	_	_
GRP132-1.005.p	0.17	0.006s	no	_	_
GRP132-2.005.p	0.17	0.003s	no	_	_
GRP133-1.004.p	0.17	0.004s	no	_	_
GRP133-2.004.p	0.17	0.009s	no	_	_
GRP134-1.005.p	0.17	0.003s	no	_	_
GRP134-2.005.p	0.17	0.004s	no	_	_
GRP135-1.005.p	0.17	0.003s	no	_	_
GRP135-2.005.p	0.17	0.006s	no	_	_
HWC004-1.p	0.00	0.004s	yes	0.017s	0.002s
HWV042-1.p	0.50	0.017s	no	_	_
HWV042-2.p	0.67	0.013s	no	_	_
HWV048-1.p	0.50	0.012s	no	_	_
HWV048-2.p	0.83	0.017s	no	_	_
HWV049-1.p	0.67	0.019s	no	_	_
HWV049-2.p	0.67	0.020 s	no	_	_
HWV053-1.p	0.67	2.403s	no	_	_
HWV054-1.p	1.00	0.918s	no	_	_
HWV062-1.p	0.50	1.668s	no	_	_
HWV063-1.p	0.88	3.864s	no	_	_
HWV066-1.p	0.50	0.398s	no	_	_
HWV067-1.p	1.00	4.444s	no	_	_

HWV070-1.p	1.00	2.345s	no	_	_
HWV071-1.p	0.67	0.048s	no	_	_
HWV074-1.p	0.83	1.075s	no	_	_
HWV075-1.p	1.00	2.319s	no	_	_
HWV076-1.p	0.50	0.052s	no	_	_
HWV077-1.p	1.00	0.143s	no	_	_
HWV079-1.p	0.50	0.028s	no	_	_
HWV080-1.p	1.00	0.428s	no	_	_
HWV081-1.p	1.00	0.132s	no	_	_
HWV082-1.p	0.83	1.379s	no	_	_
HWV085-1.p	0.83	0.837s	no	_	_
HWV086-1.p	1.00	13.424s	no	_	_
KRS021+1.p	0.00	0.080s	yes	0.027 s	0.002s
KRS022+1.p	0.00	0.007 s	yes	0.017s	$0.007\mathrm{s}$
KRS023+1.p	0.00	0.005 s	yes	0.016s	0.004s
KRS024+1.p	0.00	0.003s	yes	0.018s	0.003s
KRS025+1.p	0.00	0.004s	yes	0.021s	0.002s
KRS026+1.p	0.00	0.005 s	yes	0.021s	0.002s
KRS027+1.p	0.00	0.004s	yes	0.012s	$0.009 \mathrm{s}$
KRS040+1.p	0.00	0.006s	no	_	_
KRS041+1.p	0.00	0.011s	yes	0.037s	0.003s
KRS053+1.p	0.00	0.010s	yes	0.017s	0.002s
KRS054+1.p	0.00	0.005 s	yes	0.023s	0.003s
KRS055+1.p	0.00	0.004s	yes	0.021s	$0.007\mathrm{s}$
KRS056+1.p	0.00	0.004s	yes	0.014s	$0.007\mathrm{s}$
KRS057+1.p	0.00	0.009 s	yes	0.022s	0.002s
KRS058+1.p	0.00	0.006s	yes	0.016s	0.008s
KRS059+1.p	0.00	0.004s	yes	0.017s	0.002s
KRS060+1.p	0.00	0.008s	yes	0.017s	0.003s
KRS061+1.p	0.00	0.003s	yes	0.014s	0.002s
KRS062+1.p	0.00	0.003s	yes	0.019s	0.002s
KRS279-1.p	1.00	0.612s	no	_	=
KRS282-1.p	1.00	4.375s	no	_	=
KRS285-1.p	1.00	8.546s	no	_	=
KRS288-1.p	1.00	18.563s	no	_	_
KRS290-1.p	1.00	13.893s	no	_	_
MGT066-1.p	0.17	0.006s	no	_	_
MGT066+1.p	0.00	0.005 s	no	_	_
MSC008-1.010.p	1.00	0.003s	no	_	_
NLP005-1.p	0.00	0.007s	yes	0.033s	$0.007\mathrm{s}$
NLP006-1.p	0.00	0.003s	yes	0.025s	0.008s
NLP008-1.p	0.00	0.004s	yes	0.030s	0.008s
NLP012-1.p	0.00	0.003s	yes	0.033s	0.004s
NLP013-1.p	0.00	0.003s	yes	0.025s	0.010s

NLP023-1.p								
NLP042-1.p	1	NLP023-1.p	0.00	0.004s	yes	0.033s	0.009s	
NLP114-1-p		NLP024-1.p	0.00	0.003s	yes	0.036s	0.006s	
NLP115-1.p		NLP042-1.p	0.00	0.003s	yes	0.027s	0.005s	
NLP116-1.p		NLP114-1.p	0.00	0.002s	yes	0.021s	0.003s	
NLP118-1.p		NLP115-1.p	0.00	0.003s	yes	0.021s	0.004 s	
NLP119-1.p		NLP116-1.p	0.00	0.005s	yes	0.018s	0.004s	
NLP119-1.p		NLP118-1.p	0.00	0.003s	yes	0.026s	0.004s	
NLP121-1.p		NLP119-1.p	0.00	0.002s	-	0.021s	0.005s	
NLP123-1.p		NLP120-1.p	0.00	0.008s	yes	0.025s	0.003s	
NLP124-1.p		NLP121-1.p	0.00	0.004s	yes	0.019s	0.006s	
NLP125-1.p		NLP123-1.p	0.00	0.006s	yes	0.026s	0.003s	
NLP126-1.p		NLP124-1.p	0.00	0.004s	yes	0.022s	0.004s	
NLP127-1.p		NLP125-1.p	0.00	0.003s	yes	0.028s	0.006s	
NLP128-1.p		NLP126-1.p	0.00	0.008s	yes	0.027s	0.004s	
NLP129-1.p		NLP127-1.p	0.00	0.003s	yes	0.023s	0.006s	
PLA038-1.p         0.83         0.244s         no         —         —           PLA040-1.p         0.83         0.361s         no         —         —           PLA041-1.p         1.00         1.398s         no         —         —           PLA043-1.p         0.50         0.233s         no         —         —           PUZ001-3.p         0.00         0.003s         yes         0.016s         0.003s           PUZ018-2.p         0.17         0.002s         no         —         —           PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         —         —           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.661s         no         —         —         — </td <th></th> <td>NLP128-1.p</td> <td>0.00</td> <td>0.003s</td> <td>yes</td> <td>0.022s</td> <td>0.003s</td> <td></td>		NLP128-1.p	0.00	0.003s	yes	0.022s	0.003s	
PLA040-1.p         0.83         0.361s         no         -         -           PLA041-1.p         1.00         1.398s         no         -         -           PLA043-1.p         0.50         0.233s         no         -         -           PUZ001-3.p         0.00         0.003s         yes         0.016s         0.003s           PUZ018-2.p         0.17         0.002s         no         -         -         -           PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.01s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         -         -         -           PUZ053-1.p         1.00         0.009s         no         -         -         -           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ079+2.p         0.00         0.661s         no		NLP129-1.p	0.00	0.003s	yes	0.025s	0.004s	
PLA041-1.p         1.00         1.398s         no         -         -           PLA043-1.p         0.50         0.233s         no         -         -           PUZ001-3.p         0.00         0.003s         yes         0.016s         0.003s           PUZ018-2.p         0.17         0.002s         no         -         -           PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         -         -         -           PUZ053-1.p         1.00         0.006s         no         -         -         -           PUZ058-2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ068+2.p         0.00         0.661s         no         -         -         -           PUZ089-2.p         0.00         0.661s         no		PLA038-1.p	0.83	0.244s	no	_	_	
PLA043-1.p         0.50         0.233s         no         —         —           PUZ001-3.p         0.00         0.003s         yes         0.016s         0.003s           PUZ018-2.p         0.17         0.002s         no         —         —           PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         —         —           PUZ053-1.p         1.00         0.009s         no         —         —         —           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.661s         no         —         —         —           PUZ089+2.p         0.00         0.661s         no         —<		PLA040-1.p	0.83	0.361s	no	_	_	
PUZ001-3.p         0.00         0.003s         yes         0.016s         0.003s           PUZ018-2.p         0.17         0.002s         no         -         -           PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         -         -         -           PUZ053-1.p         1.00         0.009s         no         -         -         -         -           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s         0.043s         PUZ069+2.p         0.00         0.661s         no         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -		PLA041-1.p	1.00	1.398s	no	_	_	
PUZ018-2.p         0.17         0.002s         no         —         —           PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         —         —           PUZ053-1.p         1.00         0.009s         no         —         —           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ079+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ080+2.p         0.00         0.661s         no         —         —         —           PUZ138+2.p         0.00         0.653s         no         —         —         —           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes		PLA043-1.p	0.50	0.233s	no	_	_	
PUZ028-1.p         0.00         0.006s         yes         0.020s         0.008s           PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         -         -         -           PUZ053-1.p         1.00         0.009s         no         -         -         -           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         -         -         -           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         -         -         -           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00		PUZ001-3.p	0.00	0.003s	yes	0.016s	0.003s	
PUZ028-2.p         0.00         0.002s         yes         0.037s         0.010s           PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         -         -         -           PUZ053-1.p         1.00         0.009s         no         -         -         -           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.661s         no         -         -         -           PUZ080+2.p         0.00         0.661s         no         -         -         -           PUZ138+2.p         0.00         0.653s         no         -         -         -           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17		PUZ018-2.p	0.17	0.002s	no	_	_	
PUZ028-3.p         0.00         0.022s         yes         0.094s         0.013s           PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         -         -           PUZ053-1.p         1.00         0.009s         no         -         -           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         -         -         -           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         -         -         -           SWB031+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN317-1.p         0.00         0.006s         yes		PUZ028-1.p	0.00	0.006s	yes	0.020s	0.008s	
PUZ028-4.p         0.00         0.010s         yes         0.068s         0.004s           PUZ052-1.p         1.00         0.006s         no         —         —           PUZ053-1.p         1.00         0.009s         no         —         —           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         —         —           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         —         —           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN056-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         —         —           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s		PUZ028-2.p	0.00	0.002s	yes	0.037s	0.010s	
PUZ052-1.p         1.00         0.006s         no         -         -           PUZ053-1.p         1.00         0.009s         no         -         -           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         -         -         -           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         -         -         -           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN37-1.p         0.17         0.002s         no         -         -           SYN317-1.p         0.00         0.006s         yes		PUZ028-3.p	0.00	0.022s	yes	0.094s	0.013s	
PUZ053-1.p         1.00         0.009s         no         —         —           PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         —         —           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         —         —           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes         0.03s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         —         —           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         —         —		PUZ028-4.p	0.00	0.010s	yes	0.068s	0.004s	
PUZ068+2.p         0.00         0.650s         yes         7.995s         0.043s           PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         -         -           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         -         -         -           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         -         -           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         -         -         -		PUZ052-1.p	1.00	0.006s	no	_	_	
PUZ069+2.p         0.00         0.670s         yes         50.385s         0.048s           PUZ079+2.p         0.00         0.661s         no         —         —           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         —         —           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB031+4.p         0.00         0.009s         yes         0.077s         0.005s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         —         —           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         —         <		PUZ053-1.p	1.00	0.009s	no	_	_	
PUZ079+2.p         0.00         0.661s         no         —         —           PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         —         —           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB031+4.p         0.00         0.009s         yes         0.077s         0.005s           SWB035+1.p         0.00         0.006s         yes         0.016s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         —         —           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         —         —		PUZ068+2.p	0.00	0.650 s	yes	7.995s	0.043s	
PUZ080+2.p         0.00         0.694s         yes         26.743s         0.048s           PUZ138+2.p         0.00         0.653s         no         -         -           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB031+4.p         0.00         0.009s         yes         0.077s         0.005s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN307-1.p         0.17         0.002s         no         -         -           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         -         -		PUZ069+2.p	0.00	0.670 s	yes	50.385s	0.048s	
PUZ138+2.p         0.00         0.653s         no         —           SWB011+4.p         0.00         0.011s         yes         0.035s         0.008s           SWB031+4.p         0.00         0.009s         yes         0.077s         0.005s           SWB035+1.p         0.00         0.006s         yes         0.033s         0.006s           SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN307-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         —         —		PUZ079+2.p	0.00	0.661s	no	_	_	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		PUZ080+2.p	0.00	0.694s	yes	26.743s	0.048s	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		_	0.00	0.653s	no	_	_	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		SWB011+4.p	0.00	0.011s	yes	0.035s	0.008s	
SYN056-1.p         0.00         0.003s         yes         0.016s         0.002s           SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         -         -           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         -         -		· •		0.009 s	yes	0.077s		
SYN059-1.p         0.00         0.013s         yes         0.024s         0.004s           SYN307-1.p         0.17         0.002s         no         -         -           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         -         -		SWB035+1.p	0.00	0.006s	yes	0.033s	0.006s	
SYN307-1.p         0.17         0.002s         no         -         -           SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         -         -			I		yes	0.016s	0.002s	
SYN317-1.p         0.00         0.006s         yes         0.016s         0.002s           SYN322-1.p         0.00         0.007s         yes         0.013s         0.006s           SYN418-1.p         0.17         0.015s         no         -         -		· •	I		yes	0.024s	0.004s	
SYN322-1.p       0.00       0.007s       yes       0.013s       0.006s         SYN418-1.p       0.17       0.015s       no       -       -		1	I		no	_	_	
SYN418-1.p 0.17 0.015s no – –		_	I		yes			
		· ·	I		yes	0.013s	0.006 s	
SYN419-1.p   0.17   0.015s   no   -		_			no	_	_	
		SYN419-1.p	0.17	0.015s	no	_	_	

	1 0 00		I	1	
SYN420-1.p	0.33	0.016s	yes	1 m 6.536 s	0.502s
SYN421-1.p	0.17	0.018s	no	_	_
SYN422-1.p	0.17	0.016s	no	_	_
SYN423-1.p	0.33	0.019s	no	_	_
SYN424-1.p	0.33	0.019s	no	_	_
SYN425-1.p	0.17	0.016s	no	_	_
SYN426-1.p	0.33	0.025s	no	_	_
SYN427-1.p	0.33	0.020 s	no	_	_
SYN428-1.p	0.33	0.022s	no	_	_
SYN429-1.p	0.33	0.021s	no	_	_
SYN430-1.p	0.00	0.004s	yes	34.426s	0.088s
SYN431-1.p	0.17	0.007s	yes	0.636s	0.015s
SYN432-1.p	0.00	0.006s	yes	22.149s	0.058s
SYN433-1.p	0.00	0.010s	no	_	_
SYN434-1.p	0.33	0.004s	no	_	_
SYN435-1.p	0.33	0.004s	no	_	_
SYN437-1.p	0.33	0.009s	no	_	_
SYN438-1.p	0.17	0.004s	no	_	_
SYN441-1.p	0.33	0.006s	no	_	_
SYN446-1.p	0.17	0.007 s	no	_	_
SYN449-1.p	0.33	0.010s	no	_	_
SYN453-1.p	0.33	0.006s	no	_	_
SYN456-1.p	0.33	0.005s	no	_	_
SYN463-1.p	0.33	0.007 s	no	_	_
SYN464-1.p	0.33	0.008s	no	_	_
SYN490-1.p	0.00	0.003s	yes	0.265s	0.021s
SYN491-1.p	0.00	0.002s	yes	0.049 s	0.005s
SYN492-1.p	0.00	0.003s	yes	0.025s	0.004 s
SYN493-1.p	0.00	0.008s	yes	0.021s	0.003s
SYN494-1.p	0.00	0.002s	yes	0.057s	0.010s
SYN495-1.p	0.00	0.005s	yes	1.313s	0.037s
SYN496-1.p	0.00	0.009s	yes	0.020s	0.004s
SYN497-1.p	0.00	$0.007\mathrm{s}$	yes	0.024s	0.005s
SYN513-1.p	0.33	0.017s	no	_	_
SYN514-1.p	0.33	$0.007\mathrm{s}$	no	_	_
SYN515-1.p	0.00	0.004s	yes	0.035s	0.004 s
SYN516-1.p	0.00	0.004s	yes	0.808s	0.030s
SYN517-1.p	0.00	0.003s	yes	5.543s	0.120s
SYN518-1.p	0.33	0.014s	no	_	_
SYN519-1.p	0.33	0.018s	no	_	_
SYN520-1.p	0.33	0.012s	no	_	_
SYN521-1.p	0.00	0.004s	yes	0.030s	0.005s
SYN522-1.p	0.00	0.004s	yes	0.031s	0.004s
SYN523-1.p	0.00	0.003s	yes	0.025s	0.002s

SYN524-1.p         0.00         0.004s         yes         0.027s           SYN525-1.p         0.00         0.005s         yes         0.033s           SYN526-1.p         0.00         0.005s         yes         0.036s           SYN527-1.p         0.00         0.010s         yes         0.027s           SYN528-1.p         0.00         0.004s         yes         0.037s           SYN529-1.p         0.00         0.006s         no         -           SYN530-1.p         0.00         0.005s         yes         0.035s           SYN531-1.p         0.00         0.003s         yes         0.056s           SYN532-1.p         0.00         0.003s         yes         0.029s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN536-1.p         0.00         0.005s         yes         0.030s           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.154s           SYN539-1.p         0.00         0.005s         yes         0.	0.004s 0.004s 0.004s 0.005s 0.008s 0.005s - 0.007s 0.005s 0.009s 0.006s 0.064s - 0.009s 0.016s 0.010s 0.009s
SYN526-1.p         0.00         0.005s         yes         0.036s           SYN527-1.p         0.00         0.010s         yes         0.027s           SYN528-1.p         0.00         0.004s         yes         0.037s           SYN529-1.p         0.00         0.006s         no         -           SYN530-1.p         0.00         0.005s         yes         0.035s           SYN531-1.p         0.00         0.003s         yes         0.056s           SYN532-1.p         0.00         0.004s         yes         0.029s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN536-1.p         0.00         0.005s         yes         0.030s           SYN537-1.p         0.00         0.005s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.154s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN543-1.p         0.17         0.008s         no         - </td <td>0.005s 0.008s 0.005s - 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.010s</td>	0.005s 0.008s 0.005s - 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.010s
SYN527-1.p         0.00         0.010s         yes         0.027s           SYN528-1.p         0.00         0.004s         yes         0.037s           SYN529-1.p         0.00         0.006s         no         -           SYN530-1.p         0.00         0.005s         yes         0.035s           SYN531-1.p         0.00         0.003s         yes         0.03s           SYN532-1.p         0.00         0.004s         yes         0.029s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN536-1.p         0.00         0.005s         yes         1.356s           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN539-1.p         0.00         0.005s         yes         0.154s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN542-1.p         0.33         0.006s         no         -           SYN543-1.p         0.17         0.008s         no         -	0.008s 0.005s - 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN528-1.p         0.00         0.004s         yes         0.037s           SYN529-1.p         0.00         0.006s         no         -           SYN530-1.p         0.00         0.005s         yes         0.035s           SYN531-1.p         0.00         0.003s         yes         0.056s           SYN532-1.p         0.00         0.004s         yes         0.029s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN535-1.p         0.00         0.005s         yes         0.027s           SYN536-1.p         0.00         0.003s         no         -           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN542-1.p         0.33         0.006s         no         -           SYN544-1.p         0.17         0.008s         no         - <td>0.005s - 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s</td>	0.005s - 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN529-1.p         0.00         0.006s         no         —           SYN530-1.p         0.00         0.005s         yes         0.035s           SYN531-1.p         0.00         0.003s         yes         0.056s           SYN532-1.p         0.00         0.003s         yes         0.03s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN535-1.p         0.00         0.005s         yes         0.027s           SYN536-1.p         0.00         0.003s         no         —           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN542-1.p         0.33         0.006s         no         —           SYN544-1.p         0.17         0.008s         no         —           SYN545-1.p         0.33         0.012s         no         — <td>- 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s</td>	- 0.007s 0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN530-1.p         0.00         0.005s         yes         0.035s           SYN531-1.p         0.00         0.003s         yes         0.056s           SYN532-1.p         0.00         0.003s         yes         0.033s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN535-1.p         0.00         0.005s         yes         1.356s           SYN536-1.p         0.00         0.003s         no         -           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN542-1.p         0.33         0.006s         no         -           SYN543-1.p         0.17         0.008s         no         -           SYN544-1.p         0.17         0.016s         no         -           SYN545-1.p         0.33         0.012s         no         - <td>0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s</td>	0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN531-1.p         0.00         0.003s         yes         0.056s           SYN532-1.p         0.00         0.003s         yes         0.033s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN535-1.p         0.00         0.005s         yes         1.356s           SYN536-1.p         0.00         0.003s         no         -           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN540-1.p         0.00         0.005s         yes         0.154s           SYN541-1.p         0.00         0.005s         yes         0.046s           SYN542-1.p         0.33         0.006s         no         -           SYN543-1.p         0.17         0.008s         no         -           SYN544-1.p         0.17         0.016s         no         -           SYN545-1.p         0.33         0.012s         no         -	0.005s 0.009s 0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN532-1.p         0.00         0.003s         yes         0.033s           SYN533-1.p         0.00         0.004s         yes         0.029s           SYN534-1.p         0.00         0.004s         yes         0.027s           SYN535-1.p         0.00         0.005s         yes         1.356s           SYN536-1.p         0.00         0.003s         no         -           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN539-1.p         0.00         0.005s         yes         0.154s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN542-1.p         0.33         0.006s         no         -           SYN543-1.p         0.17         0.008s         no         -           SYN544-1.p         0.17         0.016s         no         -           SYN545-1.p         0.33         0.012s         no         -	0.009s 0.009s 0.006s 0.064s  0.009s 0.021s 0.016s 0.010s
SYN533-1.p       0.00       0.004s       yes       0.029s         SYN534-1.p       0.00       0.004s       yes       0.027s         SYN535-1.p       0.00       0.005s       yes       1.356s         SYN536-1.p       0.00       0.003s       no       -         SYN537-1.p       0.00       0.015s       yes       0.030s         SYN538-1.p       0.00       0.005s       yes       0.483s         SYN539-1.p       0.00       0.005s       yes       0.154s         SYN540-1.p       0.17       0.005s       yes       0.046s         SYN541-1.p       0.00       0.005s       yes       0.057s         SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	0.009s 0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN534-1.p       0.00       0.004s       yes       0.027s         SYN535-1.p       0.00       0.005s       yes       1.356s         SYN536-1.p       0.00       0.003s       no       -         SYN537-1.p       0.00       0.015s       yes       0.030s         SYN538-1.p       0.00       0.005s       yes       0.483s         SYN539-1.p       0.00       0.005s       yes       0.154s         SYN540-1.p       0.17       0.005s       yes       0.046s         SYN541-1.p       0.00       0.005s       yes       0.057s         SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN545-1.p       0.33       0.012s       no       -	0.006s 0.064s - 0.009s 0.021s 0.016s 0.010s
SYN535-1.p         0.00         0.005s         yes         1.356s           SYN536-1.p         0.00         0.003s         no         -           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN539-1.p         0.00         0.005s         yes         0.154s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN542-1.p         0.33         0.006s         no         -           SYN543-1.p         0.17         0.008s         no         -           SYN544-1.p         0.17         0.016s         no         -           SYN545-1.p         0.33         0.012s         no         -	0.064s - 0.009s 0.021s 0.016s 0.010s
SYN536-1.p         0.00         0.003s         no         –           SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN539-1.p         0.00         0.005s         yes         0.154s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN542-1.p         0.33         0.006s         no         –           SYN543-1.p         0.17         0.008s         no         –           SYN544-1.p         0.17         0.016s         no         –           SYN545-1.p         0.33         0.012s         no         –	
SYN537-1.p         0.00         0.015s         yes         0.030s           SYN538-1.p         0.00         0.005s         yes         0.483s           SYN539-1.p         0.00         0.005s         yes         0.154s           SYN540-1.p         0.17         0.005s         yes         0.046s           SYN541-1.p         0.00         0.005s         yes         0.057s           SYN542-1.p         0.33         0.006s         no         -           SYN543-1.p         0.17         0.008s         no         -           SYN544-1.p         0.17         0.016s         no         -           SYN545-1.p         0.33         0.012s         no         -	0.021s $0.016s$ $0.010s$
SYN538-1.p       0.00       0.005s       yes       0.483s         SYN539-1.p       0.00       0.005s       yes       0.154s         SYN540-1.p       0.17       0.005s       yes       0.046s         SYN541-1.p       0.00       0.005s       yes       0.057s         SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	0.021s $0.016s$ $0.010s$
SYN539-1.p       0.00       0.005s       yes       0.154s         SYN540-1.p       0.17       0.005s       yes       0.046s         SYN541-1.p       0.00       0.005s       yes       0.057s         SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	0.016s $0.010s$
SYN540-1.p       0.17       0.005s       yes       0.046s         SYN541-1.p       0.00       0.005s       yes       0.057s         SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	0.010s
SYN541-1.p       0.00       0.005s       yes       0.057s         SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	
SYN542-1.p       0.33       0.006s       no       -         SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	0.009s - - -
SYN543-1.p       0.17       0.008s       no       -         SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	_ _ _
SYN544-1.p       0.17       0.016s       no       -         SYN545-1.p       0.33       0.012s       no       -	<u> </u>
SYN545-1.p 0.33 0.012s no –	_
SYN546-1.p 0.33 0.020s no –	_
	_
SYN547-1.p 0.33 0.022s yes 6.409s	0.120s
SYN720-1.p 0.00 0.008s yes 0.119s	0.014s
SYN811-1.p   0.33   0.410s   no   -	_
SYN812-1.p   0.17   4.161s   no -	_
SYN814-1.p 0.33 0.518s no –	_
SYN815-1.p 0.33 1.695s no –	_
SYN816-1.p 0.33 1.718s no -	_
SYN817-1.p   0.17   1.692s   no -	_
SYN818-1.p   0.33   4.974s   no   -	_
SYN821-1.p 0.50 1.812s no –	_
SYN822-1.p 0.33 1.867s no –	_
SYN823-1.p 0.17 0.116s no –	_
SYN824-1.p 0.33 1.118s no –	_
SYN825-1.p 0.33 3.577s no –	_
SYN826-1.p 0.33 3.613s no –	_
SYN827-1.p 0.17 0.172s no –	_
SYN828-1.p 0.17 1.618s no –	_
SYN829-1.p 0.33 5.230s no –	_
SYN830-1.p 0.33 5.822s no –	_
	_
SYN831-1.p   0.33   5.053s   no	

SYN835-1.p	0.17	0.179s	no	_	_
SYN838-1.p	0.33	2.001s	no	_	_
SYN839-1.p	0.33	6.292s	no	_	_
SYN840-1.p	0.33	$5.765\mathrm{s}$	no	_	_
SYN841-1.p	0.33	5.769s	no	_	_
SYN842-1.p	0.33	6.003s	no	_	_
SYN851-1.p	0.33	1.916s	no	_	_
SYN852-1.p	0.33	6.684s	no	_	_
SYN853-1.p	0.33	6.246s	no	_	_
SYN854-1.p	0.33	6.619s	no	_	_
SYN855-1.p	0.33	6.050 s	no	_	_
SYN863-1.p	0.33	2.042s	no	_	_
SYN864-1.p	0.33	2.144s	no	_	_
SYN867-1.p	0.17	0.035s	no	_	_
SYN868-1.p	0.17	0.023s	no	_	_
SYN870-1.p	0.17	0.014s	no	_	_
SYN872-1.p	0.33	0.200 s	no	_	_
SYN888-1.p	0.33	0.241s	no	_	_
SYN902-1.p	0.33	0.275s	no	_	_
SYO583-1.p	1.00	24.277s	no	_	_
SYO584-1.p	1.00	3.549s	no	_	_
SYO585-1.p	1.00	3.456s	no	_	_
SYO586-1.p	1.00	0.604s	no	_	_
SYO590-1.p	1.00	1.047s	no	_	_
SYO593-1.p	0.67	0.231s	no	_	_
SYO595-1.p	0.67	0.192s	no	_	_
SYO599-1.p	1.00	48.557s	no	_	_
SYO603-1.p	1.00	1.192s	no	_	_

Table D.1: Results of Sat EPR TPTP problems

Another test were made but the time limit was 300 seconds instead of 180 seconds and 2GB memory limit. Only two more problems were solved within that limit. The below table D.2 shows them:

Problem	rating	transformations t.	saturation t.	model extraction t.
GRP130-2.005.p	0.17	0.007s	3m21.354s	0.009s
PUZ079+2.p	0.00	0.660s	3m34.068s	0.048s

Table D.2: More Solved Sat EPR TPTP problems

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